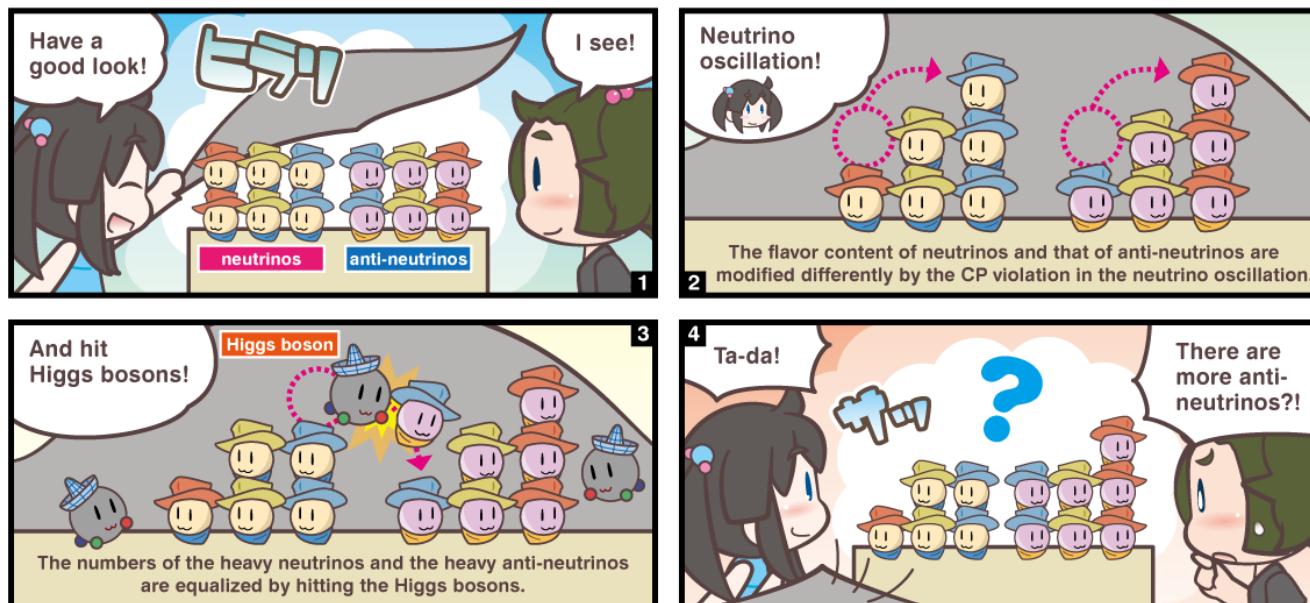


1807.06582 with Ryuichiro Kitano, Yuta Hamada  
(See also 1908.11864 with Shintaro Eijima, Ryuichiro Kitano  
and Eijima's talk.)

# Leptogenesis via active neutrino oscillation

Wen Yin, KAIST in Korea



# Contents

1. Introduction
2. Baryogenesis via active neutrino oscillation
3. Baryogenesis from PMNS matrix
4. Summary

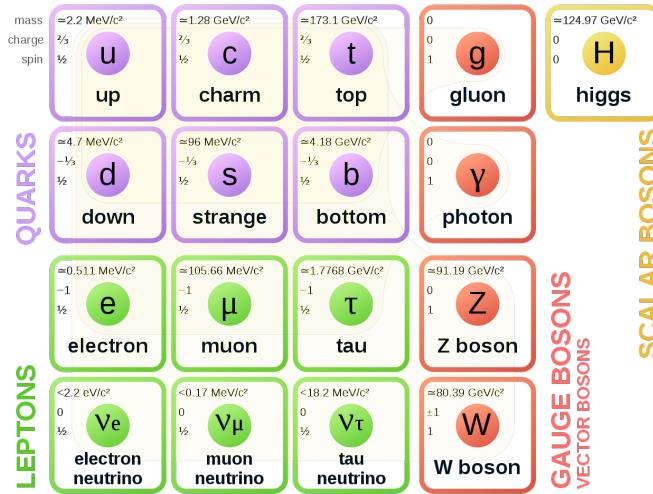
# 1. Introduction

The mysteries of particle physics and particle cosmology.

