



中山大學 物理与天文学院
SUN YAT-SEN UNIVERSITY SCHOOL OF PHYSICS AND ASTRONOMY

Probing Lepton-Number-Violating New Physics at Colliders

Gang Li (李刚)

School of Physics and Astronomy,
Sun Yat-sen University, Zhuhai

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Sept. 28, 2025, Beijing

Lepton number

Conserved quantum number in the SM:

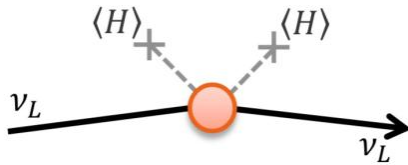
- In 1953, Konopinski and Mahmoud introduced the concept of **lepton number**, which must be conserved in reactions
- In 1959, Pontecorvo proposed that the lepton numbers of **electrons** and **muons** should be treated separately, which successfully explained the absence of $\mu \rightarrow e\gamma$ in experiments he conducted

Lepton	Conserved Quantity	Lepton Number	Anti-Lepton	Conserved Quantity	Lepton Number
e^-	L_e	+1	e^+	L_e	-1
ν_e		+1	$\bar{\nu}_e$		-1
μ^-	L_μ	+1	μ^+	L_μ	-1
ν_μ		+1	$\bar{\nu}_\mu$		-1
τ^-	L_τ	+1	τ^+	L_τ	-1
ν_τ		+1	$\bar{\nu}_\tau$		-1

L_e , L_μ and L_τ are each conserved quantities

Lepton number violation

- Majorana neutrino mass



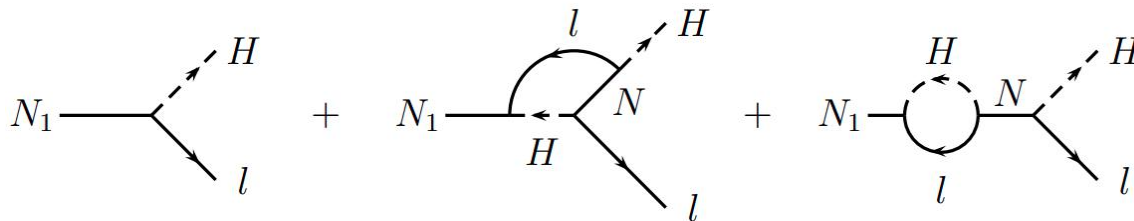
$$\mathcal{L}_M = \frac{C_5}{\Lambda} \left(\bar{L}^c \tilde{H}^* \right) \left(\tilde{H}^\dagger L \right) + \text{h.c.} \quad \Delta L = 2$$

$d = 5$ Weinberg operator

S. Weinberg 1979

a la eg. type-I, II, III seesaw mechanisms

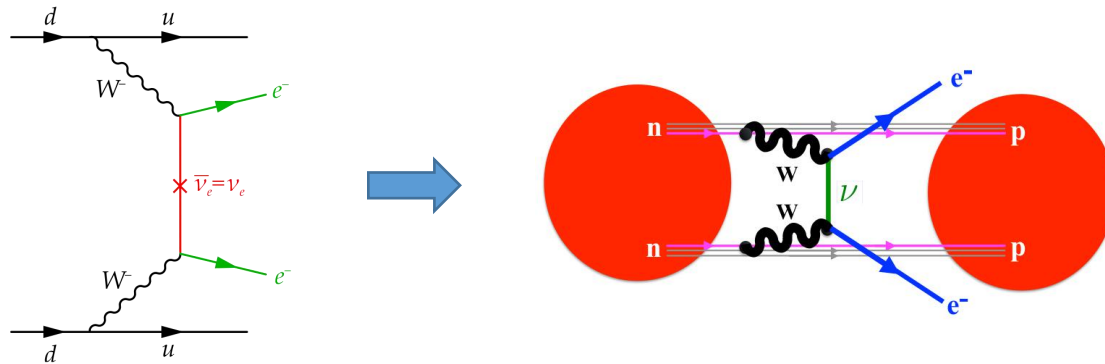
- Baryon Asymmetry in the Universe via leptogenesis



Fukugita, Yanagida, 1986

Neutrinoless double beta decay

$0\nu\beta\beta$ decay and Majorana nature of neutrinos



M. Goeppert-Mayer, Phys.Rev. 48 (1935) 512
W.H. Furry, Phys. Rev. 56 (1939) 1184

- Global experimental efforts: KamLAND-Zen, PandaX, CDEX, ...
- Current limit: $T_{1/2}^{0\nu}(\text{Xe}) > 3.8 \times 10^{26}$ year KamLAND-Zen, 2406.11438
- Future prospects: $T_{1/2}^{0\nu} \gtrsim 10^{28}$ year M. Agostini et al., Rev.Mod.Phys. 95 (2023) 2, 025002

Neutrinoless double beta decay

The most sensitive **low-energy** probe to date

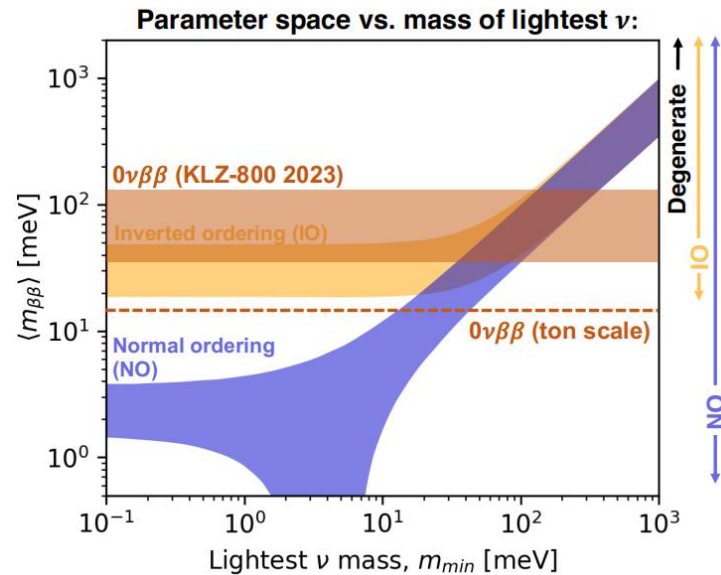
$$\left(T_{1/2}^{0\nu}\right)^{-1} = G_{0\nu} M_{0\nu}^2 \langle m_{\beta\beta} \rangle^2$$

$G_{0\nu}$: phase space factor
 $M_{0\nu}$: nuclear matrix element
 $\langle m_{\beta\beta} \rangle$: effective Majorana mass

In standard mechanism:

$$\langle m_{\beta\beta} \rangle = \left| \sum_i m_i U_{ei}^2 \right|$$

neutrino oscillation data as inputs



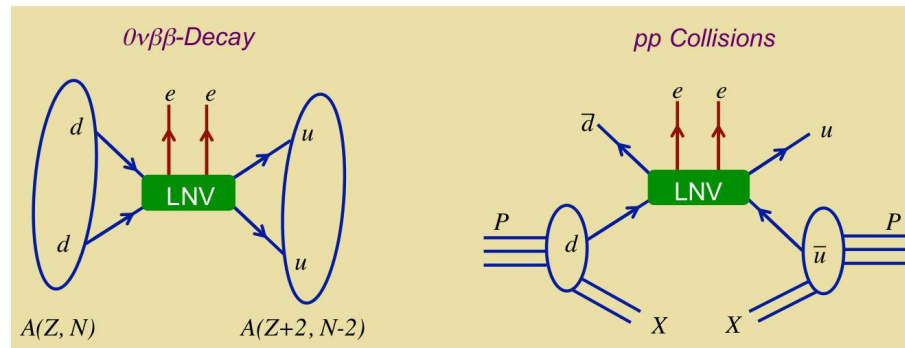
C. Adams, et al., 2212.11099

Collider opportunities

- $0\nu\beta\beta$ decay would undoubtedly imply the **Majorana nature** of neutrinos, irrespective of the origins of **$\Delta L = 2$ LNV interactions**

