

Possible studies on high-energy hadron physics at future HIAF

Shunzo Kumano (熊野 Kumano 俊三 Shunzo)

Institute of Modern Physics,
Chinese Academy of Sciences

Institute of Particle and Nuclear Studies, KEK

惠州强子谱仪HHaS合作组2025年年会

(Annual meeting of

the Huizhou Hadron Spectrometer HHaS Collaboration in 2025)

IMP, Huizhou, China, November 28-30, 2025

<https://indico.itp.ac.cn/event/375/timetable/#all.detailed>

HIAF: 9.3 GeV

→ 25 GeV

→ even higher ???

November 30, 2025

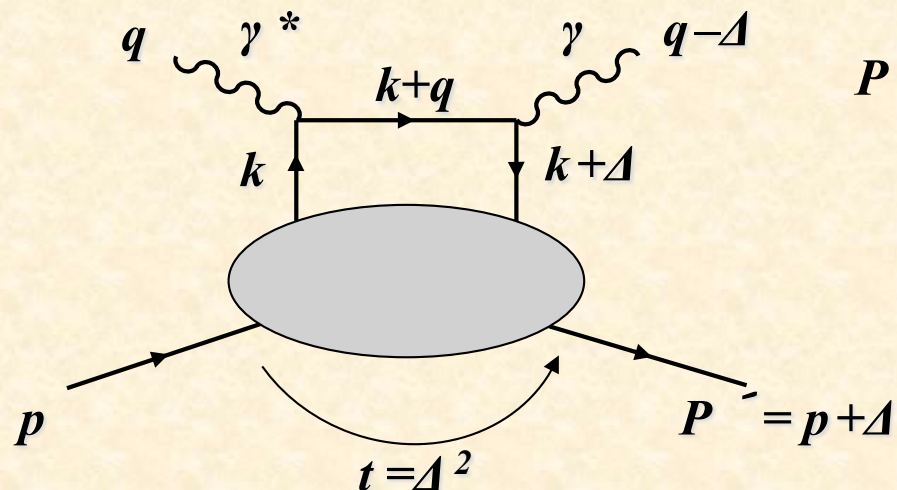
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may skip

Motivations for studying high-energy hadron physics at HIAF

Generalized Parton Distributions (GPDs)



$$P = \frac{p + p'}{2}, \quad \Delta = p' - p$$

Bjorken variable $x = \frac{Q^2}{2p \cdot q}$

Momentum transfer squared $t = \Delta^2$

Skewness parameter $\xi = \frac{p^+ - p'^+}{p^+ + p'^+} = -\frac{\Delta^+}{2P^+}$

GPDs are defined as correlation of off-forward matrix:

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p' | \bar{\psi}(-z/2) \gamma^+ \psi(z/2) | p \rangle \Big|_{z^+=0, \vec{z}_\perp=0} = \frac{1}{2P^+} \left[H(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E(x, \xi, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u(p) \right]$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p' | \bar{\psi}(-z/2) \gamma^+ \gamma_5 \psi(z/2) | p \rangle \Big|_{z^+=0, \vec{z}_\perp=0} = \frac{1}{2P^+} \left[\tilde{H}(x, \xi, t) \bar{u}(p') \gamma^+ \gamma_5 u(p) + \tilde{E}(x, \xi, t) \bar{u}(p') \frac{\gamma_5 \Delta^+}{2M} u(p) \right]$$

Forward limit: PDFs $H(x, \xi, t) \Big|_{\xi=t=0} = f(x), \quad \tilde{H}(x, \xi, t) \Big|_{\xi=t=0} = \Delta f(x),$

First moments: Form factors

Dirac and Pauli form factors F_1, F_2

$$\int_{-1}^1 dx H(x, \xi, t) = F_1(t), \quad \int_{-1}^1 dx E(x, \xi, t) = F_2(t)$$

Axial and Pseudoscalar form factors G_A, G_P

$$\int_{-1}^1 dx \tilde{H}(x, \xi, t) = g_A(t), \quad \int_{-1}^1 dx \tilde{E}(x, \xi, t) = g_P(t)$$

Second moments: Angular momenta

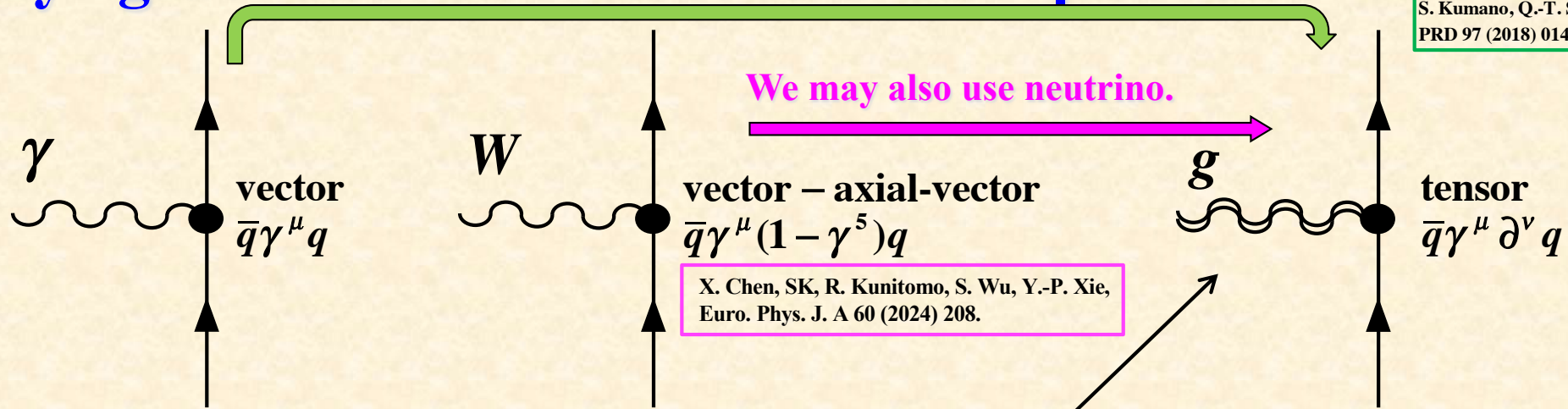
Sum rule: $J_q = \frac{1}{2} \int_{-1}^1 dx x [H_q(x, \xi, t=0) + E_q(x, \xi, t=0)], \quad J_q = \frac{1}{2} \Delta q + L_q$

$\Rightarrow$ probe L_q , key quantity to solve the spin puzzle!

Why “gravitational” interactions with quarks

We studied in 2017-2018.

S. Kumano, Q.-T. Song, O. Teryaev,
PRD 97 (2018) 014020.



X. Chen, SK, R. Kunitomo, S. Wu, Y.-P. Xie,
Euro. Phys. J. A 60 (2024) 208.

GPDs (Generalized Parton Distributions), GDAs (Generalized Distribution Amplitudes) = timelike GPDs

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-z/2) \gamma^+ q(z/2) | p \rangle \Big|_{z^+=0, \vec{z}_\perp=0} = \frac{1}{2P^+} \left[H(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E(x, \xi, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2M} u(p) \right]$$

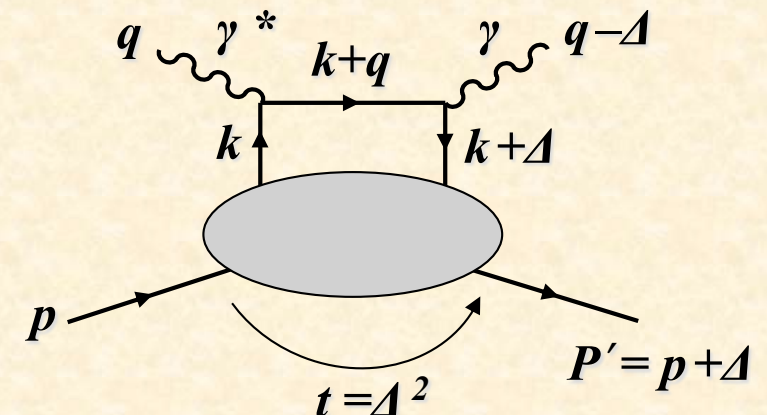
Non-local operator of GPDs/GDAs:

$$\begin{aligned} & (P^+)^n \int dx x^{n-1} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \left[\bar{q}(-z/2) \gamma^+ q(z/2) \right] \Big|_{z^+=0, \vec{z}_\perp=0} \\ &= \left(i \frac{\partial}{\partial z^-} \right)^{n-1} \left[\bar{q}(-z/2) \gamma^+ q(z/2) \right] \Big|_{z=0} \\ &= \bar{q}(0) \gamma^+ \left(i \tilde{\partial}^+ \right)^{n-1} q(0) \end{aligned}$$

= energy-momentum tensor of a quark for $n = 2$
(electromagnetic for $n = 1$)

= source of gravity

Virtual Compton
or (timelike) two-photon process

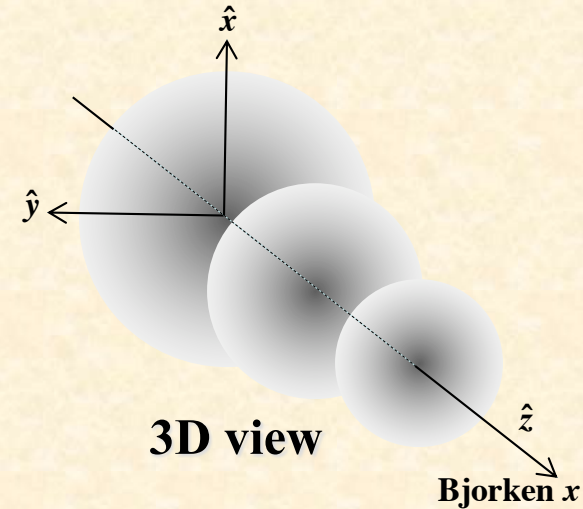


Proton (hadrons) puzzle studies by the GPDs

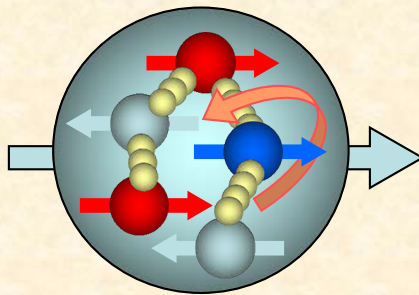
Hadron tomography



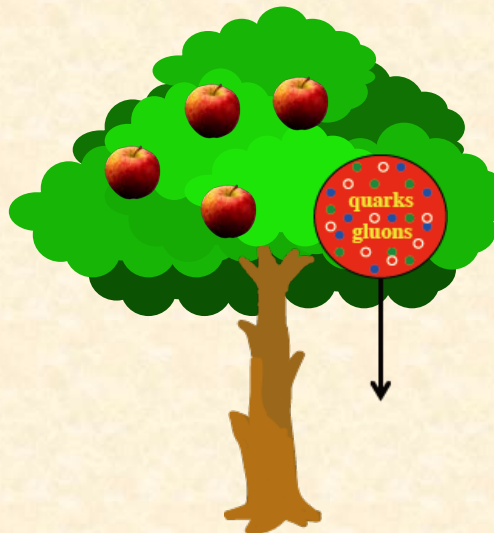
Proton radius puzzle



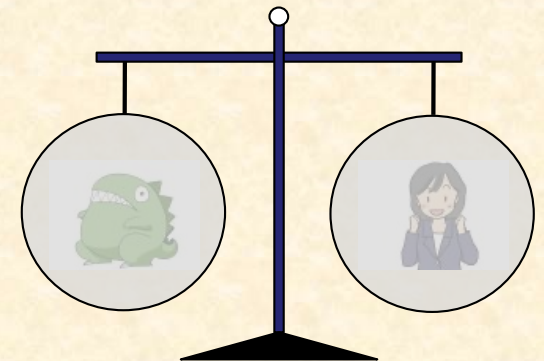
Origin of nucleon spin



Source of gravity (mass)

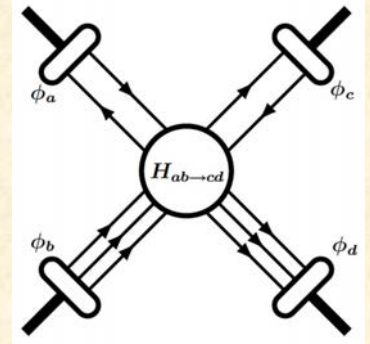


Exotic hadrons



Constituent-counting rule in perturbative QCD:

Hard exclusive processes $a + b \rightarrow c + d$



Consider the hard exclusive hadron reaction $a + b \rightarrow c + d$

$$M_{ab \rightarrow cd} = \int d[x_a] d[x_b] d[x_c] d[x_d] \phi_c([x_c]) \phi_d([x_d]) H_M([x_a], [x_b], [x_c], [x_d], Q^2) \phi_a([x_a]) \phi_b([x_b])$$

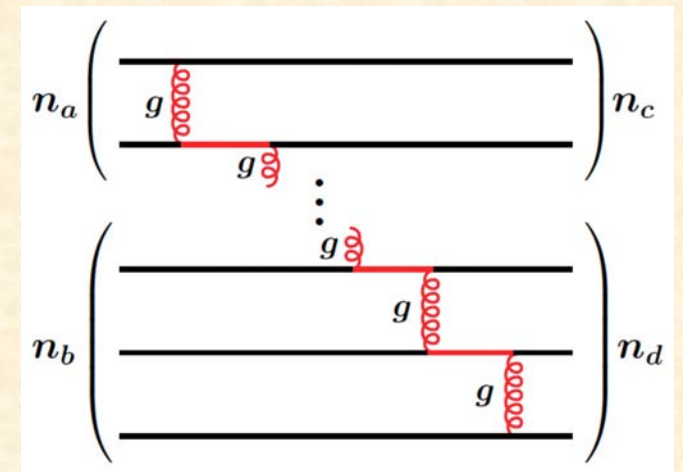
ϕ_p = proton distribution amplitude, H_M = hard amplitude (calculated in pQCD)

Rule for estimating $M_{ab \rightarrow cd}$

- (1) Feynman diagram: Draw leading and connected Feynman diagram by connecting $n / 2$ quark lines by gluons.
- (2) Gluon propagators: The factor $1/P^2$ is assigned for each gluon propagator.
There are $n / 2 - 1$ gluon propagators $\sim 1/(P^2)^{n/2-1}$.
- (3) Quark propagators: The factor $1/P$ is assigned for each quark propagator.
There are $n / 2 - 2$ gluon propagators $\sim 1/(P)^{n/2-2}$.
- (4) External quarks: The factor $\sqrt{P}$ is assigned for each external quark.

There are n gluon propagators $\sim (\sqrt{P})^n$.

$$n = n_a + n_b + n_c + n_d$$



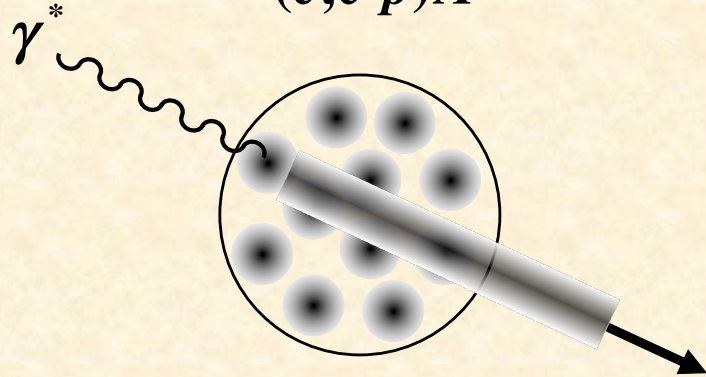
$$M_{ab \rightarrow cd} \sim \frac{1}{(P^2)^{n/2-1}} \frac{1}{(P)^{n/2-2}} (\sqrt{P})^n = \frac{(P)^{n/2}}{(P)^{n-2} (P)^{n/2-2}} = \frac{1}{(P)^{n-4}} \sim \frac{1}{s^{n/2-2}}$$

Cross section: $\frac{d\sigma_{ab \rightarrow cd}}{dt} \simeq \frac{1}{16\pi^2} \sum_{\text{spol}} |M_{ab \rightarrow cd}|^2 \sim \frac{1}{s^{n-2}}$

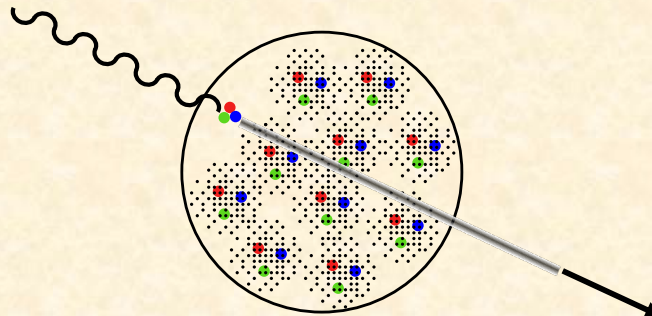
It is interesting to use this for exotic-hadron candidates.

Color transparency and hadronization

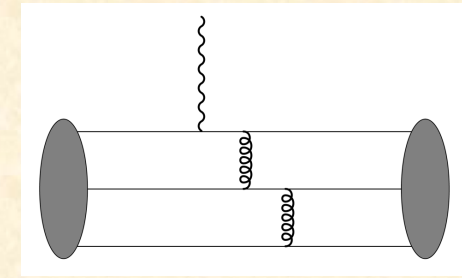
$(e, e'p)A$



Interact strongly
in the nuclear medium



No interaction
in the nuclear medium



Hard gluon exchanges at high energies

- quarks are close with each other
- struck nucleon should be compact
- nucleon could pass through the medium without interaction (color transparency)



Low energies:
Hadron degrees
of freedom



High energies:
Quark-gluon
degrees of freedom

At large momentum transfer,
a small-size hadron could freely pass
through nuclear medium. (**Transparent**)

$$T = \frac{\sigma_A}{A\sigma_N}$$

1

Nuclear transparency: $T = \frac{\sigma_A}{A\sigma_N}$

color transparency

Momentum scale

The color transparency is an important phenomena to understand the quark-hadron many-body systems from low to high energies and from low to high densities.

Possible studies on GPDs at hadron accelerator facilities

**SK, M. Strikman, K. Sudoh,
PRD 80 (2009) 074003;**

**T. Sawada, W.-C. Chang, SK, J.-C. Peng, S. Sawada, and K. Tanaka,
PRD 93 (2016) 114034.**

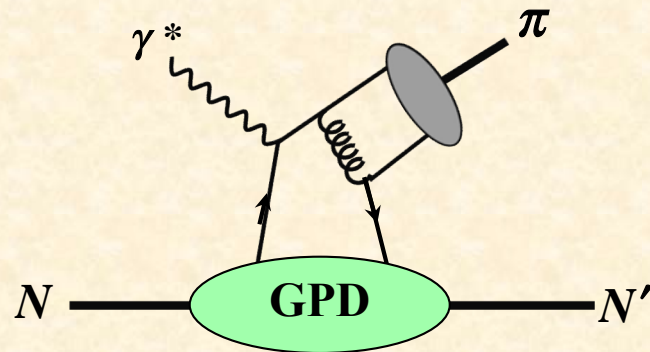
J-PARC LoI 2019-07, J.-K. Ahn *et al.* (2019).

