

Bounds on Cosmic Ray-Boosted Dark Matter

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Frontiers of Physics Outstanding Papers Awards 2019



杨炳麟，爱荷华州立大学教授，国际著名理论物理学家，曾任全球华人物理学会会长。多年来关心和支持中国科技发展，为中国物理学事业的发展作出巨大贡献。

以该综述为基础，郑州大学柳国丽、王飞教授和北京工业大学王雯宇教授进行了翻译、内容更新与扩充，将由科学出版社以学术译著的形式出版发行，预计今年12月份面市。



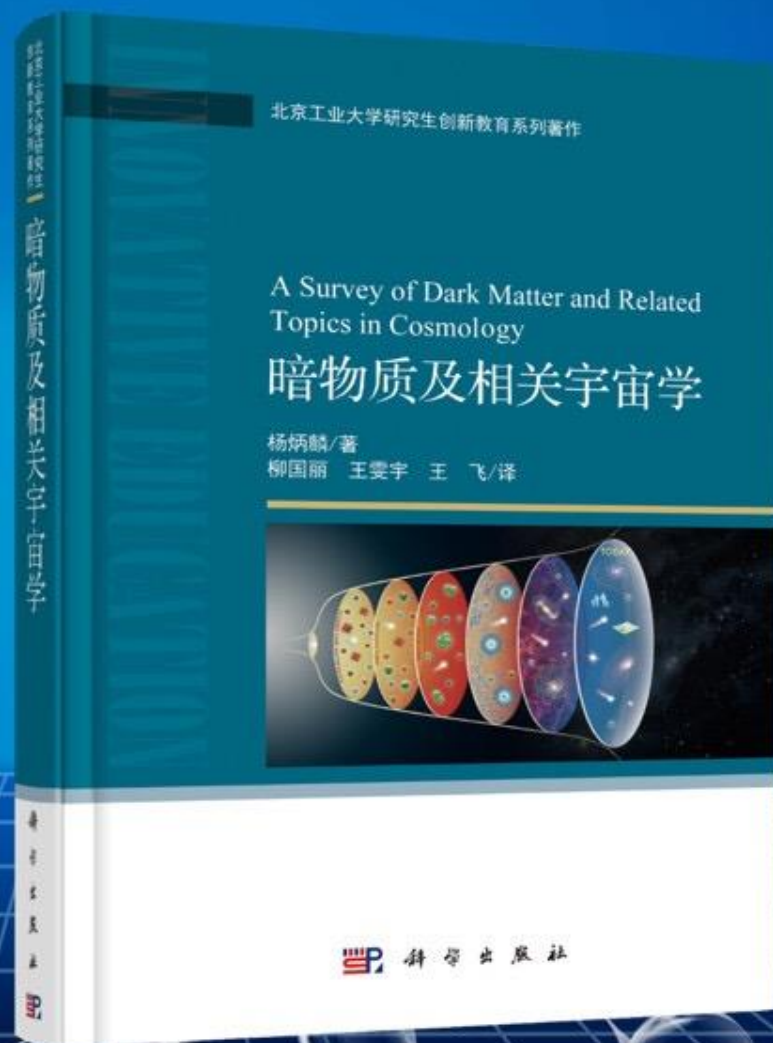
柳国丽



王雯宇



王飞



全书共13章，49万字，由科学出版社出版发行。

上篇：

- 暗物质观测证据
- 银河系暗物质分布
- 暗物质候选者
- 弱相互作用大质量粒子
- 轻暗物质粒子
- 暗物质直接、间接探测以及实验现状总结

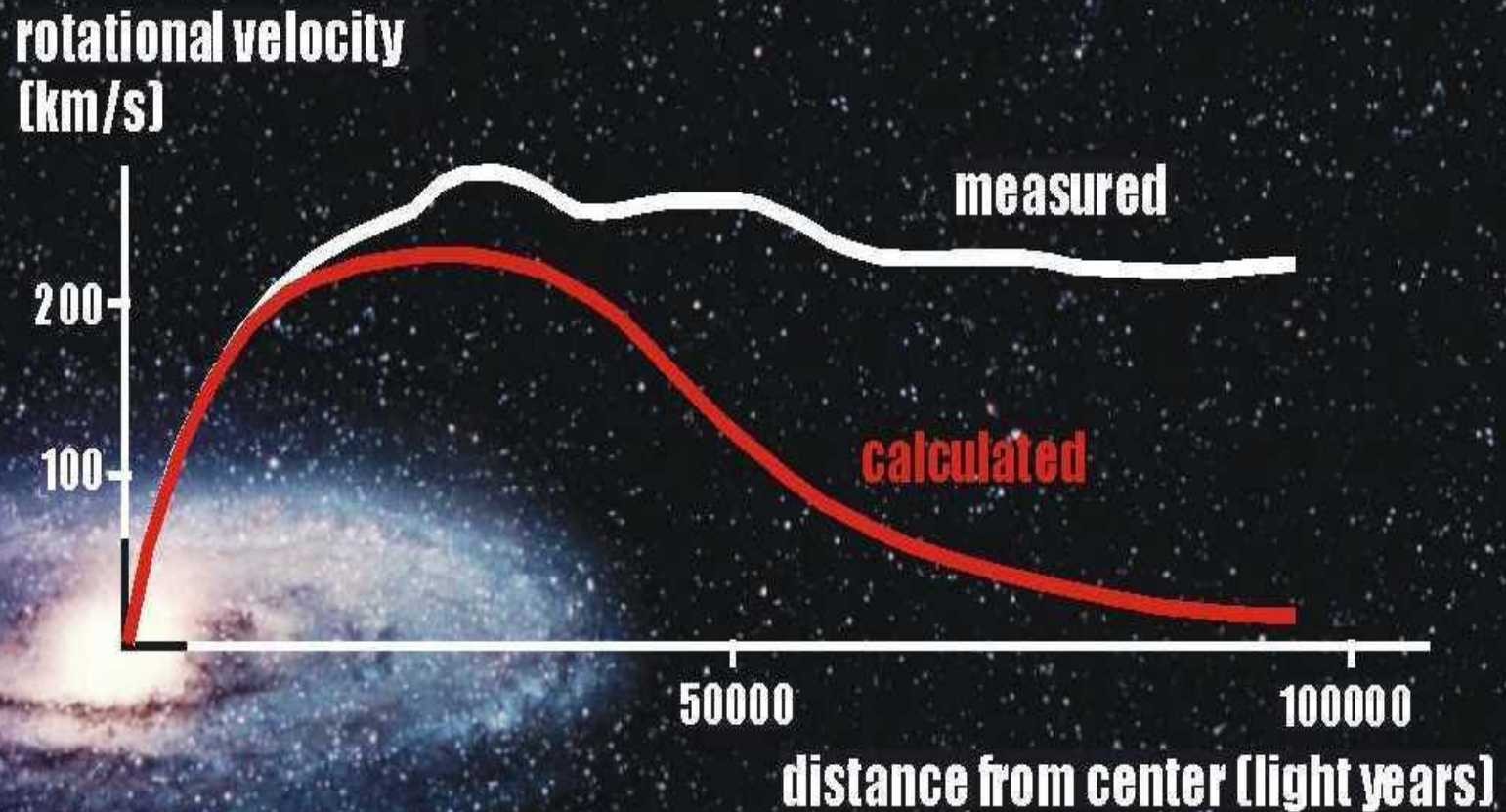
下篇：

- 宇宙学基本知识简介
- 宇宙大爆炸核合成
- 玻尔兹曼输运方程和大质量粒子的冻结
- 宇宙微波背景各向异性和宇宙扰动理论

Content

- Introduction of dark matter
- Status of WIMP dark matter
- Cosmic Ray-boosted dark matter
- Bounds on the light dark matter in the simplified models

Evidence of Dark Matter



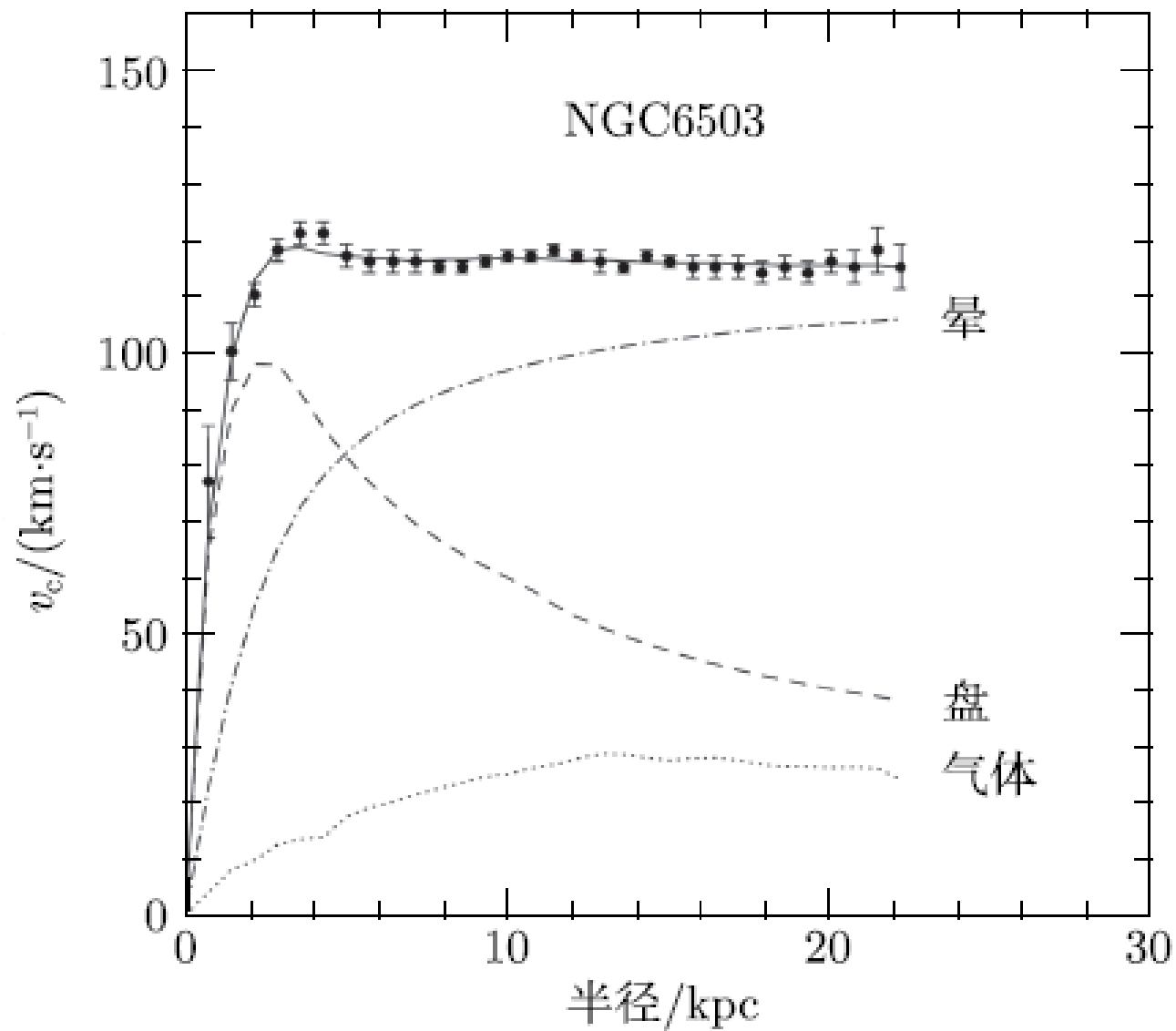
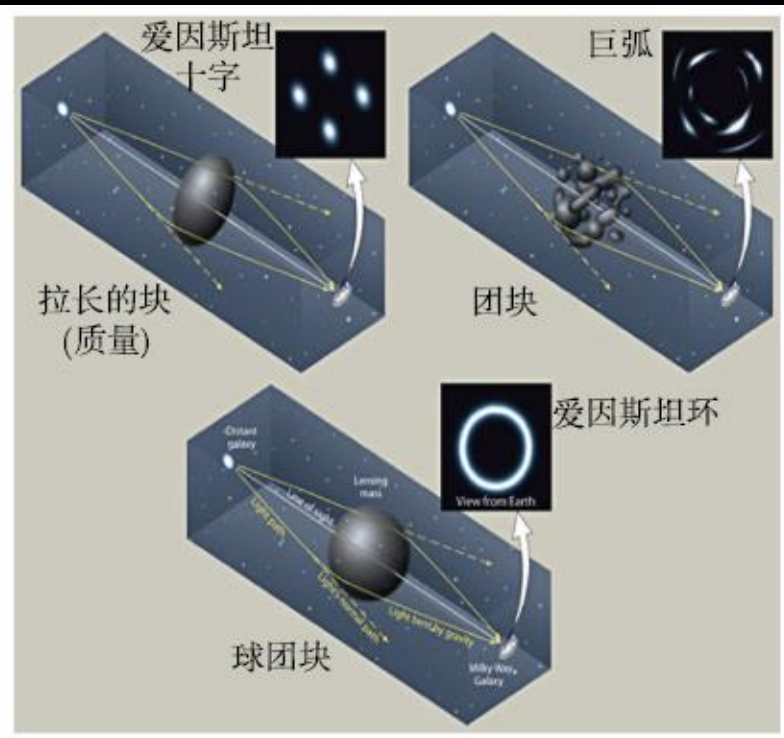
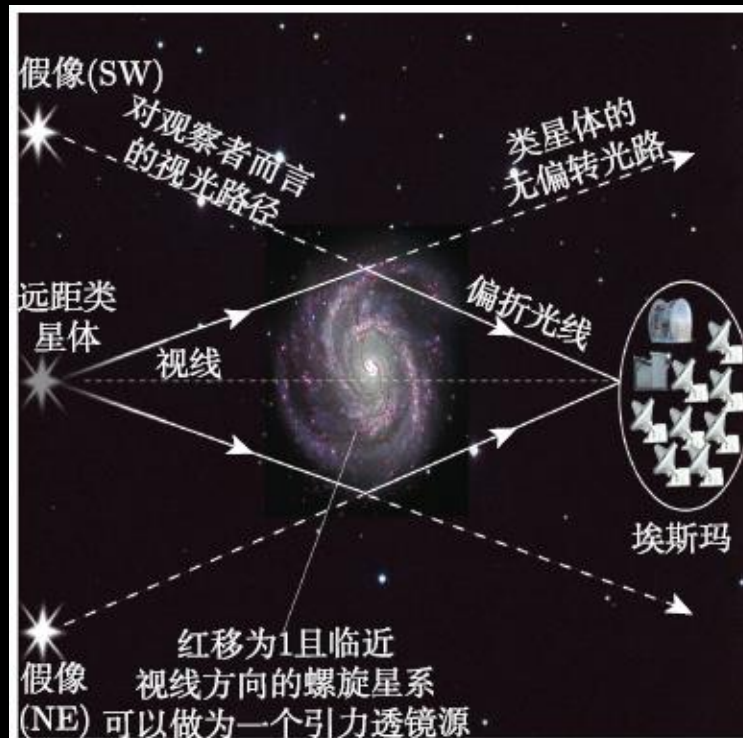