Schechter, Valle, Phys.Rev. D25 (1982) 774

- Complementary searches:



credit: M. Ramsey-Musolf

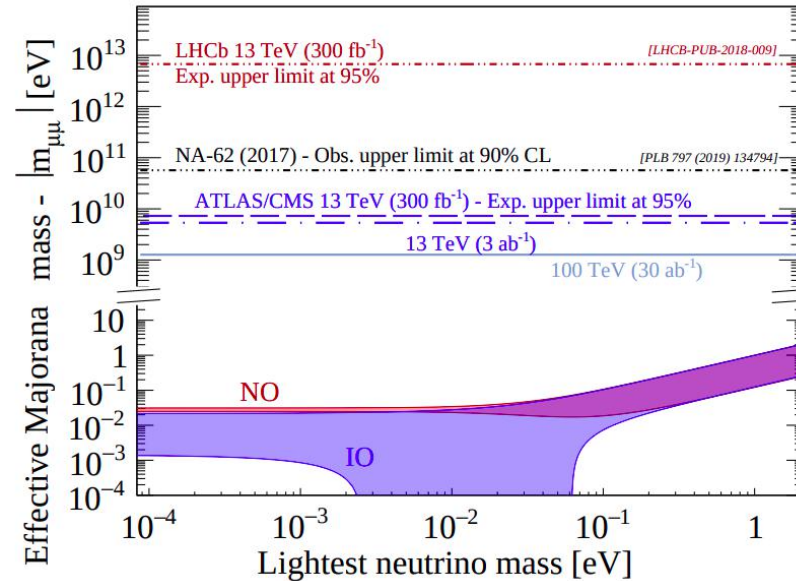
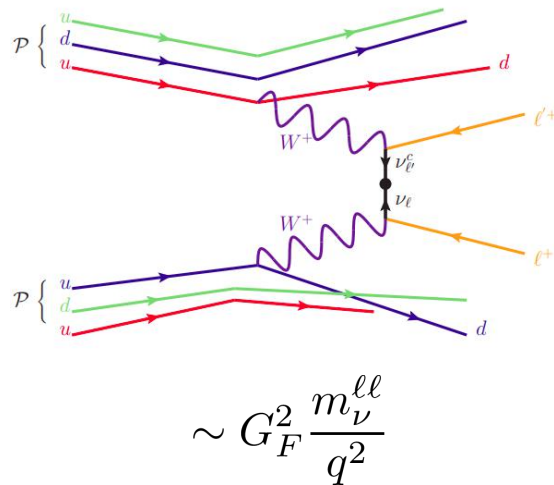
- smoking-gun signature **e^+e^+jj** , low SM backgrounds
- enhanced cross section from kinematics (**resonance, VBS**)
- more options of lepton flavors

VBS = vector boson scattering

LHC searches

- Probing Weinberg operator

VBS:



LHC Run 2

CMS : $|m_{\mu\mu}| \leq 10.8$ GeV CMS, 2206.08956 (PRL)

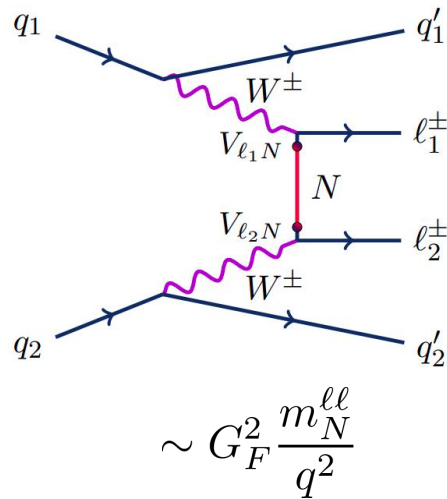
ATLAS : $|m_{\mu\mu}| \leq 16.7$ GeV ATLAS, 2305.14931 (EPJC)

low sensitivity due to large q^2

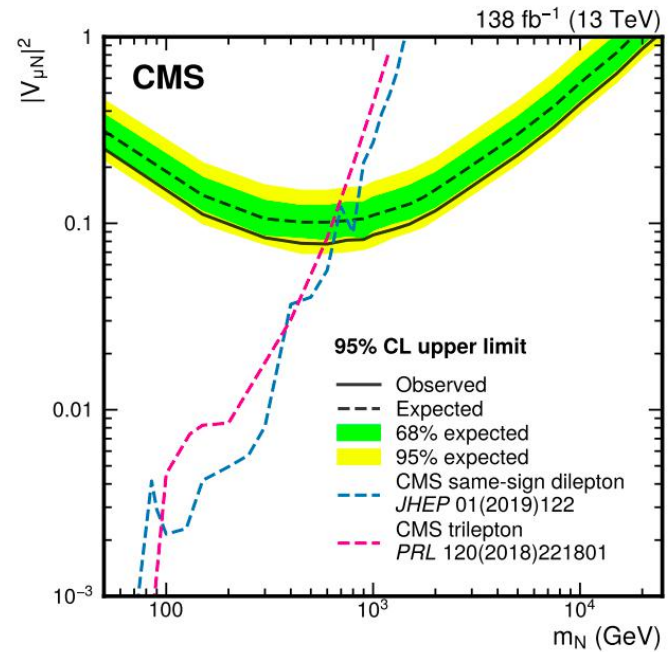
LHC searches

- Searching for sterile neutrino

VBS:



increased sensitivity due to large m_N

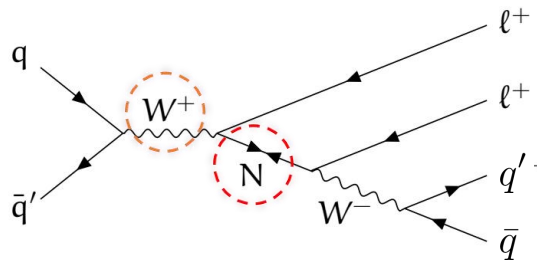


CMS, 2206.08956 (PRL)

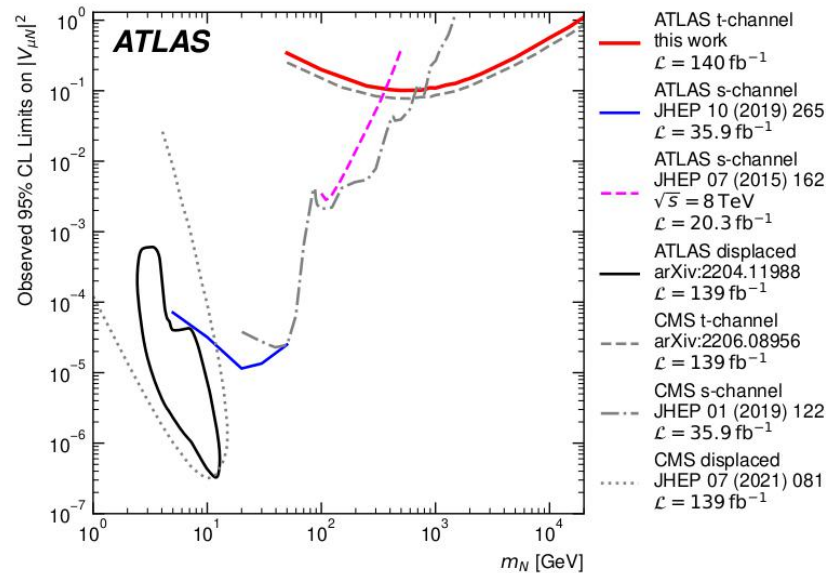
LHC searches

- Searching for sterile neutrino

Resonance:

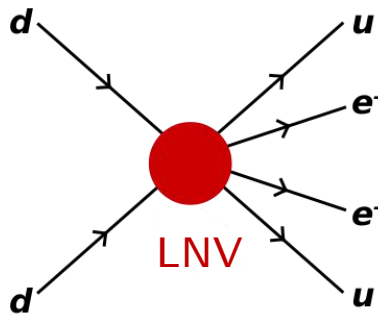


increased sensitivity for
 $m_N < m_W$



PoS LHCP2024 (2025) 032

EFT approach to LNV



LVN interactions

- LVN interactions have **odd** mass dimension

$$d \text{ is even} \iff |\Delta B - \Delta L| = 0, 4, 8, 12, \dots$$

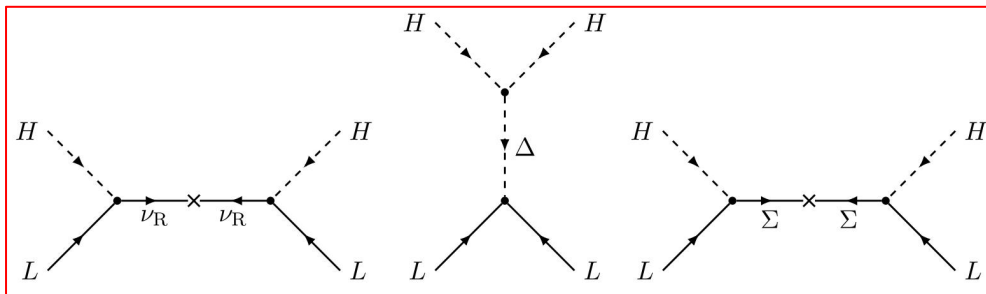
$$d \text{ is odd} \iff |\Delta B - \Delta L| = 2, 6, 10, 14, \dots$$

A. Kobach, 1604.05726 (PLB)

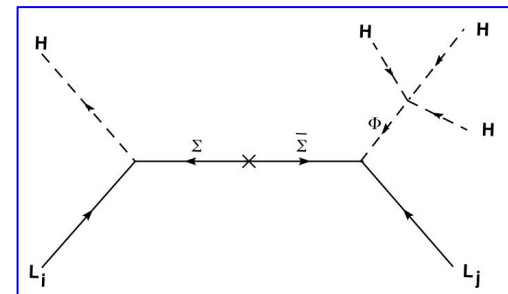
- Neutrino masses: $(\Delta B, \Delta L) = (0, \pm 2)$

$d = 5$ Weinberg operator: $(LH)(LH)$

$d = 7$ operator: $LLHH(H^\dagger H)$



Minkowski, 1977; Konetschny, Kummer, 1977;
Foot, Lew, He, Joshi, 1989



Babu, Nandi, Tavartkiladze,
0905.2710 (PRD)

$d = 7$ SMEFT

Operators with $(\Delta B, \Delta L) = (0, \pm 2)$

Type	$\mathcal{O}$	Operator
$\Psi^2 H^4$	$\mathcal{O}_{LH}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci} L_r^m) H^j H^n (H^\dagger H)$
$\Psi^2 H^3 D$	$\mathcal{O}_{LeHD}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci} \gamma_\mu e_r) H^j (H^m i D^\mu H^n)$
$\Psi^2 H^2 D^2$	$\mathcal{O}_{LHD1}^{pr}$	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci} D_\mu L_r^j) (H^m D^\mu H^n)$
	$\mathcal{O}_{LHD2}^{pr}$	$\epsilon_{im}\epsilon_{jn}(\overline{L}_p^{ci} D_\mu L_r^j) (H^m D^\mu H^n)$
$\Psi^2 H^2 X$	$\mathcal{O}_{LHB}^{pr}$	$g\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci} \sigma_{\mu\nu} L_r^m) H^j H^n B^{\mu\nu}$
	$\mathcal{O}_{LHW}^{pr}$	$g'\epsilon_{ij}(\epsilon\tau^I)_{mn}(\overline{L}_p^{ci} \sigma_{\mu\nu} L_r^m) H^j H^n W^{I\mu\nu}$
$\Psi^4 D$	$\mathcal{O}_{\bar{d}uLLD}^{prst}$	$\epsilon_{ij}(\overline{d}_p \gamma_\mu u_r) (\overline{L}_s^{ci} i D^\mu L_t^j)$
$\Psi^4 H$	$\mathcal{O}_{\bar{e}LLLLH}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\overline{e}_p L_r^i) (\overline{L}_s^{cj} L_t^m) H^n$
	$\mathcal{O}_{\bar{d}LueH}^{prst}$	$\epsilon_{ij}(\overline{d}_p L_r^i) (\overline{u}_s^c e_t) H^j$
	$\mathcal{O}_{\bar{d}LQLH1}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\overline{d}_p L_r^i) (\overline{Q}_s^{cj} L_t^m) H^n$
	$\mathcal{O}_{\bar{d}LQLH2}^{prst}$	$\epsilon_{im}\epsilon_{jn}(\overline{d}_p L_r^i) (\overline{Q}_s^{cj} L_t^m) H^n$
	$\mathcal{O}_{\bar{Q}uLLH}^{prst}$	$\epsilon_{ij}(\overline{Q}_p u_r) (\overline{L}_s^c L_t^i) H^j$

m_ν

two D^μ

one D^μ

L. Lehman, 1410.4193 (PRD);

Y. Liao and X.-D. Ma, 1607.07309 (JHEP)

$d = 9$ SMEFT

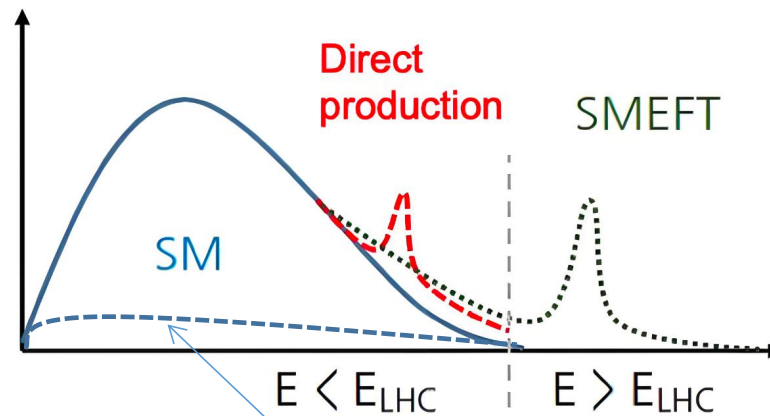
Operators with $(\Delta B, \Delta L) = (0, \pm 2)$

$L^2 H^4 H^{*2}$	$\mathcal{O}_{LLH^6} = \epsilon_{ik} \epsilon_{jl} (\overline{L^c, i} L^j) H^k H^l (H^\dagger H)^2$	m_ν
$e^2 H^4 D^2$	$\mathcal{O}_{eeH^4 D^2} = \epsilon_{ij} \epsilon_{kl} (\overline{e^c} e) (H^i D_\mu H^j) (H^k D^\mu H^l)$	
$L^2 H^3 H^{*} D^2$	$\mathcal{O}_{LLH^4 D^2 1} = \epsilon_{ik} \epsilon_{jl} (H^\dagger D_\mu H) (\overline{L^c, i} D^\mu L^j) H^k H^l$	two D^μ
	$\mathcal{O}_{LLH^4 D^2 2} = \epsilon_{ik} \epsilon_{jl} (H^\dagger D_\mu H) (\overline{L^c, i} L^j) H^k D^\mu H^l$	
	$\mathcal{O}_{LLH^4 D^2 3} = \epsilon_{ik} \epsilon_{jl} (H^\dagger H) (\overline{D_\mu L^c, i} D^\mu L^j) H^k H^l$	
	$\mathcal{O}_{LLH^4 D^2 4} = \epsilon_{ik} \epsilon_{jl} (H^\dagger H) (\overline{L^c, i} D_\mu L^j) D^\mu H^k H^l$	
	$\mathcal{O}_{LLH^4 D^2 5} = \epsilon_{ik} \epsilon_{jl} (H^\dagger H) (\overline{L^c, i} D_\mu L^j) H^k D^\mu H^l$	
	$\mathcal{O}_{LLH^4 D^2 6} = \epsilon_{ik} \epsilon_{jl} (H^\dagger D_\mu H) (\overline{L^c, i} i \sigma^{\mu\nu} L^j) D_\nu H^k H^l$	
$ud^* L^2 H H^* D$	$\mathcal{O}_{dLuLH^2 D 1} = \epsilon_{ij} (\overline{d} L^i) (\overline{u^c} \gamma_\mu L^j) (H^\dagger i D^\mu H)$	one D^μ
	$\mathcal{O}_{dLuLH^2 D 2} = \epsilon_{ik} \epsilon_{jl} (\overline{d} L^i) (\overline{u^c} \gamma_\mu L^j) \tilde{H}^k i D^\mu H^l$	
	$\mathcal{O}_{dLuLH^2 D 3} = \epsilon_{ij} (\overline{d} L^i) (\overline{u^c} \gamma_\mu L^j) [(i D^\mu H)^\dagger H]$	
	$\mathcal{O}_{dLuLH^2 D 4} = \epsilon_{ik} \epsilon_{jl} (\overline{d} L^i) (\overline{u^c} \gamma_\mu L^j) (i D^\mu \tilde{H})^k H^l$	
	$\mathcal{O}_{duLLH^2 D} = \epsilon_{ik} \epsilon_{jl} (\overline{d} \gamma_\mu u) (\overline{L^c, i} i D_\mu L^j) \tilde{H}^k H^l$	