J-PARC proposal under preparation,

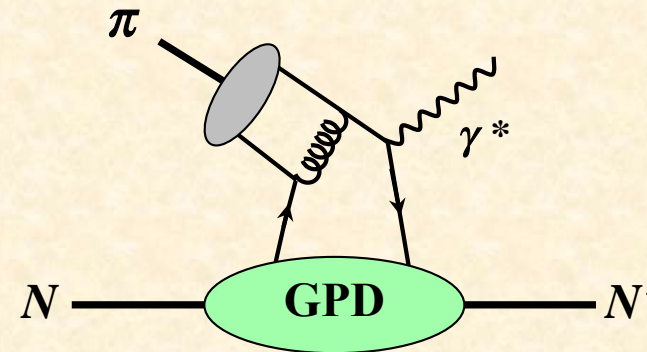
**Please get in touch with W.-C. Chang, N. Tomida
if you are interested in this project.**

GPD projects at Jlab/EicC/EIC and HIAF/J-PARC

JLab / EicC / EIC

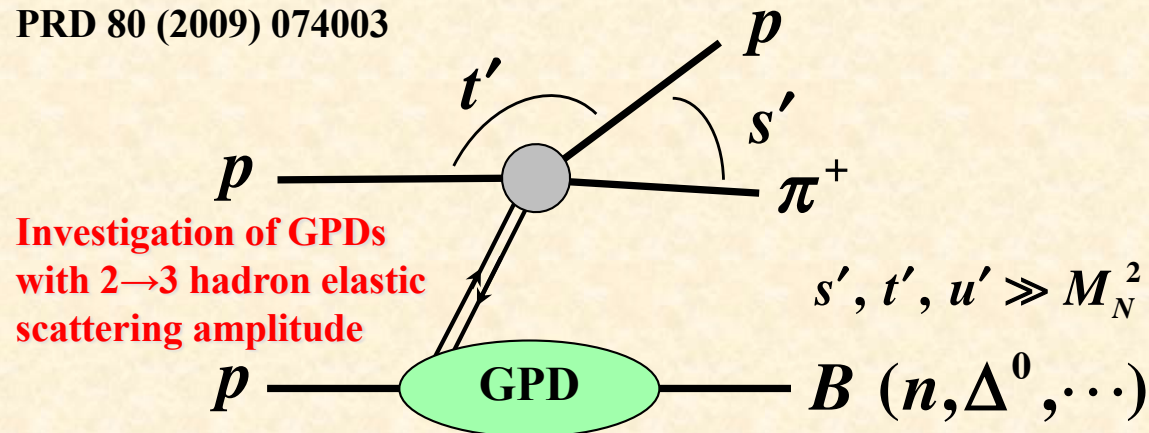


HIAF / J-PARC



$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p' | \bar{\psi}(-z/2) \gamma^+ \gamma_5 \psi(z/2) | p \rangle \Big|_{z^+=0, \vec{z}_\perp=0} = \frac{1}{2P^+} \left[\tilde{H}(x, \xi, t) \bar{u}(p') \gamma^+ \gamma_5 u(p) + \tilde{E}(x, \xi, t) \bar{u}(p') \frac{\gamma_5 \Delta^+}{2M} u(p) \right]$$

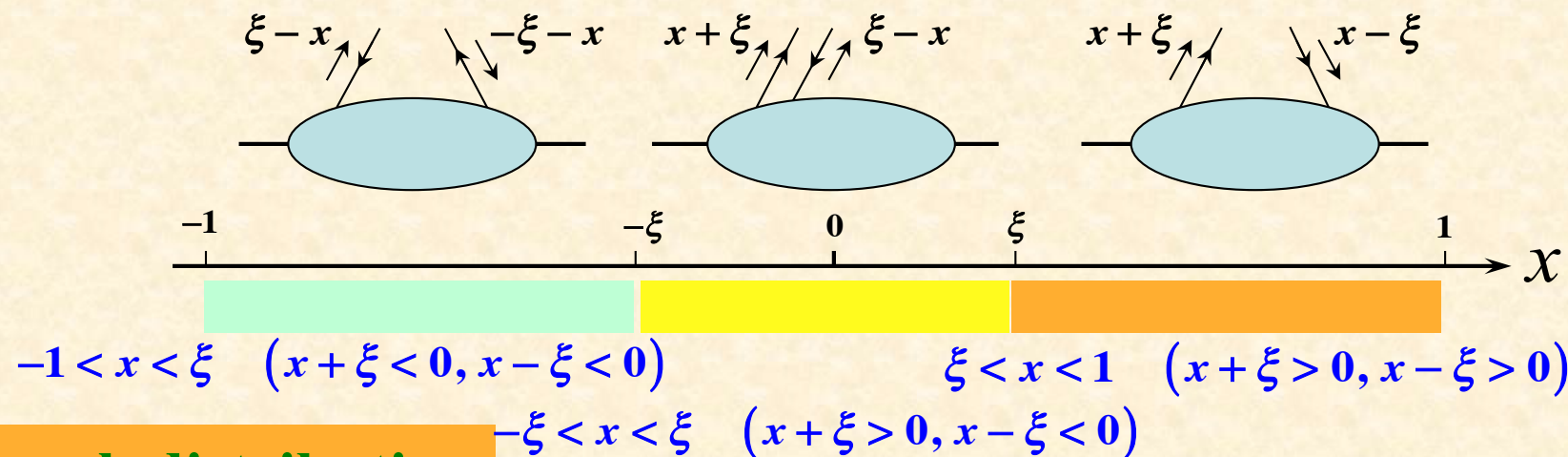
SK, M. Strikman, K. Sudoh,
PRD 80 (2009) 074003



J-W. Qiu and Z. Yu,
JHEP 08 (2022) 103;
PRD 107 (2023) 014007.

$$\begin{aligned} \pi + N &\rightarrow \gamma + \gamma + N' \\ h + M_B &\rightarrow h' + \gamma + M_D \\ h + M_B &\rightarrow h' + M_C + M_D \end{aligned}$$

GPDs in different x regions and GPDs at hadron facilities



Quark distribution

Emission of quark with momentum fraction $x+\xi$
 Absorption of quark with momentum fraction $x-\xi$

$q\bar{q}$ (meson)-like distribution amplitude

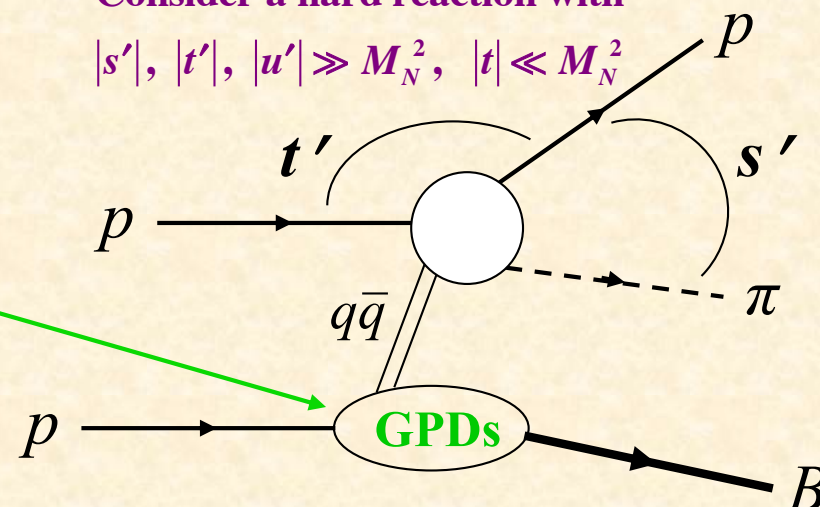
Emission of quark with momentum fraction $x+\xi$
 Emission of antiquark with momentum fraction $\xi-x$

Antiquark distribution

Emission of antiquark with momentum fraction $\xi-x$
 Absorption of antiquark with momentum fraction $-\xi-x$

Consider a hard reaction with

$$|s'|, |t'|, |u'| \gg M_N^2, \quad |t| \ll M_N^2$$



Efremov-Radyushkin
 -Brodsky-Lepage (ERBL) region

Cross section estimate (ξ dependence)

Skewness parameter: $\xi = \frac{p_N^+ - p_B^+}{p_N^+ + p_B^+}$

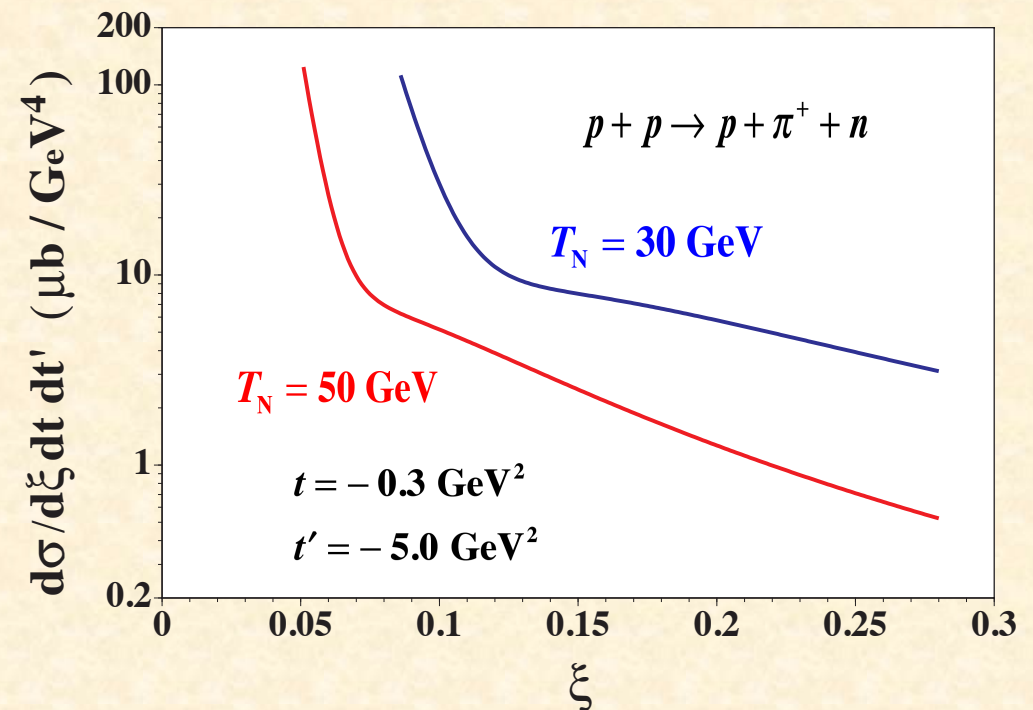
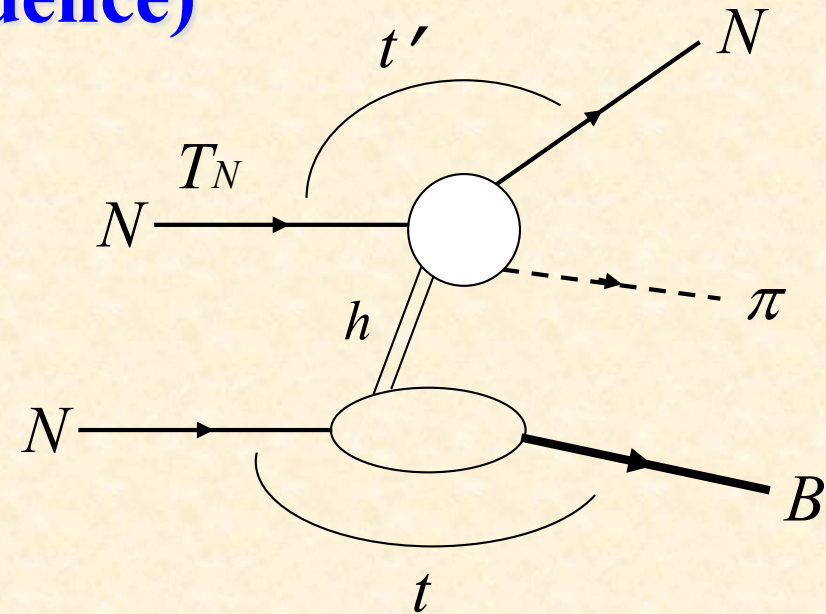
$\frac{d\sigma}{d\xi dt dt'} \left(\frac{\mu\text{b}}{\text{GeV}^2} \right)$ as a function of ξ

at fixed $T_N = 30$ (50) GeV,

$t = -0.3 \text{ GeV}^2$, $t' = -5 \text{ GeV}^2$.

At this stage, our numerical results are for rough order of magnitude estimates on cross sections by assuming π - and ρ -like intermediate states.

For the details, please look at our PRD paper in 2009.



Exclusive Drell-Yan $\pi^- + p \rightarrow \mu^+ \mu^- + n$ and GPDs

$$\frac{d\sigma_L}{dQ'^2 dt} = \frac{4\pi\alpha^2}{27} \frac{\tau^2}{Q'^2} f_\pi^2 \left[(1 - \xi^2) |\tilde{H}^{du}(-\xi, \xi, t)|^2 - 2\xi^2 \text{Re}\{\tilde{H}^{du}(-\xi, \xi, t)^* \tilde{E}^{du}(-\xi, \xi, t)\} - \xi^2 \frac{t}{4m_N^2} |\tilde{E}^{du}(-\xi, \xi, t)|^2 \right]$$

$$Q'^2 = q'^2, \quad t = (p - p')^2, \quad \tau = \frac{Q'^2}{2p \cdot q_\pi} \approx \frac{Q'^2}{s - m_\pi^2}$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p(p') | \bar{q}(-z/2) \gamma^+ \gamma_5 q(z/2) | p(p) \rangle_{z^+=0, \vec{z}_\perp=0} = \frac{1}{2P^+} \left[\tilde{H}_p^q(x, \xi, t) \bar{u}(p') \gamma^+ \gamma_5 u(p) + \tilde{E}_p^q(x, \xi, t) \bar{u}(p') \frac{\gamma_5 \Delta^+}{2M} u(p) \right]$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle n(p') | \bar{q}_d(-z/2) \gamma^+ \gamma_5 q_u(z/2) | p(p) \rangle_{z^+=0, \vec{z}_\perp=0} = \frac{1}{2P^+} \left[\tilde{H}_{p \rightarrow n}^{du}(x, \xi, t) \bar{u}(p') \gamma^+ \gamma_5 u(p) + \tilde{E}_{p \rightarrow n}^{du}(x, \xi, t) \bar{u}(p') \frac{\gamma_5 \Delta^+}{2M} u(p) \right]$$

$$\tilde{H}^{du}(x, \xi, t) = \frac{8}{3} \alpha_s \int_{-1}^1 dz \frac{\phi_\pi(z)}{1-z^2} \int_{-1}^1 dx' \left[\frac{e_d}{x-x'-i\epsilon} - \frac{e_u}{x+x'-i\epsilon} \right] [\tilde{H}^d(x', \xi, t) - \tilde{H}^u(x', \xi, t)]$$

$$\tilde{E}^{du}(x, \xi, t) = \frac{8}{3} \alpha_s \int_{-1}^1 dz \frac{\phi_\pi(z)}{1-z^2} \int_{-1}^1 dx' \left[\frac{e_d}{x-x'-i\epsilon} - \frac{e_u}{x+x'-i\epsilon} \right] [\tilde{E}^d(x', \xi, t) - \tilde{E}^u(x', \xi, t)]$$

**T. Sawada, W.-C. Chang, SK, J.-C. Peng,
S. Sawada, and K. Tanaka, PRD93 (2016) 114034.**

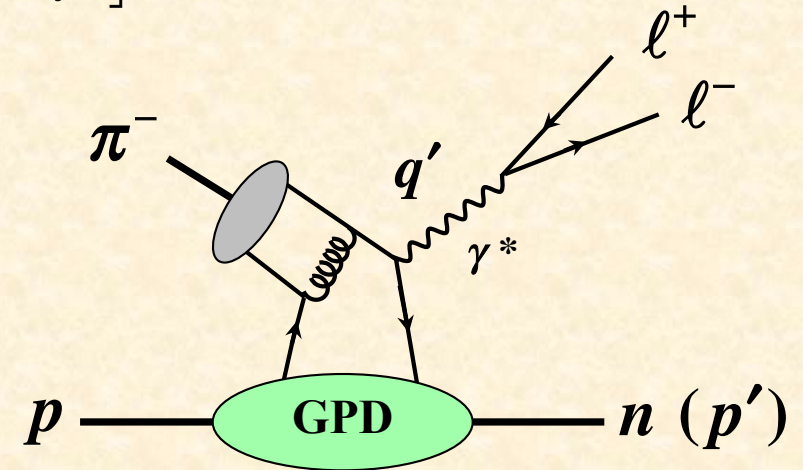
LETTER OF INTENT

Studying Generalized Parton Distributions with Exclusive Drell-Yan process

at J-PARC

JungKeun Ahn,¹ Sakiko Ashikaga,² Wen-Chen Chang,^{3,*} Seonho Choi,⁴ Stefan Diehl,⁵ Yuji Goto,⁶ Kenneth Hicks,⁷ Youichi Igarashi,⁸ Kyungseon Joo,⁵ Shunzo Kumano,^{9,10} Yue Ma,⁶ Kei Nagai,³ Kenichi Nakano,¹¹ Masayuki Niiyama,¹² Hiroyuki Nomi,^{13,8,†} Hiroaki Ohnishi,¹⁴ Jen-Chieh Peng,¹⁵ Hiroyuki Sako,¹⁶ Shin'ya Sawada,^{8,‡} Takahiro Sawada,¹⁷ Kotaro Shirotori,¹³ Kazuhiro Tanaka,^{18,10} and Natsuki Tomida¹³

LoI for a J-PARC experiment

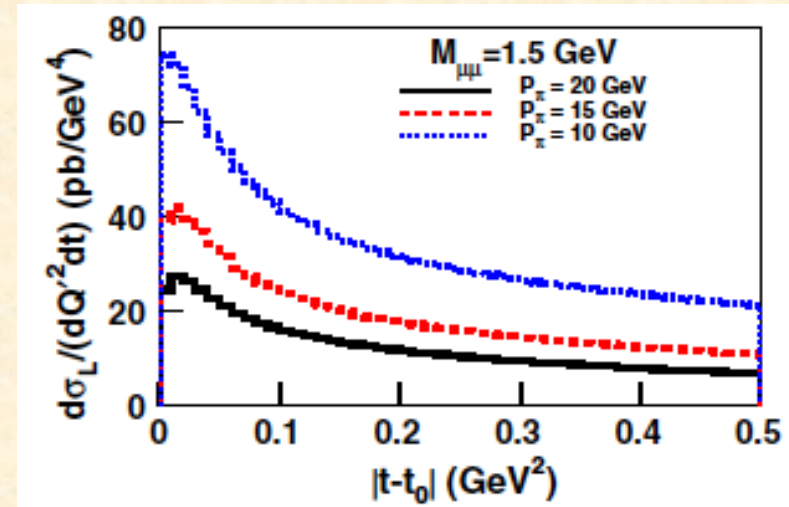
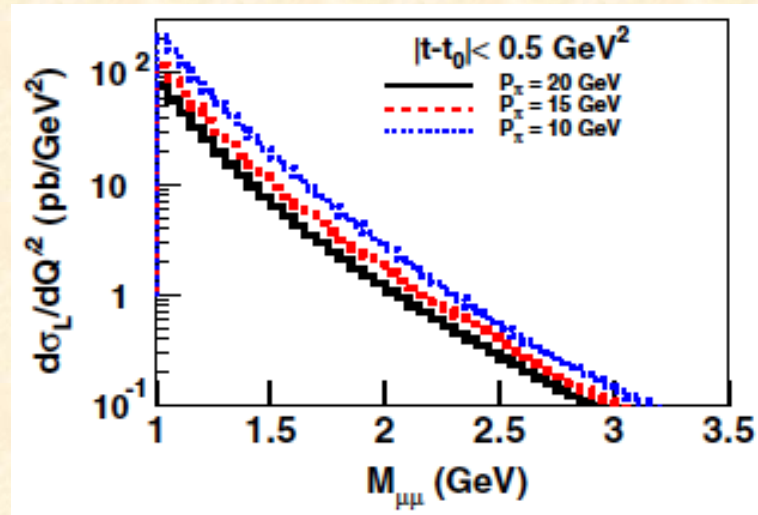


$$\pi^- (\bar{u}d) + p(uud) \rightarrow n(udd) + \gamma^* (\rightarrow \ell^+ \ell^-)$$