图 2.1.2 拟合总速度曲线 $v_c = \sqrt{v_{\text{晕}}^2 + v_{\text{盘}}^2 + v_{\text{气体}}^2}$

Observation methods

- Optics for the stars
- X-ray for the gas
- Gravitational lensing for the dark matter



光学暗物质X射线气体

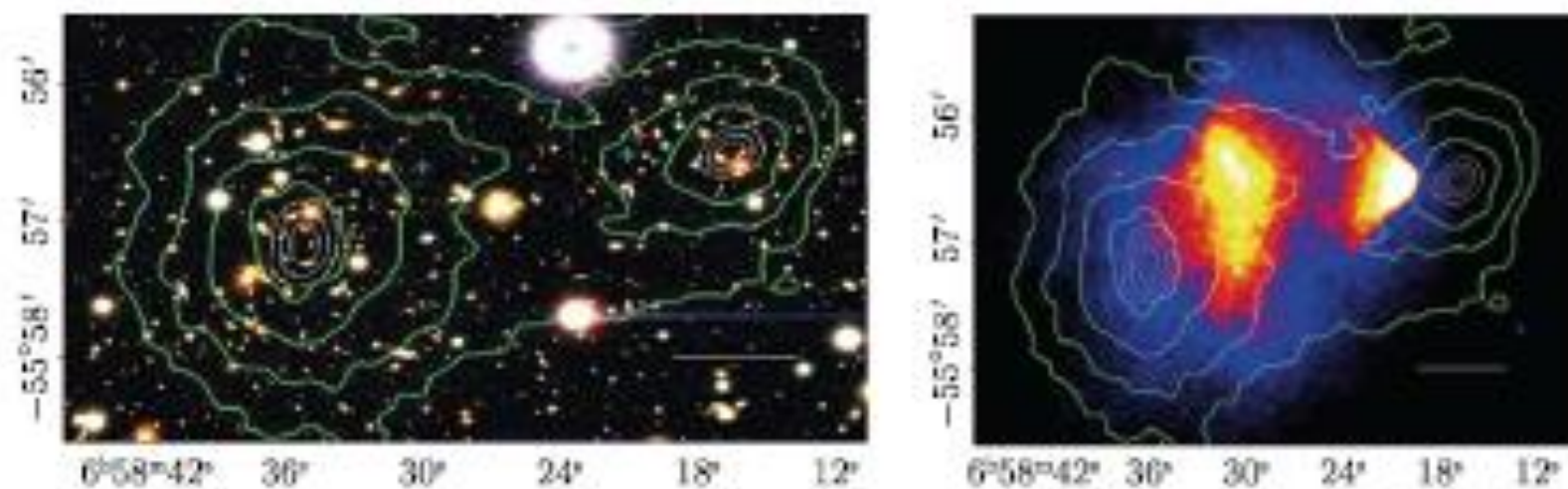


粉色：
X射线气体

图像：光学

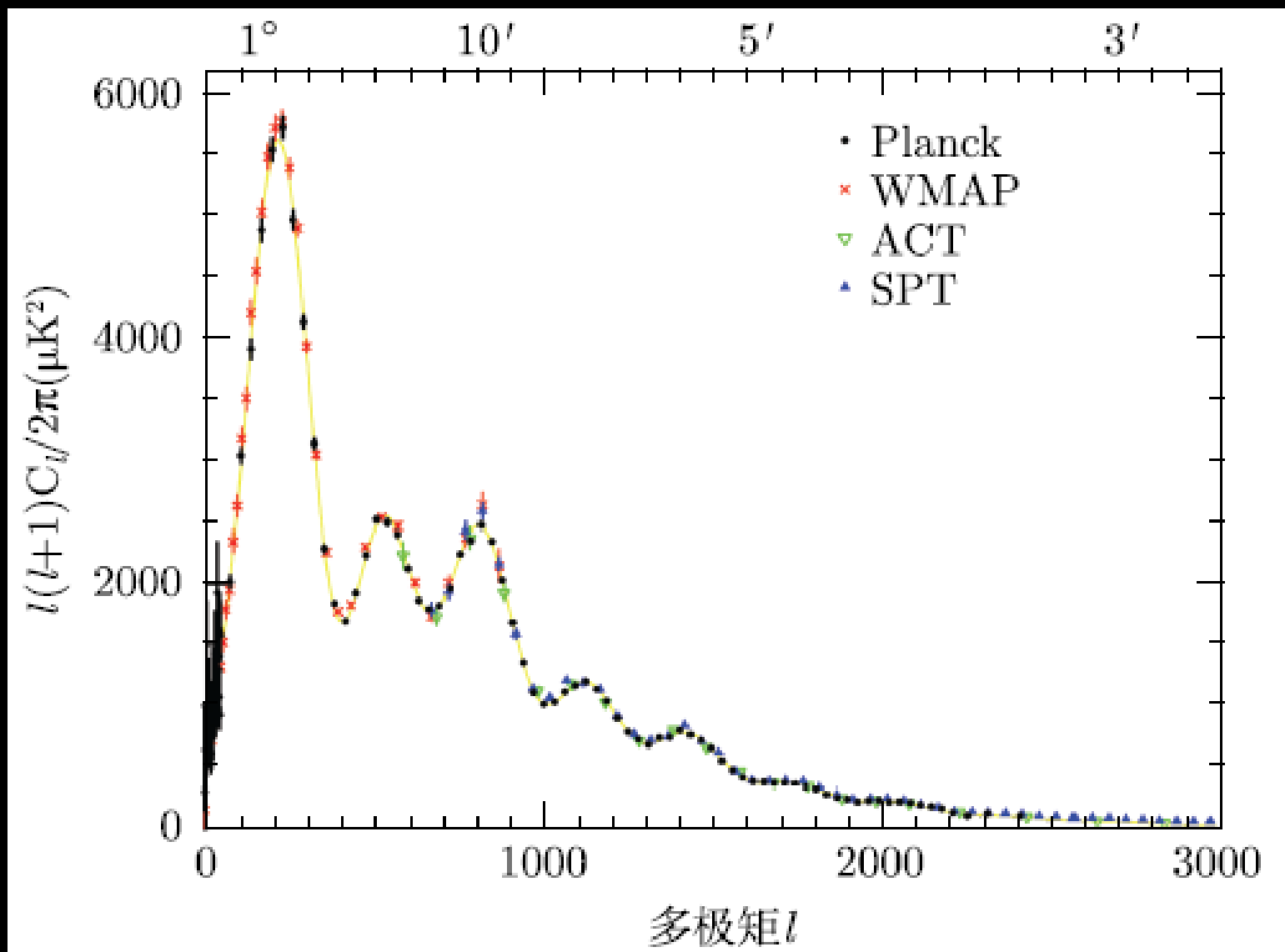
蓝色：
透镜质量

暗物质和光偏移



- 总质量类似于星系那样集中，而不是集中于气体所在位置， $M_{\text{total}}:M_{\text{gas}}:M_{\text{stars}} \sim 70:10:1$
- 气体峰(+)和质量之间的空间偏移非常显著
- 强烈支持暗物质假说而不支持修正引力

Anisotropy of CMB needs dark matter



Though existence of dark matter are believed in astrophysicists, we still need to identify it in the terrestrial laboratory !

