



Study of hyperon-nucleon interactions at BESIII

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Hadron Physics Online Forum (HAPOF) https://indico.itp.ac.cn/category/5/

2025.05.09

Outline

Introduction

BEPCII and BESIII

Study of hyperon-nucleon interactions at BESIII

PRL 130, 251902 (2023) PRC 109, L052201 (2024) PRL 132, 231902 (2024)

Summary

Scattering experiments of particle beams bombarding target materials



James Chadwick

Scattering experiments of particle beams bombarding target materials



Scattering experiment must have **particle source**, target material, and detector.

Hyperon source

Baryon octet

One of main goals of nuclear physics is to understand baryonbaryon interaction in a unified perspective



Limited by availability and short-lifetime of hyperon beams

> Hyperons are obtained by bombarding hydrogen bubble chamber or scintillating fiber target with K^- .





Hyperon source

- > Hyperons are obtained by bombarding hydrogen bubble chamber or scintillating fiber target with K^- .
- Intensity of hyperon beams is low, experimental measurements are scarce and have large uncertainty.

reaction

 $\Xi^{0} + p \rightarrow \Xi^{0} + p$

 $\Xi^{0} + p \rightarrow \Lambda + \Sigma^{\dagger}$

 $\Xi^{0} + p \rightarrow \Sigma^{0} + \Sigma^{+}$

 $\Xi^{0} + p \rightarrow \pi^{+} + \Lambda + \Lambda$

 $\Xi^{0} + p \rightarrow \pi^{0} + \Lambda + \Sigma^{+}$

 $\Xi^{0} + p \rightarrow \pi^{+} + \Xi^{-} + p$

 $\Xi^{0} + p \rightarrow \Xi^{-} + p$

 $\Xi^{0} + p \rightarrow \Sigma^{-} + \Sigma^{+}$

 $\Xi^0 + p \rightarrow \Sigma^- + K^0 + p$

 $\Xi^{o} + p \longrightarrow \pi^{+} + \pi^{+} + \Xi^{-} + n$

> No anti-hyperon source.

Reaction	Number of events
$\Lambda p \rightarrow \Lambda p$ (elastic)	584
$\Lambda p \rightarrow \Sigma^- p \pi^+$	132
$\Lambda p \rightarrow \Sigma^+ p \pi^-$	60
$\Lambda p \rightarrow \Lambda p \pi^+ \pi^-$	181
$\Lambda p \rightarrow \Sigma^{0} p$	35
various Ξ^0 p interactions	25

PLB 32, 720 (1970)

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Reaction	Momentum interval (GeV/c)	Number of events	σ (mb)
Ap →all	$\begin{array}{c} 0.5 \ \rightarrow 1.0 \\ 1.0 \ \rightarrow 1.5 \\ 1.5 \ \rightarrow 2.0 \\ 2.0 \ \rightarrow 2.5 \\ 2.5 \ \rightarrow 3.0 \\ 3.0 \ \rightarrow 4.0 \end{array}$		$\begin{array}{c} 25.8\pm \ 6.2\\ 31.3\pm \ 6.5\\ 42.8\pm \ 7.1\\ 37.5\pm \ 7.2\\ 34.1\pm \ 8.3\\ 41.8\pm 10.0 \end{array}$
$\Lambda p \rightarrow \Lambda p$	$\begin{array}{r} 0.5 \ \rightarrow 1.0 \\ 1.0 \ \rightarrow 1.5 \\ 1.5 \ \rightarrow 2.0 \\ 2.0 \ \rightarrow 2.5 \\ 2.5 \ \rightarrow 3.0 \\ 3.0 \ \rightarrow 4.0 \end{array}$	20 21 37 28 12 13	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
$\begin{array}{c} \Lambda p \rightarrow \Sigma^{O} \\ \Lambda p \rightarrow \Lambda p \pi^{O} \\ \Lambda p \rightarrow \Lambda p \pi^{+} \pi^{-} \end{array}$	$0.66 \rightarrow 4.0 \\ 0.88 \rightarrow 4.0 \\ 1.36 \rightarrow 4.0$	11 29 12	$\begin{array}{rrrr} 1.5 \pm & 0.5 \\ 4.1 \pm & 0.8 \\ 1.9 \pm & 0.6 \end{array}$
$\Sigma^+ p \rightarrow \Sigma^+ p$	$\begin{array}{c} 0.5 \ \rightarrow 1.5 \\ 1.5 \ \rightarrow 2.5 \\ 2.5 \ \rightarrow 4.0 \end{array}$	10 8 4	$\begin{array}{rrrr} 31.2\pm10.1\\ 18.7\pm&6.6\\ 15.3\pm&7.8 \end{array}$
∑⁻р →∑⁻р	$\begin{array}{c} 0.5 \ \rightarrow 1.5 \\ 1.5 \ \rightarrow 2.5 \\ 2.5 \ \rightarrow 4.0 \end{array}$	6 11 4	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
∃°р⊸⊒°р ∃ор⊸⊒ор	$\begin{array}{c} 1.0 \rightarrow 4.0 \\ 1.0 \rightarrow 4.0 \end{array}$	6 4	$\begin{array}{rrrr} 13 & \pm & 6 \\ 19 & \pm & 10 \end{array}$



