

# Scalar Mesons and the Fragmented Glueball

Eberhard Klempt

University of Bonn



ITP Hadron Physics Seminar

Beijing, 2021, April 19th

# **Scalar mesons and the fragmented glueball**

- 1. The Standard Model**
- 2. How to search for glueballs**
- 3. Coupled channel analysis**
- 4. Results and interpretation**
- 5. Summary**

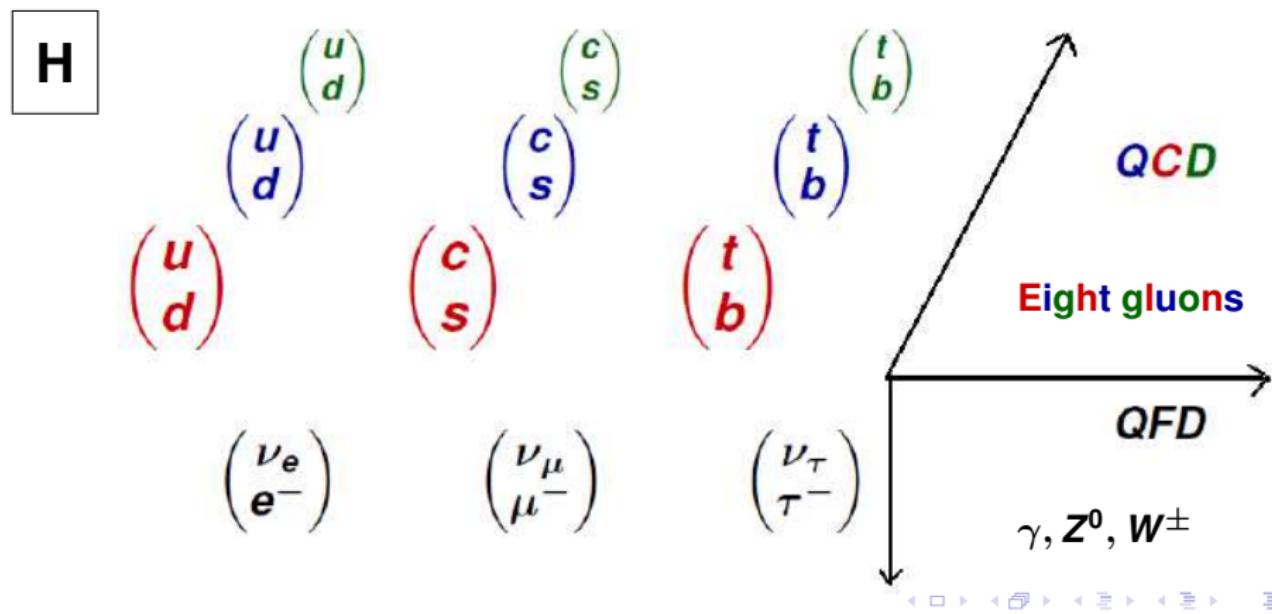
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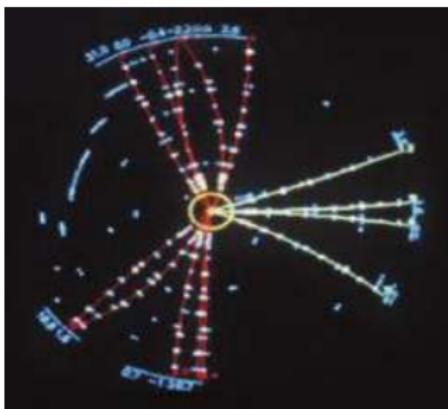
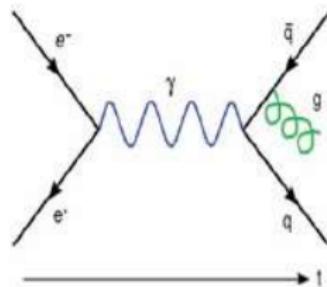
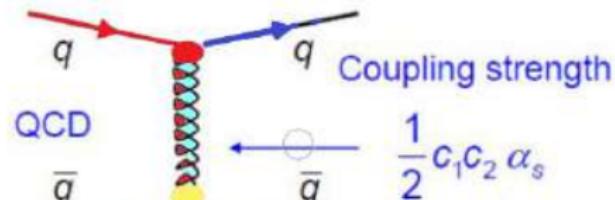
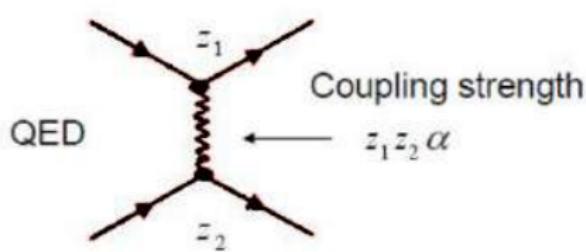
# 1. The Standard Model

## 1.1 Particles ...

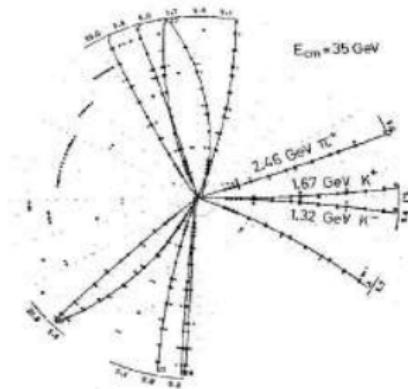
1. Fermions: Six quarks (in three colours) and six leptons
2. Bosons: Eight gluons, three vector bosons, one photon
3. The Higgs boson provides the mass



## 1.2. and interactions



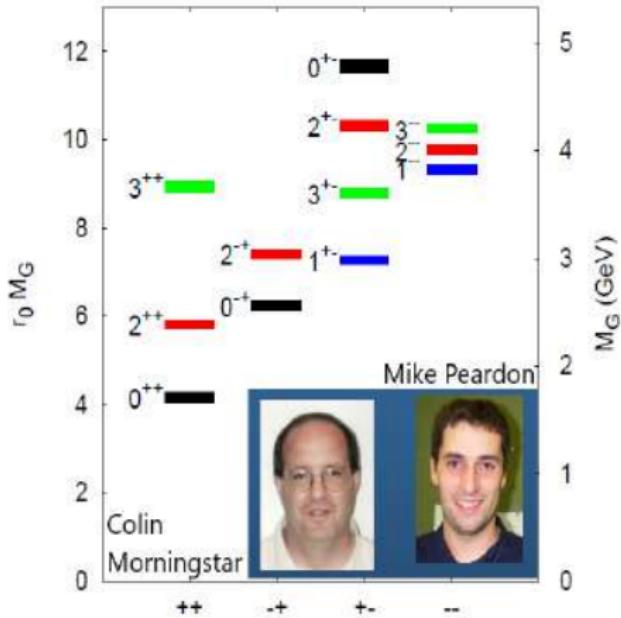
Three-jet events demonstrate the existence of gluons!



## 1.3 Glueballs



The self-interaction between gluons leads to the prediction of glueballs<sup>1</sup>



$0^{++}$   **$1710 \pm 50 \pm 80$  MeV**

$2^{++}$   **$2390 \pm 30 \pm 120$  MeV**

$0^{-+}$   **$2560 \pm 35 \pm 120$  MeV**

<sup>1</sup> Y. Chen *et al.* "Glueball spectrum and matrix elements on anisotropic lattices," Phys. Rev. D 73, 014516 (2006).

$0^{++}$   **$1980$  MeV**

$2^{++}$   **$2420$  MeV**

$0^{-+}$   **$2220$  MeV**

<sup>2</sup> A. P. Szczepaniak and E. S. Swanson, "The Low lying glueball spectrum," Phys. Lett. B 577, 61-66 (2003).

$0^{++}$   **$1850 \pm 130$  MeV**

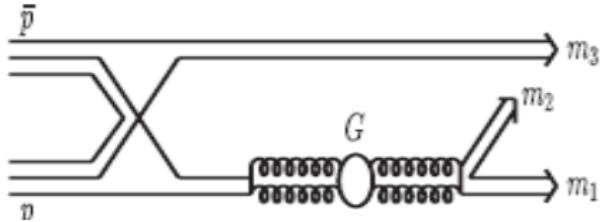
$0^{-+}$   **$2580 \pm 180$  MeV**

<sup>3</sup> M. Q. Huber, C. S. Fischer and H. Sanchis-Alepuz, "Spectrum of scalar and pseudoscalar glueballs from functional methods," Eur. Phys. J. C 80, no.11, 1077 (2020).

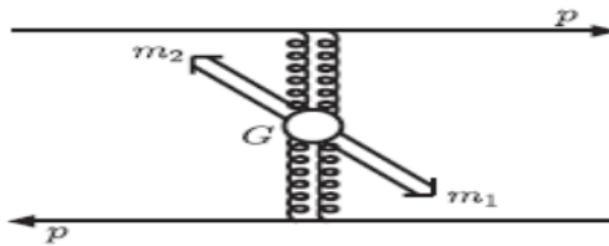
**The scalar glueball is expected in the 1700 to 2000 MeV mass range**