- Inflation
- Matter-antimatter asymmetry (Baryon asymmetry)
- Neutrino oscillation

*Standard model of particle theory(SM)*

- ...

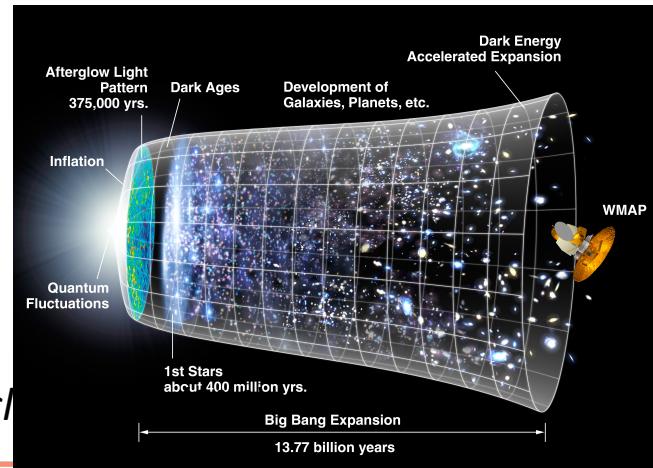
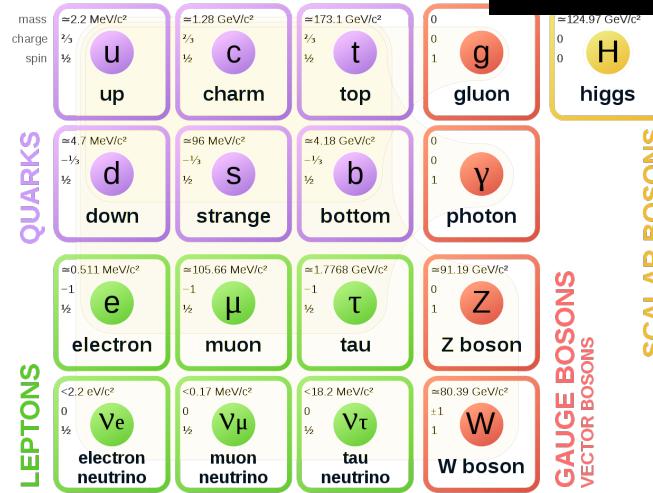


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*Standard model of particle physics*

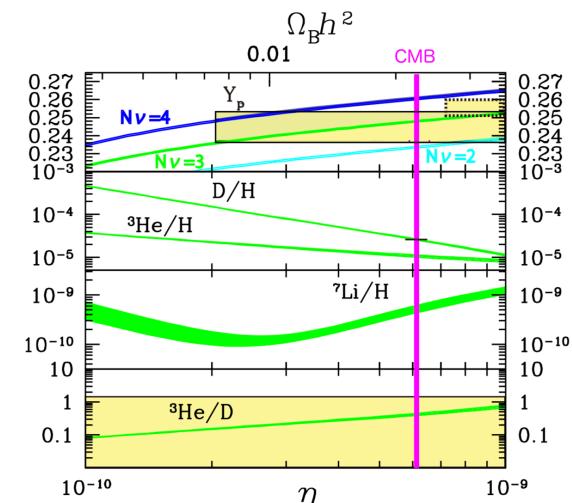
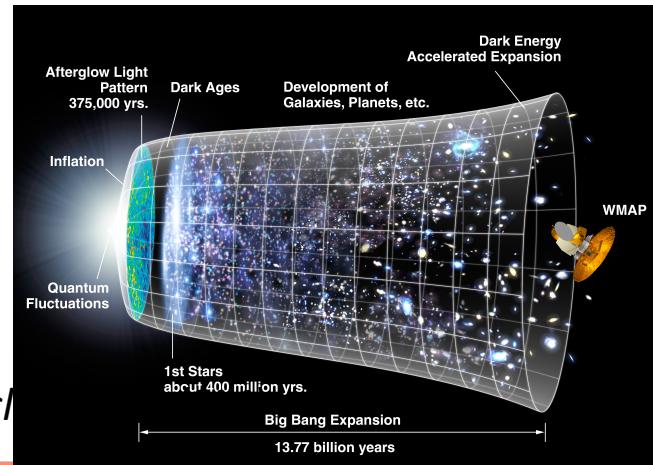
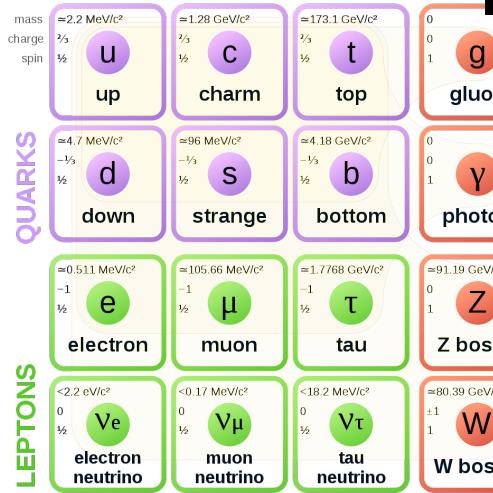