- imcomplete list here
- 384 for one generation

EFTs at the LHC

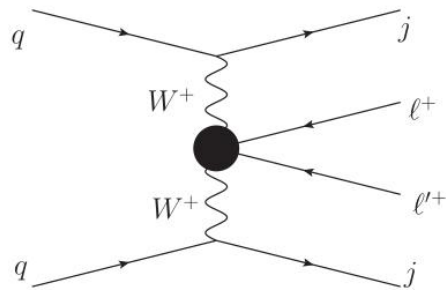
SMEFT paradigm:



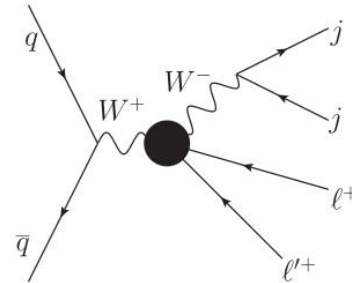
For the searches for LNV signals, there is almost no SM background

EFTs at the LHC

Operators with **two** covariant derivatives

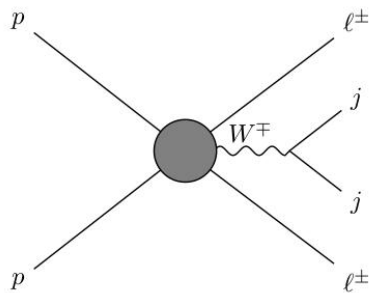


$d = 7, 9$

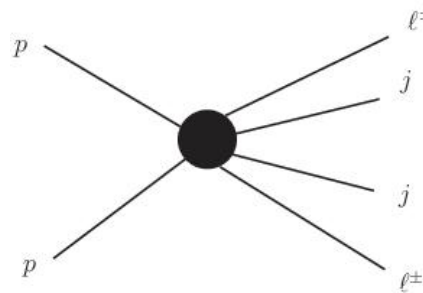


$d = 7, 9$

Operators with **one** or **zero** covariant derivative



$d = 7, 9$



$d = 9$

EFTs at the LHC

Operators with **two** covariant derivatives:

$$\left. \begin{aligned} & \frac{C_{\ell\ell'}^{(7)}}{\Lambda_{\text{LNV}}^3} \left(\bar{\tilde{L}}_{\ell} D_{\mu} L_{\ell'} \right) \left(\tilde{H}^{\dagger} D^{\mu} H \right) + \text{H.c.} \\ & \frac{C_{\ell\ell'}^{(9)}}{\Lambda_{\text{LNV}}^5} \bar{\ell}_R^c \ell'_R \left(\tilde{H}^{\dagger} D_{\mu} H \right)^2 \end{aligned} \right\} \bar{\ell}_R^c \ell'_R W_{\mu}^{+} W^{+\mu}$$

At the HL-LHC,

M. Aoki, K. Enomoto, S. Kanemura, 2002.12265 (PRD)

- $pp \rightarrow \mu^{+} \mu^{+} jj$

$$\Lambda_{\text{LNV}}^{(7)} \gtrsim 1.8 \text{ TeV}, \quad \Lambda_{\text{LNV}}^{(9)} \gtrsim 0.71 \text{ TeV}$$

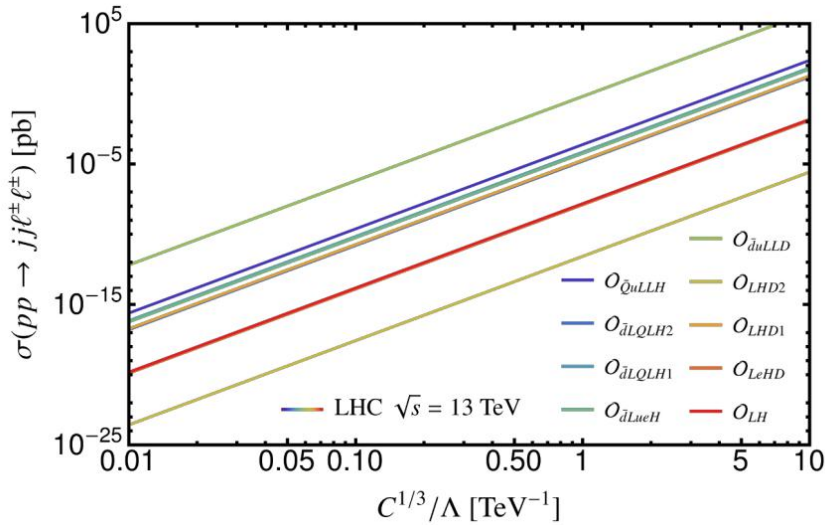
- $pp \rightarrow e^{+} \mu^{+} jj$

$$\Lambda_{\text{LNV}}^{(7)} \gtrsim 2.3 \text{ TeV}, \quad \Lambda_{\text{LNV}}^{(9)} \gtrsim 0.82 \text{ TeV}$$

EFTs at the LHC

Operators with **one** covariant derivatives:

$$\mathcal{O}_{\bar{d}uLLD}^{prst} = \epsilon_{ij} (\bar{d}_p \gamma_\mu u_r) (\bar{L}_s^c i D^\mu L_t^j)$$

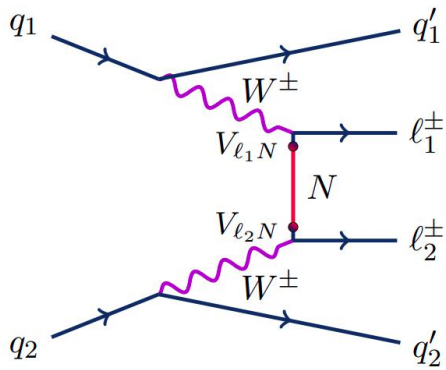


Operator	$\sigma(pp \rightarrow \mu^\pm \mu^\pm jj)$ (pb)		Λ_{LNV} [TeV]	$\Lambda_{\text{LNV}}^{\text{future}}$ [TeV]
	LHC	FCC		
$\mathcal{O}_{\bar{Q}uLLH}$	2.4×10^{-4}	0.11	1.4	5.4
$\mathcal{O}_{\bar{d}LQLH2}$	1.5×10^{-5}	4.3×10^{-3}	0.90	3.1
$\mathcal{O}_{\bar{d}LQLH1}$	6.9×10^{-5}	0.030	1.1	4.3
$\mathcal{O}_{\bar{d}LueH}$	5.7×10^{-5}	0.035	1.1	4.5
$\mathcal{O}_{\bar{d}uLLD}$	0.64	210	5.0	19
$\mathcal{O}_{LHD2}$	2.7×10^{-12}	1.7×10^{-10}	0.075*	0.18
$\mathcal{O}_{LHD1}$	1.9×10^{-5}	0.061	1.1	4.9
$\mathcal{O}_{LeHD}$	1.2×10^{-8}	3.1×10^{-8}	0.21*	0.44
$\mathcal{O}_{LH}$	1.5×10^{-8}	2.0×10^{-6}	0.35*	0.87