## 2. How to search for glueballs

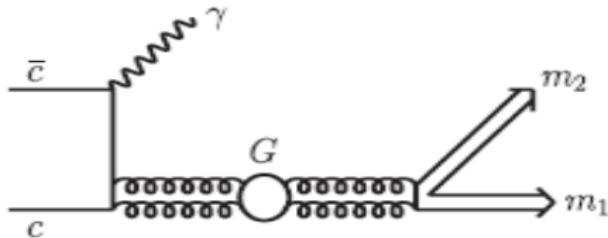
$\bar{N}N$  annihilation



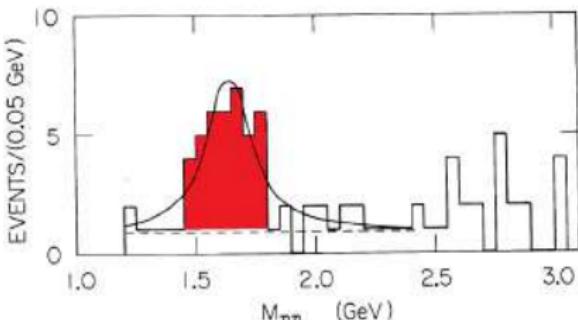
Central production



Radiative  $J/\psi$  decays



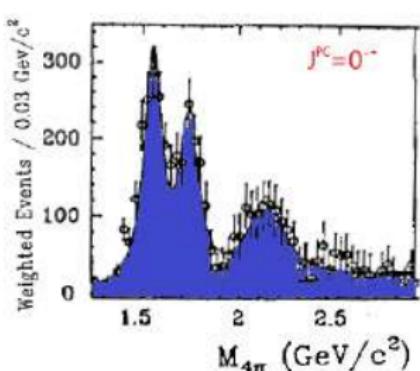
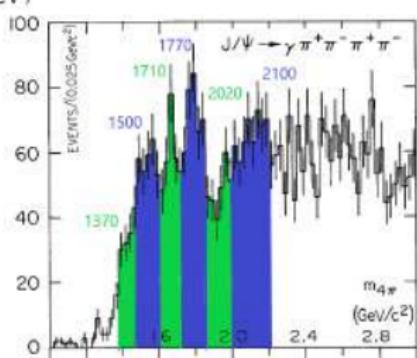
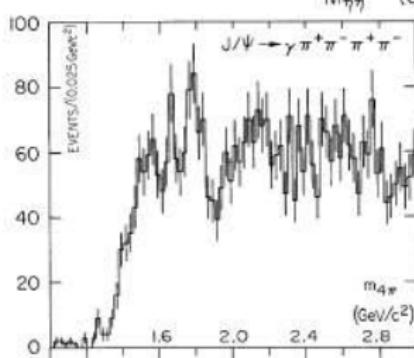
## 2.1 Radiative $J/\psi$ decays (MARKIII, DM2)



MARKIII: A radiatively produced resonance decaying into  $\eta\eta$

The tensor glueball?

C. Edwards *et al.* Phys. Rev. Lett. 48, 458 (1982).

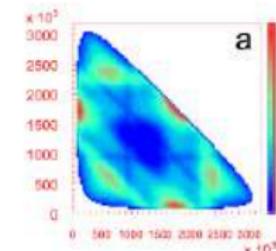


R. M. Baltrusaitis *et al.* [MARK-III], Phys. Rev. D 33, 1222 (1986). (N. Wermes)

D. Bisello *et al.* [DM2], Phys. Rev. D 39, 701 (1989).

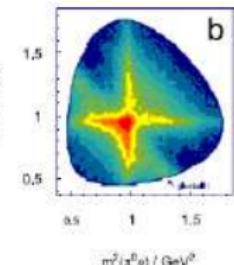
Three resonances at 1500, 1750, and 2100 MeV, first  $J^{PC} = 0^{-+}$ , D.V. Bugg:  $J^{PC} = 0^{++}$

## 2.2 $\bar{N}N$ annihilation (Crystal Barrel at LEAR)



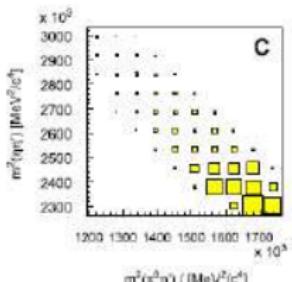
a:  $3\pi^0$ ;

J. Brose (Mainz)



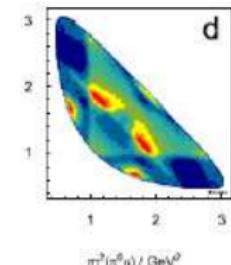
b:  $\pi^0\eta\eta$ ;

R. Hackmann (Mainz)



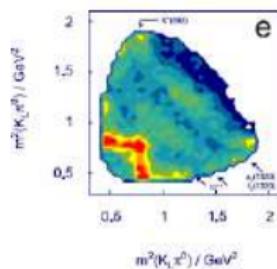
c:  $\pi^0\eta\eta'$ ;

S. Spanier (Mainz)



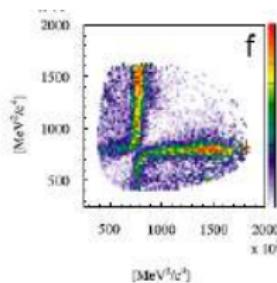
d:  $\pi^0\pi^0\eta$ ;

S. Spanier (Mainz)



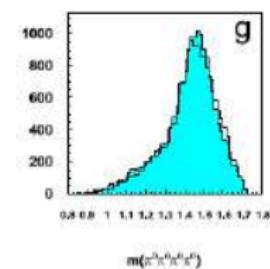
e:  $K_L K_L \pi^0$ ;

A.R. Cooper (London)



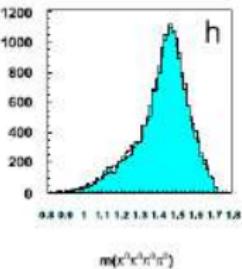
f:  $K^\pm K_L \pi^\mp$ ;

C. Völker (Munich)



g:  $4\pi^0$ ;

U. Thoma (Bonn)

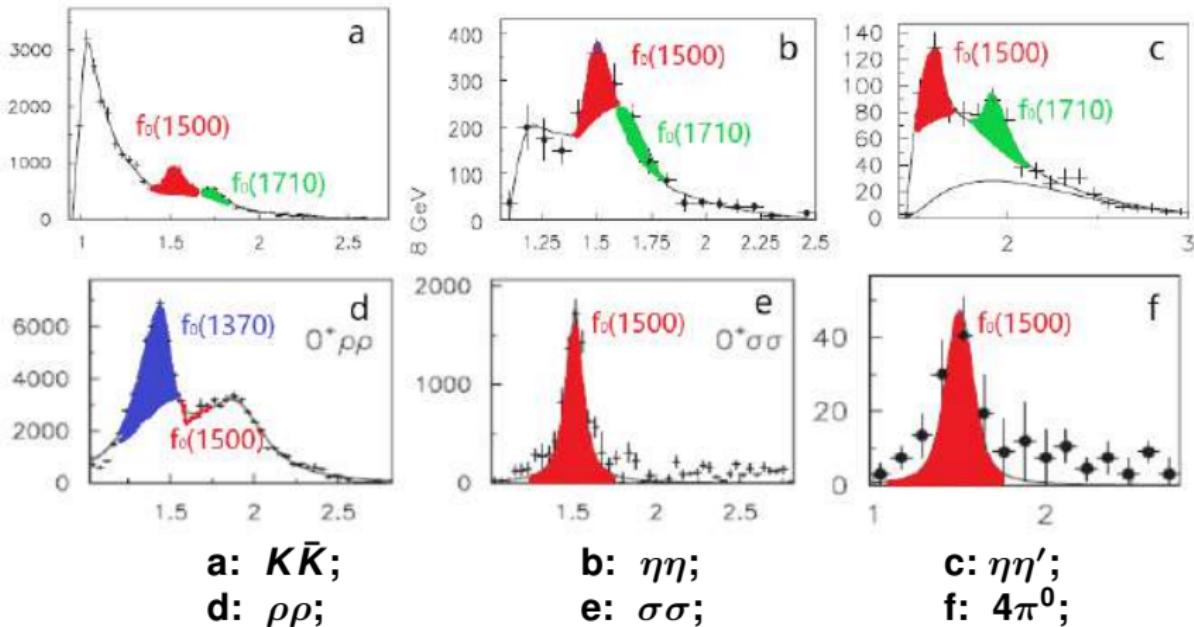


h:  $4\pi^0$

U. Thoma (Bonn)

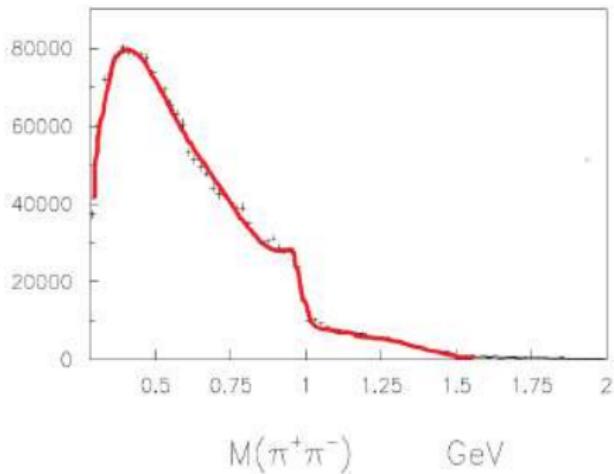
Three new scalar mesons:  $f_0(1370)$ ,  $f_0(1500)$ ,  $a_0(1475)$  !

## 2.3 Central production (WA102 experiment at SPS)

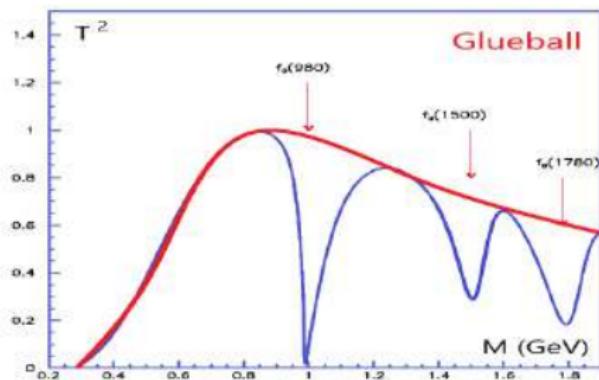


Three scalar isoscalar mesons:  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(1710)$  !

## 2.4 A global view of scalar mesons



Centrally produced  $\pi^+\pi^-$



B. S. Zou, “ $\pi\pi$  S-wave interaction and  $0^{++}$  particles,”  
Subnucl. Ser. 34, 579-582 (1997).

The  $\pi\pi$  S-wave squared amplitude

Wide “background amplitude” could be the glueball<sup>1</sup>.

<sup>1</sup> P. Minkowski and W. Ochs, “Identification of the glueballs and the scalar meson nonet of lowest mass,” Eur. Phys. J. C 9, 283-312 (1999).

Or it could be the superposition of a series of SU(3) singlet scalar mesons superimposed by “narrow” SU(3) octet states<sup>2</sup>.