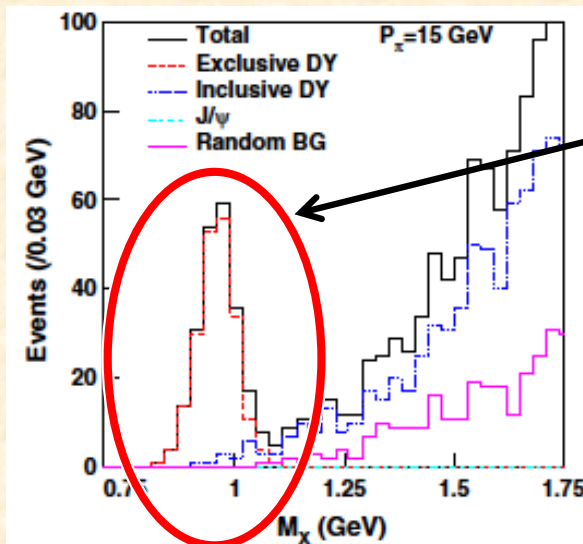
Expected Drell-Yan events at J-PARC

$$Q'^2 = q'^2, \quad t = (p - p')^2, \quad \tau = \frac{Q'^2}{2p \cdot q_\pi} \approx \frac{Q'^2}{s - m_N^2}$$

$$\frac{d\sigma_L}{dQ'^2 dt} = \frac{4\pi\alpha^2}{27} \frac{\tau^2}{Q'^2} f_\pi^2 \left[(1 - \xi^2) |\tilde{H}^{du}(-\xi, \xi, t)|^2 - 2\xi^2 \text{Re}\{\tilde{H}^{du}(-\xi, \xi, t)^* \tilde{E}^{du}(-\xi, \xi, t)\} - \xi^2 \frac{t}{4m_N^2} |\tilde{E}^{du}(-\xi, \xi, t)|^2 \right]$$



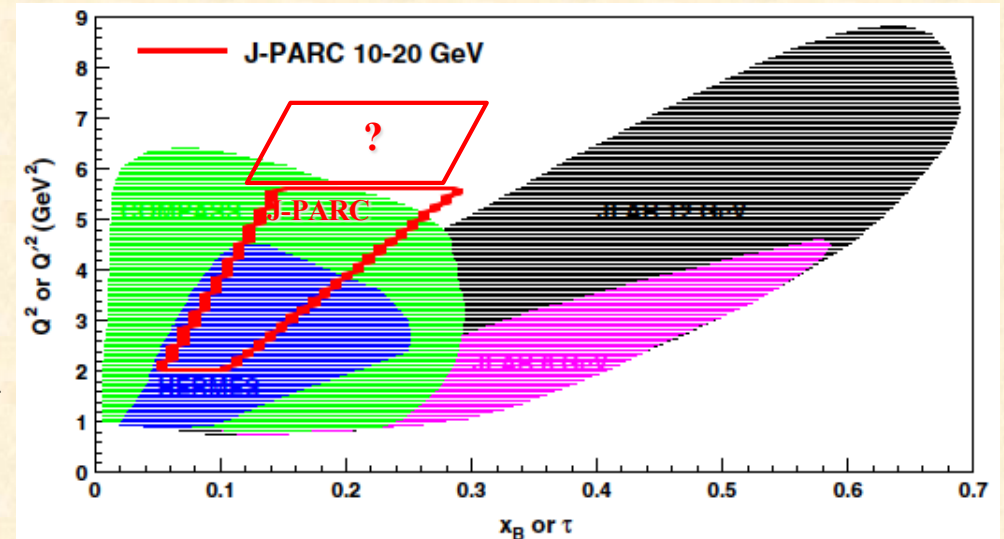
Missing mass



Exclusive
Drell-Yan

$$M_X^2 = (q + p - q')^2$$

$$q = p_\pi, \quad p = p_p, \quad q = p_{\mu^+\mu^-}$$



GPDs for exotic hadrons

**(If transition GPDs could be studied,
this exotic-hadron project becomes more realistic.)**

**H. Kawamura and SK,
Phys. Rev. D 89 (2014) 054007.**

**Recent study on $Z_c(3900)$,
C. Han, X. Wang, W. Kou, X. Chen,
Eur. Phys. J. C 84 (2024) 1067.**

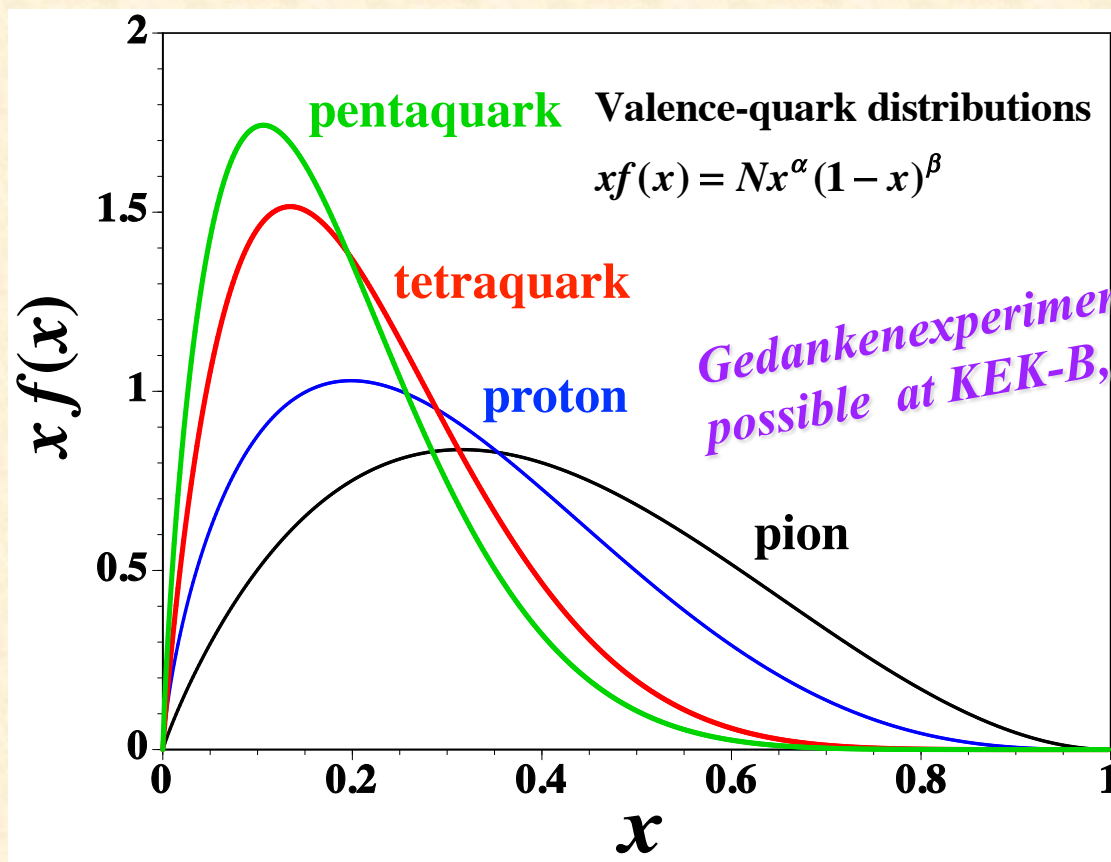
Simple function of GPDs

$$H_q^h(x, t) = f(x)F(t, x)$$

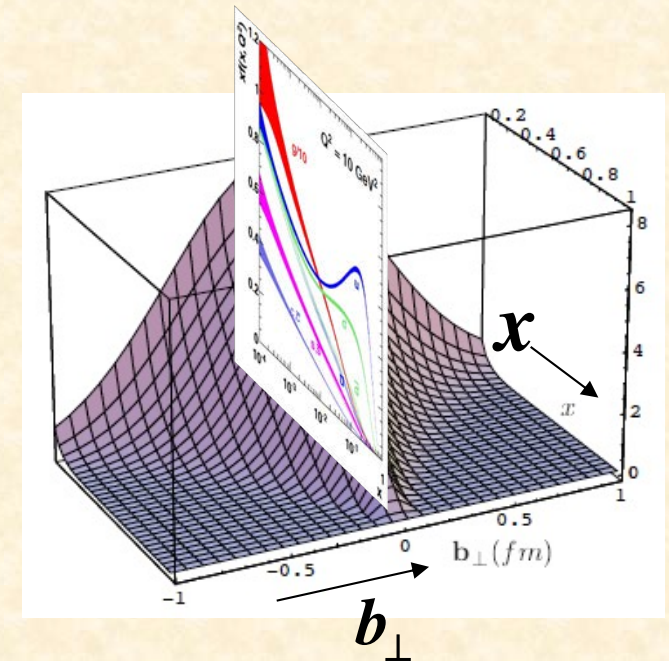
M. Guidal, M.V. Polyakov,
A.V. Radyushkin, M. Vanderhaeghen,
PRD 72, 054013 (2005).

Longitudinal-momentum distribution (PDF) for valence quarks: $f(x) = q_v(x) = c_n x^{\alpha_n} (1-x)^{\beta_n}$

- Valence-quark number sum rule (charge and baryon numbers): $\int_0^1 dx f(x) = n$
- Constituent counting rule at $x \rightarrow 1$: $\beta_n = 2n - 3 + 2\Delta S$ (n = number of constituents)
- Momentum carried by quarks $\langle x \rangle_q \simeq \int_0^1 dx x f(x)$

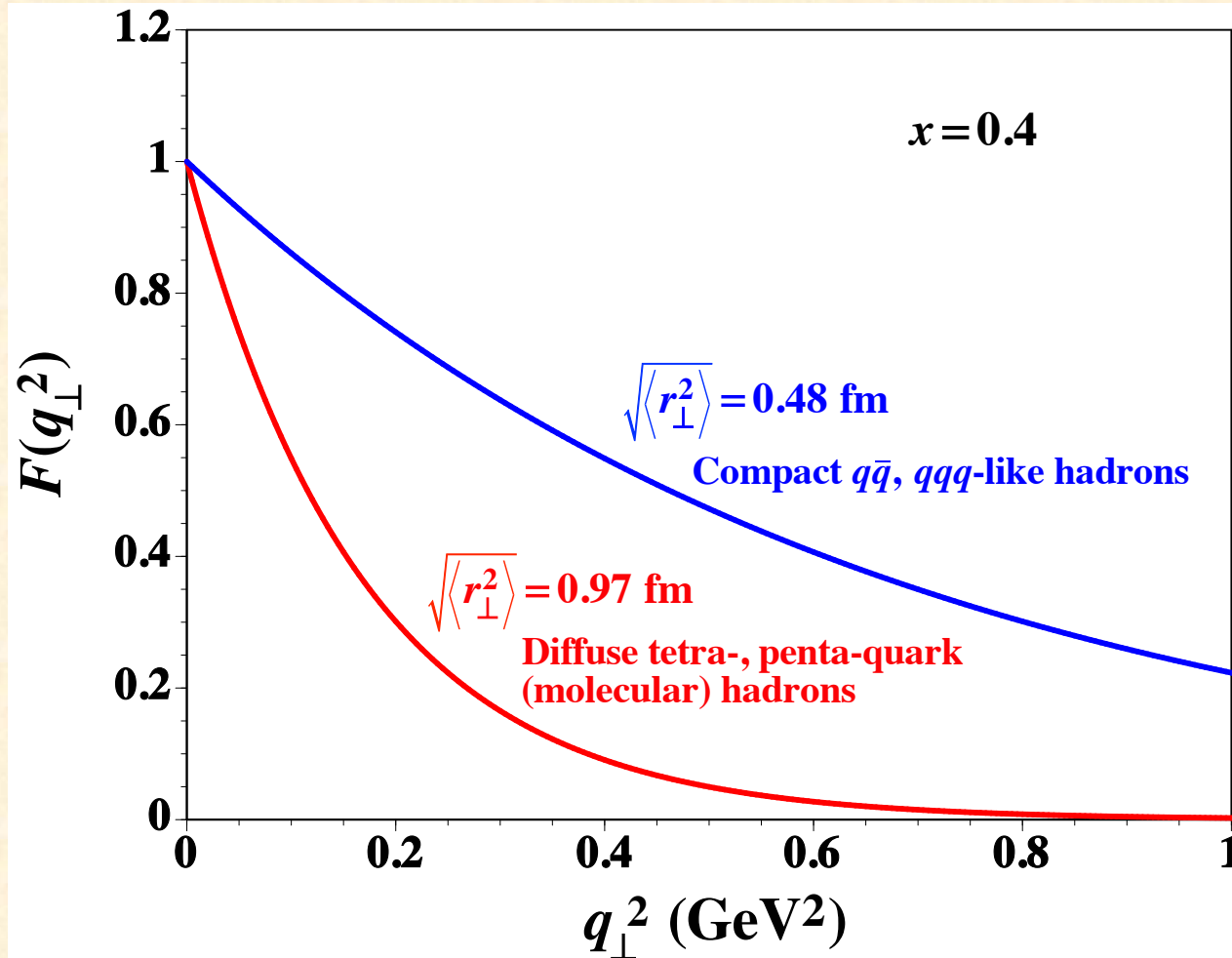
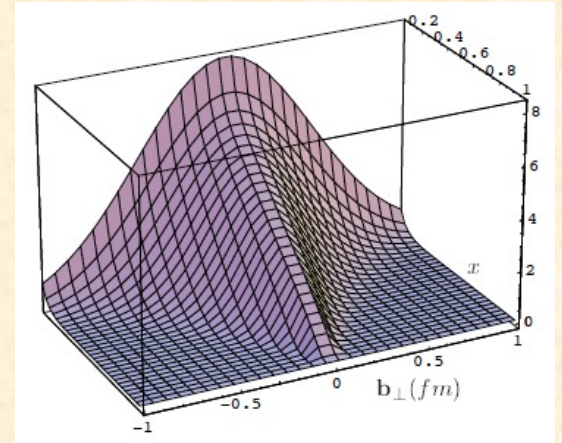


*Gedankenexperiment, but
possible at KEK-B, ILC, ...*

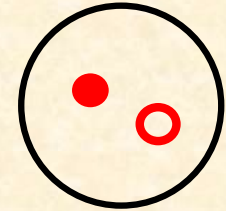


Two-dimensional transverse form factor

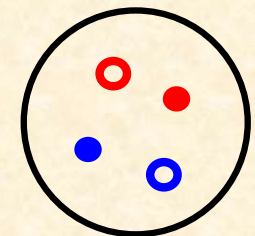
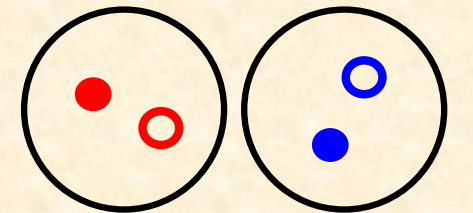
$$F(t, x) = e^{(1-x)t/(x\Lambda^2)}, \quad \langle r_{\perp}^2 \rangle = \frac{4(1-x)}{x\Lambda^2}$$



Ordinary $q\bar{q}$



Molecule $K\bar{K}$
or tetra-quark $qq\bar{q}\bar{q}$



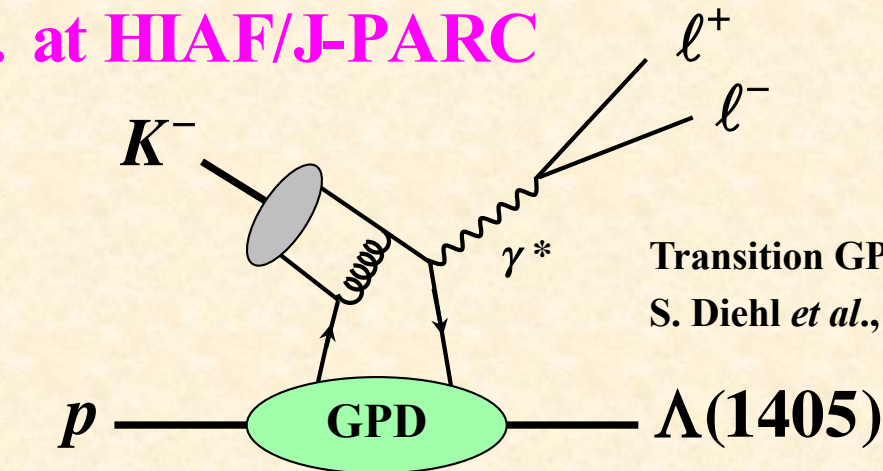
GPDs for exotic hadrons !?

Because stable targets do not exist for exotic hadrons,
it is not possible to measure their GPDs in a usual way.

→ Transition GPDs

or → $s \leftrightarrow t$ crossed quantity = GDAs at BES/Tau-charm/KEKB,
Circular/Linear Collider

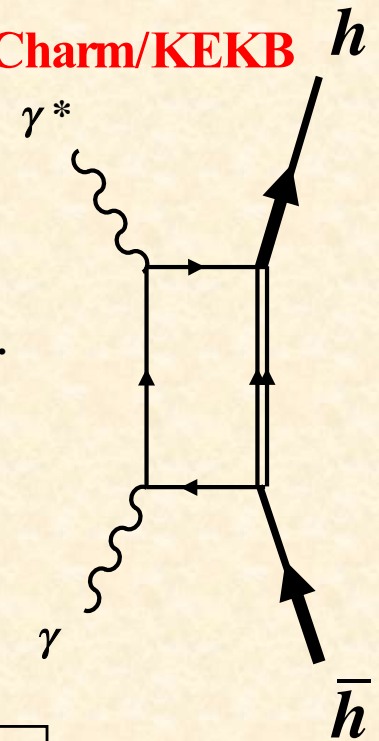
e.g. at HIAF/J-PARC



$$K^- (\bar{u}s) + p(uud) \rightarrow \Lambda_{1405}(uud\bar{u}s) + \gamma^*$$

Λ_{1405} = pentaquark ($\bar{K}N$ molecule) candidate

e.g. BES/Tau-Charm/KEKB



See H. Kawamura, SK, T. Sekihara, PRD 88 (2013) 034010;
W.-C. Chang, SK, and T. Sekihara, PRD 93 (2016) 034006
for constituent-counting rule for exotic hadron candidates.

Possible GPD studies at neutrino facilities

**X. Chen, SK, R. Kunitomo, S. Wu, Y.-P. Xie,
Euro. Phys. J. A 60 (2024) 208.**

See also

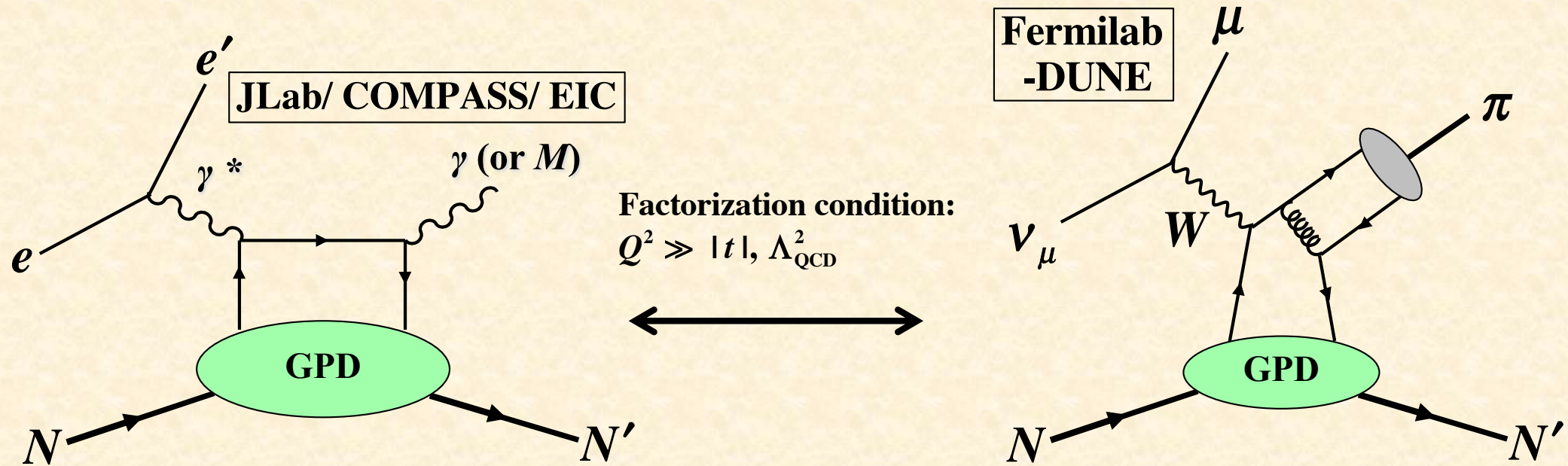
SK, EPJ Web Conf. 208 (2019) 07003.