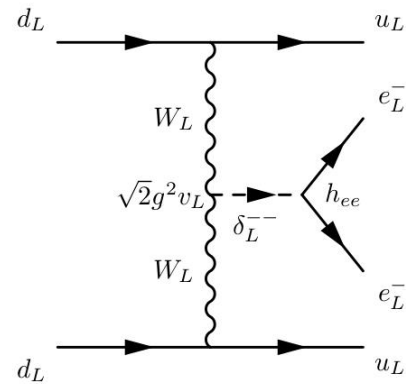
K. Fridell, L. Gráf, J. Harz, C. Hati, 2306.08709 (JHEP)

UV completions at the LHC

UVs for operators with *two* derivatives:

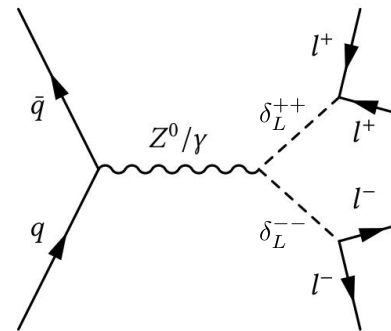
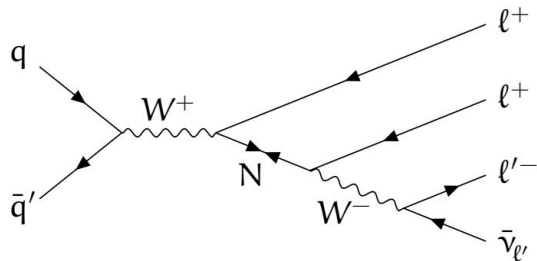


type-I seesaw



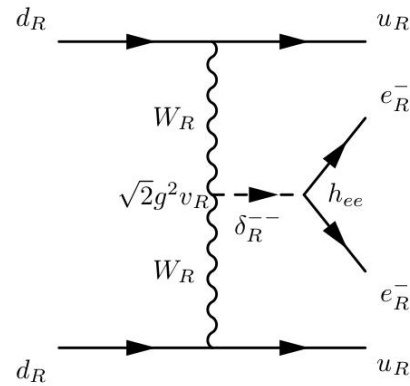
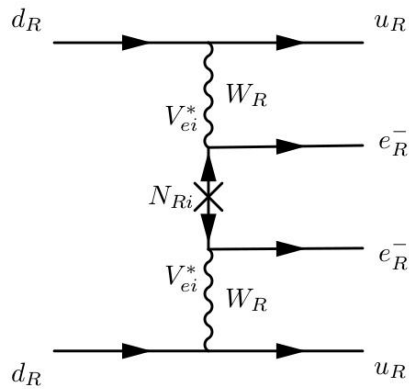
type-II seesaw

New channels:



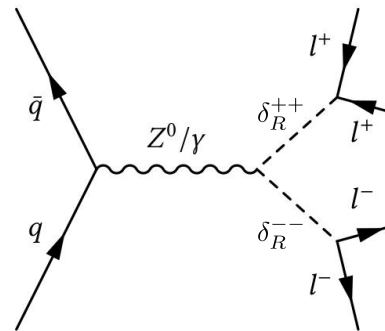
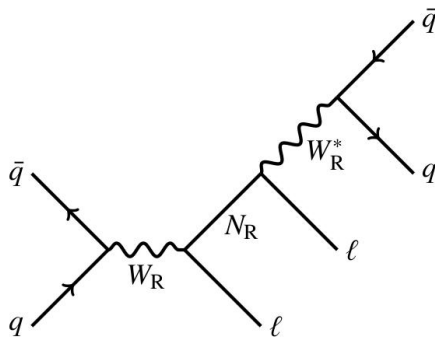
UV completions at the LHC

UVs for operators with zero derivative:



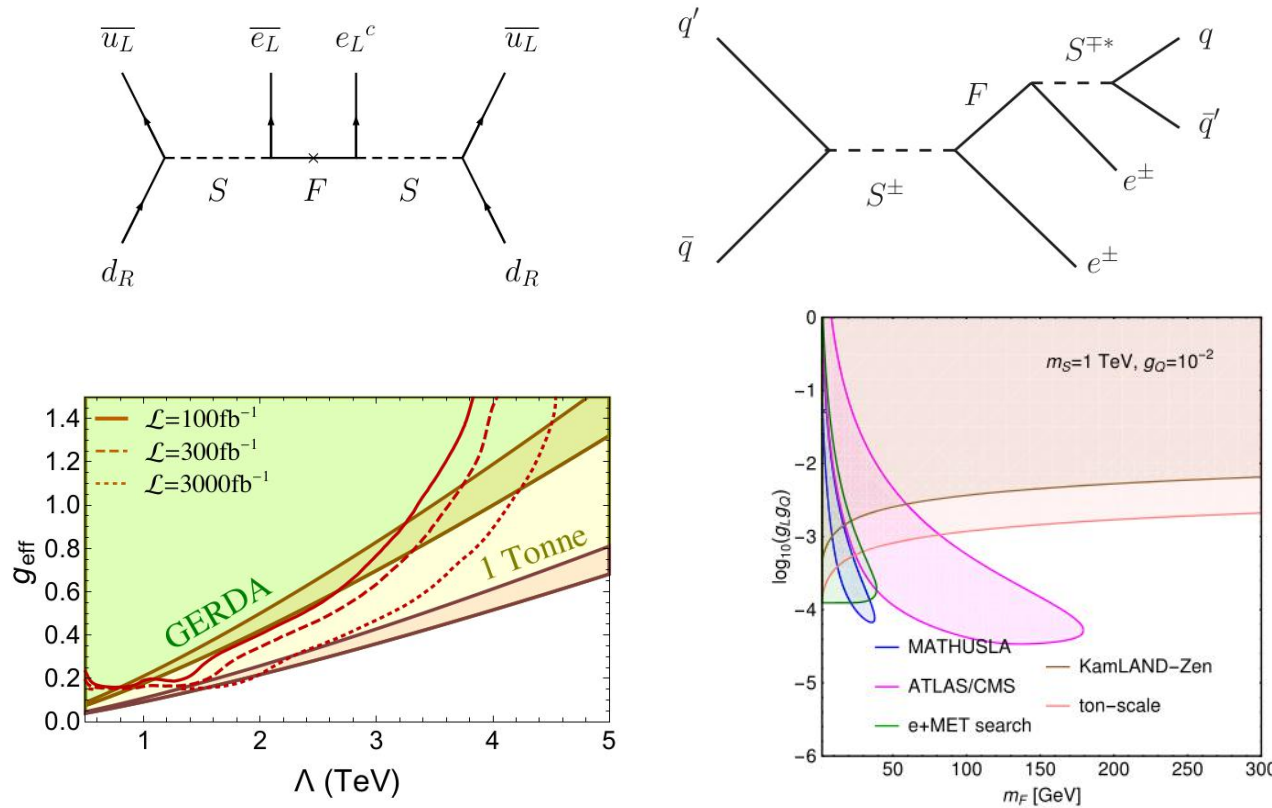
left-right symmetric models

New channels:



UV completions at the LHC

UVs for operators with zero derivative:



template: SUSY

T. Peng, M. J. Ramsey-Musolf,
P. Winslow, 1508.04444 (PRD)

GL, M. J. Ramsey-Musolf, S. Su,
J. C. Vazquez, 2109.08172 (PRD)

UV completions at the LHC

UVs for $d = 7$ operator with *one* derivative:

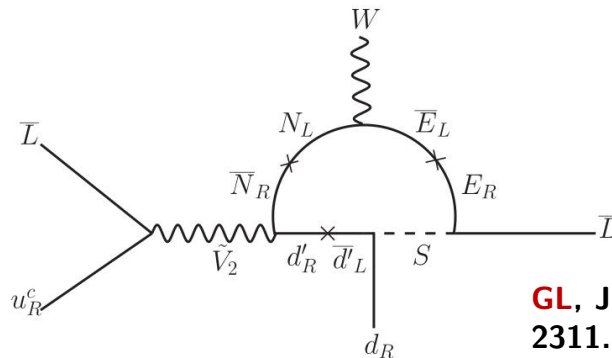
$$\mathcal{O}_{\bar{d}uLLD}^{prst} = \epsilon_{ij} (\bar{d}_p \gamma_\mu u_r) (\bar{L}_s^c i D^\mu L_t^j)$$