Direct detection

从原子核中散射出来的
WIMP和中子

原子中电子散射出来的
的光子和电子

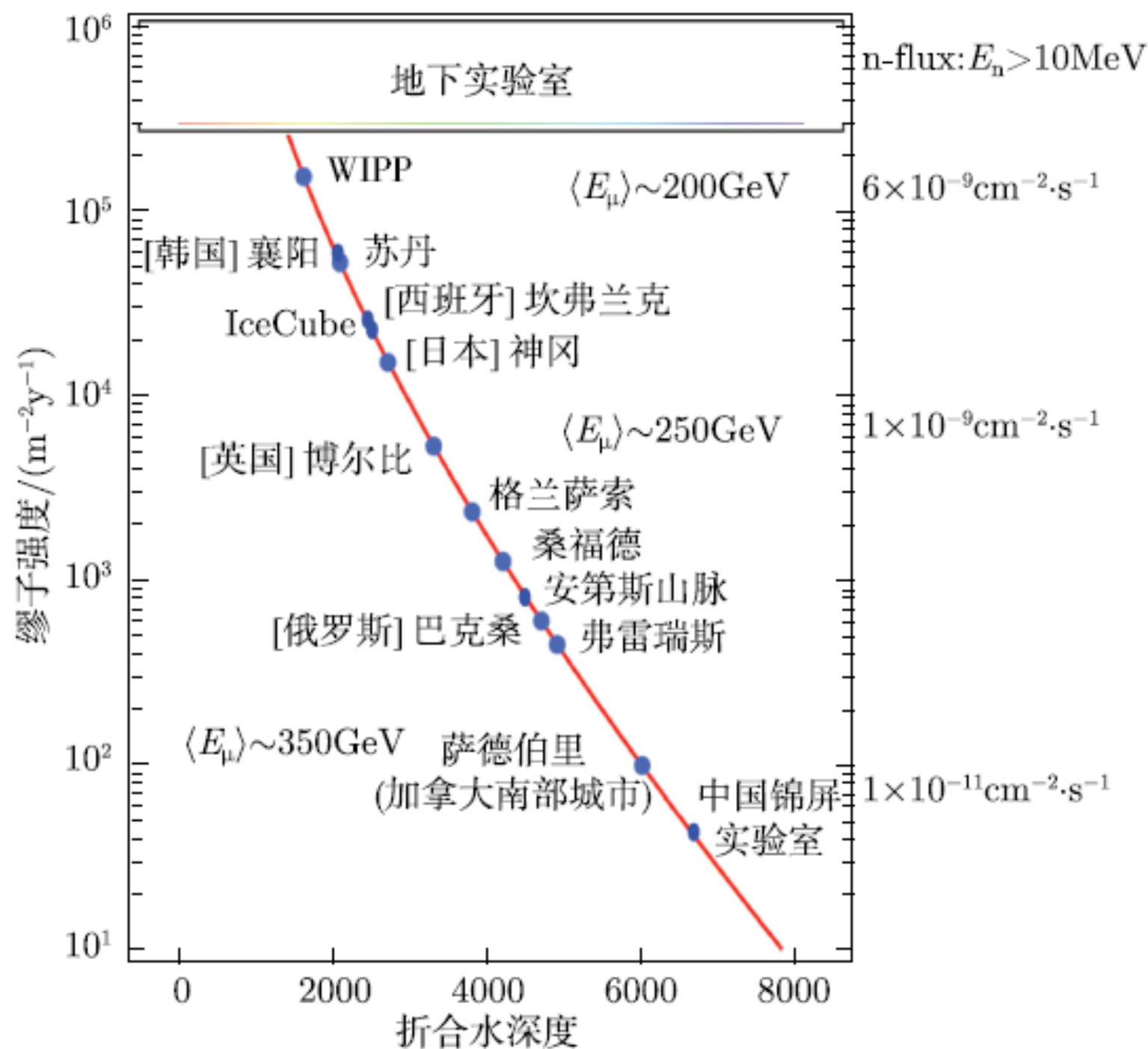
对原子核的散射

→ 核反冲能量测量

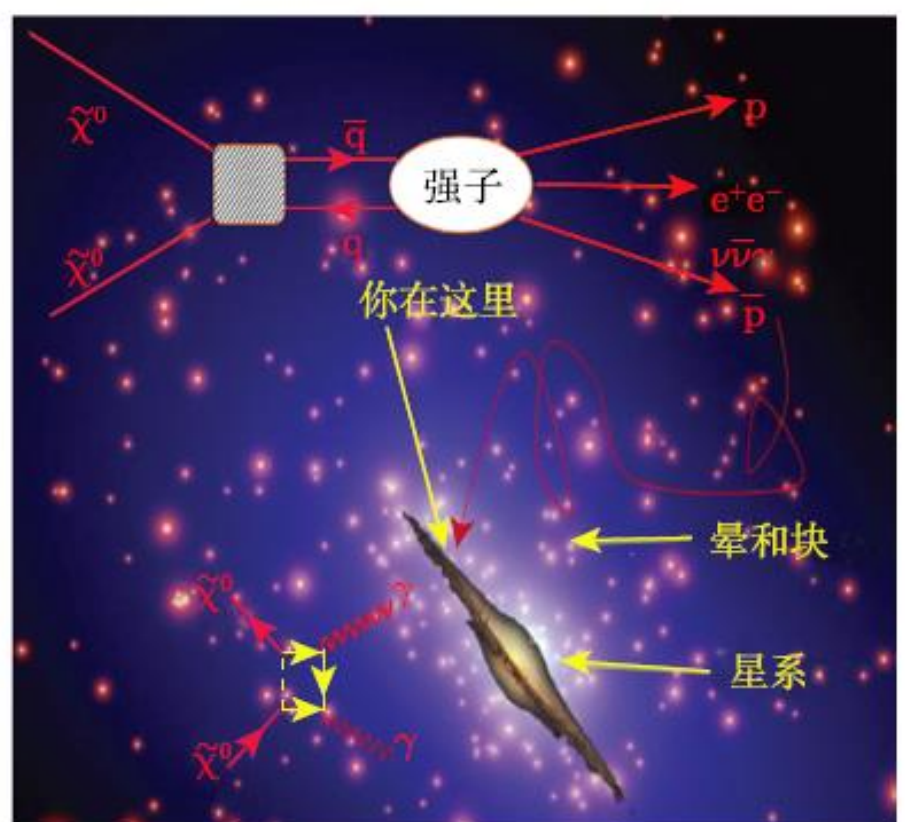
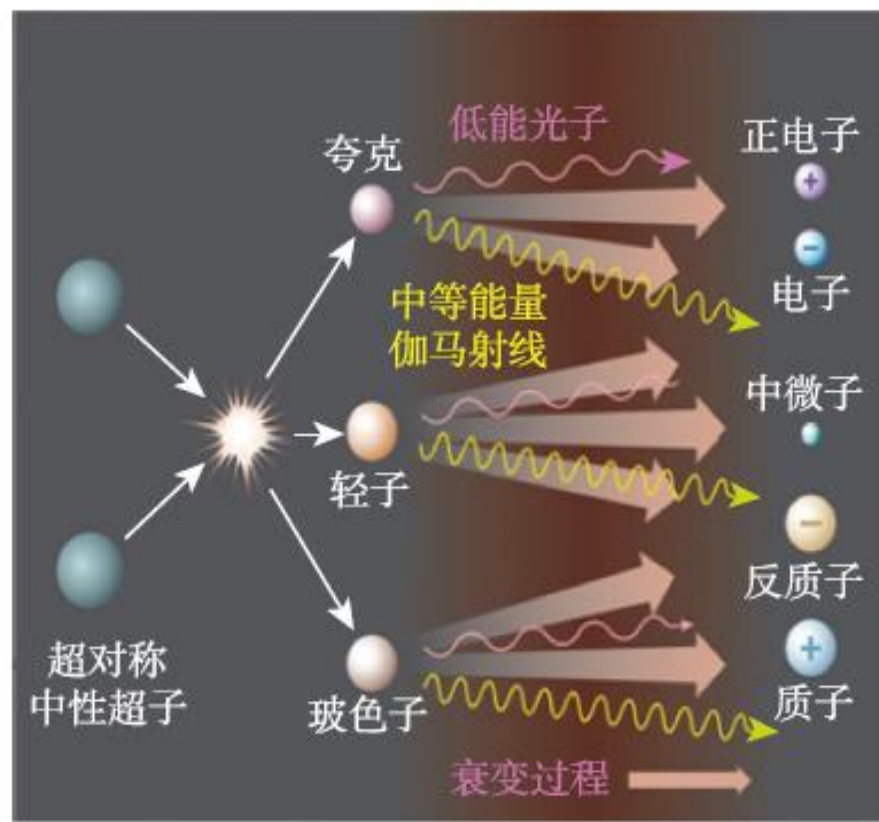




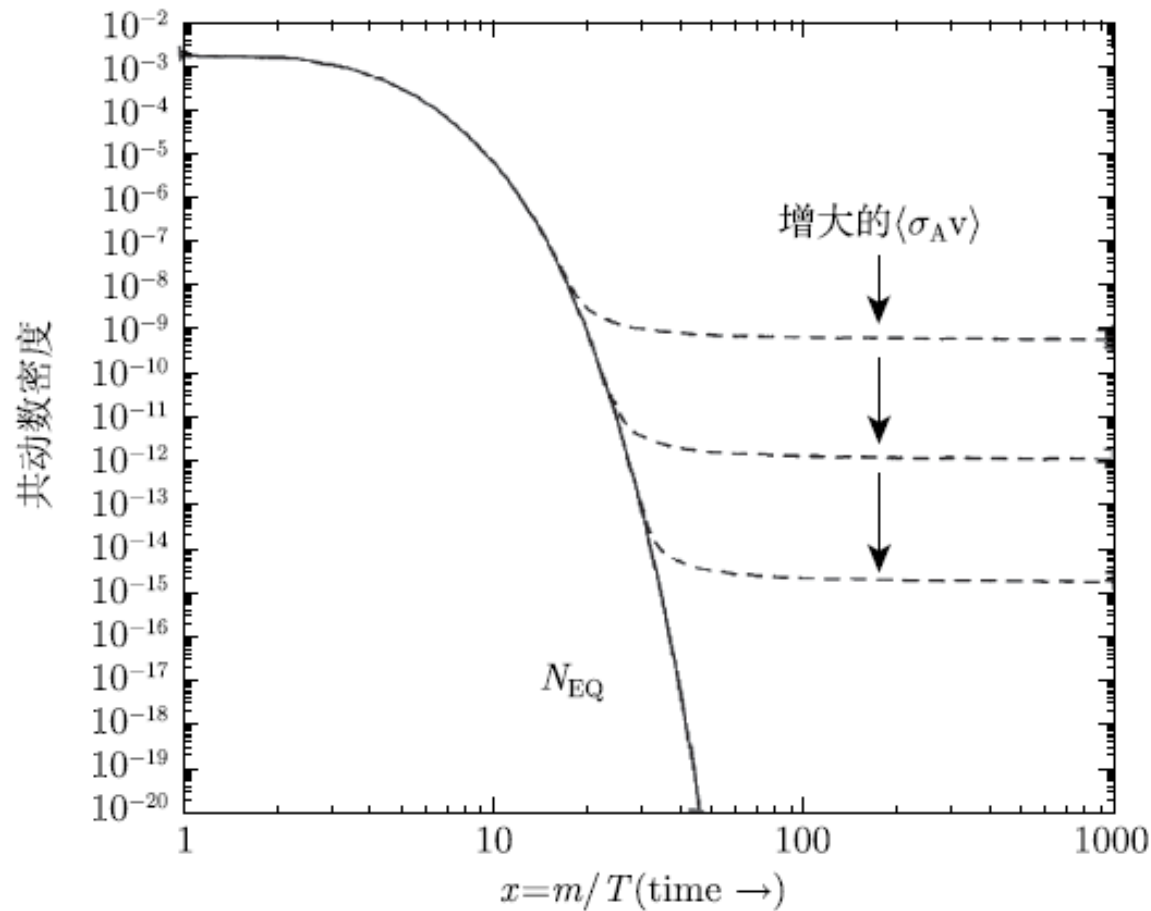
图 6.1.1 全球深地物理探测实验室的分布地图。注意 #26 ANDES 深地实验室，目前还只是一项决议，将是南半球唯一科学地下实验室