**EIC yellow report, R. Abdul Khalek *et al.*, arXiv:2103.05419,
Sec. 7.5.2, Neutrino physics by SK and R. Petti.**

SK and R. Petti, PoS (NuFact2021) 092.

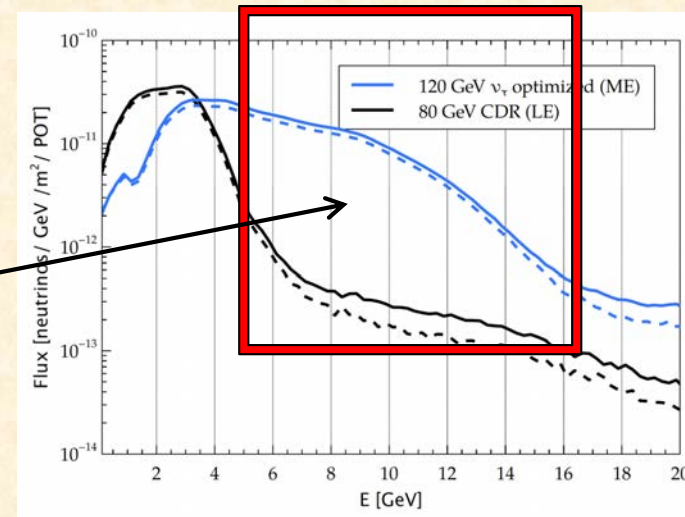
Neutrino reactions for gravitational form factors @Fermilab-DUNE

(Origins of hadron masses and pressures)



**Deep Underground Neutrino Experiment (DUNE)
at Long-Baseline Neutrino Facility (LBNF)**

**High-energy part of the LBNF ν beam
can be used for the GPD studies.**



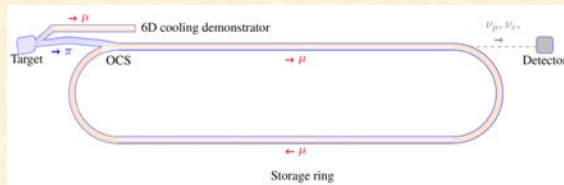
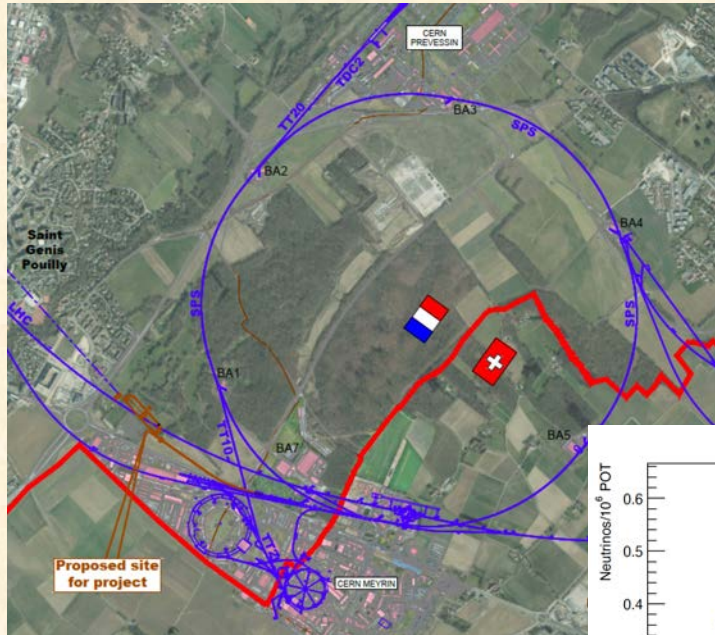
J. Rout *et al.*, PRD 102 (2020) 116018

nuSTORM (Neutrinos from Stored Muons)

Fermilab

Feasibility Study, C. C. Ahdida *et al.*, (2020);
L. A. Ruso *et al.*, arXiv:2203.07545.

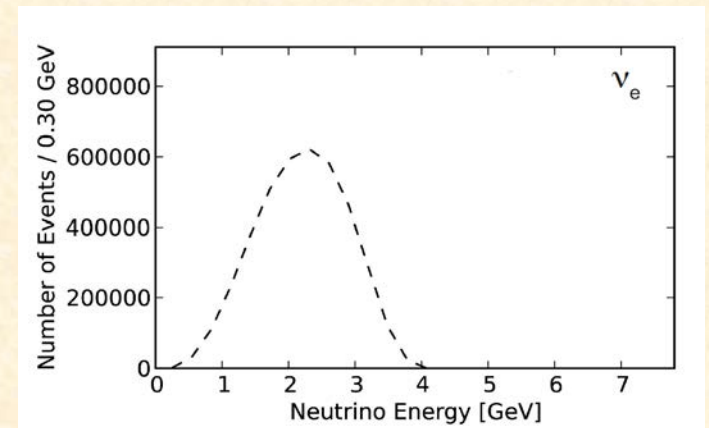
CERN



At this stage, the considered beam energy is not high enough for structure-function studies; however, high-energy option could be possible. (personal communications: Xianguo Lu)
→ SK's talk at the nuSTORM-collaboration meeting on July 15, 2024

They could be interested in the higher-energy possibility.

Letter of Intent, arXiv:1206.0294,
P. Kyberd *et al.* (2012);
Proposal, D. Adey *et al.*, arXiv:1308.6822.
No recent update.



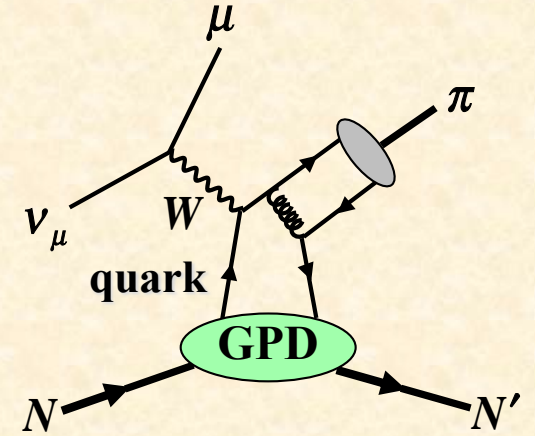
Cross section formalism

B. Pire, L. Szymanowski, J. Wagner,
Phys. Rev. D 95, 114029 (2017).

Cross section

$$\frac{d\sigma(\nu_\ell N \rightarrow \ell^- N' \pi)}{dy dQ^2 dt d\phi} = \Gamma \varepsilon \sigma_L, \quad \varepsilon \simeq \frac{1-y}{1-y+y^2/2}, \quad \Gamma = \frac{G_F^2 Q^2}{32 (2\pi)^4 (s - m_N^2)^2 y (1-\varepsilon) \sqrt{1+4x^2 m_N^2 / Q^2}}$$

$$\sigma_L = \varepsilon_L^* W_{\mu\nu} \varepsilon_L^\nu = \frac{1}{Q^2} \left[(1-\xi^2) \left\{ |C_q \mathcal{H}_q + C_g \mathcal{H}_g|^2 + |C_q \tilde{\mathcal{H}}_q|^2 \right\} + \frac{\xi^4}{1-\xi^2} \left\{ |C_q \mathcal{E}_q + C_g \mathcal{E}_g|^2 + |C_q \tilde{\mathcal{E}}_q|^2 \right\} \right. \\ \left. - 2\xi^2 \operatorname{Re} \left\{ (C_q \mathcal{H}_q + C_g \mathcal{H}_g)(C_q \mathcal{E}_q + C_g \mathcal{E}_g)^* \right\} - 2\xi^2 \operatorname{Re} \left\{ C_q \tilde{\mathcal{H}}_q (C_q \tilde{\mathcal{E}}_q)^* \right\} \right]$$



Quark contributions

$$T_q = -i \frac{C_q}{2Q} N(p') \left[\mathcal{H}_q \hat{n} + \mathcal{E}_q \frac{i\sigma^{\mu\nu} n_\mu \Delta_\nu}{2m_N} - \tilde{\mathcal{H}}_q \hat{n} \gamma_5 - \tilde{\mathcal{E}}_q \frac{\gamma_5 n \cdot \Delta}{2m_N} \right] N(p)$$

$$\mathcal{F}_q = 2f_\pi \int \frac{dz \phi_\pi(z)}{1-z} \int dx \frac{F_q(x, \xi, t)}{x - \xi + i\varepsilon}$$

= (pion distribution amplitude) · (quark GPD)

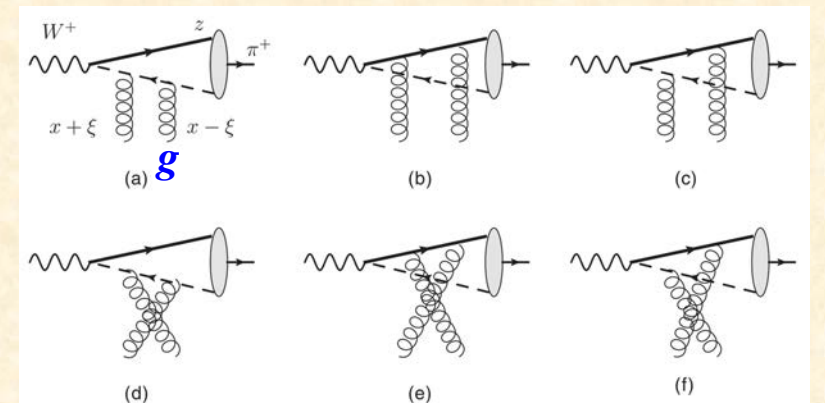
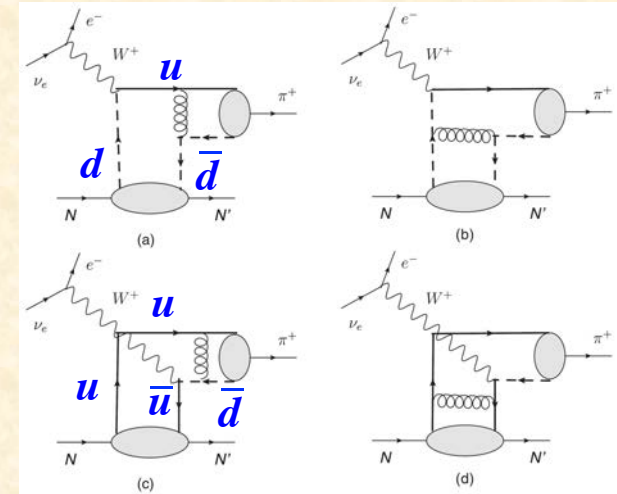
$$F_q(x, \xi, t) \equiv F_d(x, \xi, t) - F_u(-x, \xi, t)$$

$$F = H, E, \tilde{H}, \tilde{E}$$

Gluon contributions

$$T_g = -i \frac{C_g}{2Q} N(p') \left[\mathcal{H}^g \hat{n} + \mathcal{E}^g \frac{i\sigma^{\mu\nu} n_\mu \Delta_\nu}{2m_N} \right] N(p)$$

$$\mathcal{F}_g = \frac{8f_\pi}{\xi} \int \frac{dz \phi_\pi(z)}{z(1-z)} \int dx \frac{F_g(x, \xi, t)}{x - \xi + i\varepsilon}$$



Cross sections

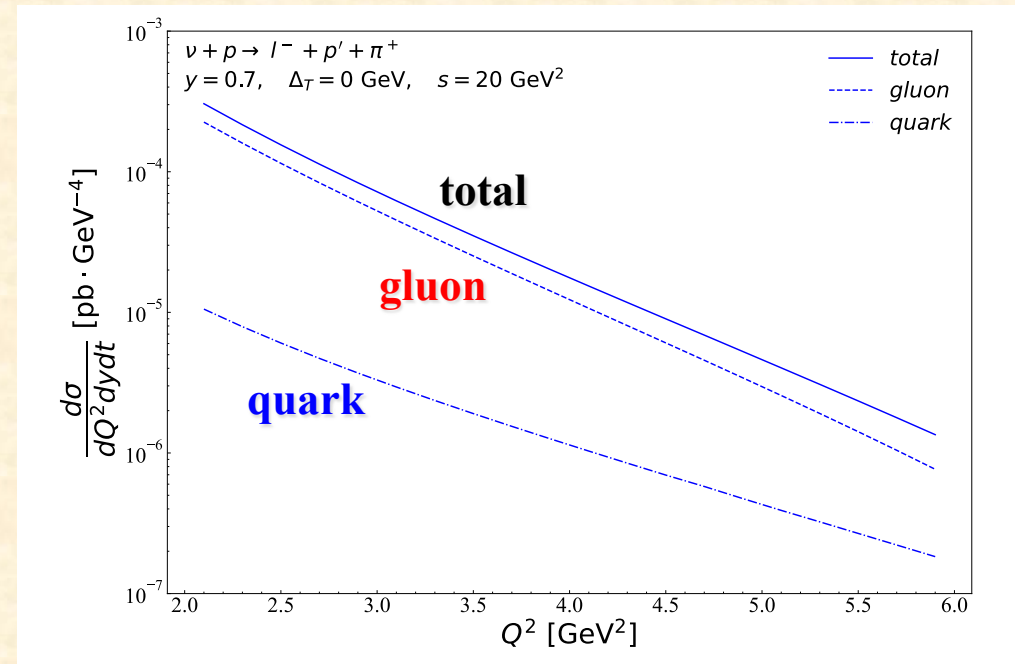
π^+ production: $\nu p \rightarrow \ell^- \pi^+ p$

$$\mathcal{F}_q = 2f_\pi \int \frac{dz \phi_\pi(z)}{1-z} \int dx \frac{F_q(x, \xi, t)}{x - \xi + i\varepsilon} \quad \text{gluon} \gg \text{quark}$$

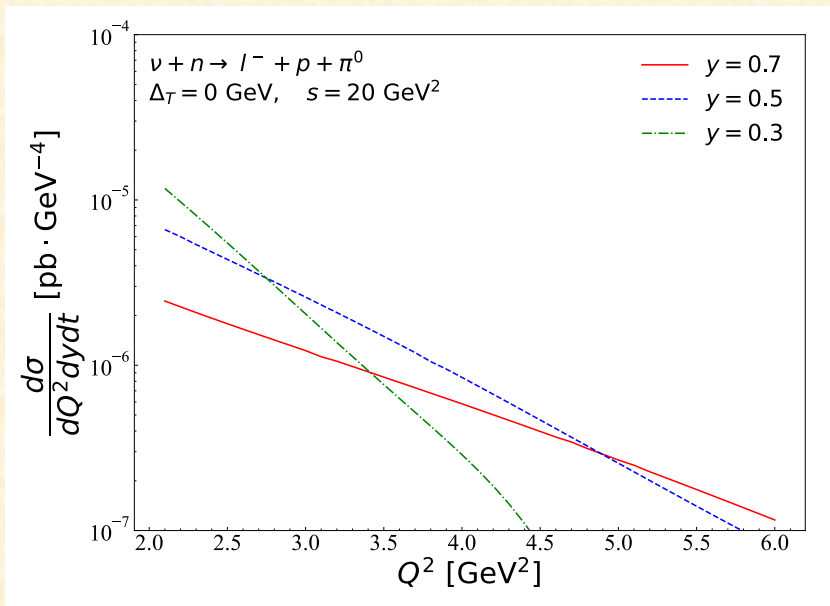
$$\mathcal{F}_g = \frac{8f_\pi}{\xi} \int \frac{dz \phi_\pi(z)}{z(1-z)} \int dx \frac{F_g(x, \xi, t)}{x - \xi + i\varepsilon}$$

$$\frac{\mathcal{F}_q}{\mathcal{F}_g} \sim \frac{\xi}{8} = \frac{0.1 \sim 0.3}{8} = 0.01 \sim 0.04$$

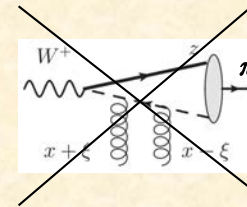
$$= \text{a few \%} \ll 1$$



π^0 production: $\nu n \rightarrow \ell^- \pi^0 p$



no gluon



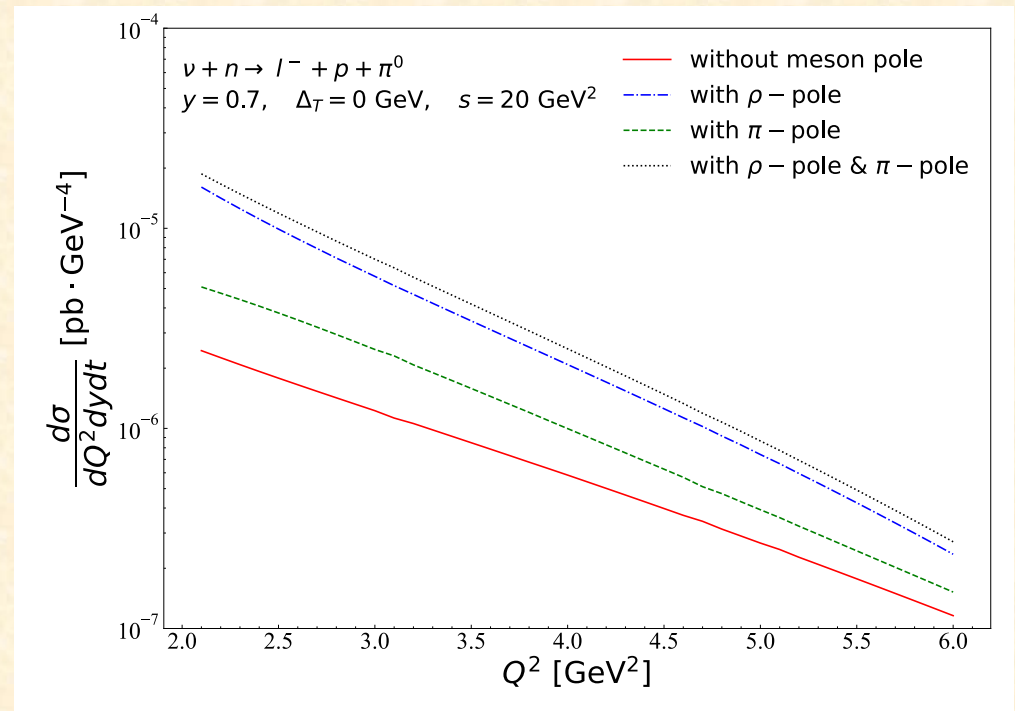
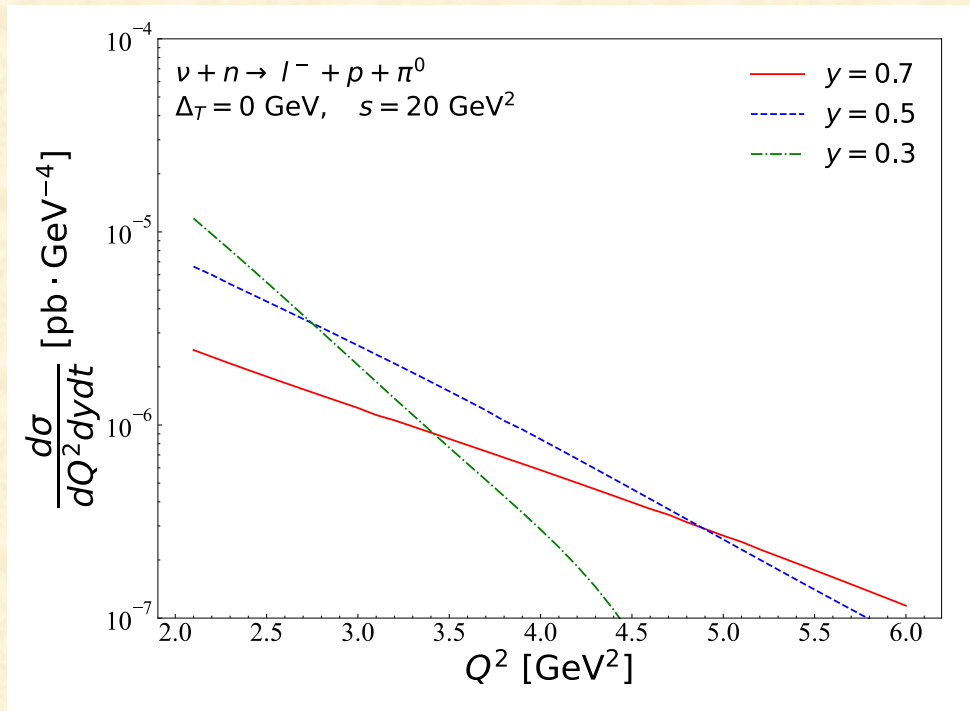
no gluon for π^0

Neutrino GPD studies are complementary to the charged-lepton projects.