<sup>2</sup> E. Klemt and A. Zaitsev, “Glueballs, Hybrids, Multiquarks. Experimental facts versus QCD inspired concepts,” Phys. Rept. 454, 1-202 (2007).

## 2.5 Supernumerosity

$\{a_0(1475), K_0^*(1430), f_0(1710), f_0(1370)\}$        $f_0(1500)$

similar:  $\{a_2(1320), K_2^*(1430), f'_2(1525), f_2(1270)\}$

Two scalar isoscalar states expected, three found!

Two  $q\bar{q}$  and one glueball with mixing.

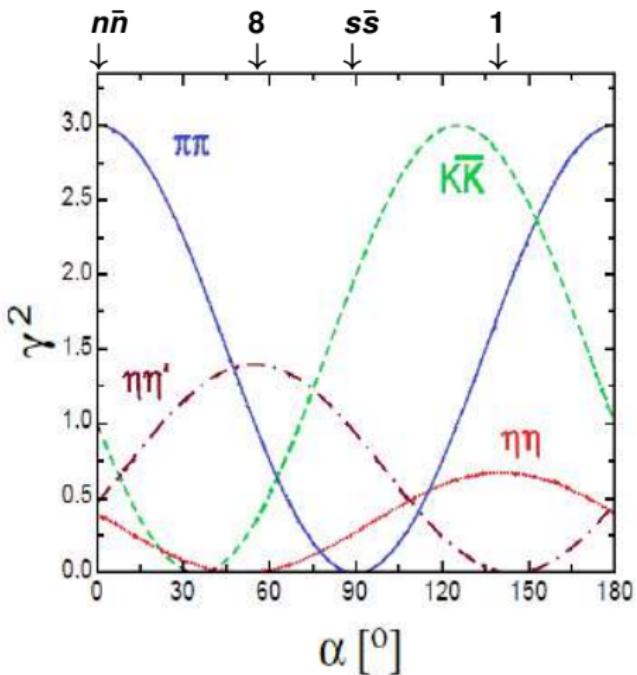
Mixing matrix<sup>1</sup>:

$$\begin{pmatrix} |f_0(1710)\rangle \\ |f_0(1500)\rangle \\ |f_0(1370)\rangle \end{pmatrix} = U \begin{pmatrix} |s\bar{s}\rangle \\ |\textcolor{red}{G}\rangle \\ |\textcolor{blue}{n}\bar{n}\rangle \end{pmatrix} = \begin{pmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{pmatrix} \begin{pmatrix} |s\bar{s}\rangle \\ |\textcolor{red}{G}\rangle \\ |\textcolor{blue}{n}\bar{n}\rangle \end{pmatrix}.$$

1 C. Amsler and F. E. Close, "Evidence for a scalar glueball," Phys. Lett. B 353, 385 (1995).  
C. Amsler and F. E. Close, "Is  $f_0(1500)$  a scalar glueball?," Phys. Rev. D 53, 295 (1996).

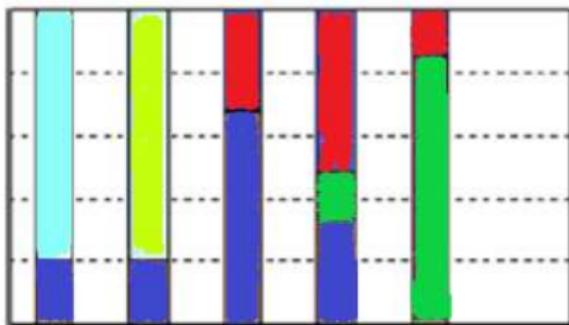
Large number of follow-up papers

## 2.6 Decays of scalar mesons



$\frac{\Gamma(f_0(1370) \rightarrow \eta\eta)}{\Gamma(f_0(1370) \rightarrow \pi\pi)}$	$= 0.02 \pm 0.02$
$\frac{\Gamma(f_0(1370) \rightarrow K\bar{K})}{\Gamma(f_0(1370) \rightarrow \pi\pi)}$	$= 0.00 - 1.00$
$\frac{\Gamma(f_0(1500) \rightarrow \eta\eta')}{\Gamma(f_0(1500) \rightarrow \eta\eta)}$	$= 0.84 \pm 0.23$
$\frac{\Gamma(f_0(1500) \rightarrow \eta\eta)}{\Gamma(f_0(1500) \rightarrow \pi^0\pi^0)}$	$= 0.23 \pm 0.04$
$\frac{\Gamma(f_0(1500) \rightarrow K\bar{K})}{\Gamma(f_0(1500) \rightarrow \pi\pi)}$	$= 0.19 \pm 0.07$
$\frac{\Gamma(f_0(1710) \rightarrow K\bar{K})}{\Gamma(f_0(1710) \rightarrow \pi\pi)}$	$= 2.56 \pm 0.92$

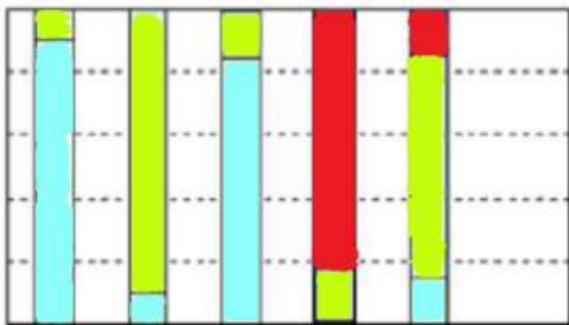
$\sigma(485) \quad 0.98 \quad 1.37 \quad 1.5 \quad 1.75 \text{ GeV}/c^2$



F. E. Close and A. Kirk, Eur. Phys. J. C 21, 531-543 (2001).

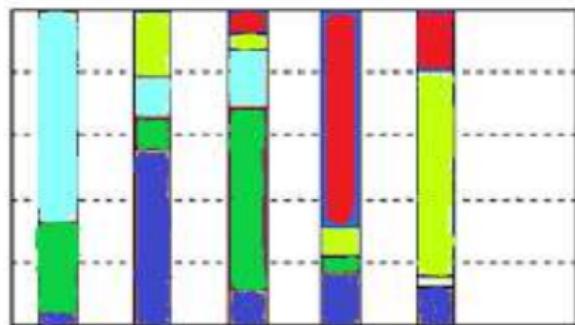
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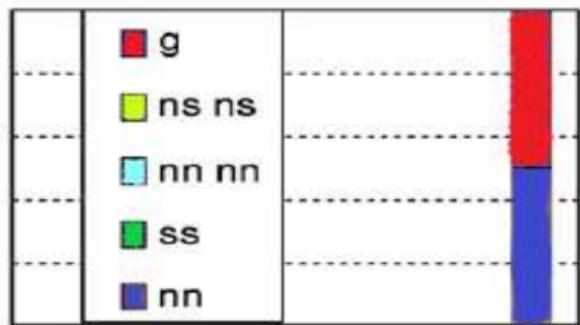


L. Maiani *et al.*, Eur. Phys. J. C 50, 609-616 (2007).

$1.79 \text{ GeV}/c^2$



A. H. Fariborz, Phys. Rev. D 74, 054030 (2006).



D. V. Bugg, [arXiv:hep-ph/0603018 [hep-ph]].

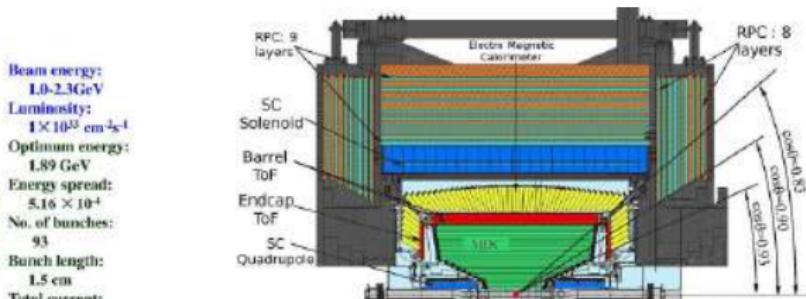
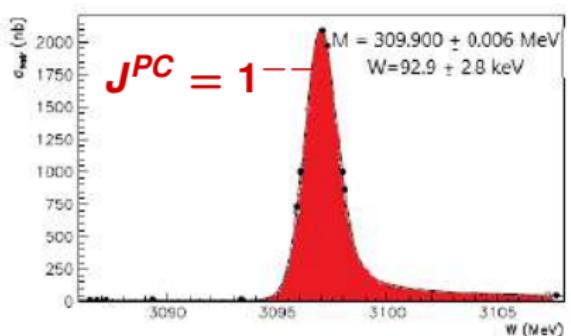
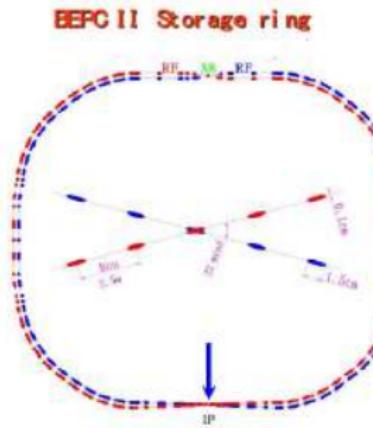
Scalar mesons could have a large tetraquark component!

### 3. Coupled channel analysis

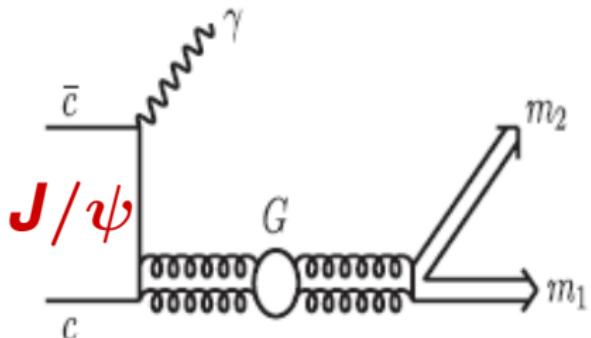
A. V. Sarantsev, I. Denisenko, U. Thoma and E. Klempt,  
 "Scalar isoscalar mesons and the scalar glueball from radiative  $J/\psi$  decays,"  
 Phys. Lett. B 816, 136227 (2021).