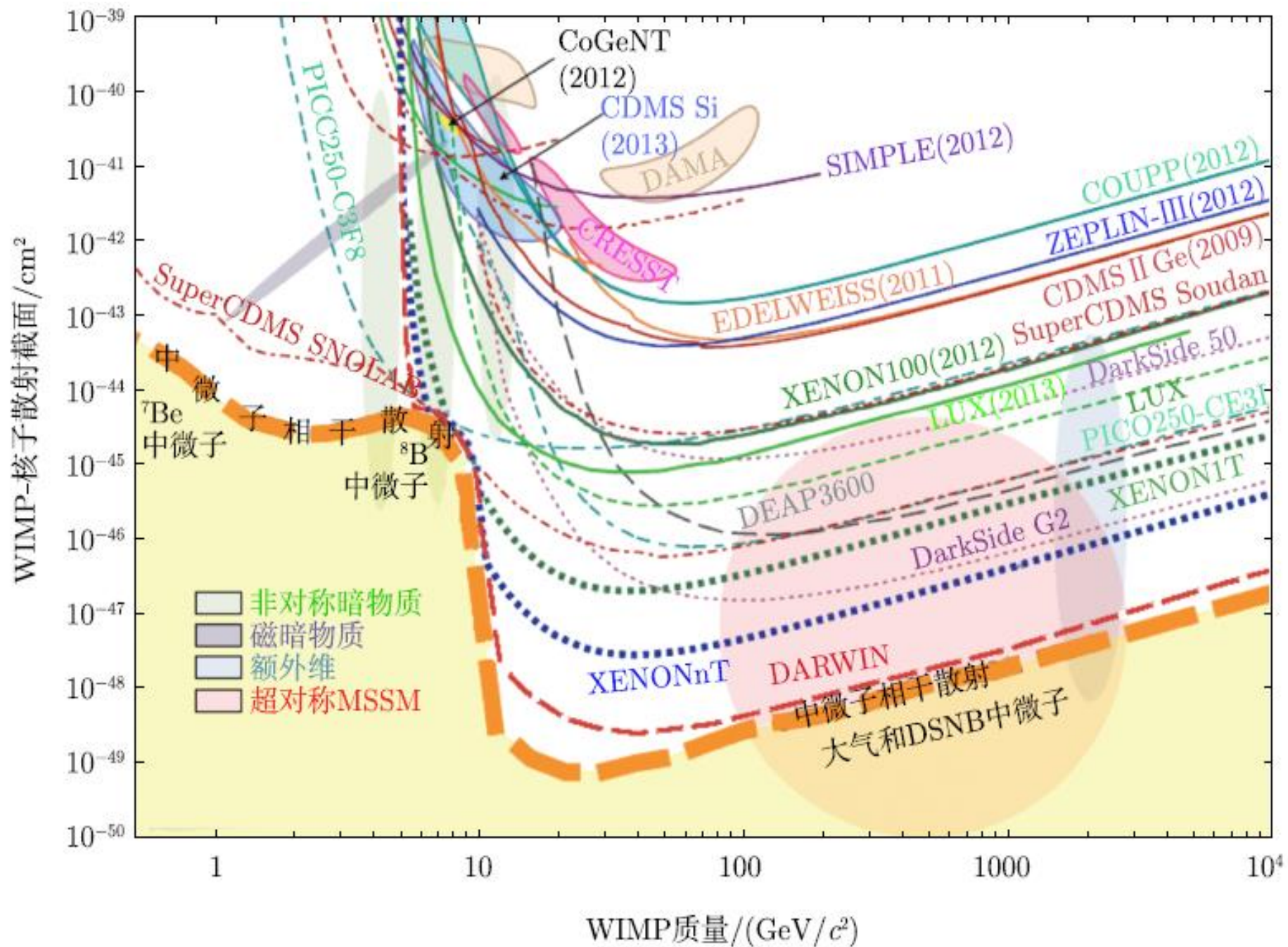
Indirect detection



WIMP miracle



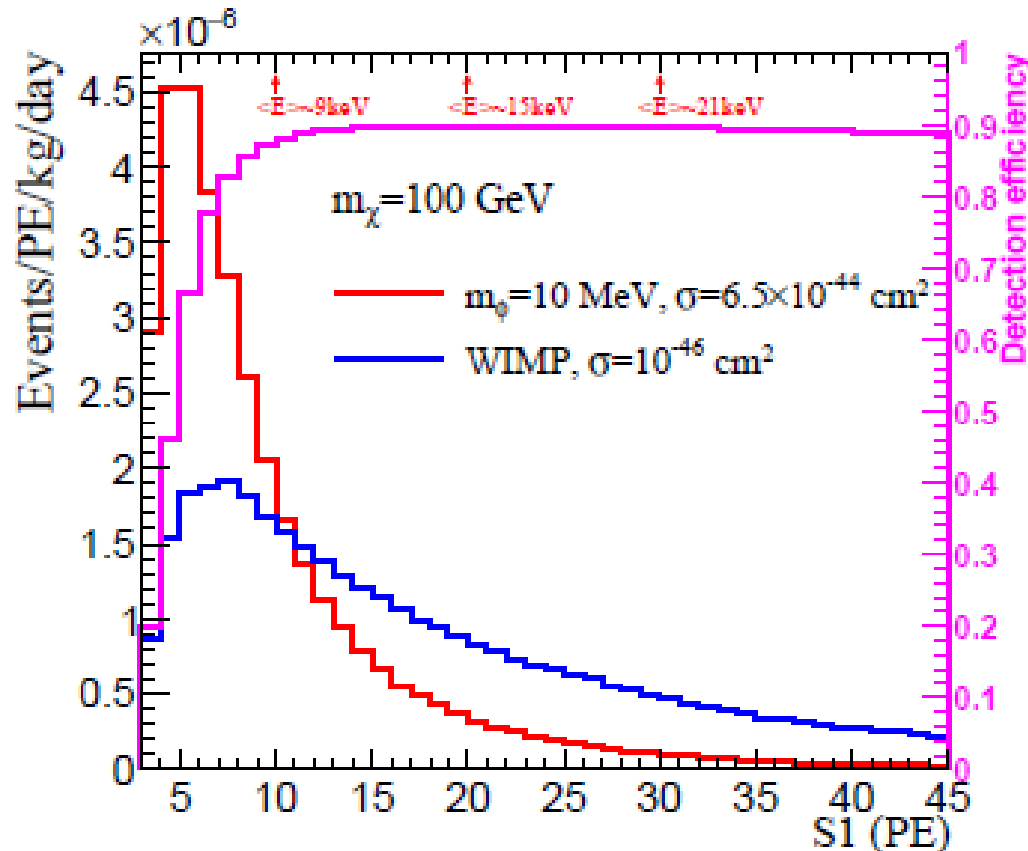
$$\Omega_\chi h^2 = 0.1 \times \left(\frac{x_f}{10}\right) \left(\frac{g_*}{100}\right)^{1/2} \frac{0.282 \text{ pb}}{a + \frac{3}{x_f} b},$$



Summary

- **Less and less space for WIMP above 1GeV!**
- **We are less sensitive to the light dark matter**

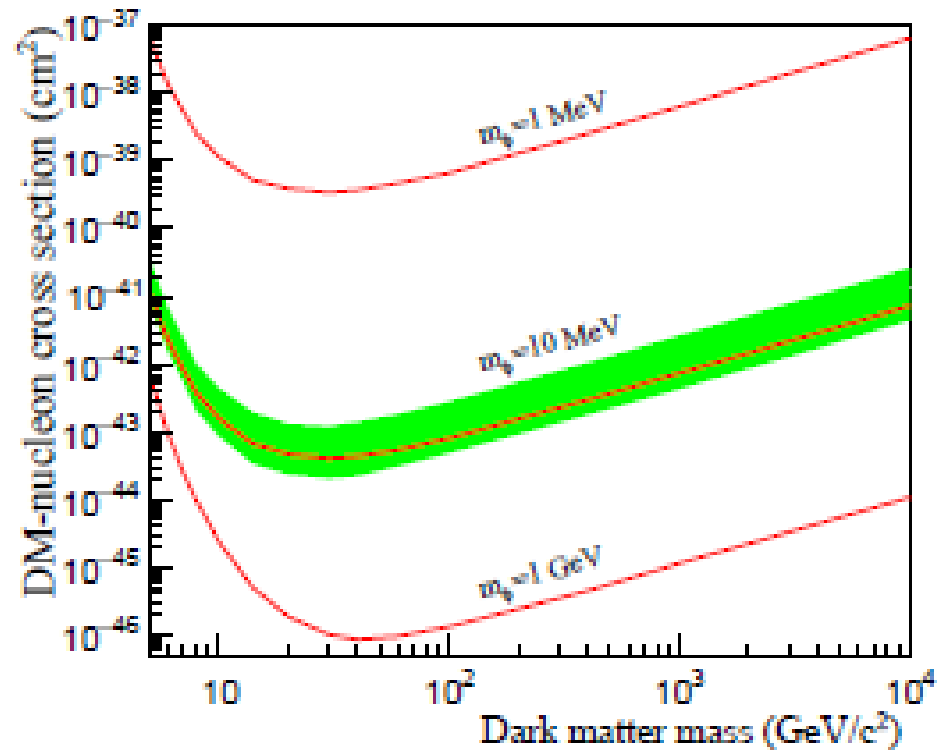
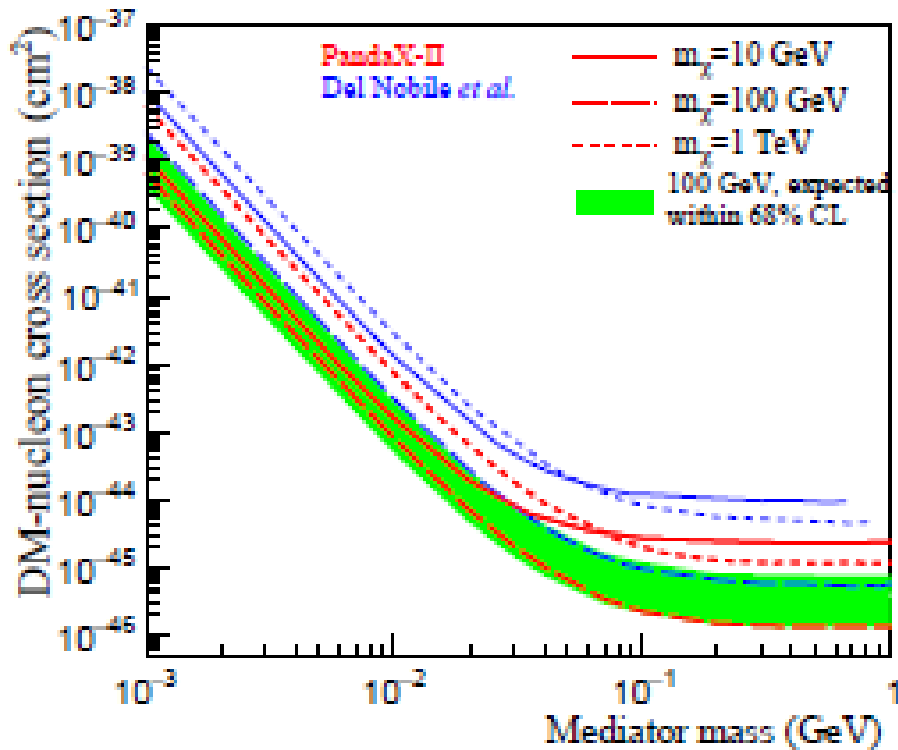
Reasons of the less sensitivity



From PANDX group arXiv:1802.06912

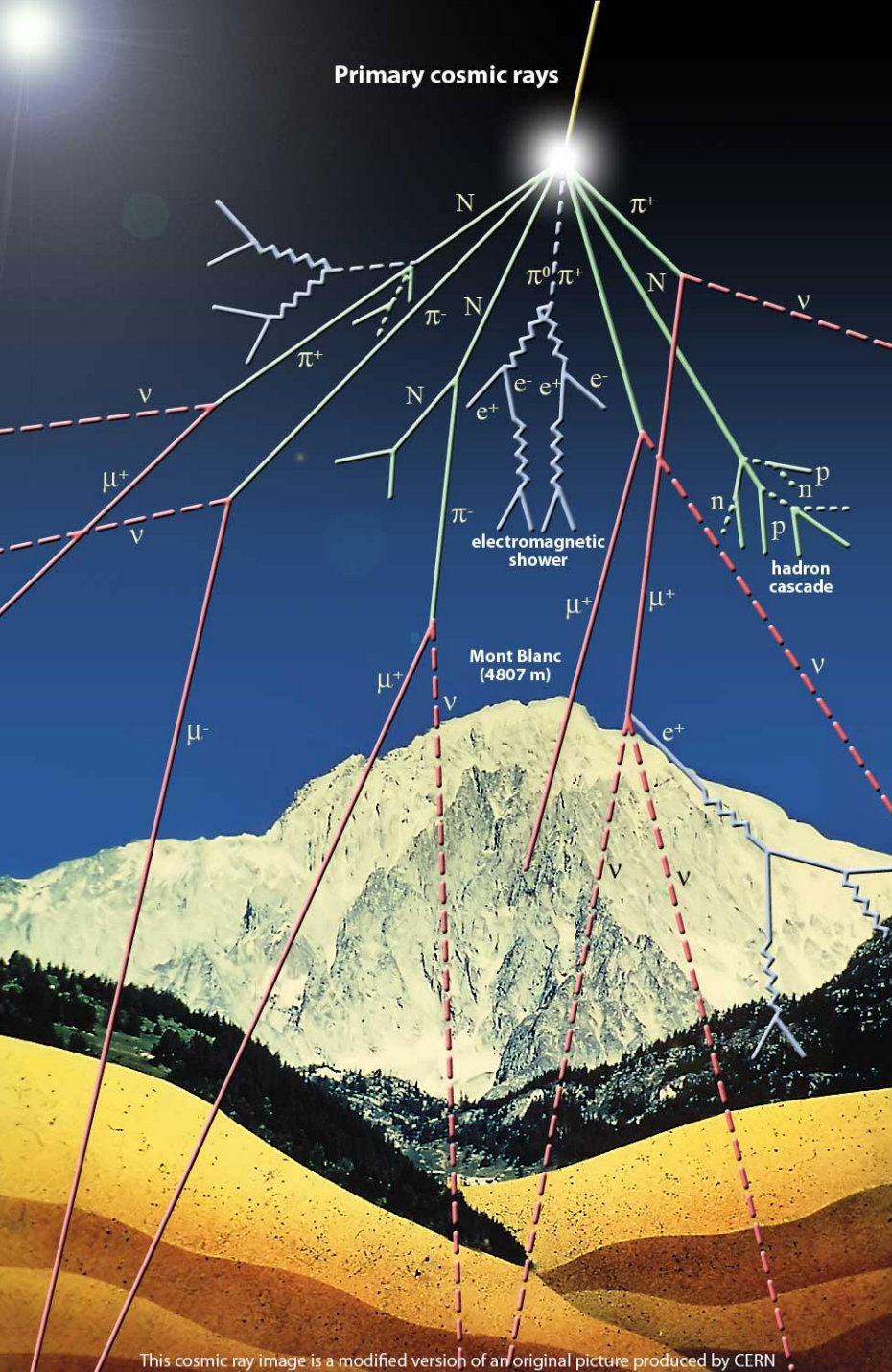
$$\frac{dR}{dE_r} = \frac{n_{\chi} \sigma_0}{4m_R^2 v_E} F^2(\sqrt{2m_A E_r}) \left(\text{erf}\left(\frac{v_{\min} + v_E}{v_0}\right) - \text{erf}\left(\frac{v_{\min} - v_E}{v_0}\right) \right)$$