(1)

(2)

(3)

(4)

(5)





events *

1

1

1

1

1

2

cross-section

4

1

1

1

1

1

events



cross-section (mb)

8

 $\mathbf{24}$

6

6

4

4



PLB 38, 123 (1972)

signature

к.Λ

Λ

Λ

к.Λ

Λ

K or Λ

к.Λ

Λ

к

K

Theory of hyperon-nucleon (YN) interaction has large uncertainty due to lack of relevant measurements



"Hyperon puzzle" of neutron stars

Hyperons are believed to be appeared in inner core of neutron stars.

 $\begin{array}{ll} B_1 \rightarrow B_2 + l + \bar{\nu}_l, \ B_2 + l \rightarrow B_1 + \nu_l \\ n \rightarrow p + e^- + \bar{\nu}_e, \ p + e^- \rightarrow n + \nu_e \\ \Lambda \rightarrow p + e^- + \bar{\nu}_e, \ p + e^- \rightarrow \Lambda + \nu_e \end{array} \begin{array}{ll} \Sigma^- \rightarrow n + e^- + \bar{\nu}_e, \ n + e^- \rightarrow \Sigma^- + \nu_e \\ \Xi^- \rightarrow \Lambda + e^- + \bar{\nu}_e, \ \Lambda + e^- \rightarrow \Xi^- + \nu_e \end{array}$

- Appearance of hyperons softens equation of state, lead to maximum mass that neutron stars can sustain is less than mass of already-observed neutron stars.
- A repulsive force is introduced to stiffen equation of state in theory, such as a combination of ΛN and ΛNN interactions. Study of hyperon-nucleon interaction is crucial to solve "hyperon puzzle" of neutron stars.



Search for H-dibaryon

- Study of hyperon-nucleon interaction can be used to search for the H-dibaryon, which has strangeness -2 and valence quark structure *uuddss*. This H-dibaryon is firstly predicted according to the bag model as early as the 1970s. Later, two lattice QCD groups also study this respectively, and both predict the existence of H-dibaryon.
- However, so far, although the H-dibaryon has been searched by many experiments, no any convincing signals has been found.
- H-dibaryon can be searched in the final states of reaction process of Ξ and nucleon. And H-dibaryon is also predicted to appear as a bound state of ΣΣ decaying strongly into ΞN or ΛΛ.





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Some recent experimental results on hyperon-nucleon scattering

PHYSICAL REVIEW LETTERS 127, 272303 (2021)

(CLAS Collaboration)

Improved Λp Elastic Scattering Cross Sections between 0.9 and 2.0 GeV/c as a Main Ingredient of the Neutron Star Equation of State



This is the first data on this reaction since the 1970s.

Some recent experimental results on hyperon-nucleon scattering

J-PARC E40 Collaboration





PRC 104, 045204 (2021)



 $\Sigma^- p \to \Sigma^- p$

Some recent experimental results on hyperon-nucleon scattering

J-PARC E40 Collaboration

-1 -0.8 -0.6 -0.4 -0.2 0 0.2 0.4 0.6 0.8 -1 -0.8 -0.6 -0.4 -0.2 0

cose



PRL 128, 072501 (2022)



0.2 0.4 0.6 0.8

700

cosθ

Beijing Electron Positron Collider II (BEPCII) and Beijing Spectrometer III (BESIII)



BESIII detector

BESIII detector



Has been in full operation since 2008, all subdetectors are in very good status!