$J/\psi$	$\rightarrow$	$\gamma\pi^0\pi^0$	$K_SK_S$	$\gamma\eta\eta'$	$\gamma\omega\phi$	BESIII
$\chi^2/N; N$		1.28; 167	1.21, 121	0.8; 21	0.2; 17	
$\bar{p}p$	$\rightarrow$	$3\pi^0$	$\pi^0\pi^+\pi^-$	$2\pi^0\eta$	$\pi^0\eta\eta$	CB (liq. H <sub>2</sub> )
$\chi^2/N, N$		1.40; 7110	1.24, 1334	1.23; 3475	1.28; 3595	
$\bar{p}p$	$\rightarrow$	$3\pi^0$		$2\pi^0\eta$	$\pi^0\eta\eta$	CB (gas. H <sub>2</sub> )
$\chi^2/N, N$		1.38; 4891		1.24; 3631	1.32; 1182	
$\bar{p}p$	$\rightarrow$	$K_LK_L\pi^0$	$K^+K^-\pi^0$	$K_SK^\pm\pi^\mp$	$K_LK^\pm\pi^\mp$	CB (liq. H <sub>2</sub> )
$\chi^2/N, N$		1.08; 394	0.97; 521	2.13; 771	0.76; 737	
$\bar{p}n$	$\rightarrow$	$\pi^+\pi^-\pi^-$	$\pi^0\pi^0\pi^-$	$K_SK^-\pi^0$	$K_SK_S\pi^-$	CB (liq. D <sub>2</sub> )
$\chi^2/N, N$		1.39; 823	1.57; 825	1.33; 378	1.62; 396	
$\pi^+\pi^-$	$\rightarrow$	$\pi^+\pi^-$	$\pi^0\pi^0$	$\eta\eta$	$\eta\eta'$	$K^+K^-$
$\chi^2/N, N$		1.32; 845	0.89; 110	0.67; 15	0.23; 9	1.06; 35
		CERN-Munich		GAMS		BNL

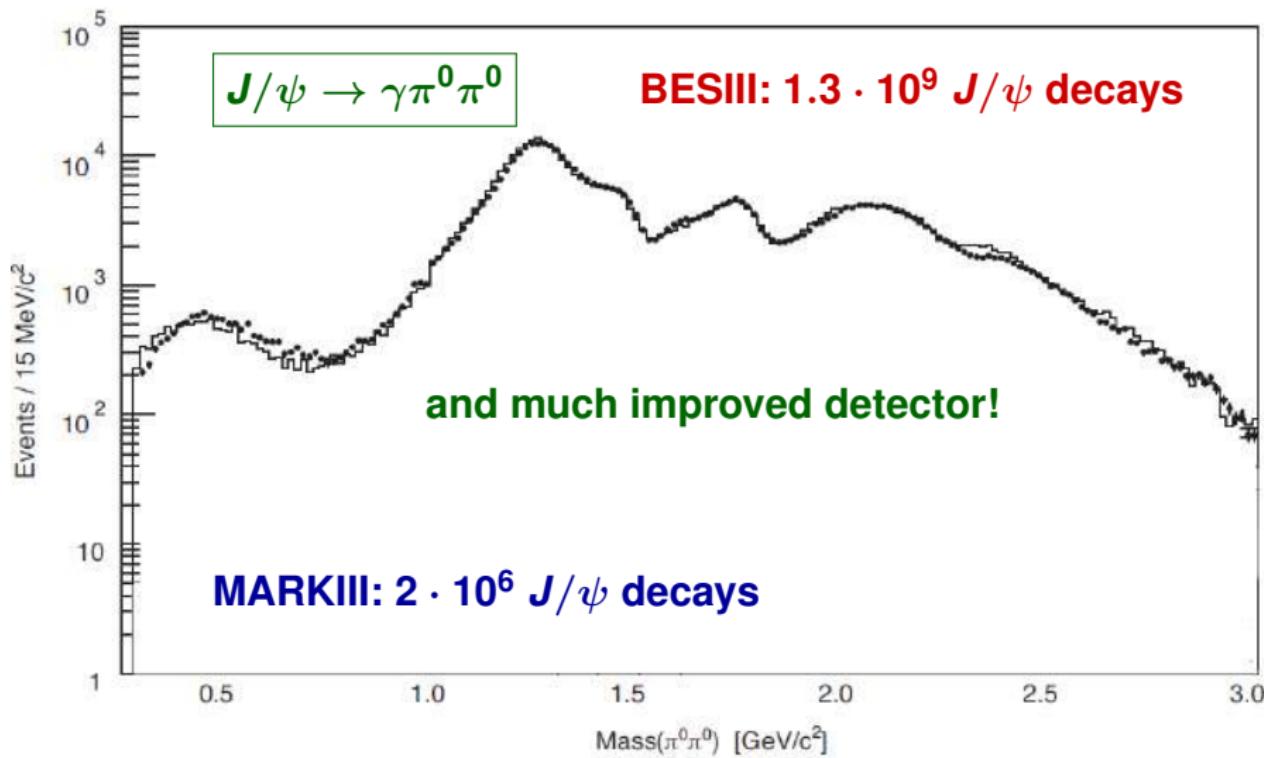
### 3.1 Data from BESIII



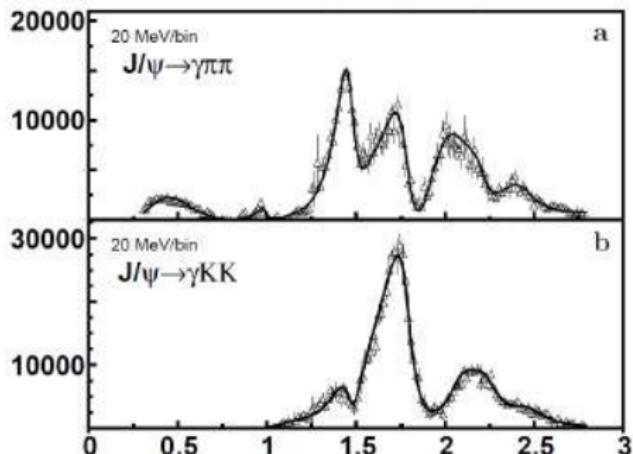
M. Ablikim *et al.* [BESIII], "Design and Construction of the BESIII Detector," Nucl. Instrum. Meth. A 614, 345-399 (2010).



V. V. Anashin *et al.* "Final analysis of KEDR data on  $J/\psi$  and  $\psi(2S)$  masses," Phys. Lett. B 749, 50-56 (2015).



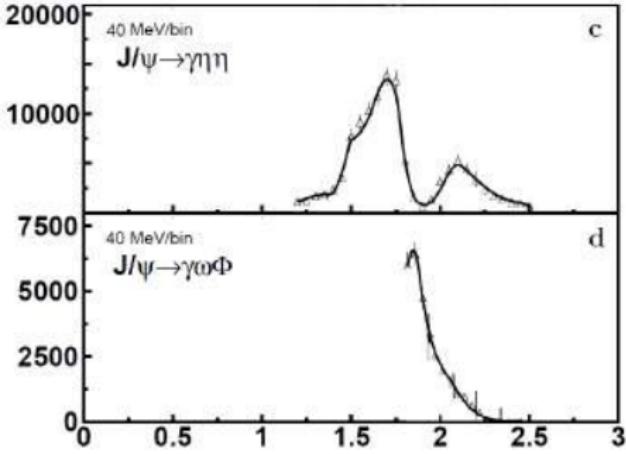
$J/\psi \rightarrow \gamma \pi^0\pi^0$  and  $K_SK_S$



$1.3 \cdot 10^9$  events

PWA in slices of energy

$\eta\eta$  and  $\omega\phi$



$0.225 \cdot 10^9$  events

Amplitude fit to data

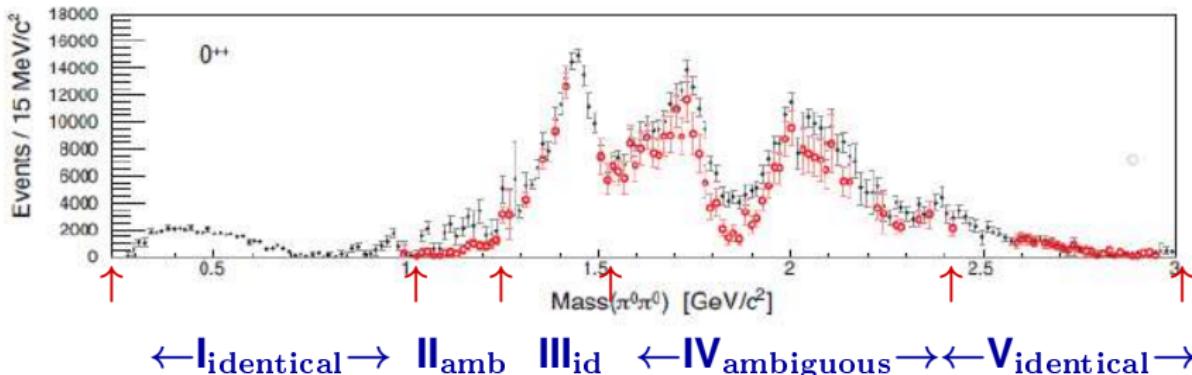
M. Ablikim *et al.* [BESIII Collaboration], “Amplitude analysis of the  $\pi^0\pi^0$  system produced in radiative  $J/\psi$  decays,” Phys. Rev. D 92 no.5, 052003 (2015).

M. Ablikim *et al.* [BESIII Collaboration], “Amplitude analysis of the  $K_SK_S$  system produced in radiative  $J/\psi$  decays,” Phys. Rev. D 98 no.7, 072003 (2018).

M. Ablikim *et al.* [BESIII Collaboration], “Partial wave analysis of  $J/\psi \rightarrow \gamma\eta\eta$ ,” Phys. Rev. D 87, no. 9, 092009 (2013).