PANDX constraints on light Mediator



From PANDX group *arXiv:1802.06912*

A short introduction to Cosmic Rays



1000个粒子/平米/秒

90% 质子
9% α 粒子
其它是重核

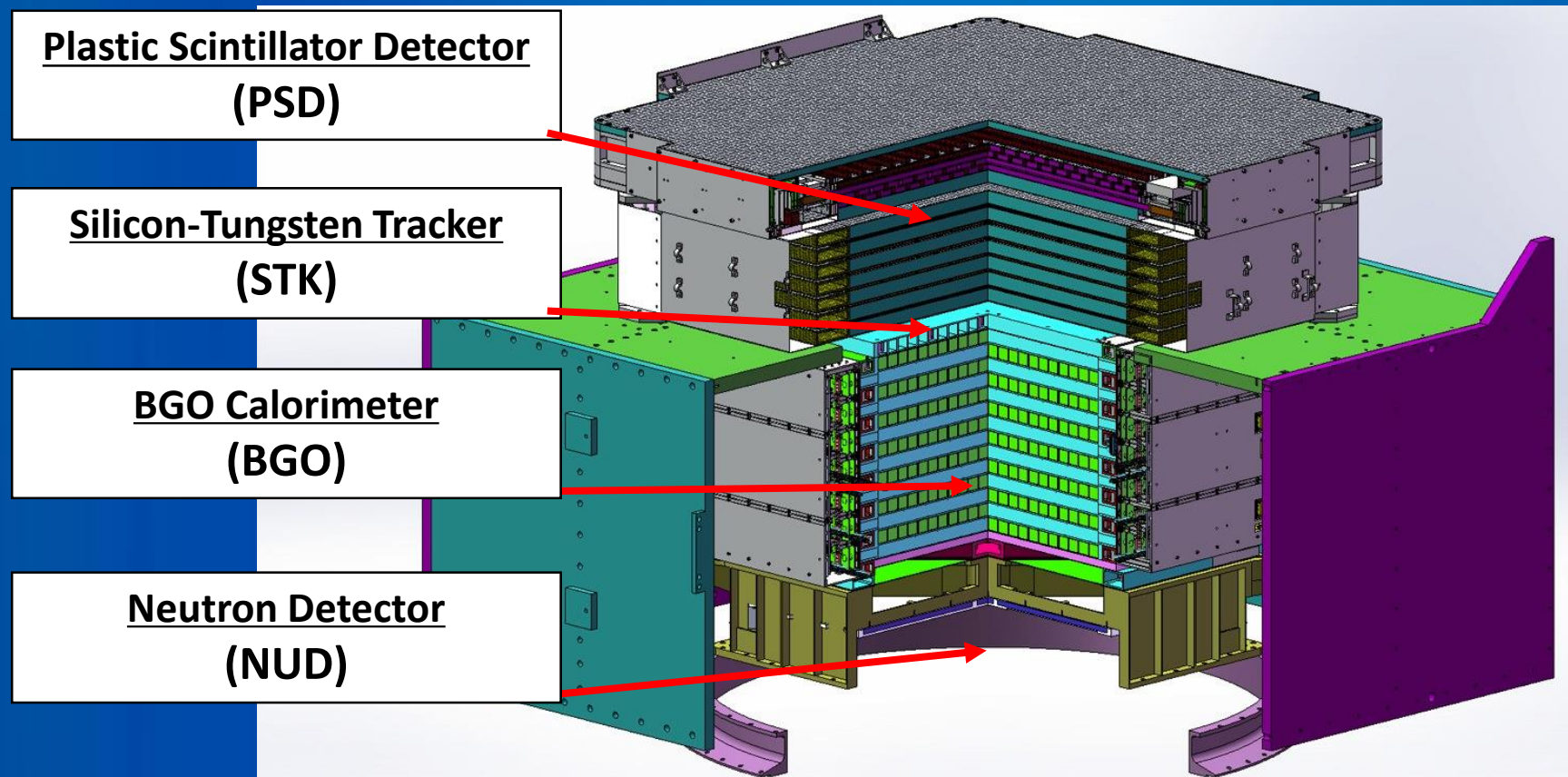
最高可达 10^{20}eV

Where? How?

探测手段：云室

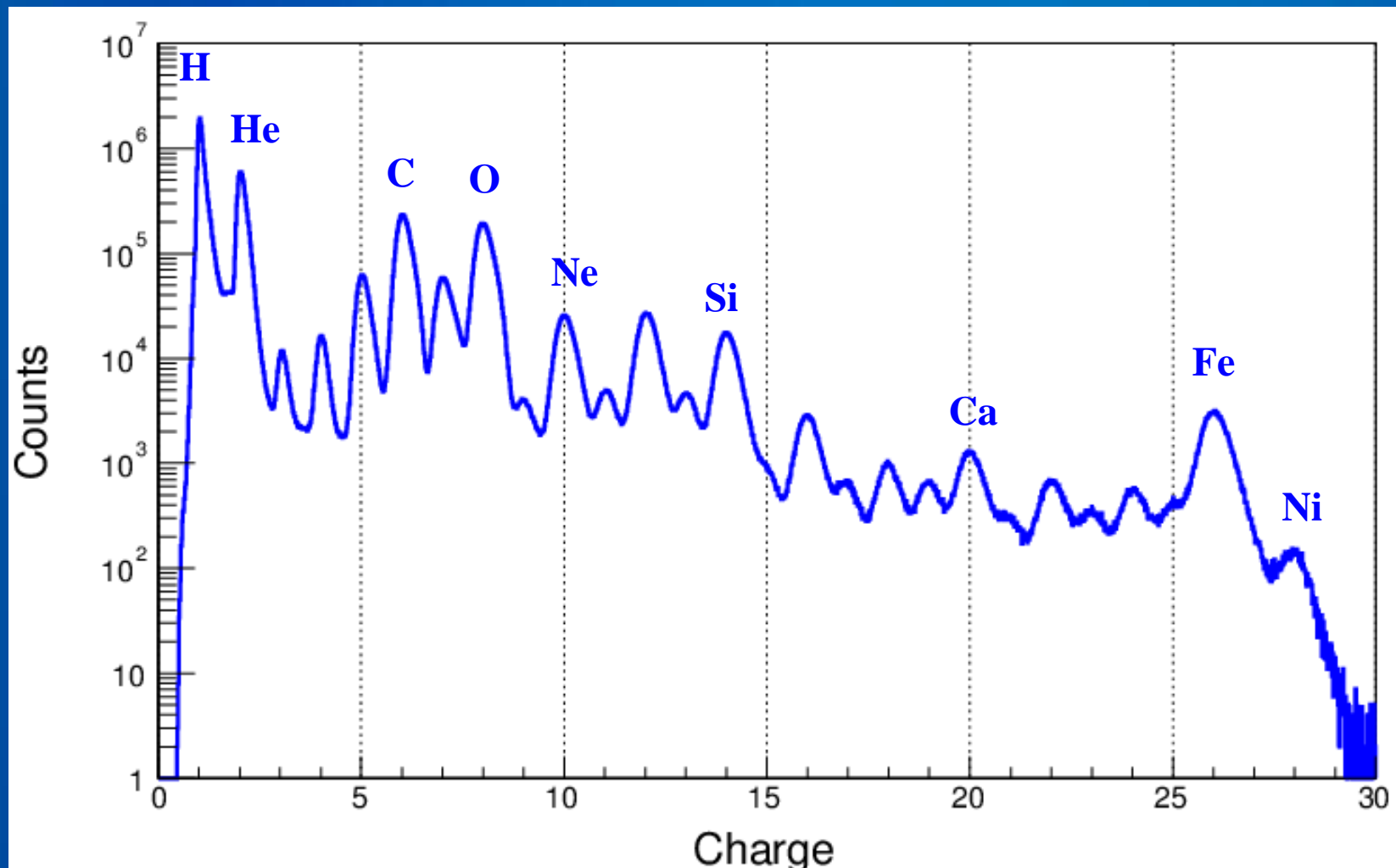


手段2:



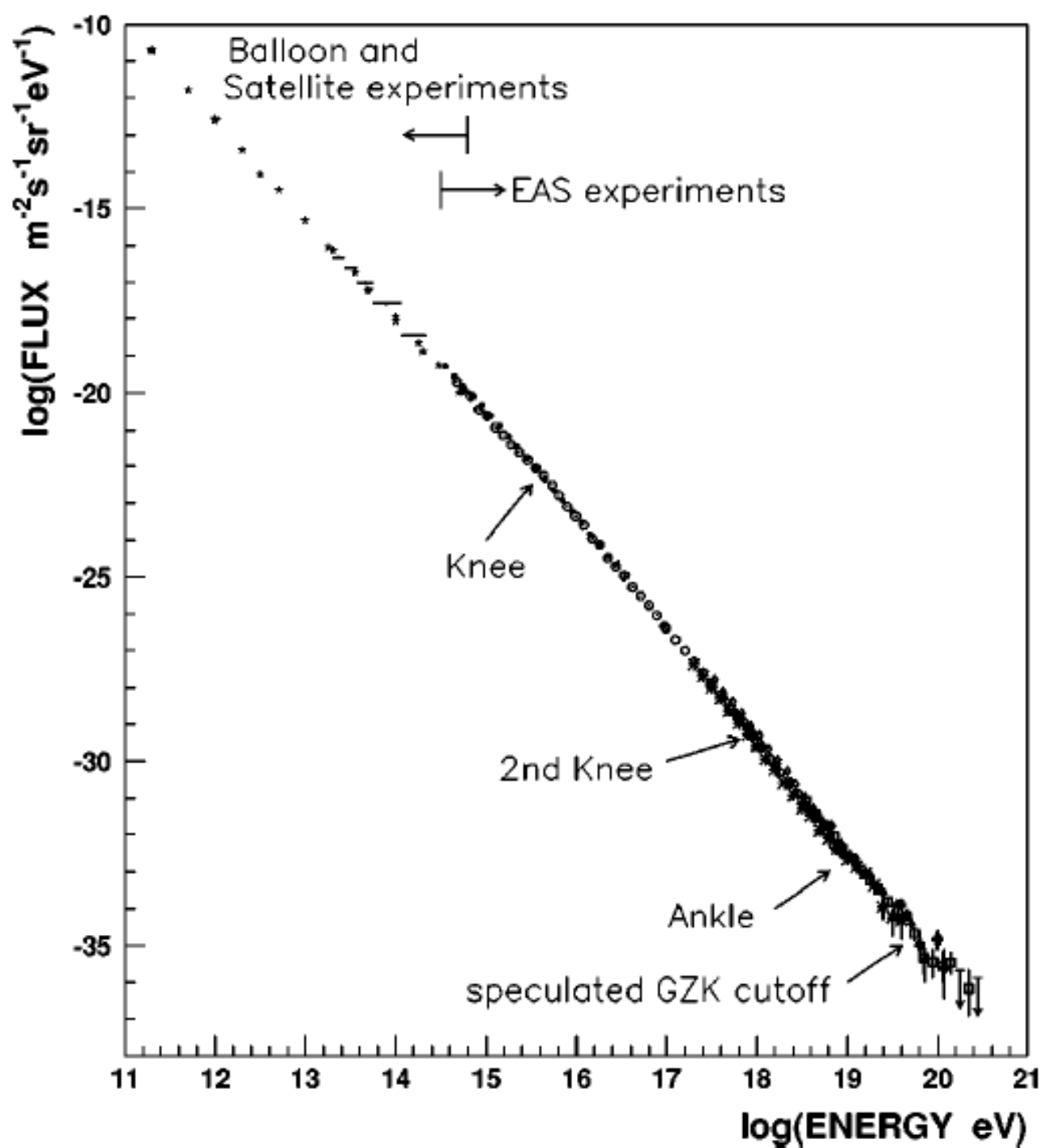
- Charge measurement (dE/dx in PSD, STK and BGO)
- Pair production and tracking (STK and BGO)
- Precise energy measurement (BGO bars)
- Hadron rejection (BGO and neutron detector)