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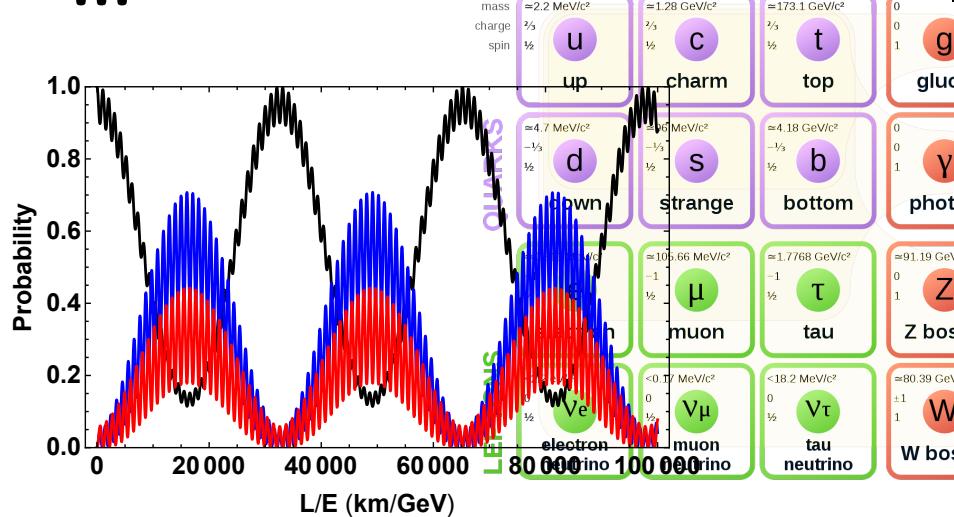
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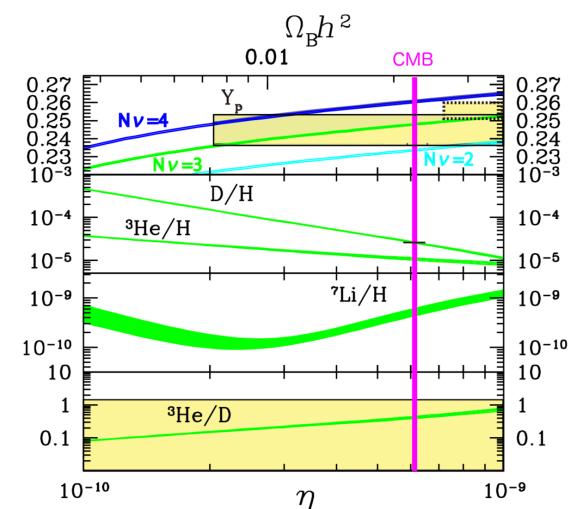
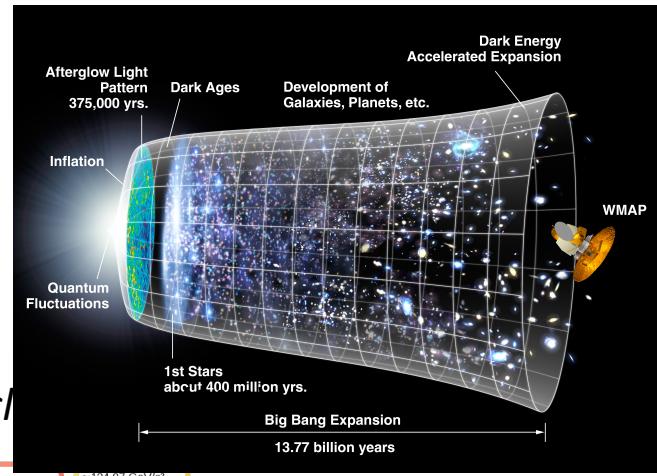
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wikipedia, Kawasaki et al, 1709.01211