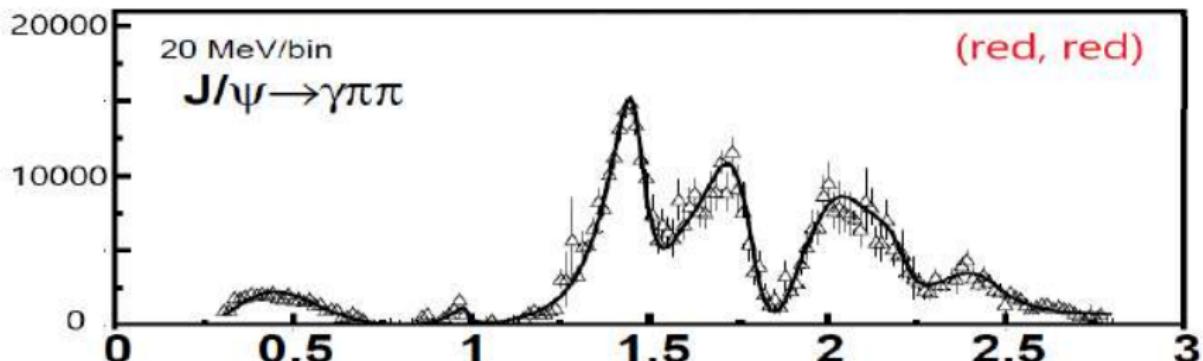
M. Ablikim *et al.* [BESIII Collaboration], “Study of the near-threshold  $\omega\phi$  mass enhancement in doubly OZI-suppressed  $J/\psi \rightarrow \gamma\omega\phi$  decays,” Phys. Rev. D 87 no.3, 032008 (2013).

## Partial waves from $J/\psi \rightarrow \pi^0\pi^0$ in slices of the $2\pi^0$ mass

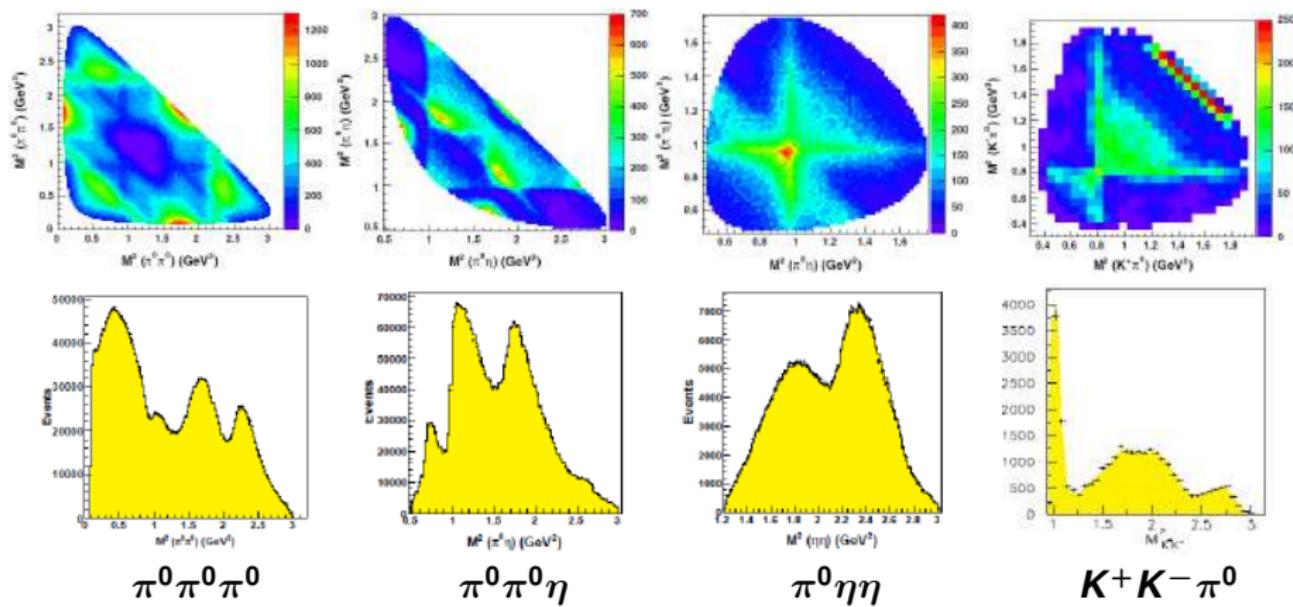


M. Ablikim *et al.* [BESIII], and A.P. Szczepaniak, P. Guo,

"Amplitude analysis of the  $\pi^0\pi^0$  system produced in radiative  $J/\psi$  decays," Phys. Rev. D 92, no.5, 052003 (2015).

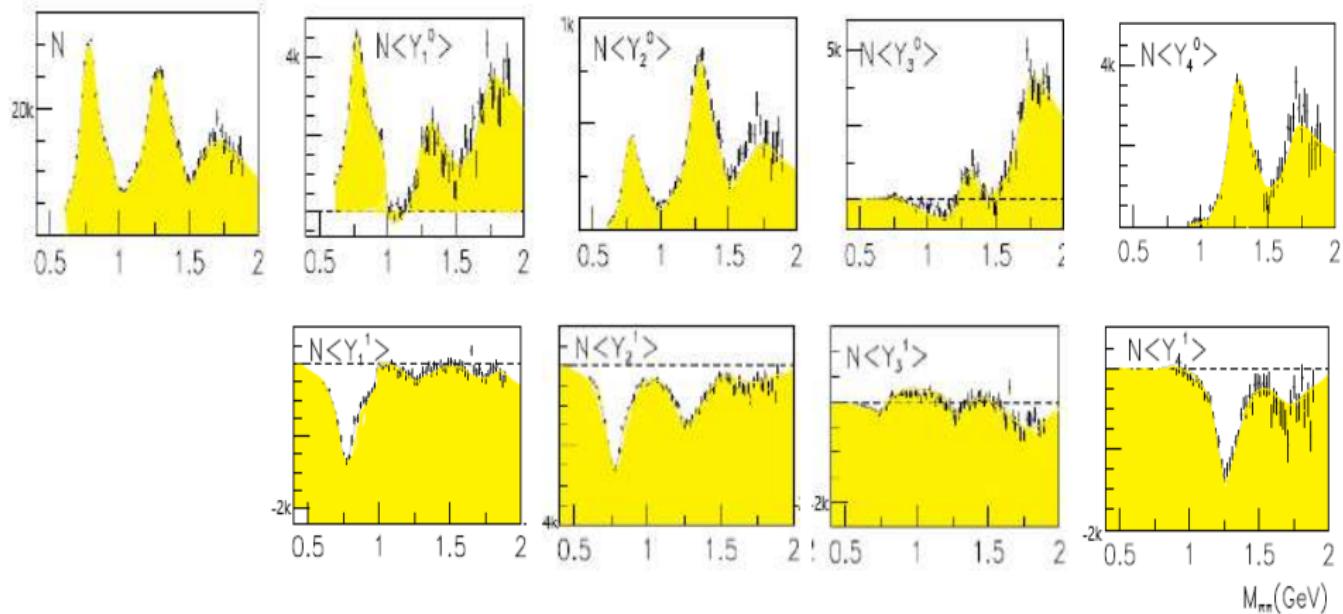


### 3.2 The Crystal Barrel data



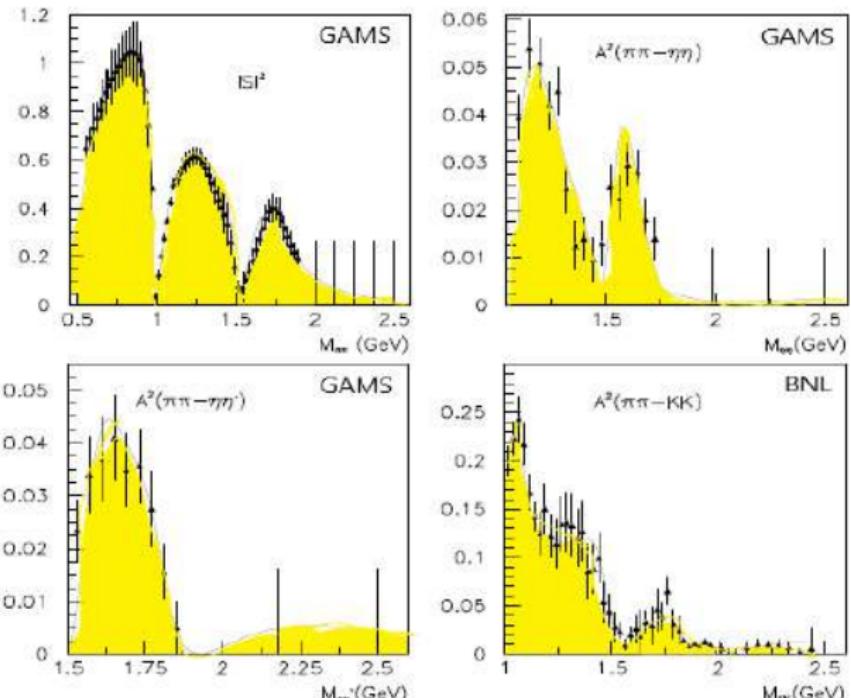
... and further Dalitz plots.

### 3.3 The CERN-Munich data on $\pi\pi \rightarrow \pi\pi$ elastic scattering



**The CERN-Munich data have different PWA solutions. The ambiguity is resolved by the GAMS data on  $\pi^- p \rightarrow \pi^0 \pi^0 n$  (at 200 GeV/c pion momenta).**

### 3.4 GAMS and BNL data on pion-induced reactions



GAMS: D. Alde *et al.*, "Study of the  $\pi^0\pi^0$  system with the GAMS-4000 spectrometer at 100 GeV/c," Eur. Phys. J. A 3, 361 (1998).