- Gluon GPDs could be probed in charged-pion production.
- Quark GPDs could be probed in π^0 production.
- Flavor dependence of quark GPDs could be investigated.

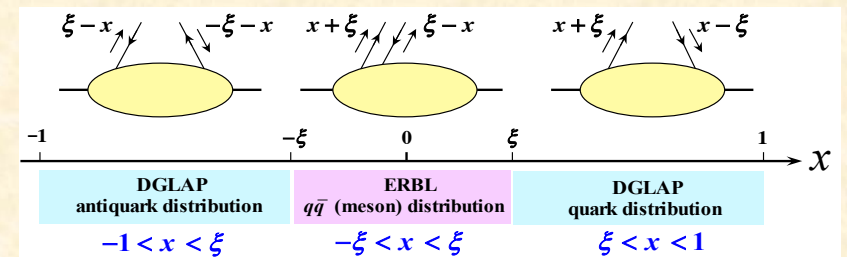
Contribution of each term to the π^0 -production cross section

$$\frac{d\sigma(\nu_\ell N \rightarrow \ell^- N' \pi)}{dy dQ^2 dt d\phi} \propto \frac{1}{Q^2} \left[(1 - \xi^2) \left\{ \left| C_q \mathcal{H}_q + \cancel{C_g \mathcal{H}_g} \right|^2 + \left| C_q \tilde{\mathcal{H}}_q \right|^2 \right\} + \frac{\xi^4}{1 - \xi^2} \left\{ \left| C_q \mathcal{E}_q + \cancel{C_g \mathcal{E}_g} \right|^2 + \left| C_q \tilde{\mathcal{E}}_q \right|^2 \right\} \right. \\ \left. - 2\xi^2 \operatorname{Re} \left\{ (C_q \mathcal{H}_q + \cancel{C_g \mathcal{H}_g}) (C_q \mathcal{E}_q + \cancel{C_g \mathcal{E}_g})^* \right\} - 2\xi^2 \operatorname{Re} \left\{ C_q \tilde{\mathcal{H}}_q (C_q \mathcal{E}_q)^* \right\} \right]$$



$$\cancel{H_g} > H_q > \tilde{H}_q > E_q, \tilde{E}_q, \cancel{E_g}$$

- π^0 production is sensitive to quark $\mathcal{H}_q$.
- GPDs in the ERBL (Efremov-Radyushkin-Brodsky-Lepage) region could be probed.



Constituent-counting rule for exotic hadrons

**H. Kawamura, SK, T. Sekihara, PRD 88 (2013) 034010;
W.-C. Chang, SK, T. Sekihara, PRD 93 (2016) 034006.**

Research purposes

It is not easy to find undoubted evidence for exotic hadrons by global observables (mass, spin, parity, decay width) at low energies.

(1) Determination of internal structure of exotic hadrons by high energy processes, where quark-gluon degrees of freedom appear.

Constituent-counting rule could be used because it counts internal constituents.

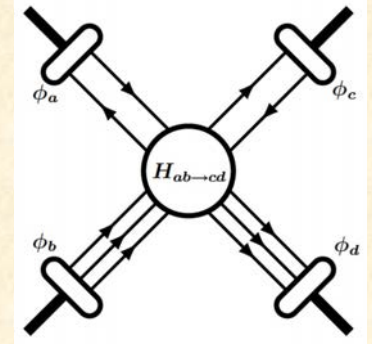
(2) Investigation on transition from hadron degrees of freedom to quark-gluon degrees of freedom for exotic hadrons.

$$\frac{d\sigma_{a+b \rightarrow c+d}}{dt} \simeq \frac{1}{16\pi s^2} \sum_{pol} |M_{a+b \rightarrow c+d}|^2 \Rightarrow \frac{d\sigma_{a+b \rightarrow c+d}}{dt} = \frac{1}{s^{n-2}} f_{a+b \rightarrow c+d}(t/s) \quad \text{constituent-counting rule}$$

$n = n_a + n_b + n_c + n_d$

Constituent-counting rule in perturbative QCD:

Hard exclusive processes $a + b \rightarrow c + d$



Consider the hard exclusive hadron reaction $a + b \rightarrow c + d$

$$M_{ab \rightarrow cd} = \int d[x_a] d[x_b] d[x_c] d[x_d] \phi_c([x_c]) \phi_d([x_d]) H_M([x_a], [x_b], [x_c], [x_d], Q^2) \phi_a([x_a]) \phi_b([x_b])$$

ϕ_p = proton distribution amplitude, H_M = hard amplitude (calculated in pQCD)

Rule for estimating $M_{ab \rightarrow cd}$

- (1) Feynman diagram: Draw leading and connected Feynman diagram by connecting $n/2$ quark lines by gluons.
- (2) Gluon propagators: The factor $1/P^2$ is assigned for each gluon propagator.

There are $n/2 - 1$ gluon propagators $\sim 1/(P^2)^{n/2-1}$.

- (3) Quark propagators: The factor $1/P$ is assigned for each quark propagator.

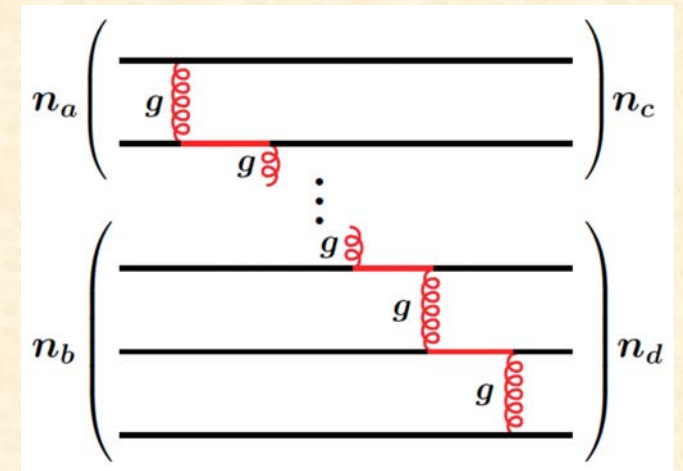
There are $n/2 - 2$ quark propagators $\sim 1/(P)^{n/2-2}$.

- (4) External quarks: The factor $\sqrt{P}$ is assigned for each external quark.

There are n external quarks $\sim (\sqrt{P})^n$.

$$M_{ab \rightarrow cd} \sim \frac{1}{(P^2)^{n/2-1}} \frac{1}{(P)^{n/2-2}} (\sqrt{P})^n = \frac{(P)^{n/2}}{(P)^{n-2} (P)^{n/2-2}} = \frac{1}{(P)^{n-4}} \sim \frac{1}{s^{n/2-2}}$$

Cross section: $\frac{d\sigma_{ab \rightarrow cd}}{dt} \simeq \frac{1}{16\pi^2} \sum_{\text{spol}} |M_{ab \rightarrow cd}|^2 \sim \frac{1}{s^{n-2}}$



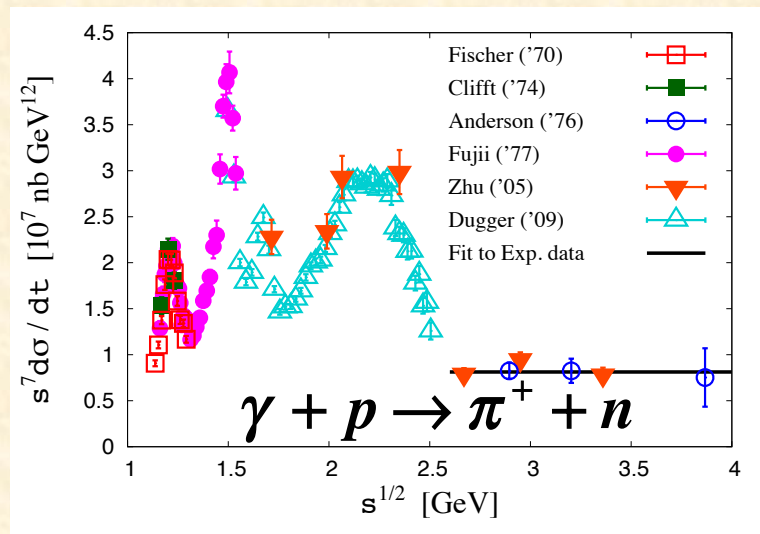
Constituent-counting rule, Transition from hadron degrees of freedom to quark-gluon ones

Typical current situation

- Transition from hadron d.o.f to quark d.o.f.
- (Looks like) Constituent-counting scaling

BNL experiment

C. White et al., PRD 49 (1994) 58.

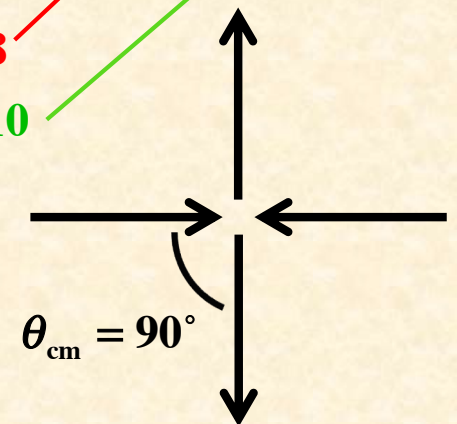


No.	Interaction	Cross section		$n-2$ ($\frac{d\sigma}{dt} \sim 1/s^{n-2}$)
		E838	E755	
1	$\pi^+ p \rightarrow p\pi^+$	132 ± 10	4.6 ± 0.3	6.7 ± 0.2
2	$\pi^- p \rightarrow p\pi^-$	73 ± 5	1.7 ± 0.2	7.5 ± 0.3
3	$K^+ p \rightarrow pK^+$	219 ± 30	3.4 ± 1.4	$8.3^{+0.6}_{-1.0}$
4	$K^- p \rightarrow pK^-$	18 ± 6	0.9 ± 0.9	≥ 3.9
5	$\pi^+ p \rightarrow p\rho^+$	214 ± 30	3.4 ± 0.7	8.3 ± 0.5
6	$\pi^- p \rightarrow p\rho^-$	99 ± 13	1.3 ± 0.6	8.7 ± 1.0
13	$\pi^+ p \rightarrow \pi^+ \Delta^+$	45 ± 10	2.0 ± 0.6	6.2 ± 0.8
15	$\pi^- p \rightarrow \pi^- \Delta^-$	24 ± 5	≤ 0.12	≥ 10.1
17	$pp \rightarrow pp$	3300 ± 40	48 ± 5	9.1 ± 0.2
18	$\bar{p}p \rightarrow \bar{p}p$	75 ± 8	≤ 2.1	≥ 7.5

JLab: L.Y. Zhu *et al.*, PRL 91, 022003 (2003);
PRC 71, 044603 (2005);
W. Chen *et al.*, PRL 103, 012301 (2009).

$$n-2: (2+3+2+3)-2=8$$

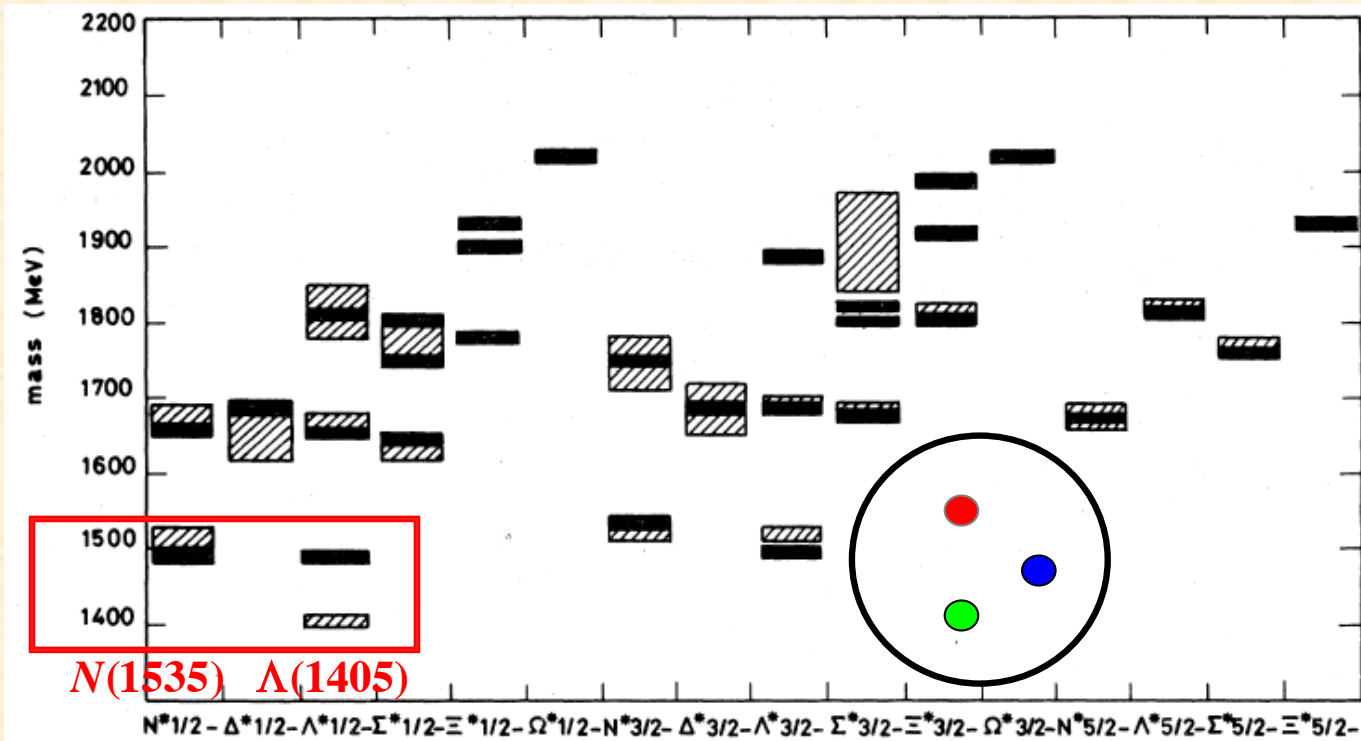
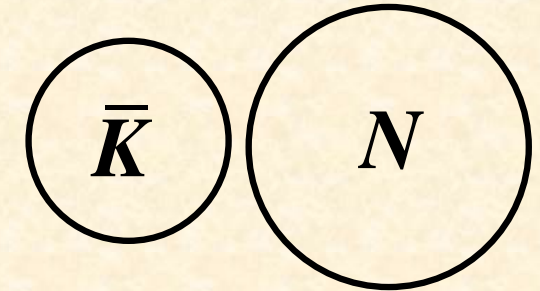
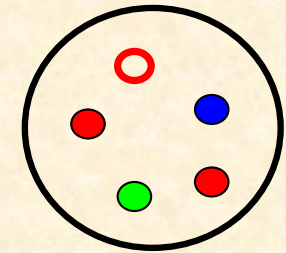
$$(3+3+3+3)-2=10$$



see R. A. Schumacher and M. M. Sargsian,
PRC 83 (2011) 025207 for hyperon production

$\Lambda(1405)$: exotic hadron?

Negative-parity baryons
N. Isgur and G. Karl,
PRD 18 (1978) 4187.



Our proposal:

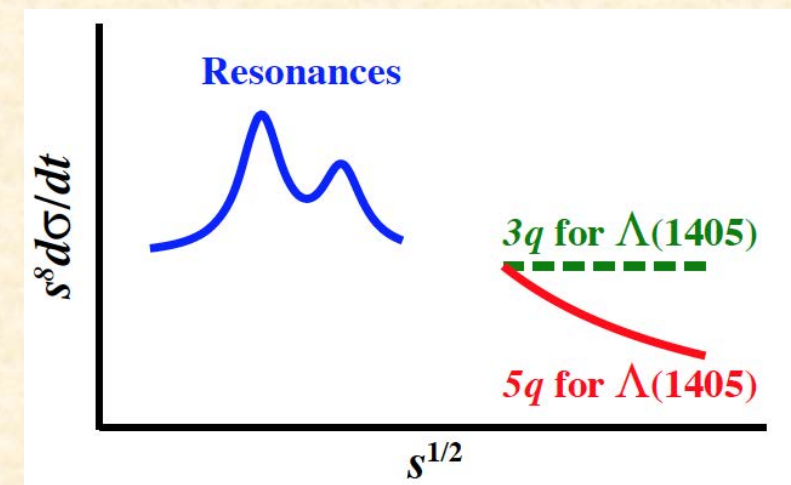
Exotic hadron production

$\pi^- + p \rightarrow K^0 + \Lambda(1405)$: J-PARC, COMPASS?

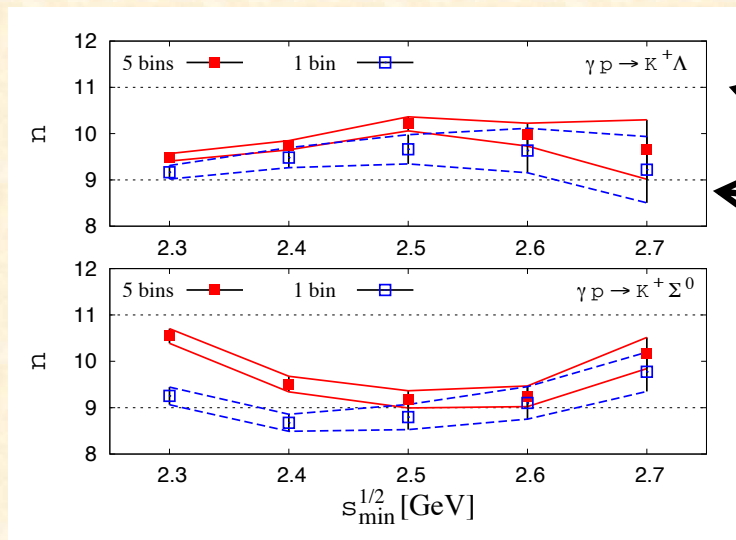
$\gamma + p \rightarrow K^+ + \Lambda(1405)$: JLab

Most spectra agree with the ones by a $3q$ -picture

- Only $\Lambda(1405)$ deviates from the measurement.
- Difficult to understand the small mass of $\Lambda(1405)$ in comparison with $N(1535)$.
→ $\bar{K}N$ molecule or penta-quark ($qqqq\bar{q}$)?