BESIII data samples



Experimental study on particle targeting at BESIII



PRL 127, 012003 (2021) CPC 48, 073003 (2024) $\bar{n}p \rightarrow \pi^+\pi^+\pi^-\pi^0$, $\pi^0 \rightarrow \gamma\gamma$



particle source: hyperon from J/ψ decays target material: beam pipe detector: **BESIII** detector

Experimental study on particle targeting at BESIII

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Hyperon/Antihyperon	$\tau ~(\times 10^{-10} { m s})$	Decay mode	$\mathcal{B}(imes 10^{-3})$	$P \; ({\rm GeV}/c)$	$E_{\rm cm}~({\rm GeV})$	$N~(imes 10^5)$	$N^{\mathrm{bp}}~(imes 10^5)$
$\Lambda/ar{\Lambda}$	2.62	$J/\psi \to \Lambda \bar{\Lambda}$	1.88	1.074	2.24	188	102
$\Sigma^+/\bar{\Sigma}^-$	0.80	$J/\psi \to \Sigma^+ \bar{\Sigma}^-$	1.07	0.992	2.28	107	15
$\Xi^0/\bar{\Xi}^0$	2.90	$J/\psi ightarrow \Xi^0 \bar{\Xi}^0$	1.17	0.818	2.35	117	51
$\Xi^-/\bar{\Xi}^+$	1.64	$J/\psi \to \Xi^- \bar{\Xi}^+$	0.97	0.807	2.35	97	23
$\Lambda/ar{\Lambda}$	2.62	$\psi(2S) \to \Lambda \bar{\Lambda}$	0.38	1.467	2.36	11	7
$\Sigma^+/\bar{\Sigma}^-$	0.80	$\psi(2S) \to \Sigma^+ \bar{\Sigma}^-$	0.24	1.408	2.40	7	2
$\Xi^0/\bar{\Xi}^0$	2.90	$\psi(2S) \to \Xi^0 \bar{\Xi}^0$	0.23	1.291	2.47	7	4
$\Xi^-/\bar{\Xi}^+$	1.64	$\psi(2S) \to \Xi^- \bar{\Xi}^+$	0.29	1.284	2.47	9	3
$\Omega^-/ar\Omega^+$	0.82	$\psi(2S) \to \Omega^- \bar{\Omega}^+$	0.06	0.774	2.67	2	0.1
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The abundant hyperon-antihyperon pairs are produced, also as antihyperon sources.

Recent results on hyperon-nucleon interactions at BESIII

- ➢ First Study of Reaction $\Xi^0 n \rightarrow \Xi^- p$ Using Ξ^0 -Nucleus Scattering at an Electron-Positron Collider PRL 130, 251902 (2023)
- First measurement of ΛN inelastic scattering with Λ from $e^+e^- → J/ψ → Λ\overline{Λ}$ PRC 109, L052201 (2024)
- First Study of Antihyperon-Nucleon Scattering $\overline{\Lambda}p$ → $\overline{\Lambda}p$ and Measurement of Λp → Λp Cross Section PRL 132, 231902 (2024)

Study of $\Xi^0 n \to \Xi^- p$



Analysis method :

 e^{-1} of 11 mrad for e^+ and e^- beams.

Using $\overline{\Xi}^0$ to tag the event and requiring the recoiling mass in Ξ^0 region. Then reconstructing Ξ^- and p in the signal side.

Study of $\Xi^0 n \to \Xi^- p$



Cross section of $\Xi^0 + {}^9\text{Be} \rightarrow \Xi^- + p + {}^8\text{Be}$

$$\sigma(\Xi^{0} + {}^{9}\text{Be} \to \Xi^{-} + p + {}^{8}\text{Be}) = \frac{N^{\text{sig}}}{\epsilon \mathcal{BL}_{\text{eff}}}$$

$$\mathcal{L}_{\text{eff}} = \frac{N_{J/\psi} \mathcal{B}_{J/\psi}}{2 + \frac{2}{3}\alpha} \int_{a}^{b} \int_{0}^{\pi} (1 + \alpha \cos^{2}\theta) e^{-\frac{x}{\sin\theta\beta\gamma L}} N(x) C(x) d\theta dx$$



Study of $\Xi^0 n \to \Xi^- p$

The measured cross section of the reaction process $\Xi^0 + {}^9\text{Be} \rightarrow \Xi^- + p + {}^8\text{Be}$ is $\sigma(\Xi^0 + {}^9\text{Be} \rightarrow \Xi^- + p + {}^8\text{Be}) = (22.1 \pm 5.3_{\text{stat}} \pm 4.5_{\text{sys}})$ mb at $P_{\Xi^0} \approx 0.818 \text{ GeV}/c.$

If we take the effective number of reaction neutrons in ⁹Be nucleus as 3, the cross section of $\Xi^0 n \to \Xi^- p$ for single neutron is determined to be $\sigma(\Xi^0 n \to \Xi^- p) = (7.4 \pm 1.8_{\text{stat}} \pm 1.5_{\text{sys}})$ mb, consistent with theoretical predictions.