It must originate from a UV-completion containing a fermion mediator:

$$\mathcal{L}_{\text{eff}}^\Psi = \frac{\partial \mathcal{L}_\Psi^{\text{int}}}{\partial \bar{\Psi}} \left(\frac{1}{m_\Psi^2} + \frac{D^2 + \frac{1}{2} X_{\mu\nu} \sigma^{\mu\nu}}{m_\Psi^4} + \dots \right) (i \not{D} + m_\Psi) \frac{\partial \mathcal{L}_\Psi^{\text{int}}}{\partial \Psi}$$

K. Fridell, L. Gráf, J. Harz, C. Hati,
2412.14268 (JHEP)

- No tree-level UV completion
- Example for one-loop UV completion:



GL, J.-H. Yu, X. Zhao,
2311.10079 (PRD)

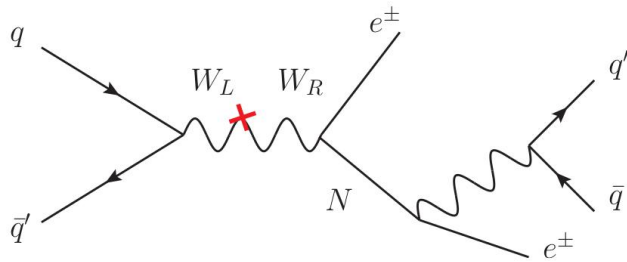
UV completions at the LHC

UVs for $d = 9$ operator with *one* derivative:

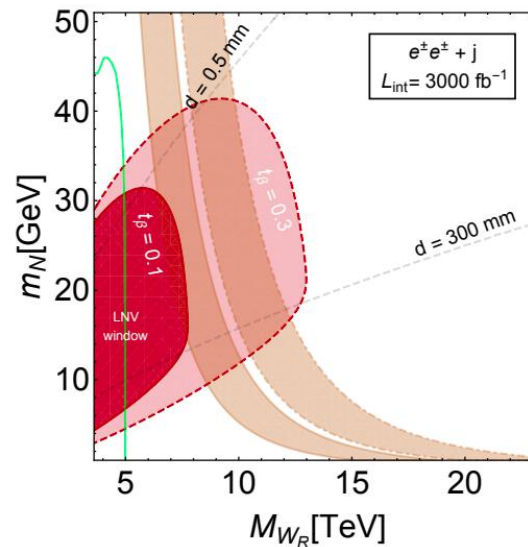
$$\mathcal{O}_{u\bar{d}e^2H^2D}^{(1)} = \epsilon^{ij} \left(\bar{d}_t^a \gamma^\mu e_r \right) (u_{sa} C e_p) H_j D_\mu H_i$$

H.-L. Li, et al., 2007.07899 (PRD)

$W_L - W_L$ mixing:
$$\begin{pmatrix} W_L^\pm \\ W_R^\pm \end{pmatrix} = \begin{pmatrix} \cos \zeta & -\sin \zeta \\ \sin \zeta & \cos \zeta \end{pmatrix} \begin{pmatrix} W_1^\pm \\ W_2^\pm \end{pmatrix}$$



GL, M. J. Ramsey-Musolf, J. C. Vasquez,
2202.01789 (PRD)



UV completions at the LHC

UVs for $d = 9$ operator with *one* derivative:

$$\mathcal{O}_{u\bar{d}e^2 H^2 D}^{(1)} = \epsilon^{ij} \left(\bar{d}_t^a \gamma^\mu e_r \right) (u_{sa} C e_p) H_j D_\mu H_i$$

H.-L. Li, et al., 2007.07899 (PRD)

Leptoquark model:

$$\begin{aligned} \mathcal{L} \supset & \lambda_{ed} (\bar{d}_R \gamma_\mu e_R) U_1^\mu + \lambda_{u\Psi} \tilde{R}_2^* \bar{u}_R^c \Psi_R \\ & + \lambda_{DH} U_1^{\mu\dagger} \tilde{R}_2 \epsilon (i D_\mu H) + f_{\Psi e} \bar{\Psi}_L H e_R + \text{H.c.} \end{aligned}$$

template: SUSY

leptoquarks:

$$\tilde{R}_2 \in (3, 2, 1/6), \quad U_1 \in (3, 1, 2/3)$$

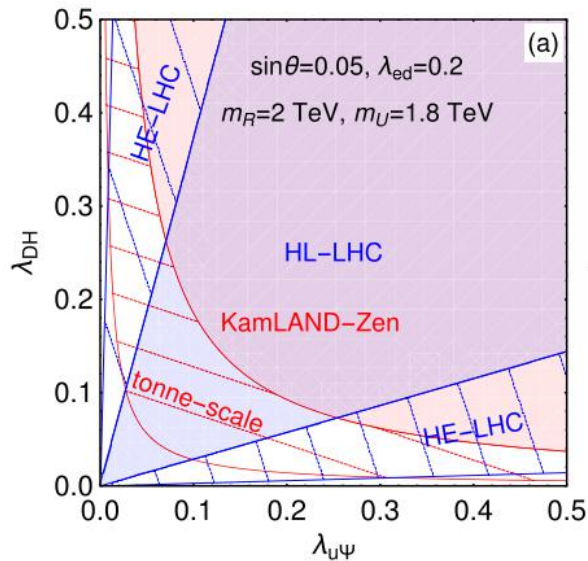
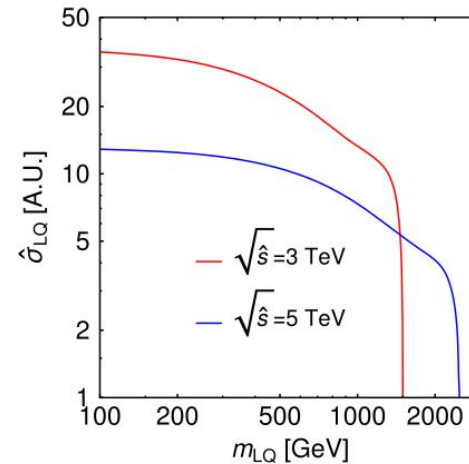
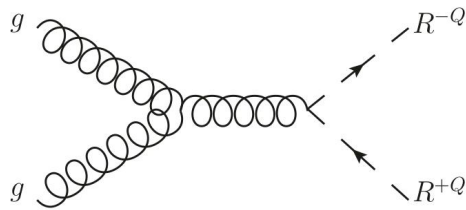
vector-like fermions:

GL, J.-H. Yu, X. Zhao, 2311.10079 (PRD)

$$\Psi_L = \begin{pmatrix} N_L \\ E_L \end{pmatrix}, \quad \Psi_R = \begin{pmatrix} N_R \\ E_R \end{pmatrix}$$

UV completions at the LHC

Leptoquark pair production

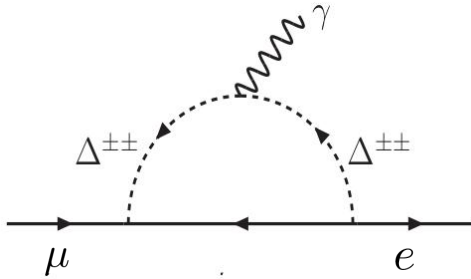


- Sensitive to the leptoquark mass
- LHC searches for TeV scale LNV are complementary to $0\nu\beta\beta$ decay searches

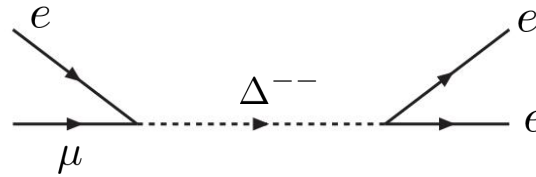
GL, J.-H. Yu, X. Zhao, 2311.10079 (PRD)

A light doubly-charged scalar

Charged lepton flavor violation:



$$\frac{m_{\Delta_L^{\pm\pm}}}{\sqrt{|\sum_{\ell} (f_L)_{\mu\ell}^{\dagger} (f_L)_{e\ell}|}} > 65 \text{ TeV}$$



$$\frac{m_{\Delta_L^{\pm\pm}}}{\sqrt{|(f_L)_{ee}^{\dagger} (f_L)_{e\mu}|}} > 208 \text{ TeV}$$