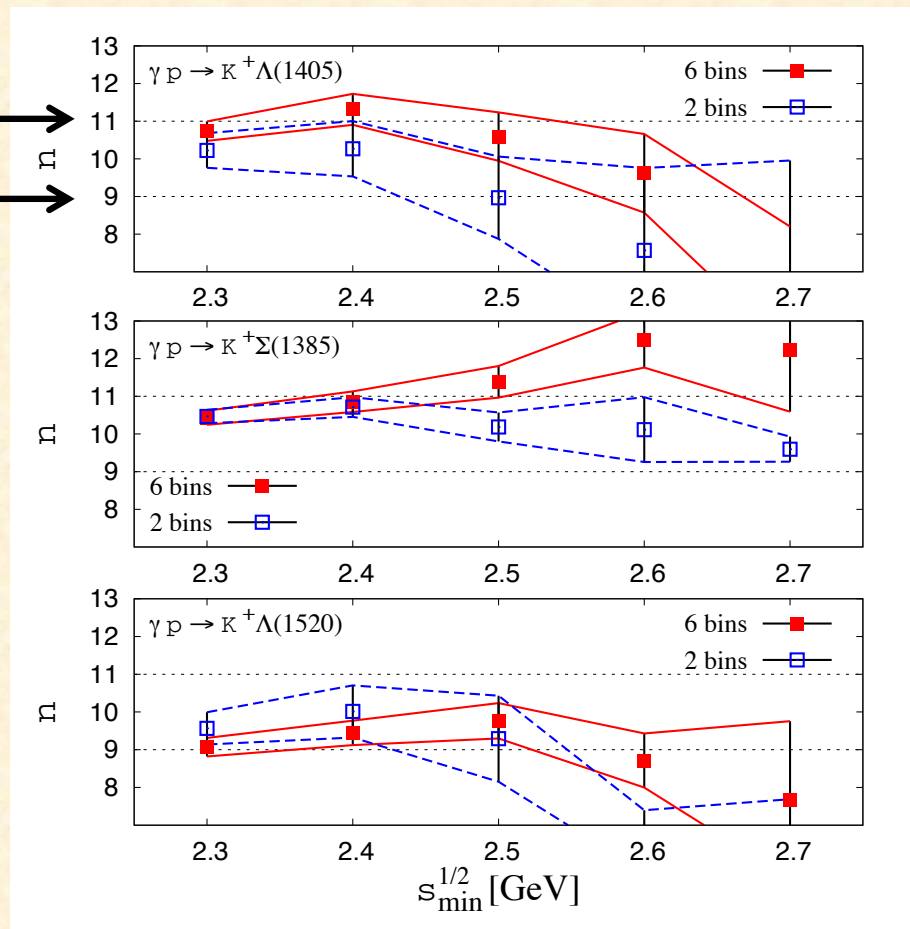
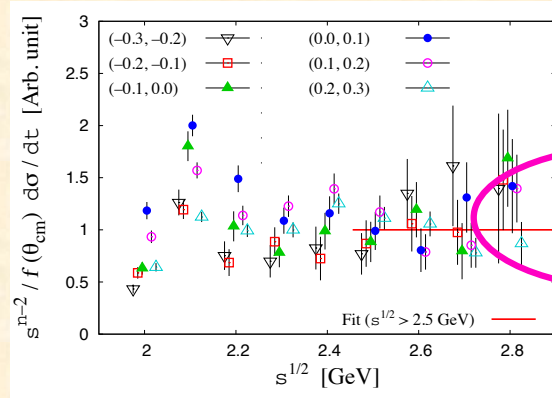


JLab hyperon productions including $\Lambda(1405)$



$n_\Lambda = 5$

$n_\Lambda = 3$



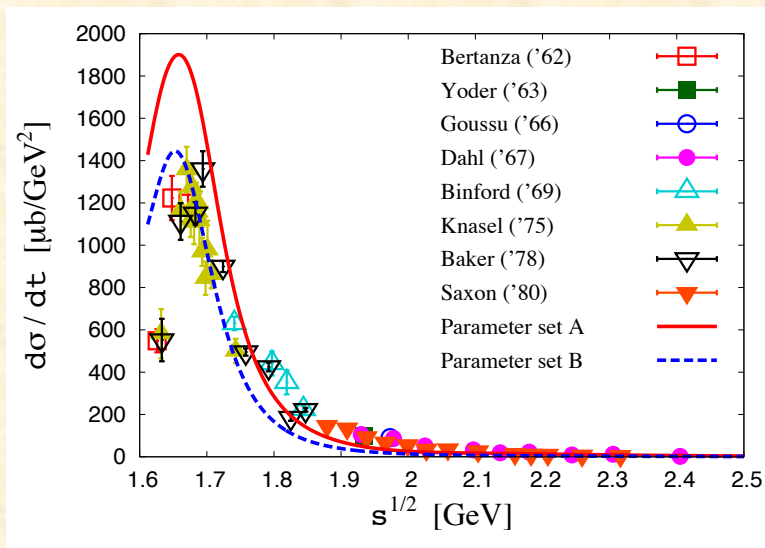
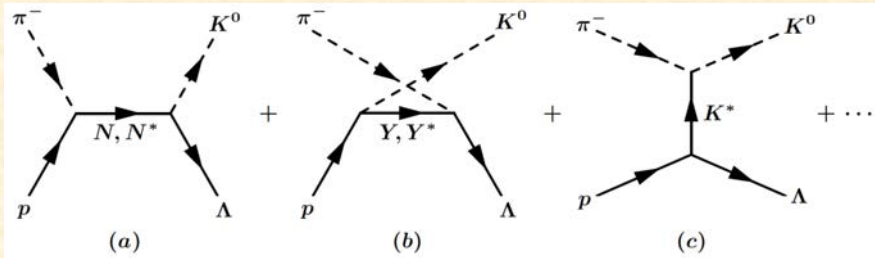
- Λ , $\Lambda(1520)$, and Σ seem to be consistent with ordinary baryons with $n = 3$.
- $\Lambda(1405)$ looks penta-quark at low energies but $n \sim 3$ at high energies???
- $\Sigma(1385)$: $n = 5$???

→ In order to clarify the nature of $\Lambda(1405)$ [qqq , $\bar{K}N$, $qqqq\bar{q}$], the JLab 12-GeV experiment plays an important role!

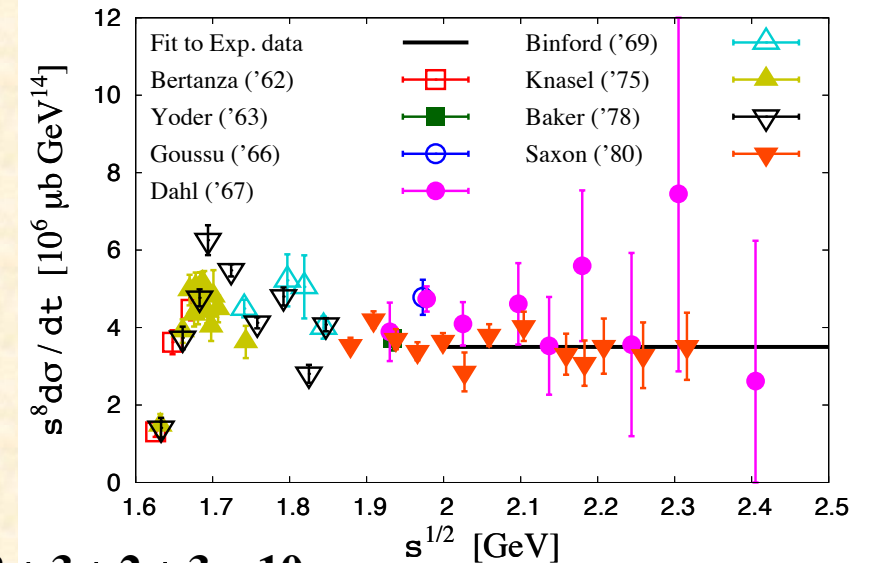
W.-C. Chang, SK, T. Sekihara,
PRD 93 (2016) 034006.

Ordinary-hadron production $\pi^- + p \rightarrow K^0 + \Lambda$ as a reference

At low energies



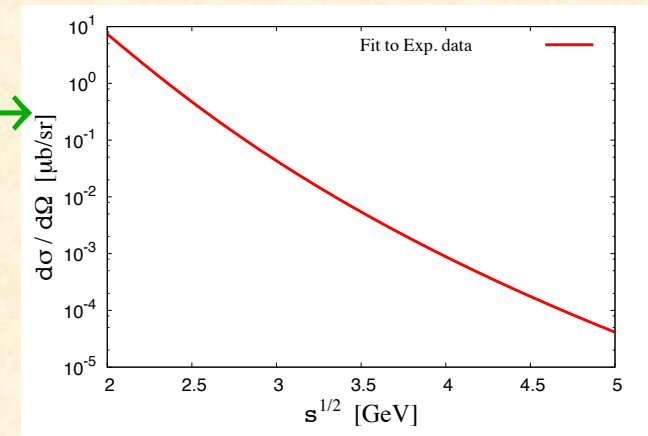
From low to higher energies



$$n = 2 + 3 + 2 + 3 = 10$$

$$\frac{d\sigma_{ab \rightarrow cd}}{dt} = \frac{\text{const}}{s^{n-2}}, \quad n = 10.1 \pm 0.6, \text{ encouraging!}$$

Our prediction
at high energies →



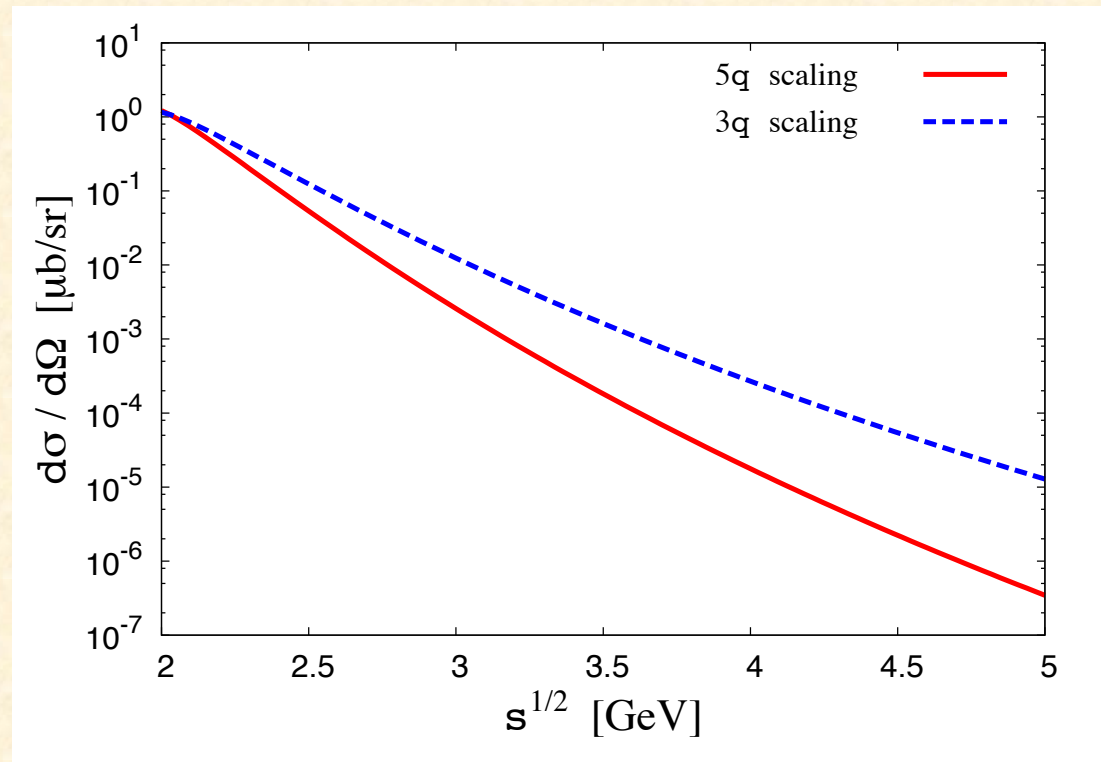
Exotic-hadron production $\pi^- + p \rightarrow K^0 + \Lambda(1405)$

Theoretical and experimental situation
is no as good as the one for the ground Λ .

$$\begin{aligned} n &= 2 + 3 + 2 + 3 = 10 \quad \text{if } \Lambda(1405) = \text{three-quark state} \\ &= 2 + 3 + 2 + 5 = 12 \quad \text{if } \Lambda(1405) = \text{five-quark state} \\ &\quad \text{(including } \bar{K}N \text{ molecule)} \end{aligned}$$

$$\frac{d\sigma_{ab \rightarrow cd}}{dt} = \frac{\text{const}}{s^{n-2}}, \quad n = 10 \text{ or } 12$$

Our prediction at high energies



Comments:

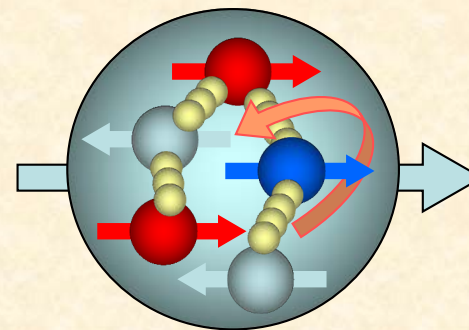
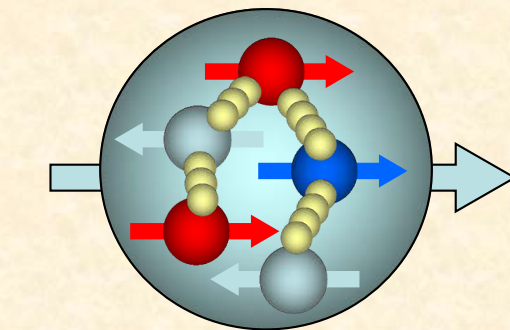
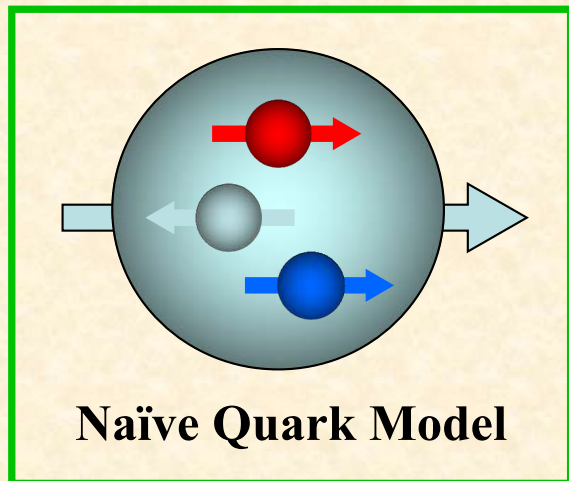
Tensor-polarization physics

S. Kumano, Euro. Phys. J. A 60 (2024) 205.

Nucleon spin

Almost none of nucleon spin is carried by quarks!

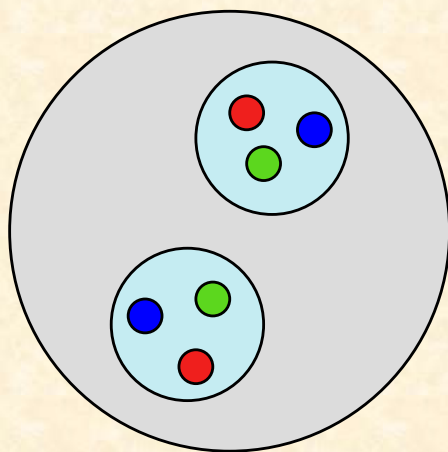
→ Nucleon spin puzzle!?



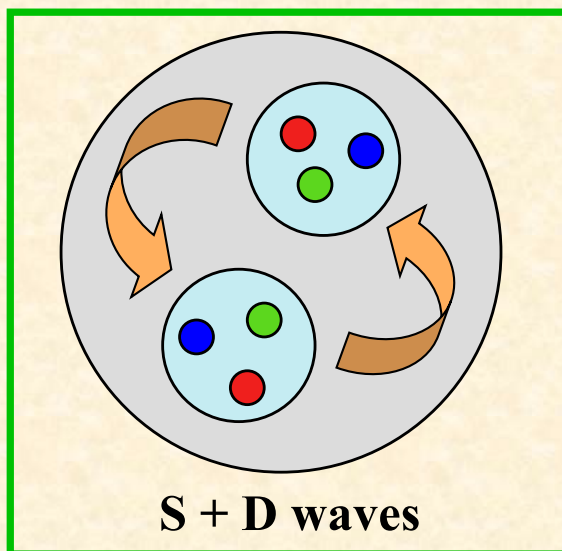
“old” standard model

Tensor structure b_1 (e.g. deuteron)

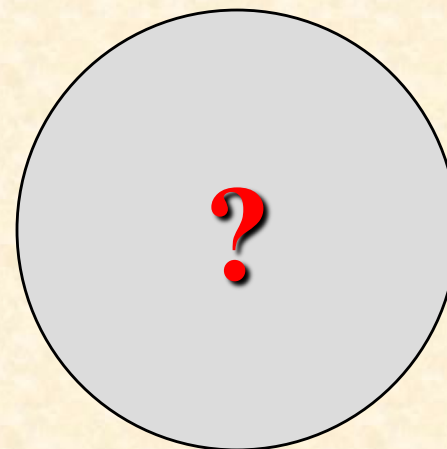
Tensor-structure puzzle!?