LO : H. Polinder, J.H., U.-G. Meißner, PLB 653 (2007) 29 NLO16: J.H., U.-G. Meißner, S. Petschauer, NPA 954 (2016) 273 NLO19: J.H., U.-G. Meißner, EPJA 55 (2019) 23

No significant H-dibaryon signals are seen

This work is the first study of hyperon-nucleon interaction in electron-positron collisions, and opens up a new direction for such research. 22

Study of $\Lambda N \rightarrow \Sigma^+ X$

PRC 109, L052201 (2024)

Reaction chain :

 $J/\psi \to \Lambda \overline{\Lambda}, \overline{\Lambda} \to \overline{p}\pi^+, \Lambda + N(\text{nucleus}) \to \Sigma^+ + X(\text{anything}), \\ \Sigma^+ \to p\pi^0, \pi^0 \to \gamma\gamma.$



Two-body decay, $P_{\Lambda} \approx 1.074 \text{ GeV/}c$, a very small horizontal crossing angle of 11 mrad for e^+ and e^- beams, resulting in a small range of 0.017 GeV/c above and below 1.074 GeV/c for P_{Λ} .

Study of $\Lambda N \rightarrow \Sigma^+ X$



 $N_{\rm ST} = 7207565 \pm 3741$



The reaction position can not be determined. These signal events mainly come from the reaction with beam pipe and inner wall of MDC.

Cross section of $\Lambda + {}^{9}\text{Be} \rightarrow \Sigma^{+} + X$

$$\sigma(\Lambda + {}^{9}\text{Be} \to \Sigma^{+} + X) = \frac{N_{\text{DT}}}{\epsilon_{\text{sig}}\mathcal{L}_{\Lambda}} \frac{1}{\mathcal{B}(\Sigma^{+} \to p\pi^{0})}$$

 $\mathcal{L}_{\Lambda} = N_{\mathrm{ST}} \frac{N_A}{N_{\mathrm{ST}}^{\mathrm{MC}}} \sum_{i}^{7} \sum_{j}^{N_{\mathrm{ST}}^{\mathrm{MC}}} \frac{\rho_T^j l^{ij}}{M^j} \mathcal{R}_{\sigma}^j$

path length of incident Λ of i_{th} event inside j_{th} layer



Z

pure surface process assumption (proportional to number of protons)

Parameter	Value
N _{DT}	795 ± 101
$\epsilon_{ m sig}$	24.32%
\mathcal{L}_{Λ}	$(17.00 \pm 0.01) \times 10^{28} \mathrm{cm}^{-2}$
$\mathcal{B}(\Sigma^+ o p\pi^0)$	$(51.57 \pm 0.30)\%$

Study of $\Lambda N \to \Sigma^+ X$

The measured cross section of the reaction process $\Lambda + {}^{9}\text{Be} \rightarrow \Sigma^{+} + X$ is $\sigma(\Lambda + {}^{9}\text{Be} \rightarrow \Sigma^{+} + X) = (37.3 \pm 4.7_{\text{stat}} \pm 3.5_{\text{sys}})$ mb at $P_{\Lambda} \approx 1.074$ GeV/c. This work represents the first attempt to investigate Λ -nucleus interaction at an $e^{+}e^{-}$ collider.

If taking the effective number of reaction protons in ⁹Be nucleus as 1.93, the cross section of $\Lambda p \rightarrow \Sigma^+ X$ for single proton is determined to be $\sigma(\Lambda p \rightarrow \Sigma^+ X) = (19.3 \pm 2.4_{\text{stat}} \pm 1.8_{\text{sys}})$ mb.



101

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0.5

PRL 132, 231902 (2024)

Taking the hydrogen in the cooling oil of the beam pipe as target material, the information on the hyperon-proton scattering can be extracted directly.