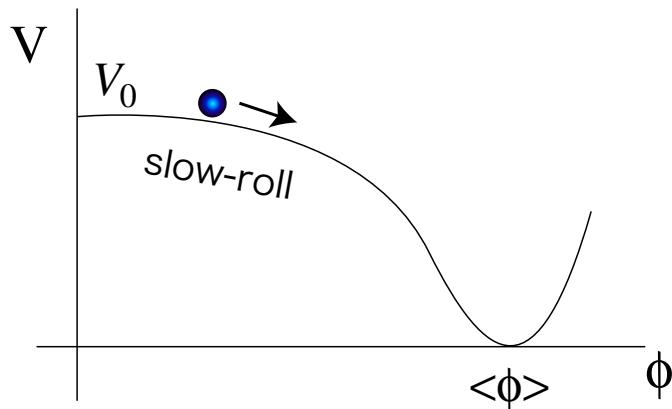
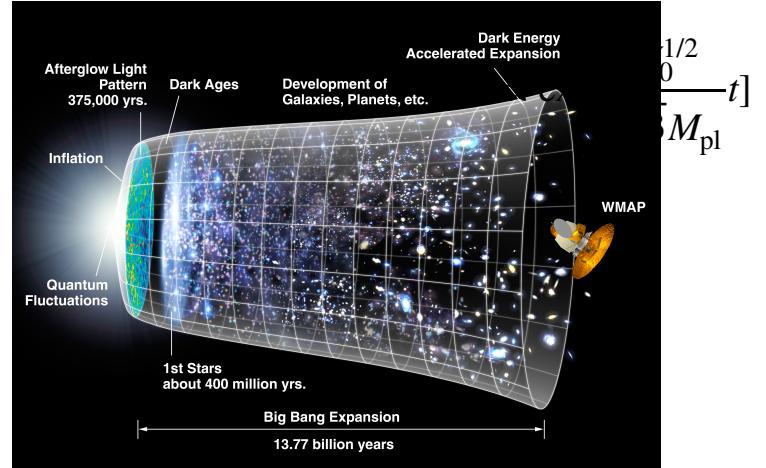


# New physics: inflation

A.Guth, 1980; K.Sato, 1980; A.Starobinsky, 1980; Kazanas, 1980; A.Linde, 1981; Albrecht, Steinhardt, 1981;

The Universe experienced an exponential expansion.

Inflation solves  
horizon and flatness  
problems.



Inflaton  $\phi$ :

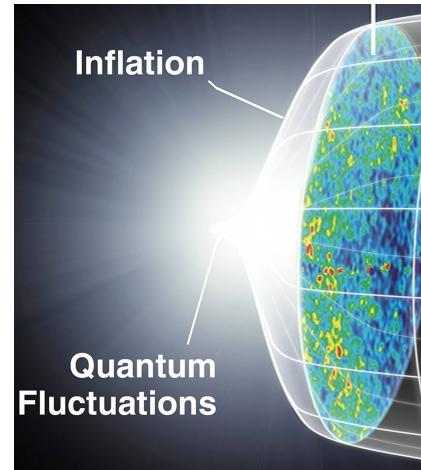
Quantum fluctuation for  
anisotropy of the Universe  
which has been observed in CMB.