In the **type-II seesaw model**, the Yukawa couplings are correlated with the neutrino masses and mixings:

$$\Delta_L = \begin{pmatrix} \Delta_L^+/\sqrt{2} & \Delta_L^{++} \\ \Delta_L^0 & -\Delta_L^+/\sqrt{2} \end{pmatrix} \quad m_{\nu} = \sqrt{2} f_L v_L = U \hat{m}_{\nu} U^T$$

$\Delta_L^{\pm\pm}$ can be $O(1)$ TeV only if all Yukawa couplings $f_L^{\ell\ell'} \lesssim 10^{-3}$

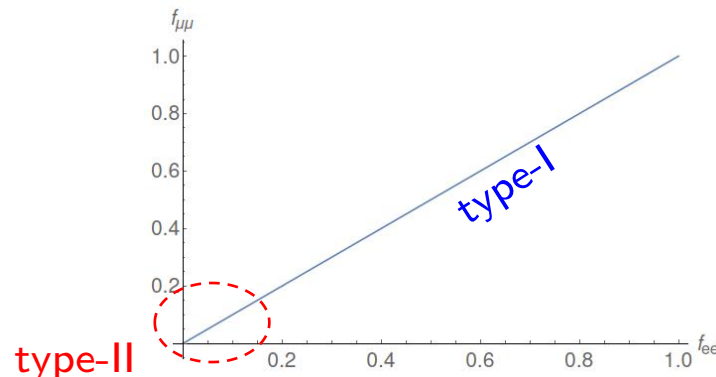
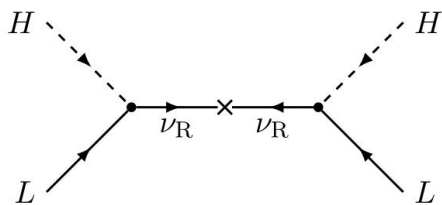
A light doubly-charged scalar

In the minimal left-right symmetric model

$$f_L = f_R \quad (\text{parity}) \qquad f_L = f_R^\dagger \quad (\text{charge conjugation})$$

- If neutrinos obtain masses via the **type-II seesaw mechanism**, Δ_R^{++} can be $O(1)$ TeV only if all Yukawa couplings $f_R^{\ell\ell'} \lesssim 10^{-3}$
- If neutrinos obtain masses via the **type-I seesaw mechanism**, $\Delta_{L,R}^{++}$ can be $O(1)$ TeV if $f_{L,R}$ are **diagonal**

$$m_\nu = -M_D M_R^{-1} M_D^T, \quad M_R = \sqrt{2} f_R v_R$$



A light doubly-charged scalar

In left-right symmetric model with D -parity breaking

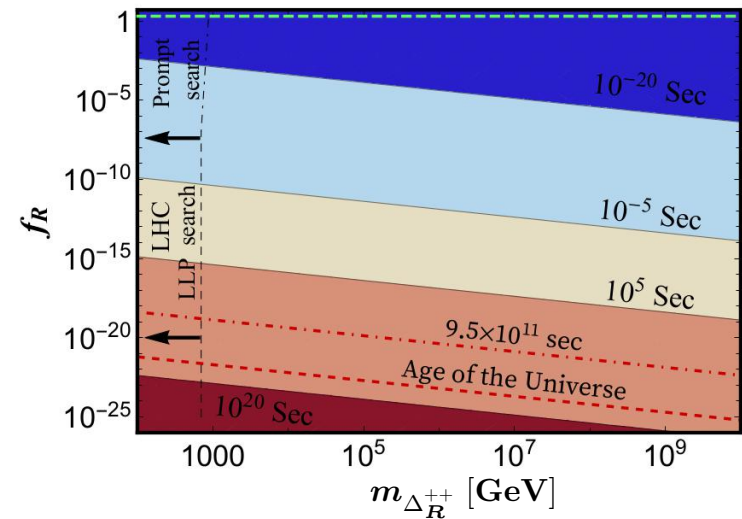
$$SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L} \otimes P \rightarrow SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$$

mass spectra:

Chang, Mohapatra, Parida, Phys.Rev.Lett. 52
(1984) 1072; Phys.Rev.D 30 (1984) 1052

$$\begin{aligned}\mu_{\Delta_L}^2 &= \mu_{\Delta}^2 + M\langle\eta\rangle + \lambda_2\langle\eta\rangle^2 \\ \mu_{\Delta_R}^2 &= \mu_{\Delta}^2 - M\langle\eta\rangle + \lambda_2\langle\eta\rangle^2\end{aligned}$$

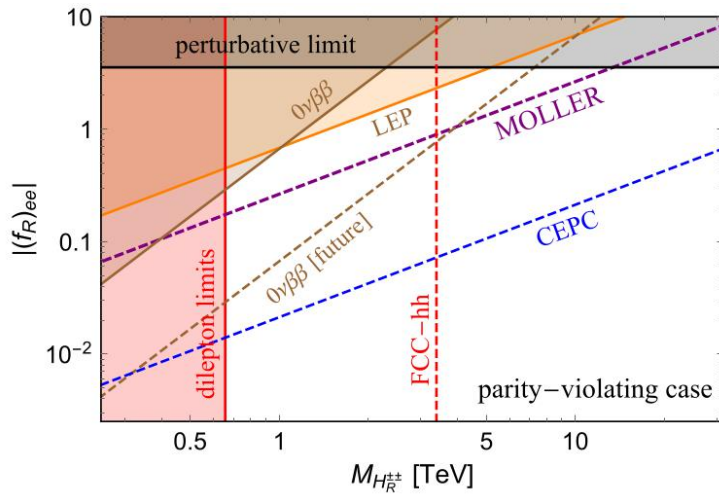
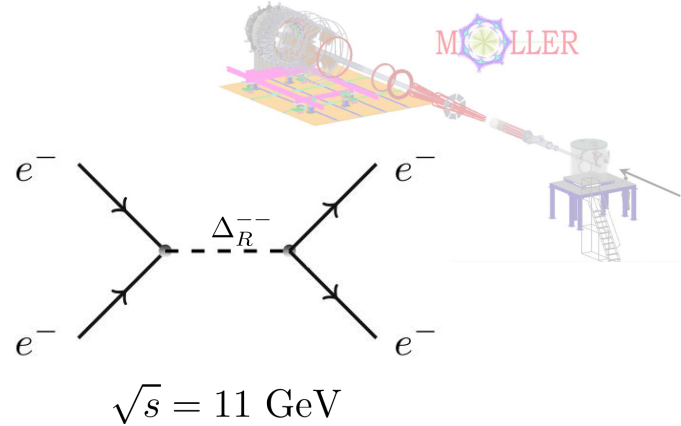
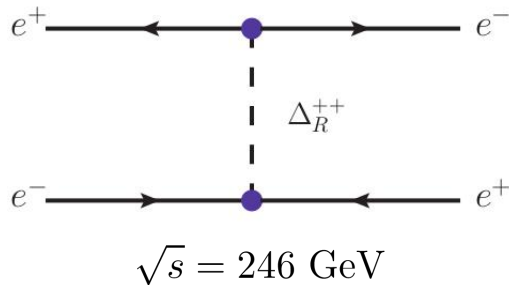
Δ_L^{++} is at the D -parity breaking scale,
while Δ_R^{++} can be much lighter, and the
Yukawa coupling matrix f_R is **arbitrary**