ΛX

3.37

Two-body decay, $P_{\Lambda/\overline{\Lambda}} \approx 1.074 \text{ GeV}/c$



Study of $\Lambda p \rightarrow \Lambda p$ and $\Lambda p \rightarrow \Lambda p$ 20 $\Lambda p \to \Lambda p$ Events / 2 MeV/c $\Lambda p \to \Lambda p$ + DATA M(p_{oil}) (GeV/c²) Sig. MC 15 Incl. MC 10 0.8 5 0.6 0^L 0 0.05 P(p_i) (GeV/c) 0.1 0.1 0.2 0.3 0.4 0.5 P(p_{oil}) (GeV/c) 0 $J/\psi \to \Lambda\Lambda$ $P(p_{oil}) \equiv |\vec{P}_{\Lambda} + \vec{P}_{p} - (\vec{P}_{e^{+}e^{-}} - \vec{P}_{\bar{\Lambda}})| < 0.04 \text{ GeV}/c$ $\Lambda p_{\rm oil} \rightarrow \Lambda p$ $M(p_{oil}) \equiv \sqrt{|E_{\Lambda} + E_p - (E_{e^+e^-} - E_{\overline{\Lambda}})|^2 - |\vec{P}_{\Lambda} + \vec{P}_p - (\vec{P}_{e^+e^-} - \vec{P}_{\overline{\Lambda}})|}$ $\overline{\Lambda}p \rightarrow \overline{\Lambda}p$ 20 $\overline{\Lambda}p\to\overline{\Lambda}p$ Events / 2 MeV/c + DATA - Sig. MC M(p_{oil}) (GeV/c²) 15 — Incl. MC 0.8 10 5 0.6 0<u></u> 0.05 P(p_{oil}) (GeV/c) 0.1 0.2 0.3 0.4 0.5 P(p_{oil}) (GeV/c) 0.1 0

28

The center-of-mass energy for the incident $\Lambda/\overline{\Lambda}$ and a static p is about 2.243 GeV/ c^2 .





$\cos heta_{\Lambda/ar\Lambda}$	$N_i^{ m sig}$	ϵ_i (%)	$(d\sigma/d\Omega)$ (mb/sr)
[-0.9, -0.7]	$(5.0^{+2.6}_{-1.9}, 0.0^{+1.1}_{-0.0})$	(6.94,4.93)	$(1.7^{+0.9}_{-0.7}, 0.0^{+0.5}_{-0.0})$
(-0.7, -0.5]	$(1.0^{+1.4}_{-0.7}, 0.0^{+1.1}_{-0.0})$	(14.13,10.44)	$(0.2^{+0.2}_{-0.1}, 0.0^{+0.3}_{-0.0})$
(-0.5, -0.3]	$(1.0^{+1.4}_{-0.7}, 1.0^{+1.4}_{-0.7})$	(17.32,13.27)	$(0.2^{+0.2}_{-0.1}, 0.2^{+0.3}_{-0.1})$
(-0.3, -0.1]	$(11.0^{+3.7}_{-3.0}, 0.0^{+1.1}_{-0.0})$	(17.74,14.66)	$(1.5^{+0.5}_{-0.4}, 0.0^{+0.2}_{-0.0})$
(-0.1, 0.1]	$(6.9^{+3.0}_{-2.3}, 0.0^{+1.1}_{-0.0})$	(19.11,15.79)	$(0.9^{+0.4}_{-0.3}, 0.0^{+0.2}_{-0.0})$
(0.1, 0.3]	$(5.0^{+2.6}_{-1.9}, 2.0^{+1.8}_{-1.1})$	(19.53,16.82)	$(0.6^{+0.3}_{-0.2}, 0.3^{+0.3}_{-0.2})$
(0.3, 0.5]	$(12.0^{+3.8}_{-3.1}, 7.0^{+3.0}_{-2.3})$	(19.21,17.68)	$(1.5^{+0.5}_{-0.4}, 1.0^{+0.4}_{-0.3})$
(0.5, 0.7]	$(13.0^{+3.9}_{-3.3}, 25.0^{+5.3}_{-4.7})$	(19.71,17.60)	$(1.6^{+0.5}_{-0.4}, 3.4^{+0.7}_{-0.6})$
(0.7, 0.9]	$(6.0^{+2.8}_{-2.1}, 37.0^{+6.4}_{-5.8})$	(9.80,9.93)	$(1.5^{+0.7}_{-0.5}, 9.0^{+1.6}_{-1.4})$

Cross sections in $-0.9 \le \cos\theta_{\Lambda/\overline{\Lambda}} \le 0.9$ are measured to be $\sigma(\Lambda p \to \Lambda p) = (12.2 \pm 1.6_{\text{stat}} \pm 1.1_{\text{sys}}) \text{ mb and}$ $\sigma(\overline{\Lambda}p \to \overline{\Lambda}p) = (17.5 \pm 2.1_{\text{stat}} \pm 1.6_{\text{stat}}) \text{ mb}$

Total cross sections are determined to be $\sigma_t(\Lambda p \rightarrow \Lambda p) = (14.2 \pm 1.8_{\text{stat}} \pm 1.3_{\text{sys}}) \text{ mb and}$ $\sigma_t(\overline{\Lambda}p \rightarrow \overline{\Lambda}p) = (27.4 \pm 3.2_{\text{stat}} \pm 2.5_{\text{sys}}) \text{ mb}$



