

Majoron Potential by Majorana fermion Loops

We present a diagrammatic framework for radiative Majoron potentials induced by an explicit Majorana mass M . Classifying one-loop diagrams by the number of fermion-number-violating (N_{FNV}) and fermion-number-preserving (N_{FNP}) propagators yields a heavy-mass scaling rule: pure FNV amplitudes behave as M^{4-n} , while mixed diagrams receive additional suppression from momentum numerators. After removing the dominant tadpole by a matching condition, the bubble diagram provides the leading Majoron mass $\propto y^2 M^2$. The mixed FNV/FNP triangle supplies the complete next-to-leading $\mathcal{O}(yv/M)$ correction through a $\cos \theta$ harmonic after vacuum alignment. We analyze the one-loop Coleman-Weinberg potential for the full two-field space $V_{\text{eff}}(r, \theta)$, derive the quantum-shifted vacuum and scalar Hessian, and identify the parameter conditions required for local stability. The heavy Majorana fermion decouples from irrelevant operators but leaves non-decoupling threshold corrections to relevant symmetry-breaking operators. At finite temperature, the explicit breaking spurion M induces a thermal tadpole $\propto MT^2 r \cos \theta$. This term prevents the origin from ever being a stationary point, ensuring that the radial vacuum expectation value remains non-zero at all temperatures. Consequently, the system undergoes a smooth crossover rather than a true symmetry-restoring phase transition, and the pseudo-Goldstone description remains rigorously valid across all temperature regimes. The resulting effective potential is a periodic non-linear sigma model whose Wilson coefficients follow a two-parameter lattice classification.

Primary author(s) : Mr KHAN, Mussawir (State Key Laboratory of Particle Astrophysics, Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China)

Presenter(s) : Mr KHAN, Mussawir (State Key Laboratory of Particle Astrophysics, Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China)