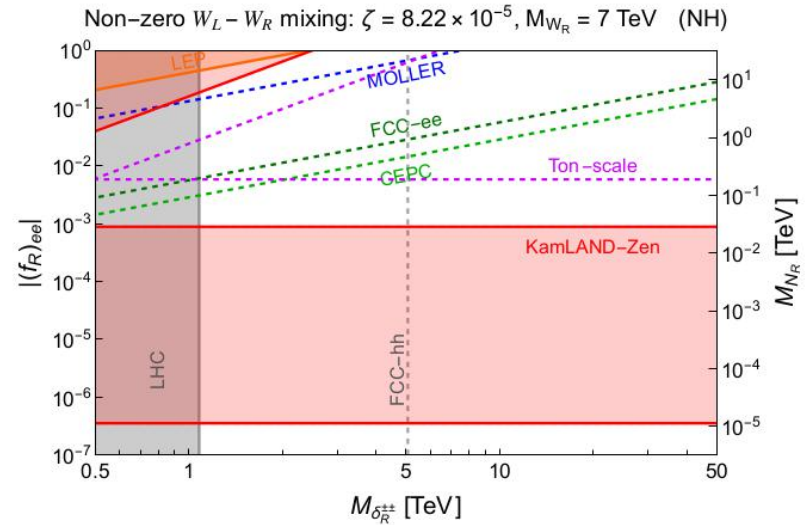
E. Akhmedov, et al., 2401.15145 (PLB)

LN V at lepton colliders

- CEPC/FCC-ee, MOLLER



P. S. Bhupal Dev, M. J. Ramsey-Musolf,
Y. Zhang, 1806.08499 (PRD)



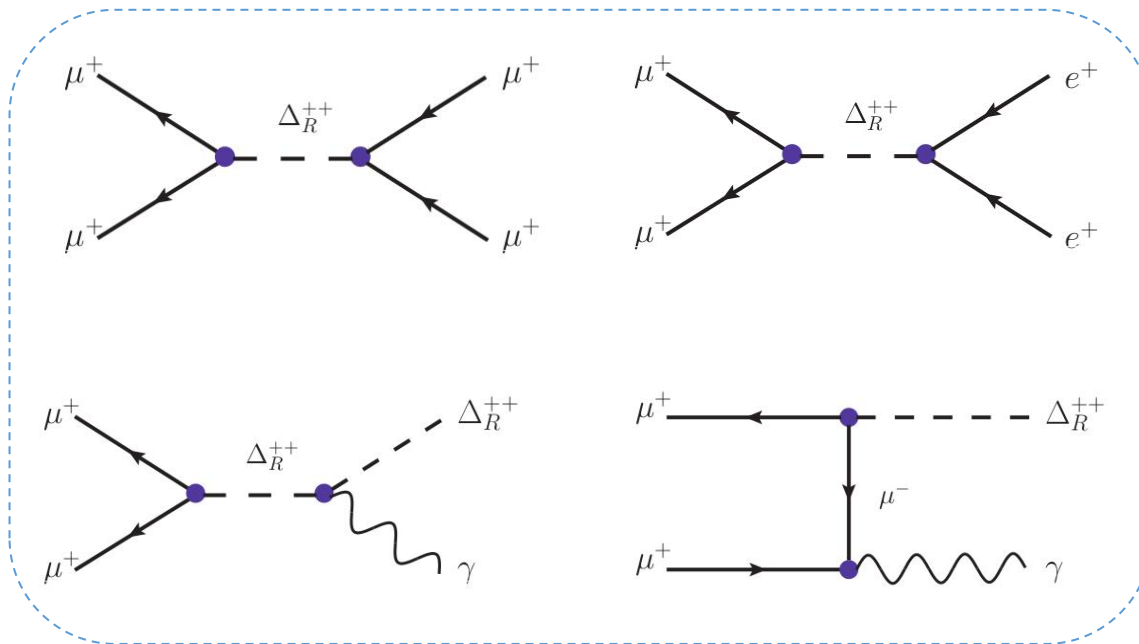
GL, M. J. Ramsey-Musolf, S. Urrutia
Quiroga, J. C. Vasquez, 2408.06306

LVN at lepton colliders

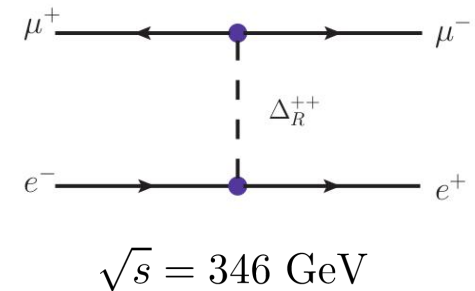
- μ TRISTAN

μ^+ beam obtained from ultra-cold muon technology developed for the muon $g - 2$ experiment at J-PARC is accelerated up to 1 TeV

Y. Hamada, et al., Prog. 2201.06664 (PTEP)



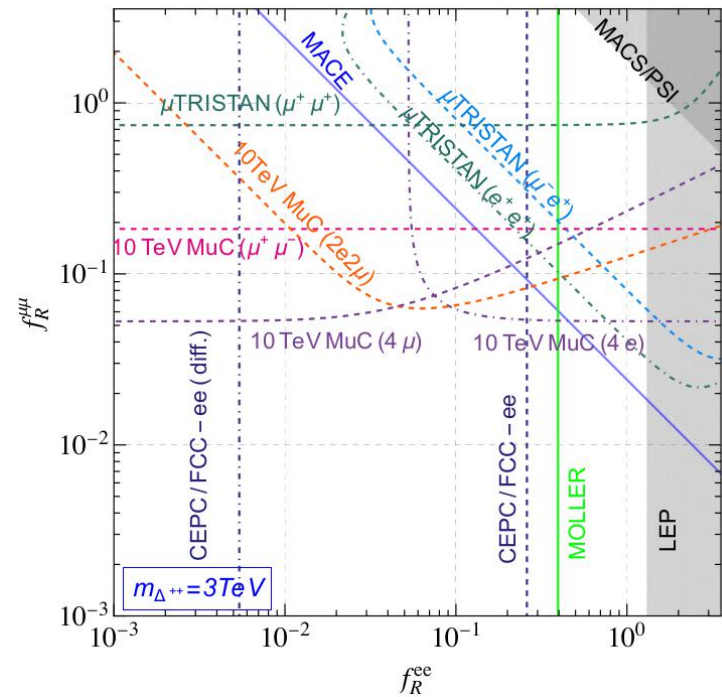
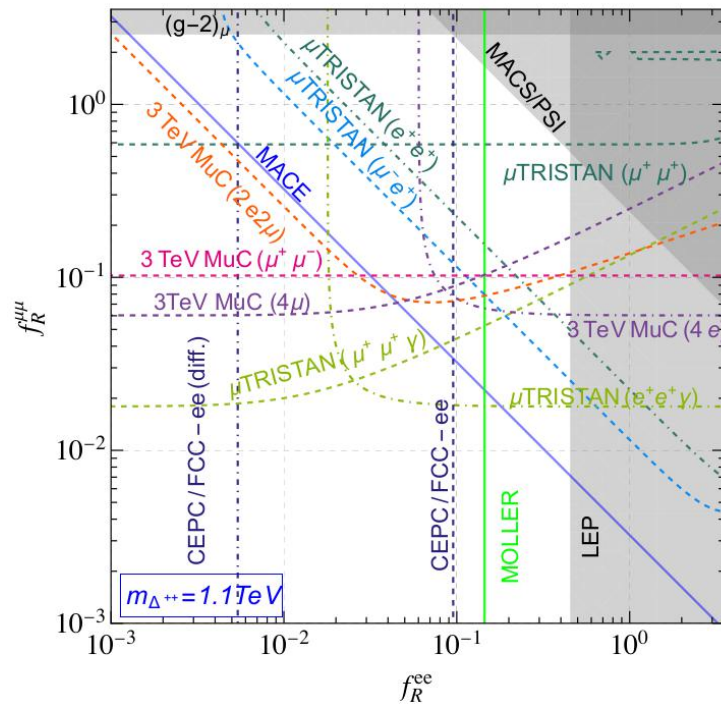
$$\sqrt{s} = 2 \text{ TeV}$$



$$\sqrt{s} = 346 \text{ GeV}$$

LVN at lepton colliders

Low- and high-energy probes of diagonal couplings



GL, Jin Sun, 2510.xxxxx

Summary

- Colliders provide unique opportunities for probing lepton-number-violating new physics
- EFTs help to identify optimal LNV interactions, which are constructed using covariant derivatives
- UV completions for SMEFT with 0, 1, 2 covariant derivatives are discussed
- We investigate the sensitivity of lepton colliders to a specific LNV scenario: a light doubly-charged scalar

Thank you