More (anti)hyperon-nucleon scattering can be studied at BESIII

Elastic scattering	Inelastic scattering
$\Lambda p o \Lambda p$	$\Lambda p \to \Sigma^0 p, \Lambda p \pi^0, \Sigma^+ p \pi^-$
$ar{\Lambda} p o ar{\Lambda} p$	$ar{\Lambda}p ightarrow ar{\Sigma}^0 p, ar{\Lambda}p\pi^0, ar{\Sigma}^-p\pi^+$
$\Sigma^+ p \to \Sigma^+ p$	$\Sigma^+ p \to \Lambda p \pi^+, \ \Sigma^+ p \pi^0, \ \Sigma^0 p \pi^+$
$\bar{\Sigma}^- p o \bar{\Sigma}^- p$	$\bar{\Sigma}^- p \to \bar{\Lambda} p \pi^-, \ \bar{\Sigma}^- p \pi^0, \ \bar{\Sigma}^0 p \pi^-$
$\Xi^0 p o \Xi^0 p$	$\Xi^0 p ightarrow \Lambda \Sigma^+, \Sigma^0 \Sigma^+, \Xi^0 p \pi^0, \Xi^- p \pi^+$
$ar{\Xi}^0 p o ar{\Xi}^0 p$	$ar{\Xi}^0 p ightarrow ar{\Xi}^0 p \pi^0, \ ar{\Xi}^+ p \pi^-$
$\Xi^- p ightarrow \Xi^- p$	$\Xi^- p \to \Lambda\Lambda, \Lambda\Sigma^0, \Sigma^0\Sigma^0, \Xi^- p\pi^0, \Xi^0 p\pi^-$
$\bar{\Xi}^+ p ightarrow \bar{\Xi}^+ p$	$\bar{\Xi}^+ p ightarrow \bar{\Xi}^+ p \pi^0, \ \bar{\Xi}^0 p \pi^+$
$\Omega^- p \to \Omega^- p$	$\Omega^- p \to \Lambda \Xi^0, \ \Sigma^0 \Xi^0, \ \Sigma^+ \Xi^-$
$\bar{\Omega}^+ p \to \bar{\Omega}^+ p$	



 $\Lambda p \rightarrow \Lambda p / \overline{\Lambda} p \rightarrow \overline{\Lambda} p$ is studied using three-body decays $J/\psi \rightarrow pK\Lambda$, momentumdependent cross section measurement.







1. Using a novel method, hyperon-nucleon scattering can also be measured at BESIII.

$$\succ \Xi^{0}n \to \Xi^{-}p$$
$$\succ \Lambda N \to \Sigma^{+}X$$
$$\succ \Lambda p \to \Lambda p$$
$$\succ \overline{\Lambda}p \to \overline{\Lambda}p$$



2. This is the first study of hyperon-nucleon interactions in electron-positron collisions, and opens up a new direction for such research. Especially, antihyperon-nucleon scattering is studied for the first time.

3. With more statistics in future super tau-charm facilities, the momentumdependent cross section or differential cross section distributions can be studied based on the hyperons from multibody decays of J/ψ or other charmonia.

Thanks for your attention!

Back Up

A. Angular distribution of the process $J/\psi \rightarrow \Xi^0 \overline{\Xi}^0$

The measured angular distribution of the process $J/\psi \to \Xi^0 \bar{\Xi}^0$ in experiment is :

$$\frac{dN(\theta)}{d(\cos\theta)} \propto (1 + \alpha \cos^2\theta),\tag{1}$$

where $\cos\theta$ is from -1 to +1.

Because

$$\int_{-1}^{1} \frac{dN(\theta)}{d(\cos\theta)} d(\cos\theta) = N_{J/\psi} \mathcal{B}(J/\psi \to \Xi^0 \bar{\Xi}^0), \tag{2}$$

we can get

$$\frac{dN(\theta)}{d(\cos\theta)} = \frac{N_{J/\psi}\mathcal{B}(J/\psi \to \Xi^0 \bar{\Xi}^0)}{\int_{-1}^{1} (1 + \alpha \cos^2\theta) d(\cos\theta)} (1 + \alpha \cos^2\theta) = \frac{N_{J/\psi}\mathcal{B}(J/\psi \to \Xi^0 \bar{\Xi}^0)}{2 + \frac{2}{3}\alpha} (1 + \alpha \cos^2\theta).$$
(3)

Therefore, the following formula can be obtained :

$$\frac{dN(\theta)}{d\theta} = \frac{N_{J/\psi}\mathcal{B}(J/\psi \to \Xi^0 \bar{\Xi}^0)}{2 + \frac{2}{3}\alpha} (1 + \alpha \cos^2\theta) \sin\theta, \tag{4}$$

where θ is from 0 to π .