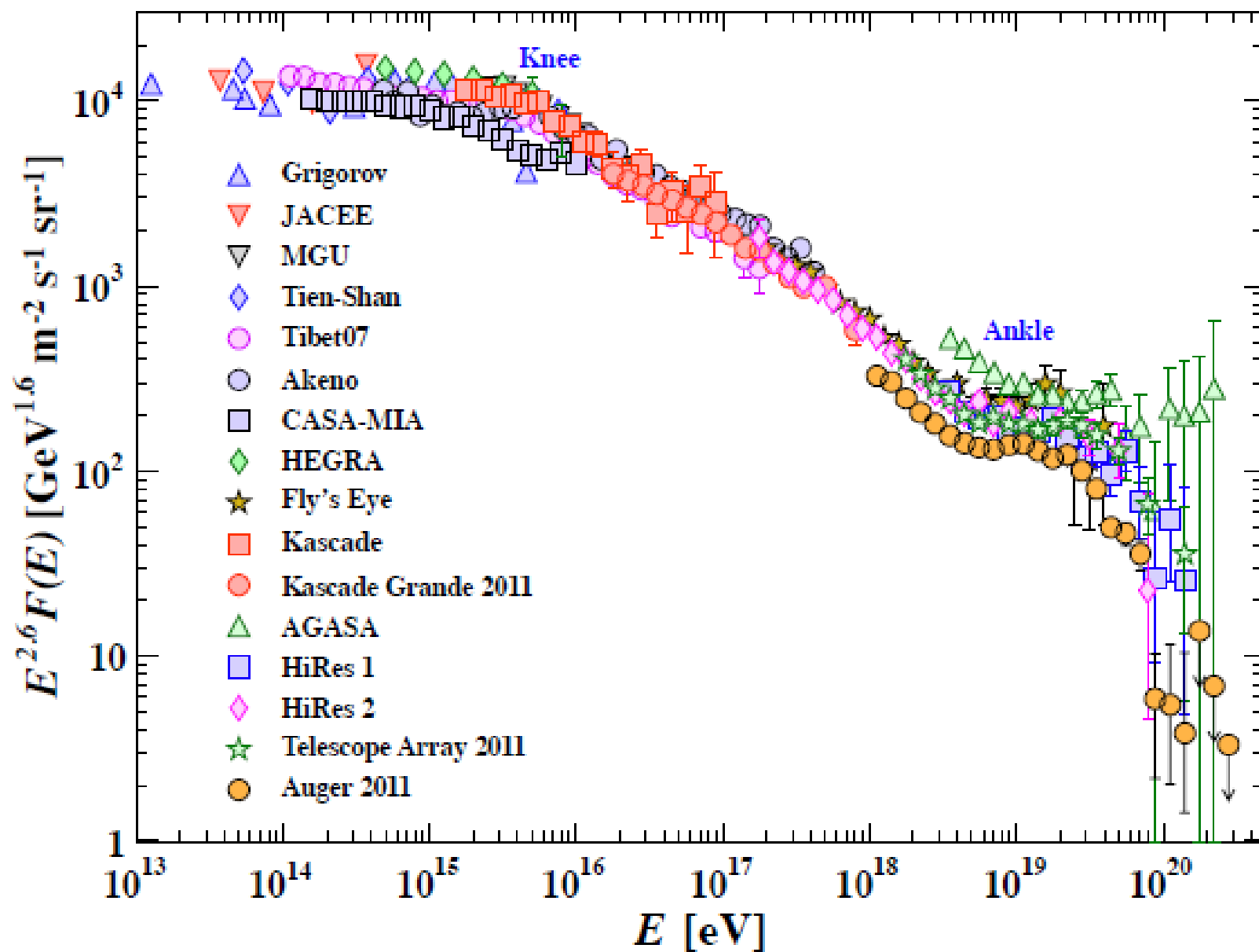
On-orbit performance: Charge measurement



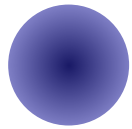
For protons and Irons, the charge resolutions are 0.13e and 0.32e, respectively.

幂律谱

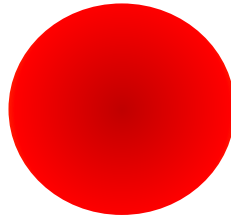




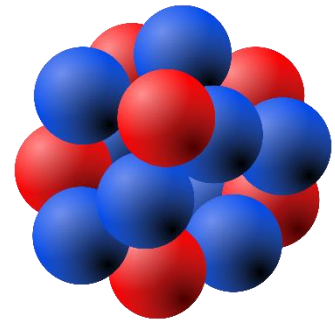
Story of CRDM



CR



DM



Nucleus

From CR to DM flux

After a single collision by the CR

$$T_{\chi} = T_{\chi}^{\max} \frac{1 - \cos \theta}{2}, \quad T_{\chi}^{\max} = \frac{T_i^2 + 2m_i T_i}{T_i + (m_i + m_{\chi})^2 / (2m_{\chi})},$$

The minimal incoming energy required for CR

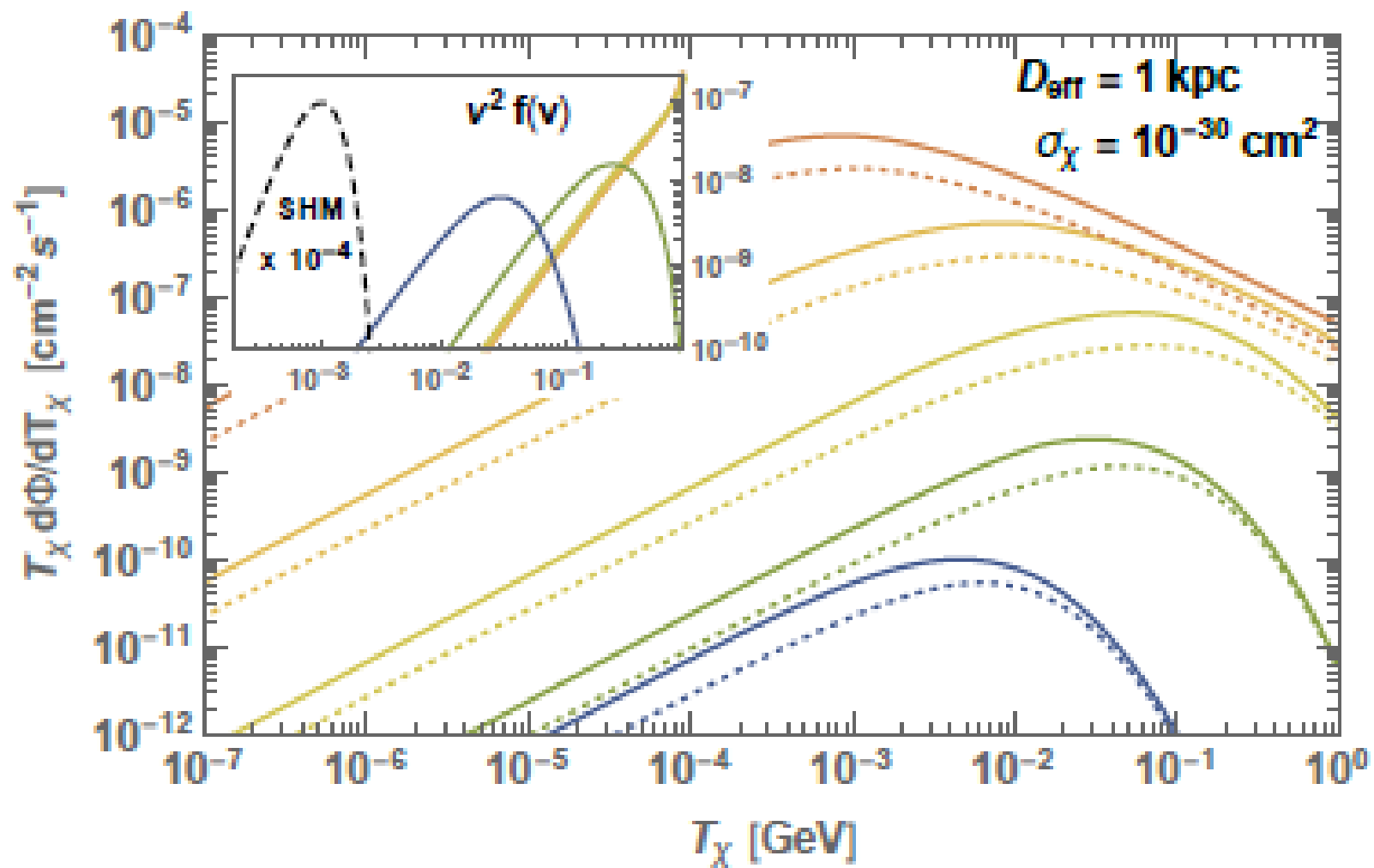
$$T_i^{\min} = \left(\frac{T_{\chi}}{2} - m_i \right) \left[1 \pm \sqrt{1 + \frac{2T_{\chi}}{m_{\chi}} \frac{(m_i + m_{\chi})^2}{(2m_i - T_{\chi})^2}} \right],$$

CR i in a differential volume

$$d\Gamma_{\text{CR}_i \rightarrow \chi} = \sigma_{\chi i} \times \frac{\rho_\chi}{m_\chi} \frac{d\Phi_i^{\text{LIS}}}{dT_i} dT_i dV$$

The CR induced DM flux

$$\begin{aligned} \frac{d\Phi_\chi}{dT_\chi} &= D_{\text{eff}} \frac{\rho_\chi^{\text{local}}}{m_\chi} \times \\ &\times \sum_i \sigma_{\chi i}^0 G_i^2(2m_\chi T_\chi) \int_{T_i^{\text{min}}}^{\infty} dT_i \frac{d\Phi_i^{\text{LIS}}/dT_i}{T_\chi^{\text{max}}(T_i)} \end{aligned}$$



From T. Bringmann et. al. [arXiv:1810.10543](https://arxiv.org/abs/1810.10543)

Attenuation of CRDM flux





DM flux at the depth z

$$\frac{d\Phi_\chi}{dT_\chi^z} = \left(\frac{dT_\chi}{dT_\chi^z} \right) \frac{d\Phi_\chi}{dT_\chi} = \frac{4m_\chi^2 e^{z/\ell}}{(2m_\chi + T_\chi^z - T_\chi^z e^{z/\ell})^2} \frac{d\Phi_\chi}{dT_\chi}$$

in which

$$\ell^{-1} \equiv \sum_N n_N \sigma_{\chi N} \frac{2m_N m_\chi}{(m_N + m_\chi)^2}$$

is the mean free path of a DM particle.

CRDM scattering in detectors

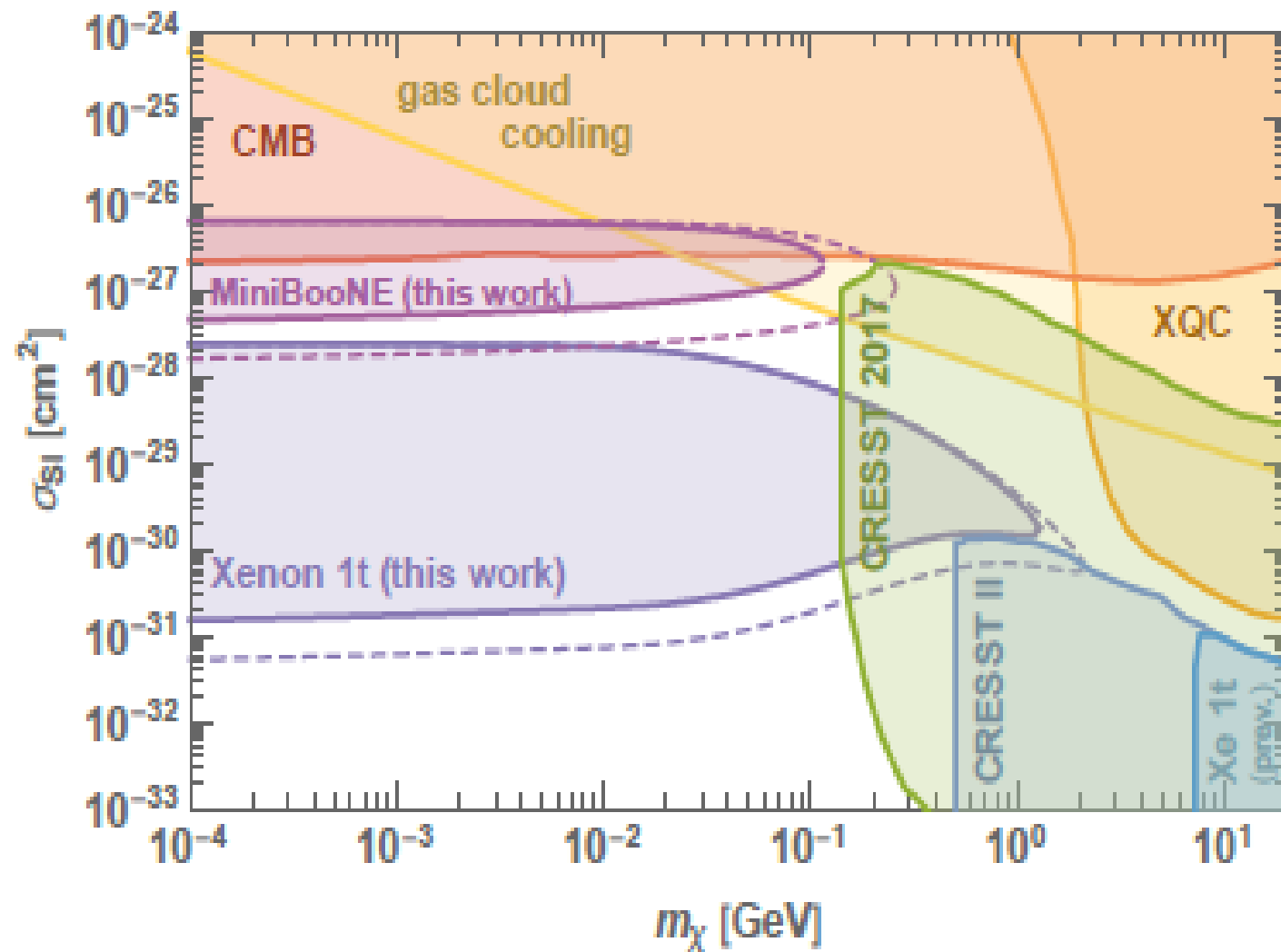
$$\frac{d\Gamma_N}{dT_N} = \sigma_{\chi N}^0 G_N^2 (2m_N T_N) \int_{T_\chi(T_\chi^z, \min)}^{\infty} \frac{dT_\chi}{T_{r,N}^{\max}(T_\chi^z)} \frac{d\Phi_\chi}{dT_\chi}.$$