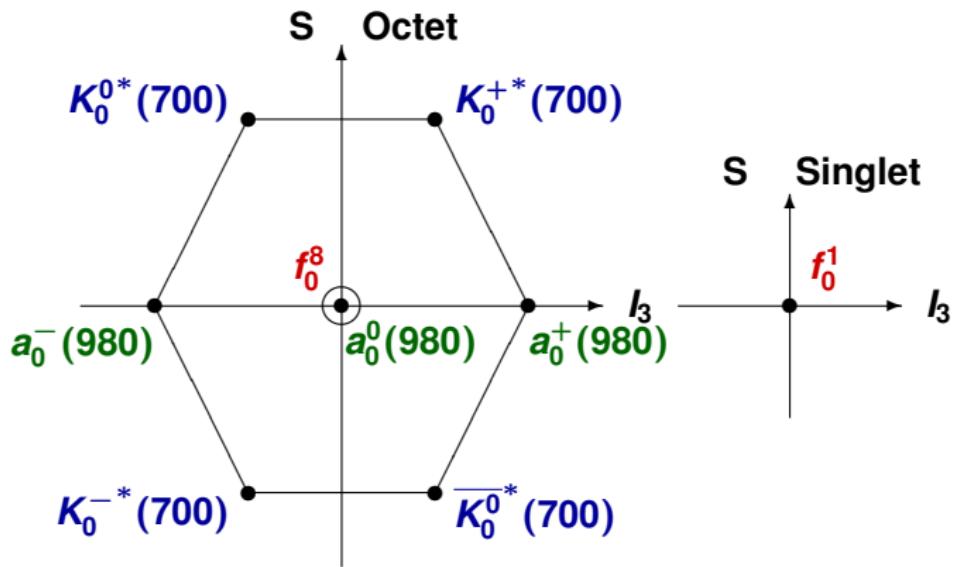
BNL: S. J. Lindenbaum and R. S. Longacre, "Coupled channel analysis of  $J^{PC} = 0^{++}$  and  $2^{++}$  isoscalar mesons with masses below 2 GeV," Phys. Lett. B 274, 492 (1992).

## 4. Results and interpretation

Pole masses and widths (in MeV) of scalar mesons. The RPP values are listed as small numbers for comparison.

Name	$f_0(500)$	$f_0(1370)$	$f_0(1710)$	$f_0(2020)$	$f_0(2200)$
$M$	$410 \pm 20$ $400 \rightarrow 550$	$1370 \pm 40$ $1200 \rightarrow 1500$	$1700 \pm 18$ $1704 \pm 12$	$1925 \pm 25$ $1992 \pm 16$	$2200 \pm 25$ $2187 \pm 14$
$\Gamma$	$480 \pm 30$ $400 \rightarrow 700$	$390 \pm 40$ $100 \rightarrow 500$	$255 \pm 25$ $123 \pm 18$	$320 \pm 35$ $442 \pm 60$	$150 \pm 30$ $\sim 200$
Name	$f_0(980)$	$f_0(1500)$	$f_0(1770)$	$f_0(2100)$	$f_0(2330)$
$M$	$1014 \pm 8$ $990 \pm 20$	$1483 \pm 15$ $1506 \pm 6$	$1765 \pm 15$	$2075 \pm 20$ $2086^{+20}_{-24}$	$2340 \pm 20$ $\sim 2330$
$\Gamma$	$71 \pm 10$ $10 \rightarrow 100$	$116 \pm 12$ $112 \pm 9$	$180 \pm 20$	$260 \pm 25$ $284^{+60}_{-32}$	$165 \pm 25$ $250 \pm 20$

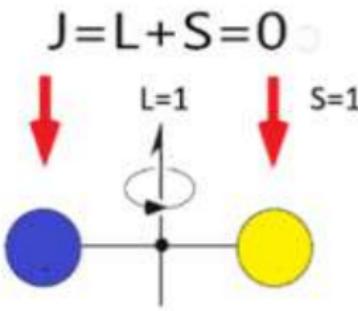
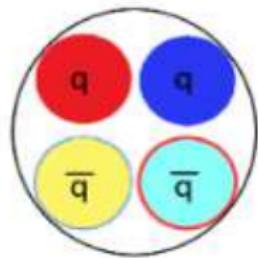
## 4.1 The low-mass scalar mesons



$$f_0(500) = \sin \theta \, f_0^8 + \cos \theta \, f_0^1$$

$$f_0(980) = \cos \theta \, f_0^8 - \sin \theta \, f_0^1$$

## Tetraquarks



The energy to excite  $q\bar{q}$  to  $L = 1$  is approximately equivalent to the creation of a new  $q\bar{q}$  pair.<sup>1</sup>

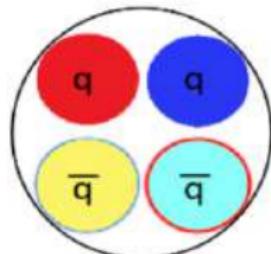
<sup>1</sup> R. L. Jaffe, "Multi-Quark Hadrons. 1. The Phenomenology of  $(2Q2\bar{Q})$  Mesons," Phys. Rev. D 15, 267 (1977).

Scalar mesons are ideally mixed

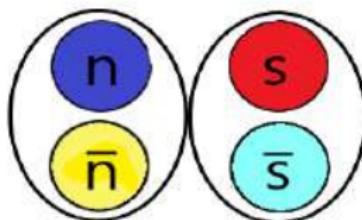
with  $f_0(500) = u\bar{u}d\bar{d}$  and

$$f_0(980) = \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d})s\bar{s}$$

# Dynamical generated scalar mesons<sup>1</sup>



Tetraquark



$K\bar{K}$  molecule



Nathan Isgur

<sup>1</sup> J. D. Weinstein and N. Isgur, “ $K\bar{K}$  Molecules,” Phys. Rev. D 41, 2236 (1990).

Scalar mesons are dynamically generated  
with  $f_0(500) = \pi\pi$  and  
 $f_0(980) = K\bar{K}$

# The $f_0(500) - f_0(980)$ mixing angle

$$g(f_0(500) \rightarrow \pi\pi) = -\frac{\sqrt{3}}{4} \cos \theta g_1 - \sqrt{\frac{3}{10}} \sin \theta g_8 ,$$

$$g(f_0(500) \rightarrow K\bar{K}) = -\frac{1}{2} \cos \theta g_1 + \frac{1}{\sqrt{10}} \sin \theta g_8 ,$$

$$g(f_0(500) \rightarrow \eta_8\eta_8) = \frac{1}{4} \cos \theta g_1 - \frac{1}{\sqrt{10}} \sin \theta g_8 ,$$

$$g(f_0(980) \rightarrow \pi\pi) = \frac{\sqrt{3}}{4} \sin \theta g_1 - \sqrt{\frac{3}{10}} \cos \theta g_8 ,$$

$$g(f_0(980) \rightarrow K\bar{K}) = \frac{1}{2} \sin \theta g_1 + \frac{1}{\sqrt{10}} \cos \theta g_8 ,$$

$$g(f_0(980) \rightarrow \eta_8\eta_8) = -\frac{1}{4} \sin \theta g_1 - \frac{1}{\sqrt{10}} \cos \theta g_8 .$$

$$\theta = (19 \pm 5)^\circ$$

J. A. Oller, "The Mixing angle of the lightest scalar nonet," Nucl. Phys.

A 727, 353-369 (2003).

$f_0(500) \approx$  singlet;

$f_0(980) \approx$  octet

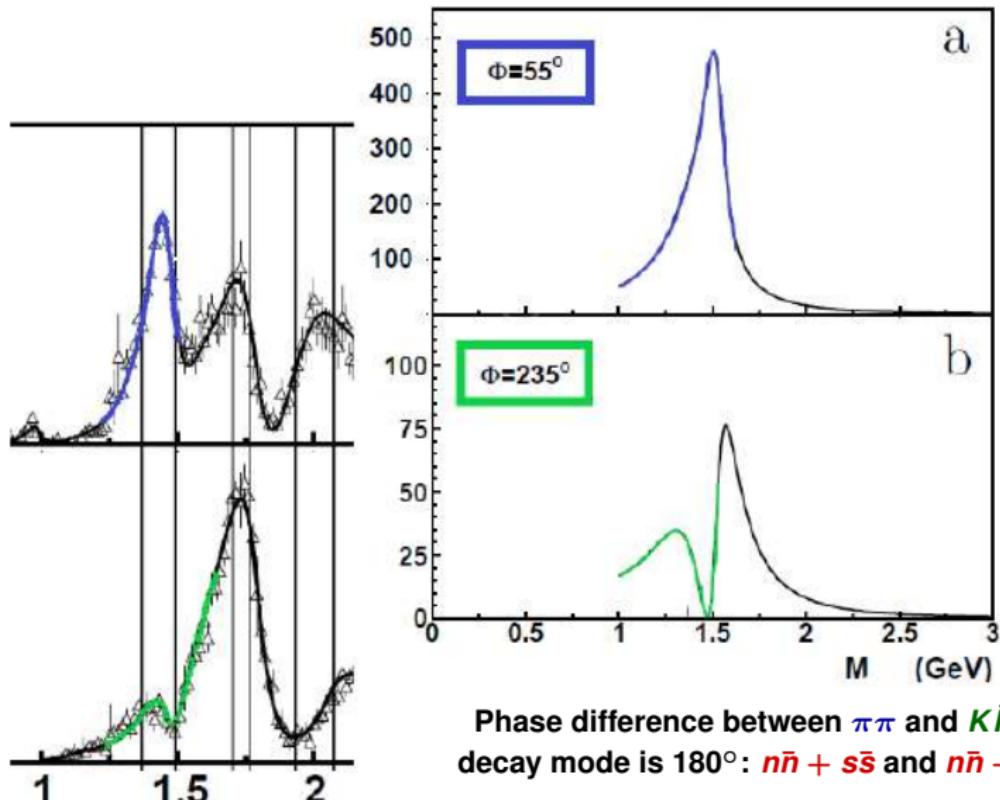
$$\theta = (14 \pm 4)^\circ$$

E. K., "Scalar mesons and the fragmented glueball",  
in preparation.

(19 ± 5)°	(39 ± 6)°	(17 ± 3)°	(1 <sup>+15</sup> <sub>-9</sub> )°	(12 ± 4)°	(32 ± 3)°
[1]	[2]	[3]	[4]	[5]	[6]
≈10°	(3 ± 8)°	(12 ± 3)°	(0 ± 5)°	(8 ± 2)°	
[7]	[8]	$D^+ \rightarrow \pi^+ \pi^+ \pi^-$	$D^0 \rightarrow \pi^0 \pi^+ \pi^-$	$J/\psi \rightarrow \gamma \pi \pi$	

- [1] J. A. Oller, Nucl. Phys. A 727, 353 (2003). [2] A. V. Anisovich *et al.*, Eur. Phys. J. A 12, 103 (2001). [3] W. Ochs, J. Phys. G 40, 043001 (2013).  
 [4] J. W. Li *et al.*, Eur. Phys. J. C 72, 2229 (2012). [5] R. Aaij *et al.* [LHCb], Phys. Rev. D 92, 032002 (2015). [6] R. Aaij *et al.* [LHCb], Phys. Rev. D 89, 092006 (2014). [7] X. Liu, Z. T. Zou, Y. Li and Z. J. Xiao, Phys. Rev. D 100, 013006 (2019). [8] N. R. Son *et al.*, Phys. Rev. D 102, 016013 (2020).