$b_1 = 0$



standard model $b_1 \neq 0$



$b_1^{\text{experiment}} \neq b_1^{\text{“standard model”}}$

“Standard-model” prediction for b_1 of deuteron

$$b_1(x) = \int \frac{dy}{y} \delta_T f(y) F_1^N(x/y, Q^2), \quad y = \frac{Mp \cdot q}{M_N P \cdot q} \simeq \frac{2p^-}{P^-}$$

$$\delta_T f(y) = f^0(y) - \frac{f^+(y) + f^-(y)}{2}$$

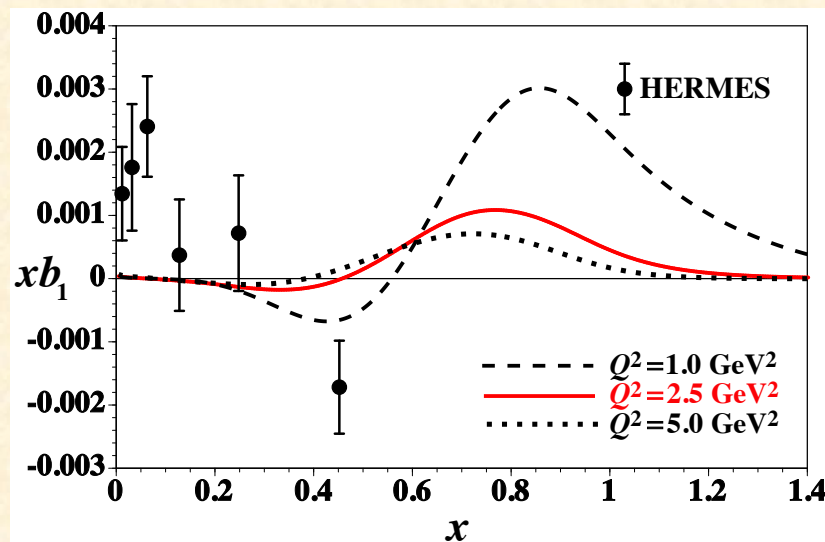
$$= \int d^3 p \, y \left[-\frac{3}{4\sqrt{2}\pi} \phi_0(p) \phi_2(p) + \frac{3}{16\pi} |\phi_2(p)|^2 \right] (3 \cos^2 \theta - 1) \delta\left(y - \frac{p \cdot q}{M_N v}\right)$$

S-D term **D-D term**

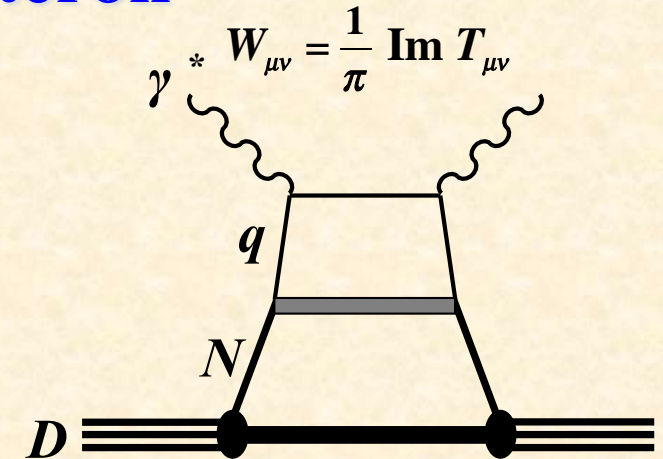
Nucleon momentum distribution:

$$f^H(y) \equiv f_{\uparrow}^H(y) + f_{\downarrow}^H(y) = \int d^3 p \, y |\phi^H(\vec{p})|^2 \delta\left(y - \frac{E - p_z}{M_N}\right)$$

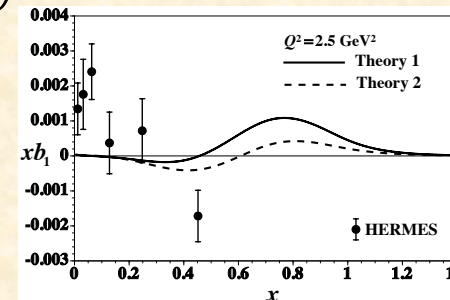
D-state admixture: $\phi^H(\vec{p}) = \phi_{\ell=0}^H(\vec{p}) + \phi_{\ell=2}^H(\vec{p})$



W. Cosyn, Yu-Bing Dong, SK, M. Sargsian,
Phys. Rev. D 95 (2017) 074036.



**Standard model
of the deuteron**



$|b_1(\text{theory})| \ll |b_1(\text{HERMES})|$
at $x < 0.5$

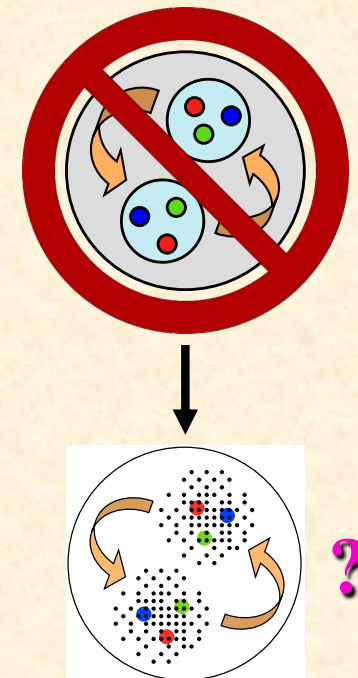
**Standard convolution model does not
work for the deuteron tensor structure!?**

G. A. Miller, PRC 89 (2014) 045203,

Interesting suggestions:

hidden-color, 6-quark, $\dots$

$|6q\rangle = |NN\rangle + |\Delta\Delta\rangle + |CC\rangle + \dots$



Gluon transversity $\Delta_T g$

Note on our notations:

Tensor-polarized gluon distribution: $\delta_T g$

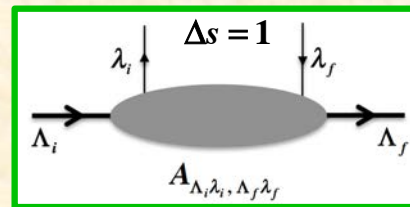
Gluon transversity: $\Delta_T g$

Helicity amplitude $A(\Lambda_i, \lambda_i, \Lambda_f, \lambda_f)$, conservation $\Lambda_i - \lambda_i = \Lambda_f - \lambda_f$

Longitudinally-polarized quark in nucleon: $\Delta q(x) \sim A\left(+\frac{1}{2} + \frac{1}{2}, +\frac{1}{2} + \frac{1}{2}\right) - A\left(+\frac{1}{2} - \frac{1}{2}, +\frac{1}{2} - \frac{1}{2}\right)$

Quark transversity in nucleon:

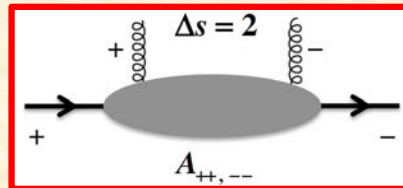
$\Delta_T q(x) \sim A\left(+\frac{1}{2} + \frac{1}{2}, -\frac{1}{2} - \frac{1}{2}\right)$, $\lambda_i = +\frac{1}{2} \rightarrow \lambda_f = -\frac{1}{2}$ quark spin flip ($\Delta s = 1$)



Gluon transversity in deuteron:

$\Delta_T g(x) \sim A(+1 + 1, -1 - 1)$,

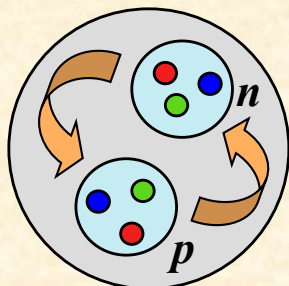
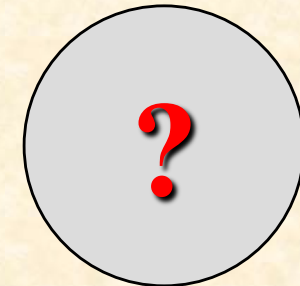
$A\left(+\frac{1}{2} + \frac{1}{2}, -\frac{1}{2} - \frac{1}{2}\right)$ not possible for nucleon



Note: Gluon transversity does not exist for spin-1/2 nucleons.

$b_1 (\delta_T q, \delta_T g) \neq 0 \Leftrightarrow$ still $\Delta_T g = 0$

What would be the mechanism(s)
for creating $\Delta_T g \neq 0$?



S + D waves

Physics beyond “the standard model” in nuclear physics?
(Physics beyond the standard model in particle physics???)

JLab PAC-38 (2011) proposal, PR12-11-110

Full approval in 2023

The Deuteron Tensor Structure Function b_1

2011

A Proposal to Jefferson Lab PAC-38.
(Update to LOI-11-003)

J.-P. Chen (co-spokesperson), P. Solvignon (co-spokesperson),
K. Allada, A. Camsonne, A. Deur, D. Gaskell,
C. Keith, S. Wood, J. Zhang
Thomas Jefferson National Accelerator Facility, Newport News, VA 23606

N. Kalantarians (co-spokesperson), O. Rondon (co-spokesperson)
Donal B. Day, Hovhannes Baghdasaryan, Charles Hanretty
Richard Lindgren, Blaine Norum, Zhihong Ye
University of Virginia, Charlottesville, VA 22903

PR12-13-011

The Deuteron Tensor Structure Function b_1

2023

A Proposal to Jefferson Lab PAC-40
(Update to PR12-11-110)

K. Allada, A. Camsonne, J.-P. Chen,[†]
A. Deur, D. Gaskell, M. Jones, C. Keith, J. Pierce,
P. Solvignon,[†] S. Wood, J. Zhang
Thomas Jefferson National Accelerator Facility, Newport News, VA 23606

Rui
Seon

O. Rondon Aramayo,[‡] D. Crabb, D. B. Day,
C. Hanretty, D. Keller,[‡] R. Lindgren, S. Liuti, B. Norum,
Zhihong Ye, X. Zheng
University of Virginia, Charlottesville, VA 22903

N. Kalantarians[‡]
Hampton University, Hampton VA 23668

T. Badman, J. Calarco, J. Dawson,
S. Phillips, E. Long,[‡] K. Slifer^{‡,§}, R. Zielinski
University of New Hampshire, Durham, NH 03861

G. Ron
Hebrew University of Jerusalem, Jerusalem

W. Bertozzi, S. Gilad, J. Huang
A. Kelleher, V. Sulkosky
Massachusetts Institute of Technology, Cambridge, MA 02139

b_1 experiment

Gluon transversity

A Letter of Intent to Jefferson Lab PAC 44, June 6, 2016 Search for Exotic Gluonic States in the Nucleus

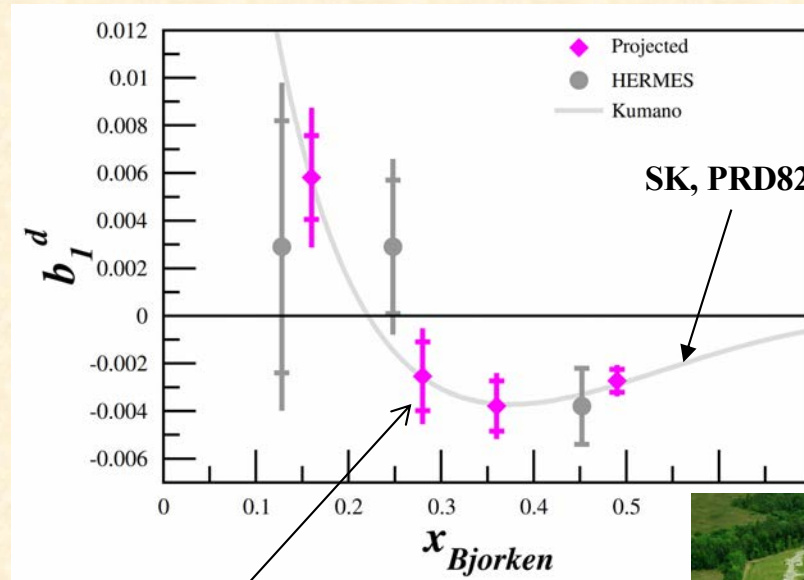
M. Jones, C. Keith, J. Maxwell^{*}, D. Meekins
Thomas Jefferson National Accelerator Facility, Newport News, VA 23606

W. Detmold, R. Jaffe, R. Milner, P. Shanahan
Laboratory for Nuclear Science, MIT, Cambridge, MA 02139

D. Crabb, D. Day, D. Keller, O. A. Rondon
University of Virginia, Charlottesville, VA 22904

J. Pierce

Oak Ridge National Laboratory, Oak Ridge, TN 37831



Expected errors by JLab

See J. Poudel, A. Bacchetta, J.-P. Chen, N. Santiesteban, EPJA 61 (2025) 81 for updated information.



Eur. Phys. J. A (2025) 61:81
<https://doi.org/10.1140/epja/s10050-025-01558-w>

Review

THE EUROPEAN
PHYSICAL JOURNAL A



Experimental study of tensor structure function of deuteron

Jiwan Poudel^{1,a}, Alessandro Bacchetta², Jian-Ping Chen¹, Nathaly Santiesteban³

¹ Jefferson Lab, 12000 Jefferson Ave, Newport News, VA 23606, USA

² University of Pavia, Via Bassi 6, I-27100 Pavia, Italy

³ University of New Hampshire, 9 Library Way, Durham, NH 03824, USA

Experimental possibility at Fermilab in 2020's

**Polarized fixed-target experiments
at the Main Injector,
Proton beam = 120 GeV** © Fermilab



Fermilab-E1039 (SpinQuest)

Drell-Yan experiment with a polarized proton target

Co-Spokespersons: A. Klein, X. Jiang, Los Alamos National Laboratory

List of Collaborators:

D. Geesaman, P. Reimer
Argonne National Laboratory, Argonne, IL 60439
C. Brown, D. Christian
Fermi National Accelerator Laboratory, Batavia IL 60510
M. Diefenthaler, J.-C. Peng
University of Illinois, Urbana, IL 61081
W.-C. Chang, Y.-C. Chen
Institute of Physics, Academia Sinica, Taiwan
S. Sawada
KEK, Tsukuba, Ibaraki 305-0801, Japan
T.-H. Chang
Ling-Tung University, Taiwan
J. Huang, X. Jiang, M. Leitch, A. Klein, K. Liu, M. Liu, P. McGaughey
Los Alamos National Laboratory, Los Alamos, NM 87545
E. Beise, K. Nakahara
University of Maryland, College Park, MD 20742
C. Aidala, W. Lorenzon, R. Raymond
University of Michigan, Ann Arbor, MI 48109-1040
T. Badman, E. Long, K. Slifer, R. Zielinski
University of New Hampshire, Durham, NH 03824
R.-S. Guo
National Kaohsiung Normal University, Taiwan
Y. Goto
RIKEN, Wako, Saitama 351-01, Japan
L. El Fassi, K. Myers, R. Ransome, A. Tadepalli, B. Tice
Rutgers University, Rutgers NJ 08544
J.-P. Chen
Thomas Jefferson National Accelerator Facility, Newport News, VA 23606
K. Nakano, T.-A. Shibata
Tokyo Institute of Technology, Tokyo 152-8551, Japan
D. Crabb, D. Day, D. Keller, O. Rondon
University of Virginia, Charlottesville, VA 22904

**Fermilab experimentalists are interested
in the gluon transversity by replacing
the E1039 proton target for the deuteron one.
(Spokesperson of E1039: D. Keller)
However, there was no theoretical formalism
until our work.**

**SK and Q.-T. Song,
PRD 101 (2020) 054011 & 094013**

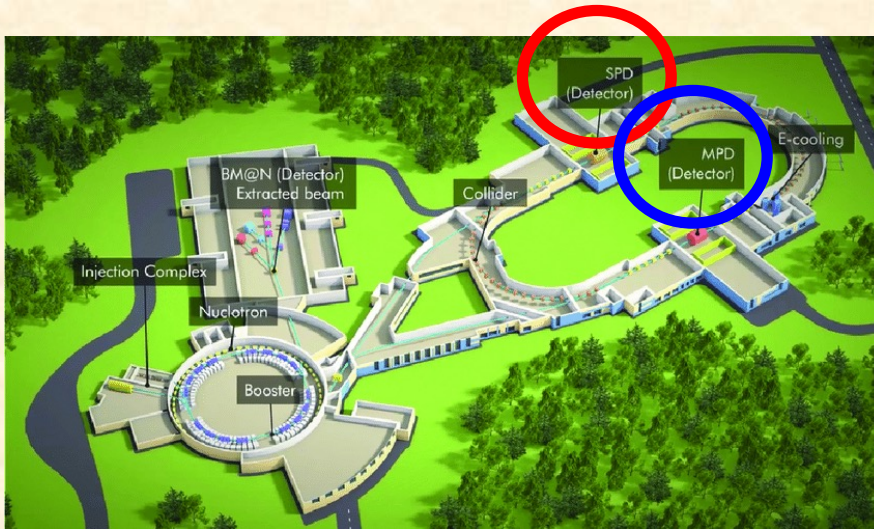
The Transverse Structure of the Deuteron with Drell-Yan

D. Keller¹

¹University of Virginia, Charlottesville, VA 22904

Proposal for a Fermilab-PAC in 2023.

Nuclotron-based Ion Collider fAcility (NICA)



SPD (Spin Physics Detector for physics with polarized beams)

MPD (MultiPurpose Detector for heavy ion physics)

$$\vec{p} + \vec{p}: \sqrt{s_{pp}} = 12 \sim 27 \text{ GeV}$$

$$\vec{d} + \vec{d}: \sqrt{s_{NN}} = 4 \sim 14 \text{ GeV}$$

$\vec{p} + \vec{d}$ is also possible.

On the physics potential to study the gluon content of proton and deuteron at NICA SPD, A. Arbuzov *et al.* (NICA project), Nucl. Part. Phys. 119 (2021) 103858.

Unique opportunity in high-energy spin physics,
especially on the deuteron spin physics.

→ Theoretical formalisms need to be developed.

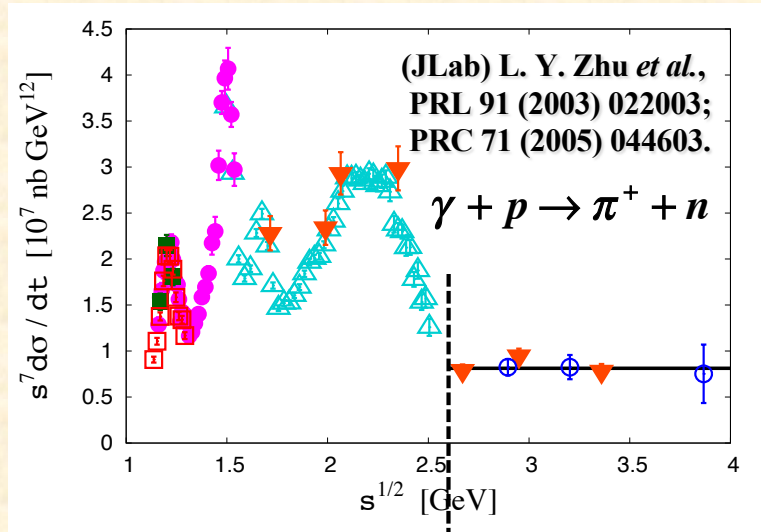


Future possibility at HIAF on color transparency

S. Kumano,

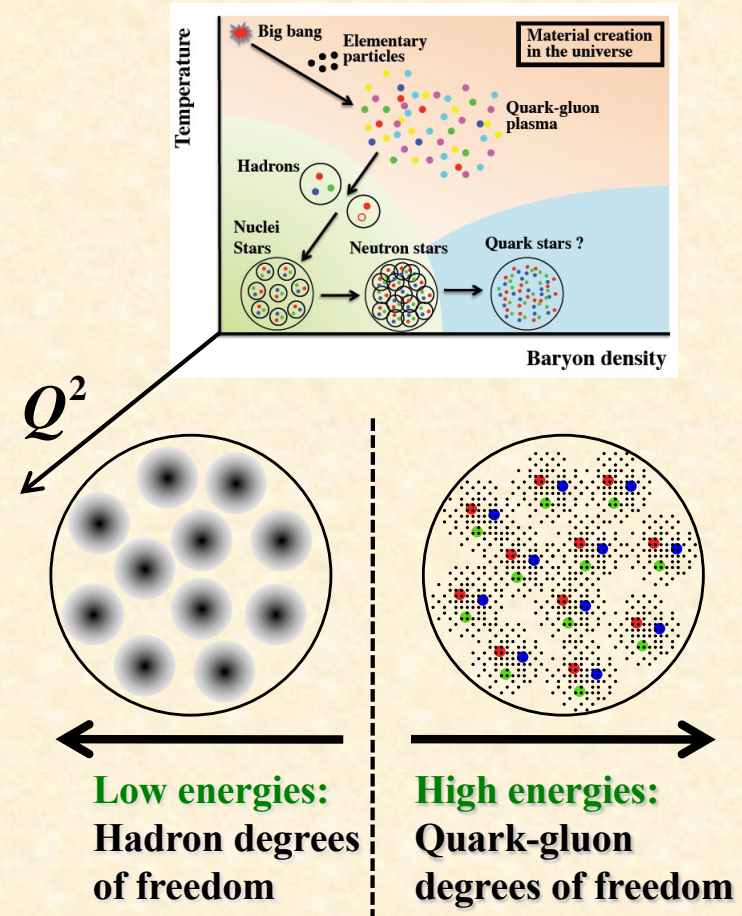
**arXiv:2205.03012, Physics 2022, 4, 565-577, Proceedings
of the Workshop on the Future of Color Transparency
and Hadronization Studies at Jefferson Lab and Beyond,
June 7-8, 2021 (Online).**

Hadron degrees of freedom (d.o.f.) $\Leftrightarrow$ Quark d.o.f.