B. Number of the nuclei (Be, C, Au) per unit volume for beam pip

The beam pipe is composed of gold (Au), beryllium (Be) and oil (84.923%C, 15.077%H, C:H=1:2.13), as shown in Fig. 15. The distance from a position to the *z* axis is defined as *x*, so the number of the nuclei (Au, Be, C) per unit volume N(x) is :

$$N(x) = \begin{cases} \frac{\rho_{Au}}{A_{Au} \cdot lu} = \frac{19.32 g/\text{cm}^3}{197 \cdot 1.6605 \times 10^{-27} \text{kg}} = 5.91 \times 10^{22} \text{ cm}^{-3}, & 3.148564 \text{ cm} \le x \le 3.15 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.15 \text{ cm} < x \le 3.23 \text{ cm} \\ \frac{\rho_{OII}}{(A_{C} + A_{H} \cdot 2.13) \cdot lu} = \frac{0.81 g/\text{cm}^3}{(12 + 1 \cdot 2.13) \cdot lu} = 3.45 \times 10^{22} \text{ cm}^{-3}, & 3.23 \text{ cm} < x \le 3.31 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.31 \text{ cm} < x \le 3.31 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.31 \text{ cm} < x \le 3.37 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.31 \text{ cm} < x \le 3.37 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.31 \text{ cm} < x \le 3.37 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{ kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.31 \text{ cm} < x \le 3.37 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{ kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.31 \text{ cm} < x \le 3.37 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{1.85 g/\text{cm}^3}{9 \cdot 1.6605 \times 10^{-27} \text{ kg}} = 1.24 \times 10^{23} \text{ cm}^{-3}, & 3.31 \text{ cm} < x \le 3.37 \text{ cm} \\ \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{\rho_{Be}}{A_{Be} \cdot lu} = \frac{\rho_{Be}}{0.16005 \times 10^{-27} \text{ kg}} = \frac{\rho_{Be}}{0.16005 \times$$

Figure 15: The sketch map of beam pip, the length units are centimeter (cm). The solid line is x-axis, and the dashed line is z-axis.

C. Ratio of cross section of $\Xi^0 + {}^AX \rightarrow \Xi^- + p + {}^{A-1}X$ for Be, C and Au nuclei

There is no definite conclusion about the ratio of cross section of reaction process $\Xi^0 + {}^A X \to \Xi^- + p + {}^{A-1}X$ for Be, C and Au nuclei. Generally, from the measurements of other particles interact with nuclei, the cross section is proportional to A^{α} , where A is the number of nucleon in the nuclei and α is about from $\frac{2}{3}$ to 1 [45, 46, 47]. $\alpha = \frac{2}{3}$ is the most common situation, which is corresponding to a pure surface process and the reaction is due to the interaction with single nucleon on the nuclei surface.

Here for the reaction process $\Xi^0 + {}^A X \to \Xi^- + p + {}^{A-1}X$, we also assume the $\alpha = \frac{2}{3}$ to get the ratio of cross section for Be, C and Au nuclei. We assume the reaction is due to the interaction with single neutron on the nuclei surface, which is a pure surface process. So the cross section is proportional to $A^{\frac{2}{3}} \times \frac{N}{A} = \frac{N}{A^{\frac{1}{3}}}$, where A is the number of nucleons and N is the number of neutron. We can get $\sigma^{\text{Be}} : \sigma^{\text{C}} : \sigma^{\text{Au}} = \frac{5}{9^{\frac{1}{3}}} : \frac{6}{12^{\frac{1}{3}}} : \frac{118}{197^{\frac{1}{3}}} = 2.4037 : 2.6207 : 20.2796 = 1 : 1.090 : 8.437$. We define $\sigma(x) = C(x)\sigma^{\text{Be}} = C(x)\sigma(\Xi^0 + {}^9\text{Be} \to \Xi^- + p + {}^8\text{Be})$, where C(x) is :

Phys. Rev. D 27, 2580 (1983) Z. Phys. C 76, 35 (1997) Nucl. Phys. A 697, 209 (2002)

> $\sigma \propto A^{\alpha}$ α is about $\frac{2}{3} \sim 1$.

$$\alpha = \frac{2}{3}$$

$$C(x) = \begin{cases} 8.437, & 3.148564 \text{ cm} \le x \le 3.15 \text{ cm} \\ 1, & 3.15 \text{ cm} < x \le 3.23 \text{ cm} \\ 1.090, & 3.23 \text{ cm} < x \le 3.31 \text{ cm} \\ 1, & 3.31 \text{ cm} < x \le 3.37 \text{ cm} \end{cases}$$

(6) We use $\alpha = 1$ to estimate the systematic uncertainty.