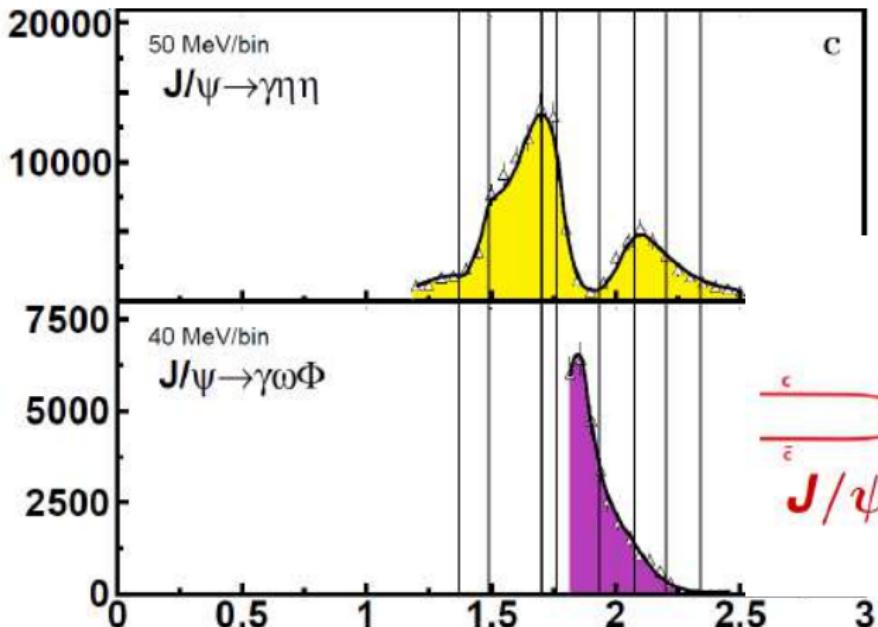
## 4.2 The $f_0(1370) - f_0(1500)$ mixing angle



Phase difference between  $\pi\pi$  and  $K\bar{K}$   
decay mode is  $180^\circ$ :  $n\bar{n} + s\bar{s}$  and  $n\bar{n} + s\bar{s}$  !

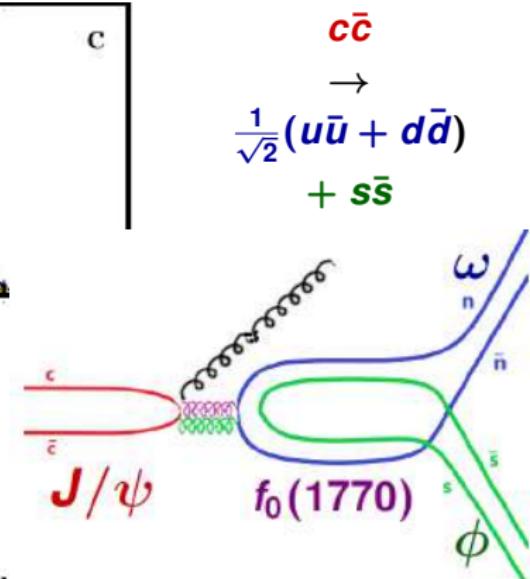
$f_0(1370)$  and  $f_0(1500)$  are SU(3) singlet and SU(3) octet-like  
and not  $n\bar{n}$  and  $s\bar{s}$  !

## 4.3 The $f_0(1770)$ wave function



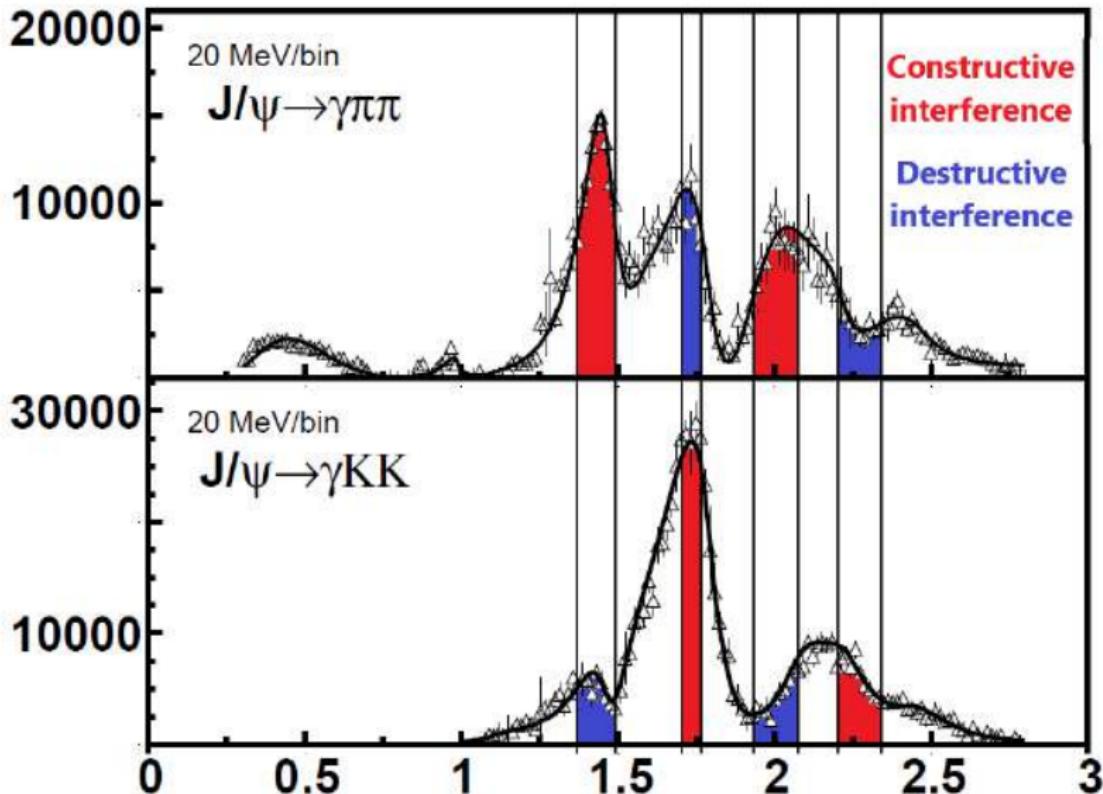
Doubly OZI rule violating and strong yield !

$f_0(1770) \rightarrow \omega\phi$  decay mode proceeds via the  $f_0(1770)$  SU(3) octet component

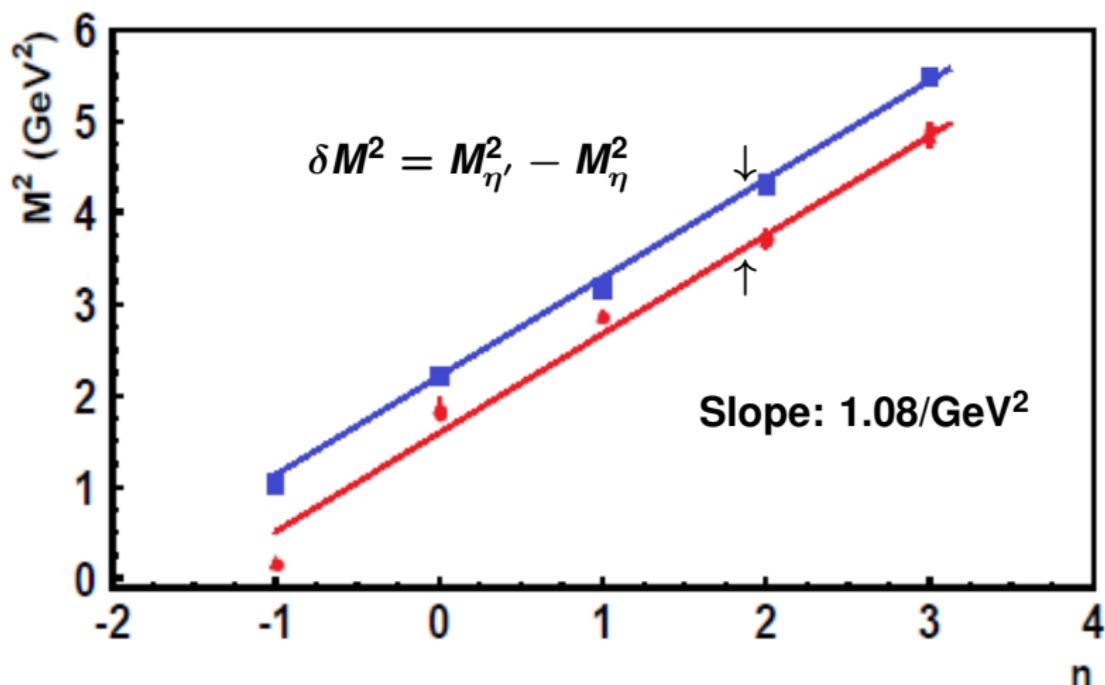


Tetraquark component in the  $f_0(1770)$  wave function !