Low energies:
 Hadron degrees
 of freedom
 (Resonances)

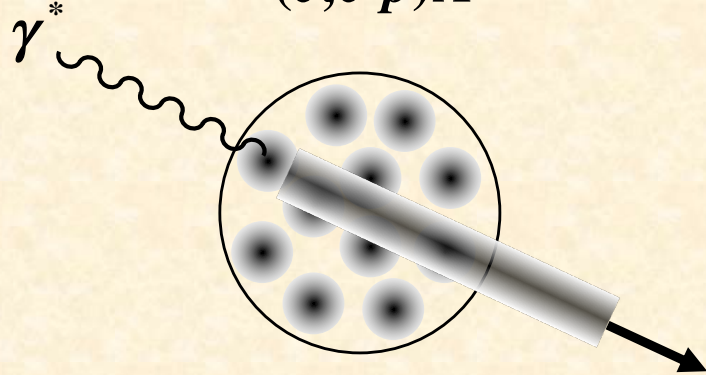
High energies:
 Quark-gluon
 degrees of freedom
 (Perturbative QCD:
 Constituent-counting rule)



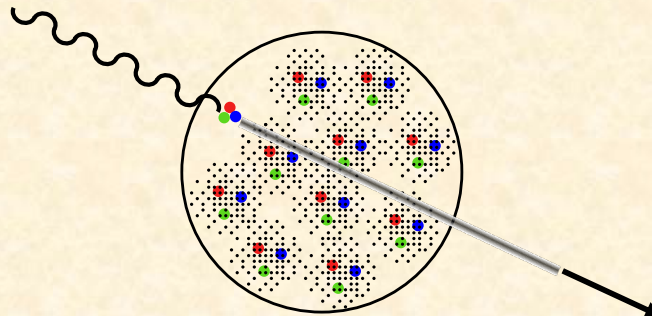
Nuclei should be described by quark and gluon degrees of freedom in principle; however, descriptions in terms of hadron degrees of freedom are often effective.

Color transparency and hadronization

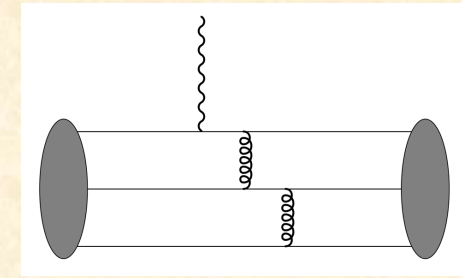
$(e, e'p)A$



Interact strongly
in the nuclear medium

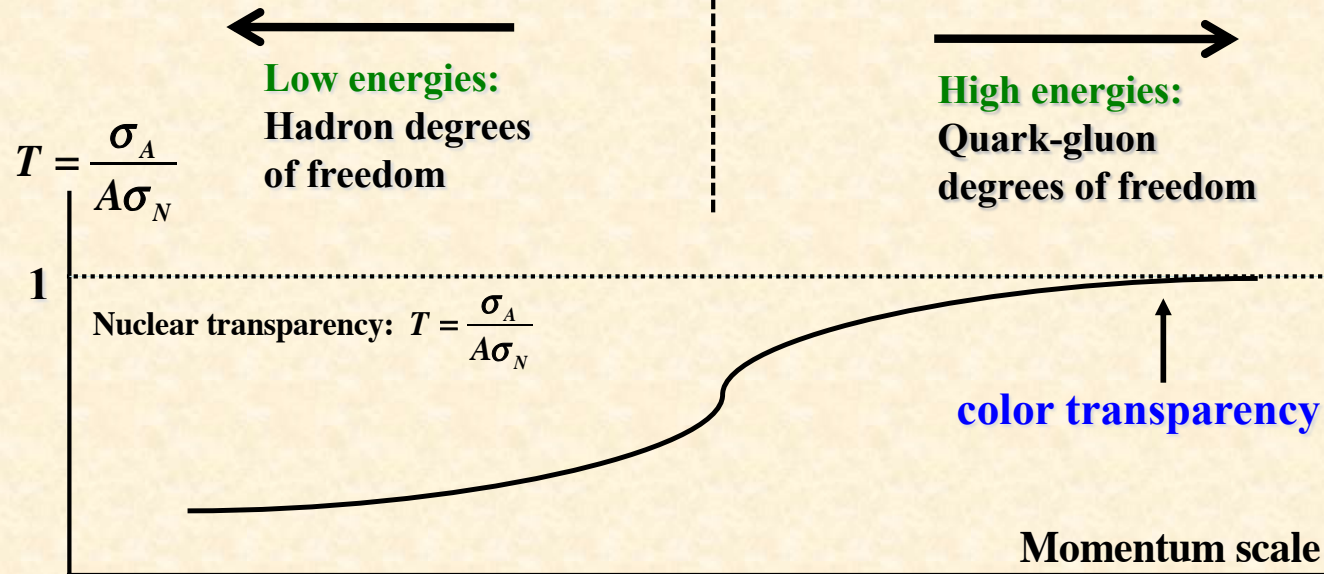


No interaction
in the nuclear medium



Hard gluon exchanges at high energies

- quarks are close with each other
- struck nucleon should be compact
- nucleon could pass through the medium without interaction (color transparency)



The color transparency is an important phenomena to understand the quark-hadron many-body systems from low to high energies and from low to high densities.

Mystery on color-transparency experiments

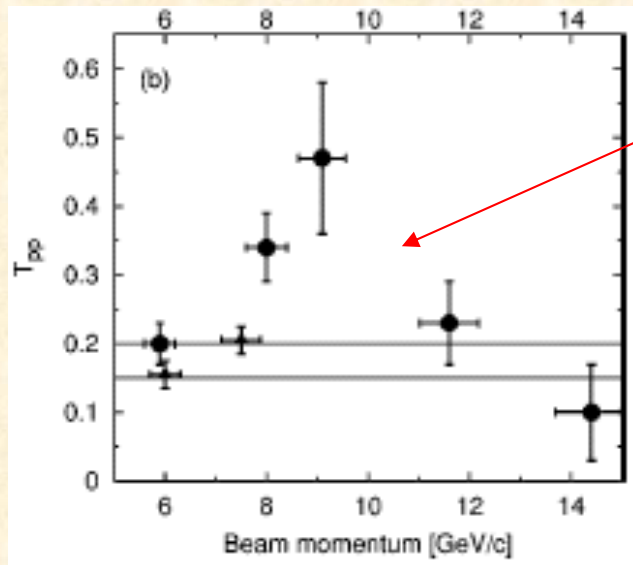
At large momentum transfer, a small-size hadron could freely pass through nuclear medium.

Experimentenets: $pA \rightarrow pp(A-1)$, $eA \rightarrow ep(A-1)$

Nuclear transparency: $T = \frac{\sigma_A}{A\sigma_N}$

Color transparency: $T \rightarrow \text{larger } (=1) \text{ as the hard scale} \rightarrow \text{larger}$

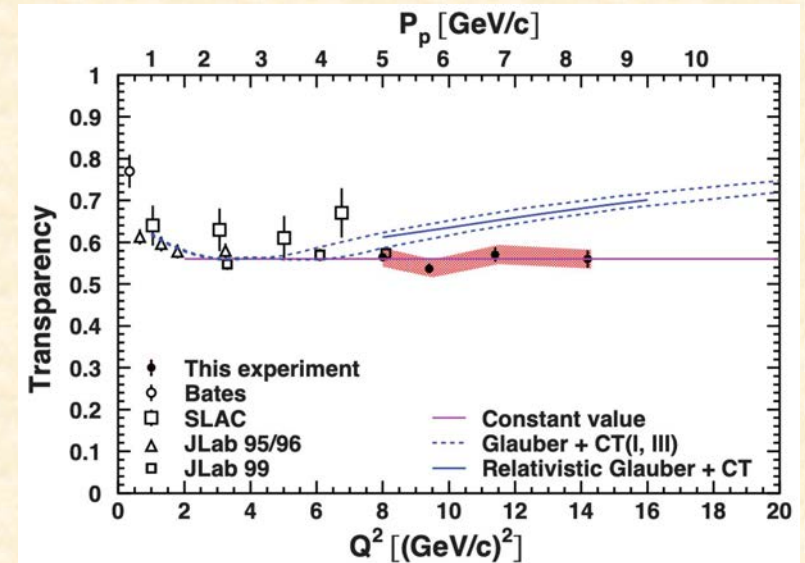
(BNL-EVA) J. Aclander *et al.*,
PRC 70 (2004) 015208



reason for this drop?

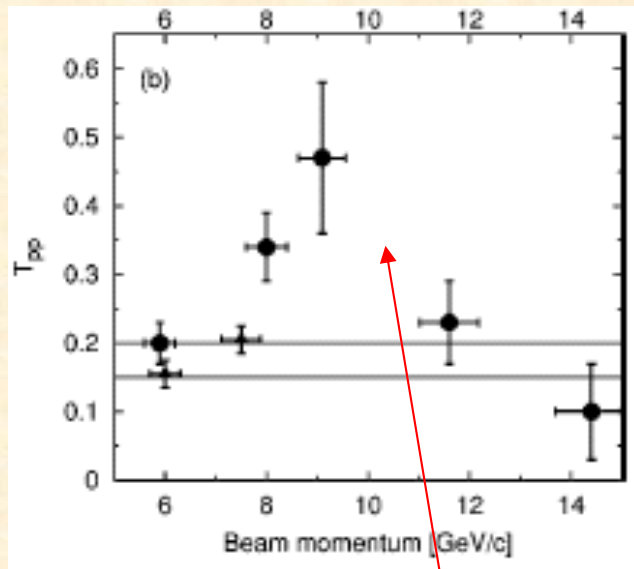
It should be checked
at hadron accelerator facilities
such as J-PARC.

JLab (Hall-C):
D. Bhetuwal *et al.*, PRL 126 (2021) 082301.



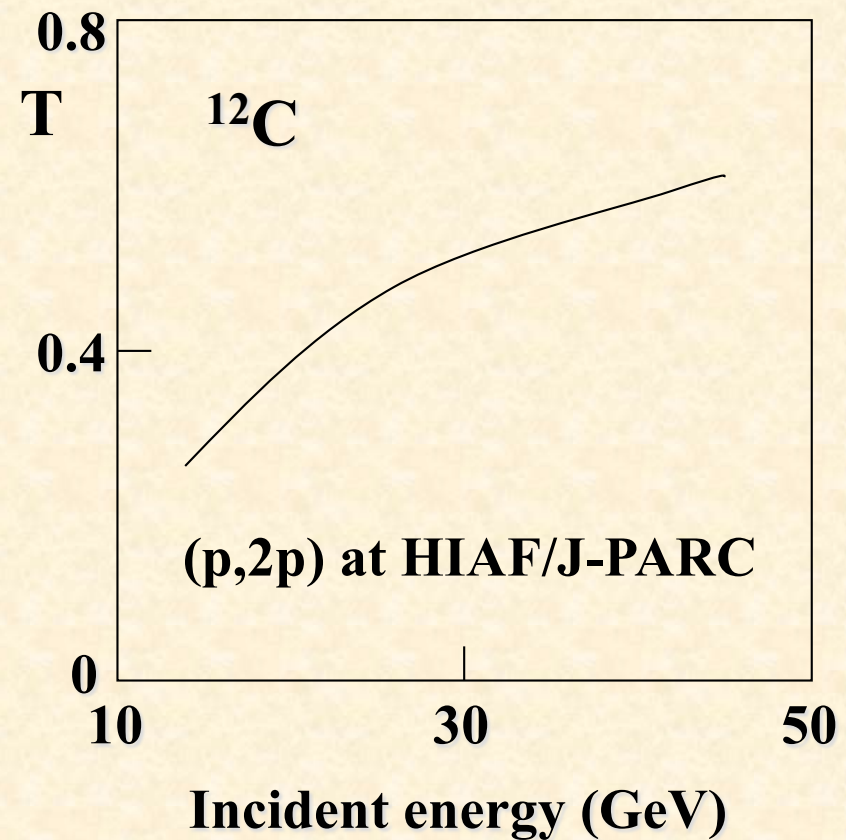
Color transparency at HIAF

(BNL-EVA) J. Aclander *et al.*,
PRC 70 (2004) 015208



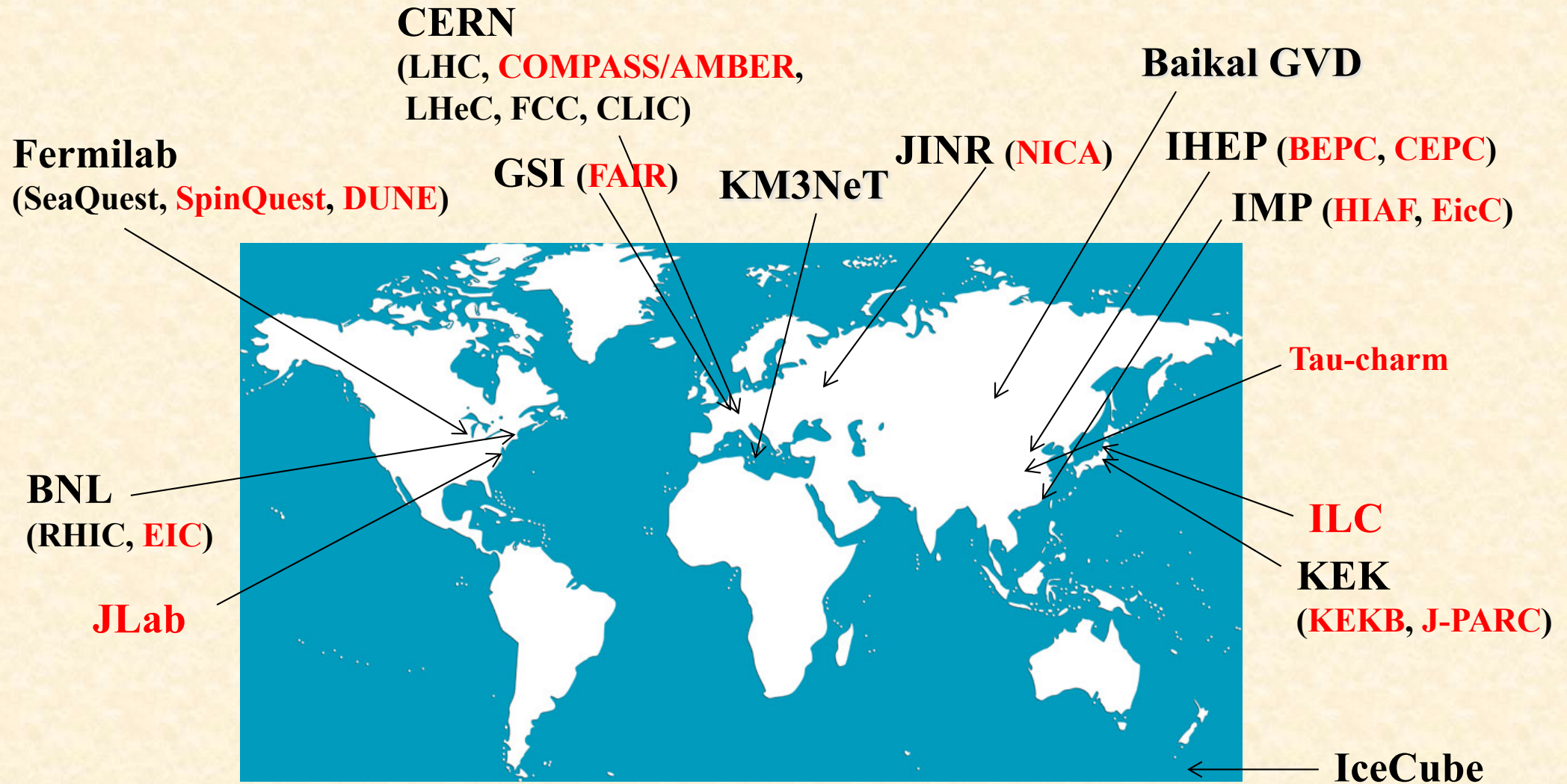
reason for this drop?

The mysterious BNL result could be clarified by possible HIAF/J-PARC experiments.



**Future prospects
on high-energy hadron physics
at hadron accelerator facilities**

High-energy hadron physics experiments

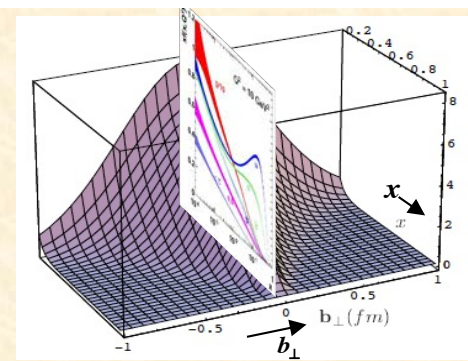


Facilities on hadron structure functions on GPDs including future possibilities.

By hadron tomography

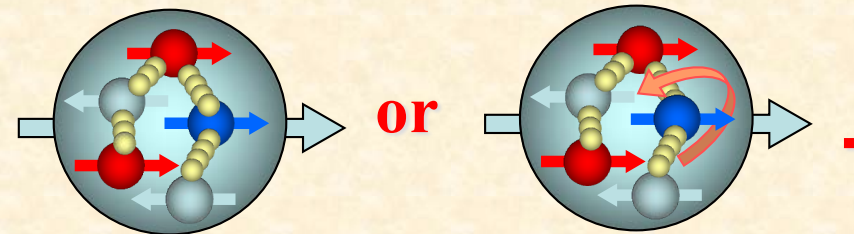


3D view
of hadrons

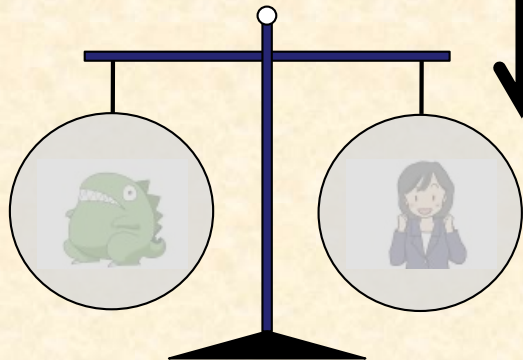


Origin of nucleon spin

By the tomography, we determine



Exotic hadrons



By tomography,
we determine

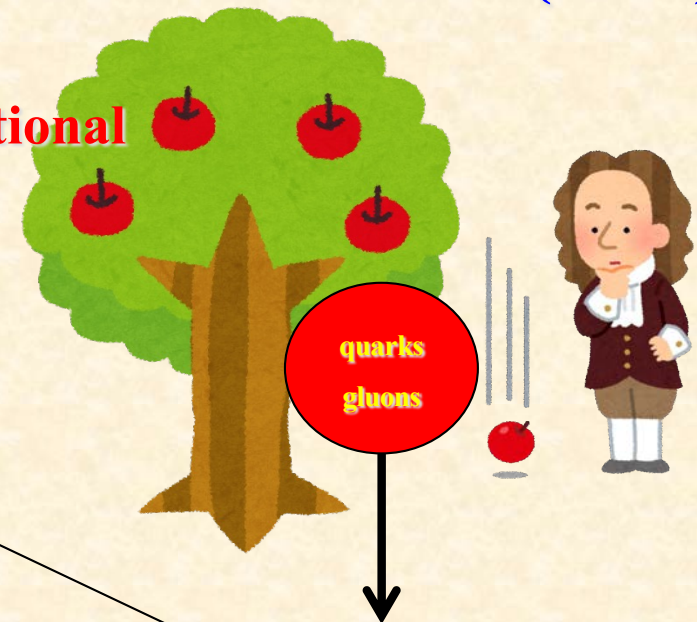


or



Origin of gravitational source (mass)

By tomography,
we determine gravitational
sources in terms of
quarks and gluons.



Summary

GPDs

**3D structure of hadrons, Origin of hadron masses and pressures,
Origin of nucleon spin, Exotic hadron structure**

Constituent-counting rule

**High energies = Quark and gluon degrees of freedom
It could be appropriate to use high-energy processes
for determination of internal configurations
of exotic-hadron candidates.**

Tensor polarization

New aspect in high-energy spin physics.

Color transparency

**Hadron interactions in nuclear medium
from low to high energies and from low to high densities.**

Hadron-experimental facilities

HIAF, J-PARC, GSI, NICA, Fermilab, LHC, AMBER, ...

The End

The End