D. Efficiency curve $\epsilon(x)$

The average efficiency in beam pipe region is determined to be $\epsilon = 18675/997312 = (1.873 \pm 0.014)\%$. The beam pipe region is small, so we can take the efficiency in beam pipe region as a constant. Therefore, the efficiency curve is $\epsilon(x) = 1.873\%$.

E. Cross section of the reaction process $\Xi^0 + {}^9\text{Be} \rightarrow \Xi^- + p + {}^8\text{Be}$

As shown in Fig. 16, at the position of θ and within the range of $d\theta$, the number of Ξ^0 that can reach the position of *x* is :

$$\frac{dN(\theta)}{d\theta}d\theta e^{-\frac{t}{\tau}}\sqrt{1-\frac{v^2}{c^2}} = \frac{dN(\theta)}{d\theta}d\theta e^{-\frac{x}{\sin\theta v}}\sqrt{1-\frac{v^2}{c^2}} = \frac{dN(\theta)}{d\theta}d\theta e^{-\frac{x}{\sin\theta \frac{D}{m}\tau}} = \frac{dN(\theta)}{d\theta}d\theta e^{-\frac{x}{\sin\theta \frac{$$

Figure 16: The sketch map of beam pip, the length units are centimeter (cm). The solid line is x-axis, and the dashed line is z-axis.

Then these Ξ^0 particles interact with neutron *n* in the target material in the *dx* range at *x* position to produce the reaction process $\Xi^0 + n \rightarrow \Xi^- + p$. So the number of signal events survived for the reaction process is :

$$\frac{dN(\theta)}{d\theta}d\theta e^{-\frac{x}{\sin\theta}\frac{\sqrt{E^2-m^2c^4}}{mc^2}L}\sigma(x)N(x)\frac{dx}{\sin\theta}\epsilon(x)\mathcal{B},$$
(8)

where $\mathcal{B} = \mathcal{B}(\bar{\Xi}^0 \to \bar{\Lambda}\pi^0)\mathcal{B}(\bar{\Lambda} \to \bar{p}\pi^+)\mathcal{B}(\pi^0 \to \gamma\gamma)\mathcal{B}(\Xi^- \to \Lambda\pi^-)\mathcal{B}(\Lambda \to p\pi^-).$

So the total number of signal events N^{sig} survived for the reaction process is :

$$N^{\text{sig}} = \int_{a}^{b} \int_{0}^{\pi} \frac{N_{J/\psi} \mathcal{B}(J/\psi \to \Xi^{0} \bar{\Xi}^{0})}{2 + \frac{2}{3}\alpha} (1 + \alpha \cos^{2}\theta) e^{-\frac{x}{\sin\theta} \frac{\sqrt{E^{2} - m^{2}c^{4}}}{mc^{2}}} \sigma(x) N(x) \epsilon(x) \mathcal{B}d\theta dx.$$
(9)

Therefore, the cross section formula of $\Xi^0 + {}^9\text{Be} \rightarrow \Xi^- + p + {}^8\text{Be}$ is :

$$\sigma(\Xi^{0} + {}^{9}\text{Be} \rightarrow \Xi^{-} + p + {}^{8}\text{Be}) = \frac{N^{\text{sig}}}{\frac{N_{J/\psi}\mathcal{B}(J/\psi \rightarrow \Xi^{0}\Xi^{0})\mathcal{B}}{2 + \frac{2}{3}\alpha} \int_{a}^{b} \int_{0}^{\pi} (1 + \alpha \cos^{2}\theta) e^{-\frac{x}{\sin\theta}\frac{\sqrt{E^{2}-m^{2}c^{4}}}{mc^{2}}L} C(x)N(x)\epsilon(x)d\theta dx}$$
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Figure 16: The sketch map of beam pip, the length units are centimeter (cm). The solid line is x-axis, and the dashed line is z-axis.



The properties of particle X are same as those of Λ except for mass. The X mass is set to be 2.243 GeV/ c^2 , which is center-of-mass energy for Λ and static p. And only the events where the position of X decays is in hydrogen region of beam pipe are used.

To guarantee the $\overline{\Lambda}$ momentum is same as actual one. The e^+e^- energy is set to be

$$E_{e^+e^-} = \sqrt{P_{\bar{\Lambda}}^2 c^2 + m_{\bar{\Lambda}}^2 c^4} + \sqrt{P_{\bar{\Lambda}}^2 c^2 + m_{X}^2 c^4}.$$



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