Comparison with the WIMP scattering

$$\begin{aligned}\Gamma_N^{\text{DM}} &= \int_{T_1}^{T_2} dT_N \sigma_{\chi N}^{\text{DM}} \int_0^\infty dT_{\text{DM}} \frac{d\Phi_{\text{DM}}}{dT_{\text{DM}}} \frac{\Theta [T_N^{\text{max}}(T_{\text{DM}}) - T_N]}{T_N^{\text{max}}(T_{\text{DM}})} \\ &\simeq \kappa \frac{\sigma_{\chi N}^{\text{DM}}}{m_{\text{DM}}} (\bar{v} \rho_{\text{DM}})^{\text{local}} \quad \text{for } m_{\text{DM}} \gg m_N, \quad (15)\end{aligned}$$

We can get

$$\begin{aligned}\sigma_\chi^{\text{SI,lim}} &= \kappa (\bar{v} \rho_{\text{DM}})^{\text{local}} \left(\frac{m_\chi + m_N}{m_\chi + m_p} \right)^2 \left(\frac{\sigma_{\text{DM}}^{\text{SI,lim}}}{m_{\text{DM}}} \right)_{m_{\text{DM}} \rightarrow \infty} \\ &\quad \times \left(\int_{T_1}^{T_2} dT_N \int_{T_\chi(T_\chi^{\text{z,min}})}^\infty \frac{dT_\chi}{T_{r,N}^{\text{max}}} \frac{d\Phi_\chi}{dT_\chi} \right)^{-1} \quad (16)\end{aligned}$$



From T. Bringmann et. al. [arXiv:1810.10543](https://arxiv.org/abs/1810.10543)

Our work

Simplified models for scalar and vector mediator

Scalar: $g_{\chi s} \phi \bar{\chi} \chi + g_{N s} \phi \bar{N} N$

Vector: $g_{\chi v} V_\mu \bar{\chi} \gamma^\mu \chi + g_{N v} V_\mu \bar{N} \gamma^\mu N$

For the scalar

$$\left(\frac{d\sigma_{\chi N}}{dT_{\chi}} \right)_{\text{scalar, CR}} = \frac{g_{Ns}^2 g_{\chi s}^2 A^2 F(q^2) (2m_{\chi} + T_{\chi}) (2m_N^2 + m_{\chi} T_{\chi})}{8\pi T_l (T_l + 2m_l) (m_s^2 + 2m_{\chi} T_{\chi})^2}$$

$$\frac{d\sigma_{\chi T}}{dE_T} = \frac{g_{Ns}^2 g_{\chi s}^2 A^2 F(q^2) m_T (2m_N^2 + E_T m_T) (E_T m_T + 2m_{\chi}^2)}{8\pi m_N^2 T_{\chi} (m_s^2 + 2E_T m_T)^2 (2m_{\chi} + T_{\chi})}$$

For the vector

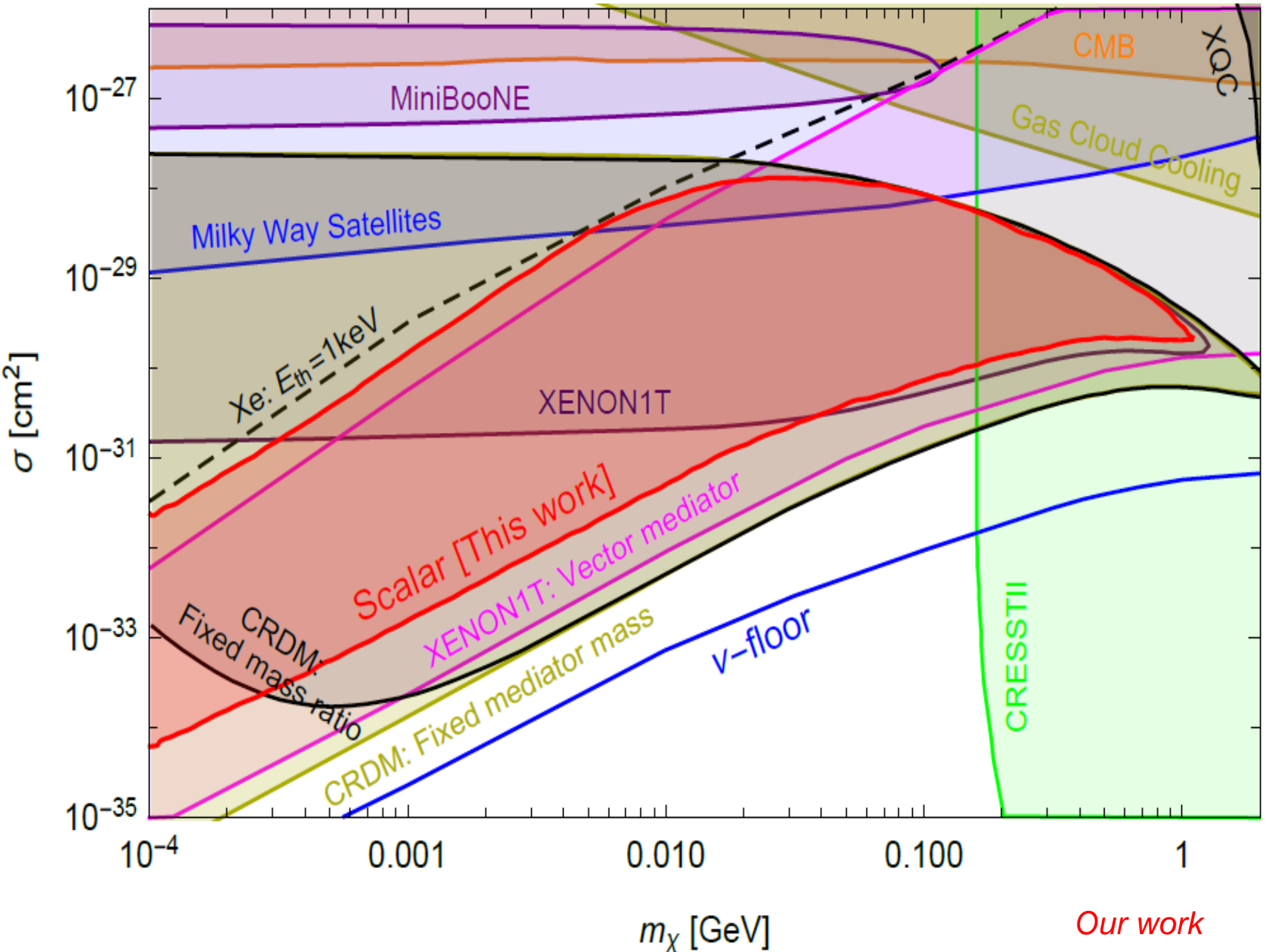
$$\left(\frac{d\sigma_{\chi N}}{d\Gamma_{\chi}} \right)_{\text{vector, CR}} = g_{\chi\nu}^2 g_{N\nu}^2 A^2 F^2(q^2) \frac{\left(2m_{\chi} (m_N + T_l)^2 - T_{\chi} \left((m_N + m_{\chi})^2 + 2m_{\chi} T_l \right) + m_{\chi} T_{\chi}^2 \right)}{4\pi (2m_{\chi} T_{\chi} + m_{\nu}^2)^2 (T_l^2 + 2m_l T_l)} \quad (7)$$

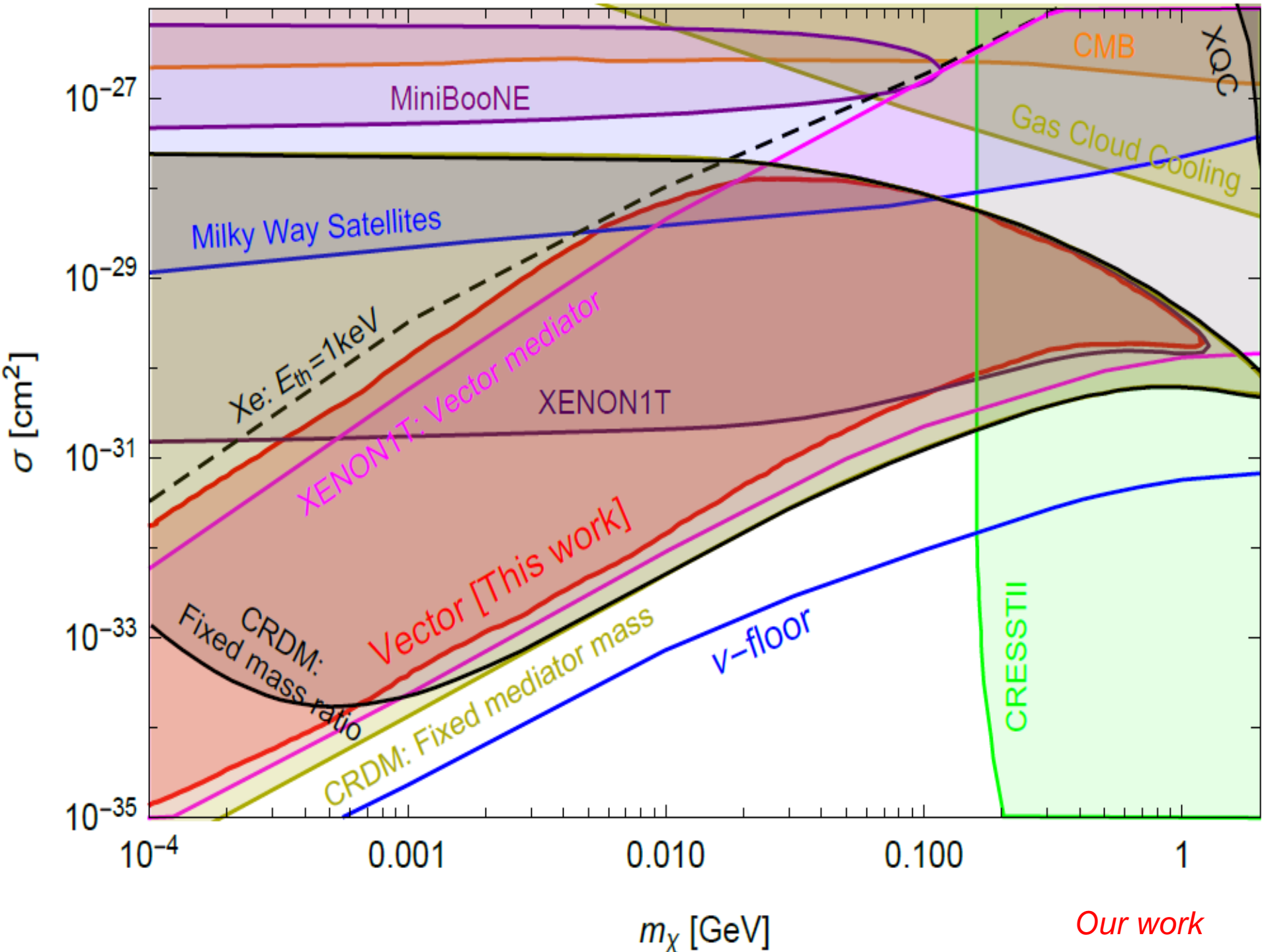
$$\frac{d\sigma_{\chi T}}{dE_T} = \frac{g_{N\nu}^2 g_{\chi\nu}^2 m_T \left(2m_N^2 (m_{\chi} + T_{\chi})^2 - E_T \left(m_N^2 (2(m_{\chi} + T_{\chi}) + m_T) + m_T m_{\chi}^2 \right) + E_T^2 m_N^2 \right)}{4\pi m_N^2 T_{\chi} (2E_T m_T + m_{\nu}^2)^2 (2m_{\chi} + T_{\chi})} \times A^2 F(q^2) \quad (5)$$