## 4.4 Interference in $\pi\pi$ and $K\bar{K}$

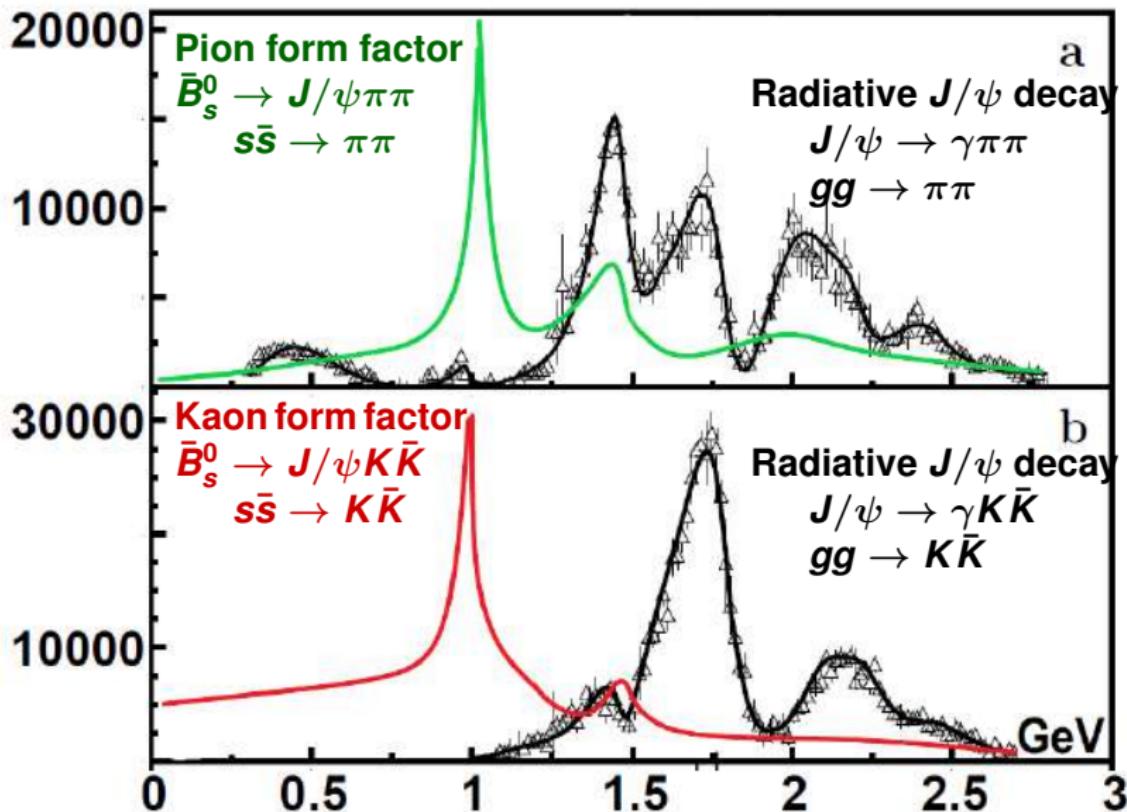


## 4.5 ( $M^2, n$ ) trajectories of scalar mesons



... and where is the scalar glueball ?

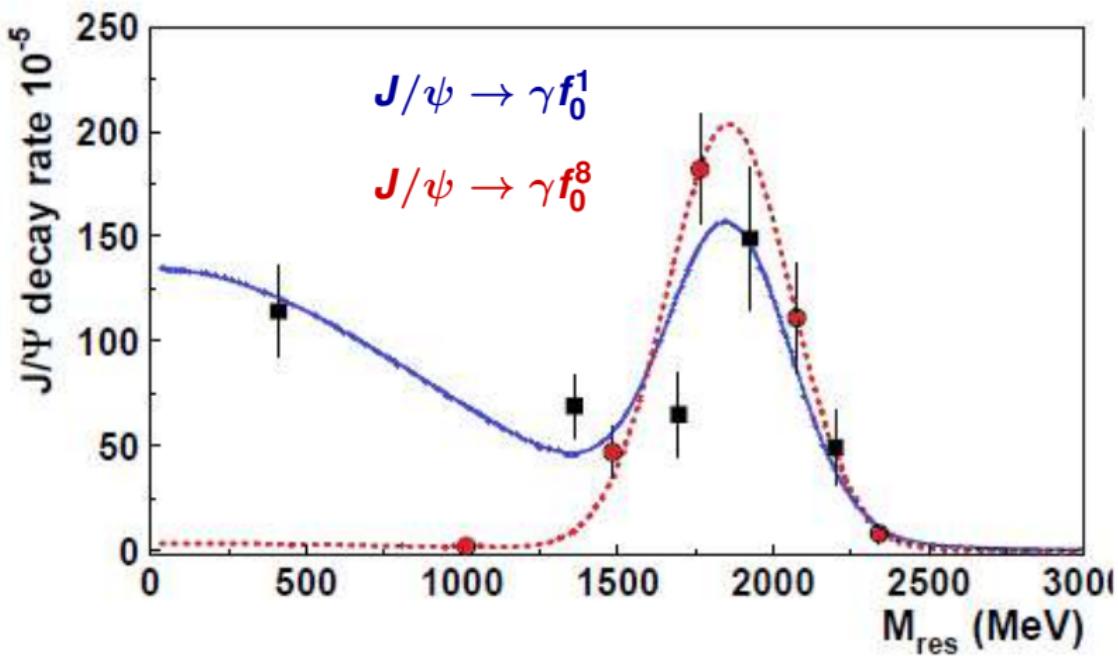
## 4.6 Evidence for strong glue-glue interactions



## 4.7 The fragmented glueball

Yields in radiative  $J/\psi$  decays (in units of  $10^{-5}$ )

$BR_{J/\psi \rightarrow \gamma f_0 \rightarrow}$	$\gamma\pi\pi$	$\gamma K\bar{K}$	$\gamma\eta\eta$	$\gamma\eta\eta'$	$\gamma\omega\phi$	missing $\gamma 4\pi$	$\gamma\omega\omega$	total
$f_0(500)$	$105 \pm 20$	$5 \pm 5$	$4 \pm 3$	$\sim 0$	$\sim 0$	$\sim 0$	$\sim 0$	$114 \pm 21$
$f_0(980)$	$1.3 \pm 0.2$	$0.8 \pm 0.3$	$\sim 0$	$\sim 0$	$\sim 0$	$\sim 0$	$\sim 0$	$2.1 \pm 0.4$
$f_0(1370)$	$38 \pm 10$	$13 \pm 4$ $42 \pm 15$	$3.5 \pm 1$	$0.9 \pm 0.3$	$\sim 0$	$14 \pm 5$ $27 \pm 9$	$69 \pm 12$	
$f_0(1500)$	$9.0 \pm 1.7$ $10.9 \pm 2.4$	$3 \pm 1$ $2.9 \pm 1.2$	$1.1 \pm 0.4$ $1.7^{+0.6}_{-1.4}$	$1.2 \pm 0.5$ $6.4^{+1.0}_{-2.2}$	$\sim 0$	$33 \pm 8$ $36 \pm 9$	$47 \pm 9$	
$f_0(1710)$	$6 \pm 2$	$23 \pm 8$	$12 \pm 4$	$6.5 \pm 2.5$	$1 \pm 1$	$7 \pm 3$	$56 \pm 10$	
$f_0(1770)$	$24 \pm 8$	$60 \pm 20$	$7 \pm 1$	$2.5 \pm 1.1$	$22 \pm 4$	$65 \pm 15$	$181 \pm 26$	
$f_0(1750)$	$38 \pm 5$	$99^{+10}_{-6}$	$24^{+12}_{-7}$		$25 \pm 6$	$97 \pm 18$	$31 \pm 10$	
$f_0(2020)$	$42 \pm 10$	$55 \pm 25$	$10 \pm 10$			$(38 \pm 13)$		$145 \pm 32$
$f_0(2100)$	$20 \pm 8$	$32 \pm 20$	$18 \pm 15$			$(38 \pm 13)$		$108 \pm 25$
$f_0(2200)$	$5 \pm 2$	$5 \pm 5$	$0.7 \pm 0.4$			$(38 \pm 13)$		$49 \pm 17$
$f_0(2100)/f_0(2200)$	$62 \pm 10$	$109^{+8}_{-19}$	$11.0^{+6.5}_{-3.0}$			$115 \pm 41$		
$f_0(2330)$	$4 \pm 2$	$2.5 \pm 0.5$ $20 \pm 3$	$1.5 \pm 0.4$					$8 \pm 3$



$$M_{\text{glueball}} = (1865 \pm 25) \text{ MeV}, \Gamma_{\text{glueball}} = (370 \pm 50^{+30}_{-20}) \text{ MeV}$$

$$Y_{J/\psi \rightarrow \gamma G_0} = (5.8 \pm 1.0) \cdot 10^{-3}$$

## 4.8 The wave function of scalar mesons

$$\begin{aligned}f_0(1500) &= \alpha \frac{1}{\sqrt{6}} (u\bar{u} + d\bar{d} - 2s\bar{s}) \\&+ \beta \frac{1}{\sqrt{6}} (u\bar{u}s\bar{s} + d\bar{d}s\bar{s} - 2u\bar{u}d\bar{d}) \\&+ \gamma \cdot (\text{meson} - \text{meson cloud}) \\&+ \delta(gg) \\&+ \epsilon(q\bar{q}g) \\&+ \dots \quad \text{and some singlet contribution} \\&+ \{\alpha' \frac{1}{\sqrt{3}} (u\bar{u} + d\bar{d} + s\bar{s}) + \beta' \frac{1}{\sqrt{3}} (u\bar{u}s\bar{s} + d\bar{d}s\bar{s} + u\bar{u}d\bar{d})\}\end{aligned}$$

The five Fock states are not realized independently as five mesons !

They are components of the mesonic wave functions.

There is no scalar glueball that intrudes the spectrum of scalar mesons

## 5. Summary

- ▶ The BESIII collaboration reported data on radiative  $J/\psi$  decays with unprecedented statistics
- ▶ The data reveal high intensities in the yield of scalar mesons
- ▶ The data can be fit with ten scalar isoscalar resonances.
- ▶ The scalar resonances can be grouped into a class of mainly-singlet and mainly-octet states
- ▶ The two groups fall onto linear  $(n, M^2)$ -trajectories
- ▶ Octet scalar isoscalar resonances are produced mainly in the 1700 - 2100 MeV mass range
- ▶ Singlet scalar resonances are produced over the full mass range. Their intensity peaks in the 1700 - 2100 MeV mass range
- ▶ The enhanced production of scalar mesons in the 1700 - 2100 MeV mass range is due to gluon-gluon in the initial state
- ▶ The peak is the scalar glueball of lowest mass.

Thank you for your patience!

## The scalar mixing angle