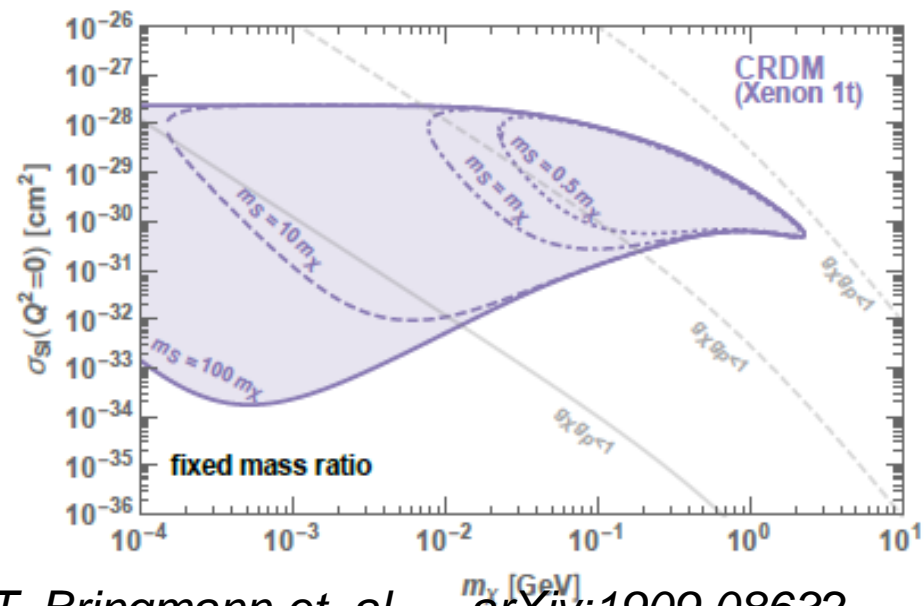
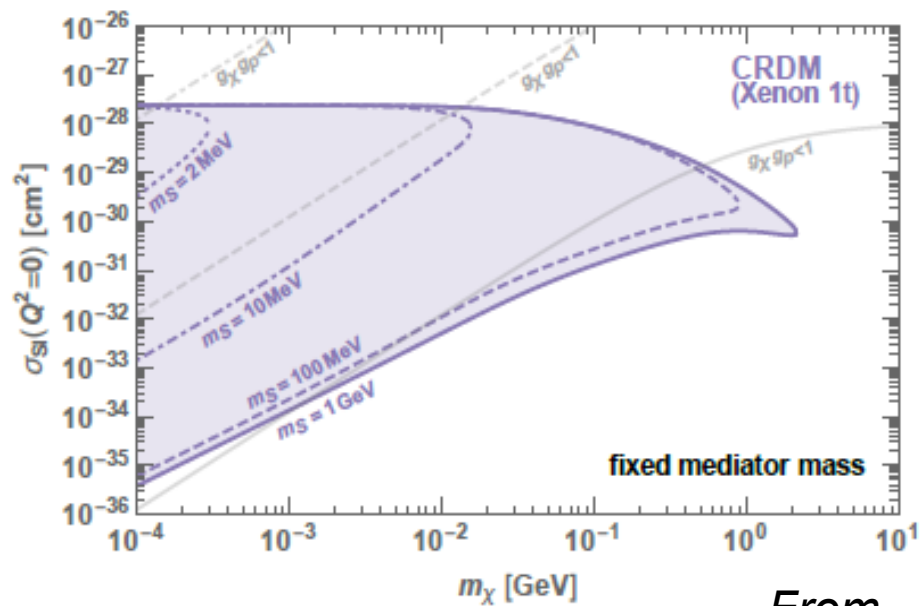
We calculate the mean free path of a DM particle in the integral .

$$\frac{d\Gamma_N}{dT_N} = \sigma_{\chi N}^0 G_N^2 (2m_N T_N) \int_{T_\chi(T_\chi^z, \min)}^{\infty} \frac{dT_\chi}{T_{r,N}^{\max}(T_\chi^z)} \frac{d\Phi_\chi}{dT_\chi} .$$

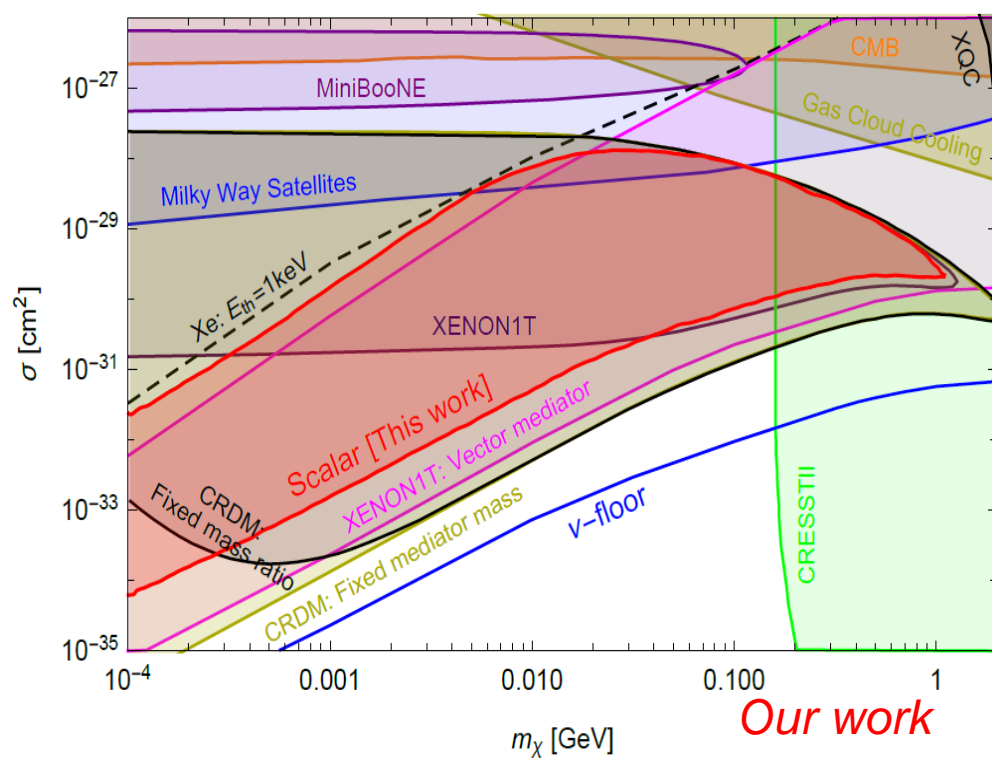
$$\ell^{-1} \equiv \sum_N n_N \sigma_{\chi N} \frac{2m_N m_\chi}{(m_N + m_\chi)^2}$$



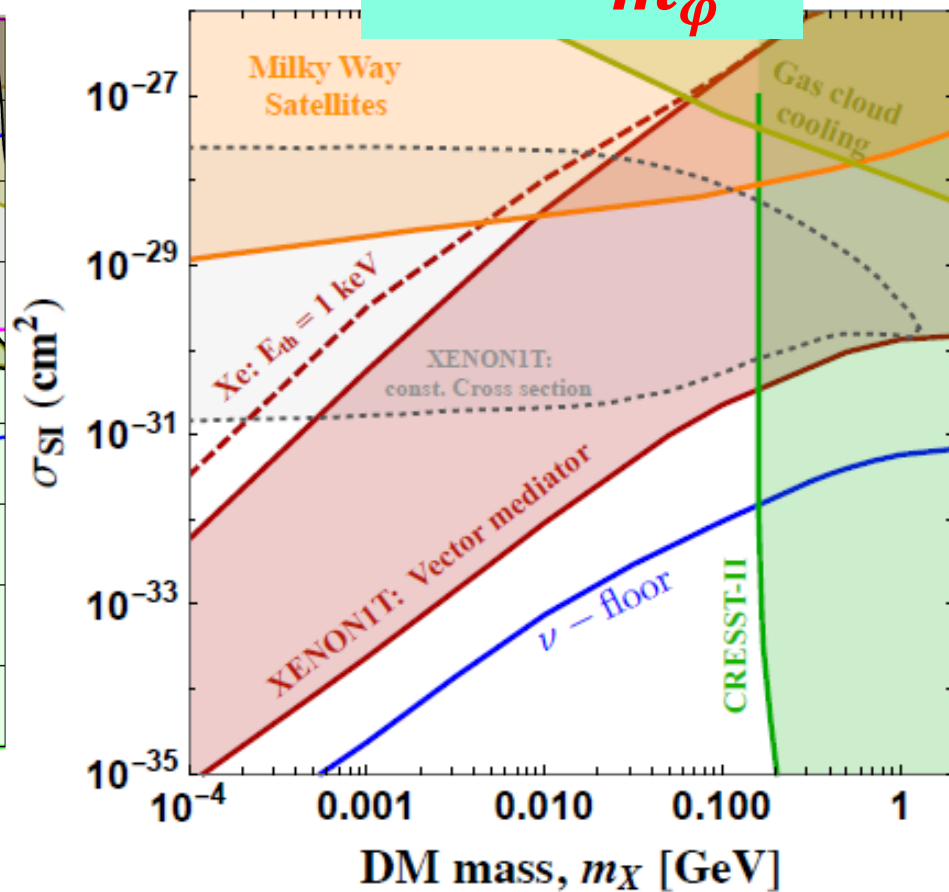
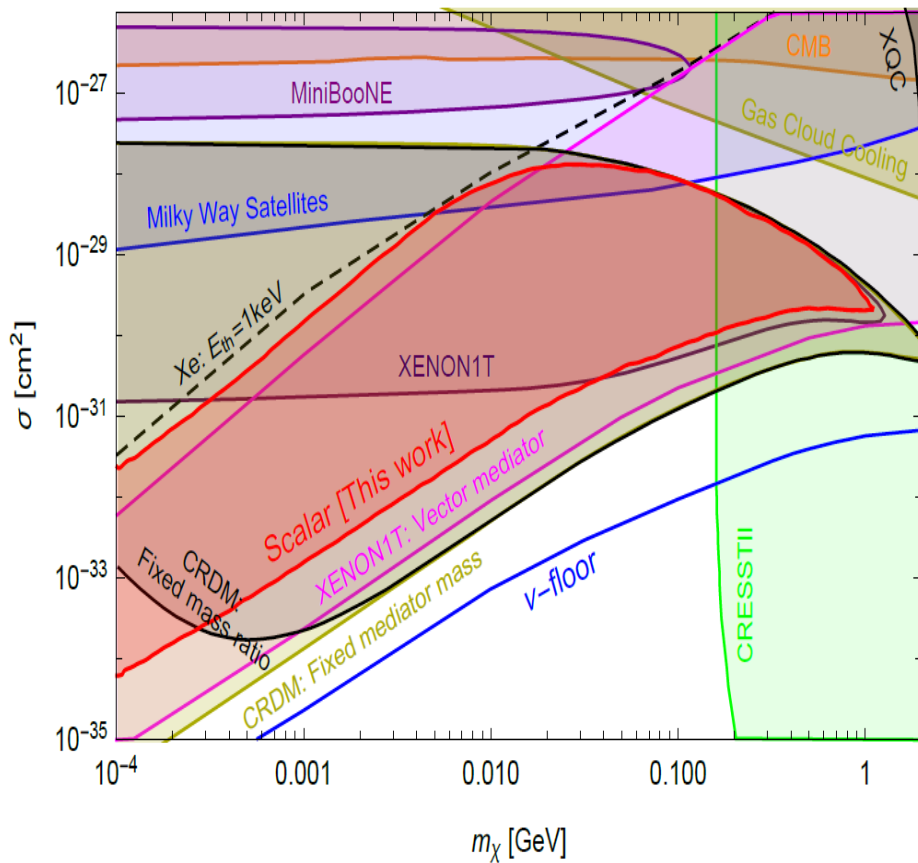




From ... T. Bringmann et. al. [arXiv:1909.08632](https://arxiv.org/abs/1909.08632)



$$\sigma^{SI} = \frac{4g^4\mu^2}{m_\phi^4}$$



From J. Dent et. al. [arXiv:1907.03782](https://arxiv.org/abs/1907.03782)

Note that: Definition of the cross section is also important!

$$\frac{d\Gamma_N}{dT_N} = \sigma_{\chi N}^0 G_N^2(2m_N T_N) \int_{T_\chi(T_\chi^z, \min)}^{\infty} \frac{dT_\chi}{T_{r,N}^{\max}(T_\chi)} \frac{d\Phi_\chi}{dT_\chi}.$$

$$\begin{aligned} \frac{d\Phi_\chi}{dT_\chi} &= D_{\text{eff}} \frac{\rho_\chi^{\text{local}}}{m_\chi} \times \\ &\times \sum_i \sigma_{\chi i}^0 G_i^2(2m_\chi T_\chi) \int_{T_i^{\min}}^{\infty} dT_i \frac{d\Phi_i^{\text{LIS}}/dT_i}{T_\chi^{\max}(T_i)} \end{aligned}$$

The cross section in the fundamental theory is a differential form

CONCLUSION

- Space in Dark Matter less than 1 GeV has rich physics
- CRDM is very good scenario for light DM
 - The attenuation is important
 - The definition of cross section is an issue

THANKS!