# New physics: inflation

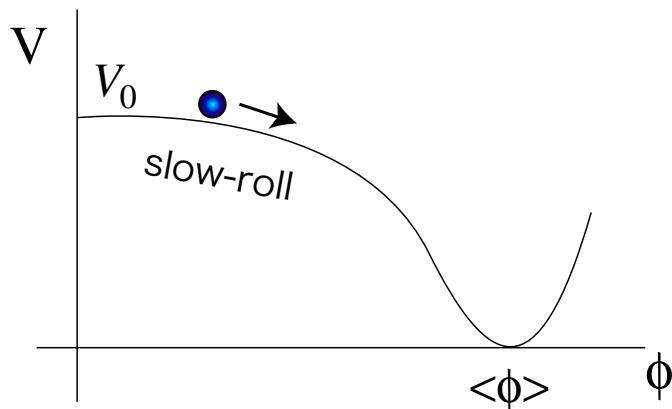
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$$a \propto \exp\left[\frac{V_0^{1/2}}{\sqrt{3}M_{pl}}t\right]$$



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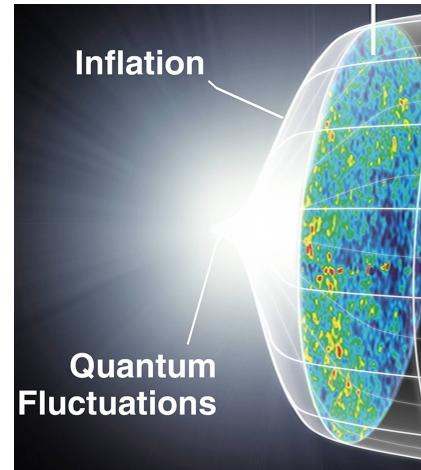
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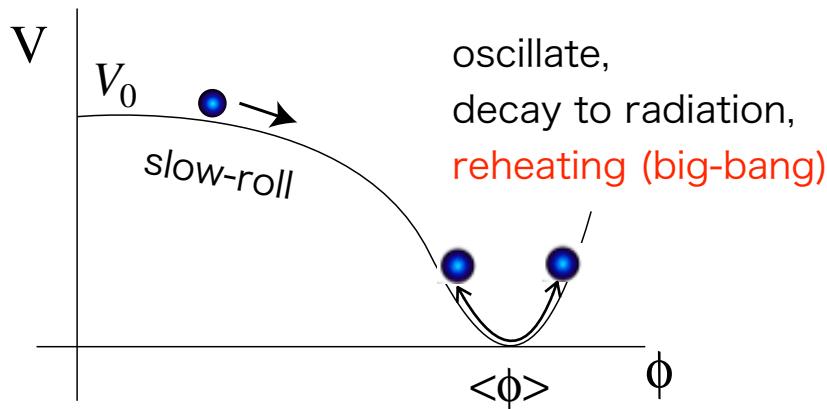
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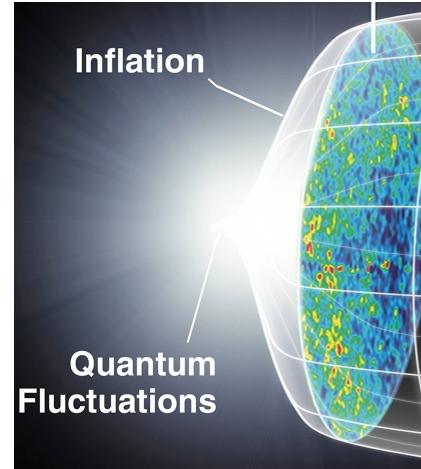
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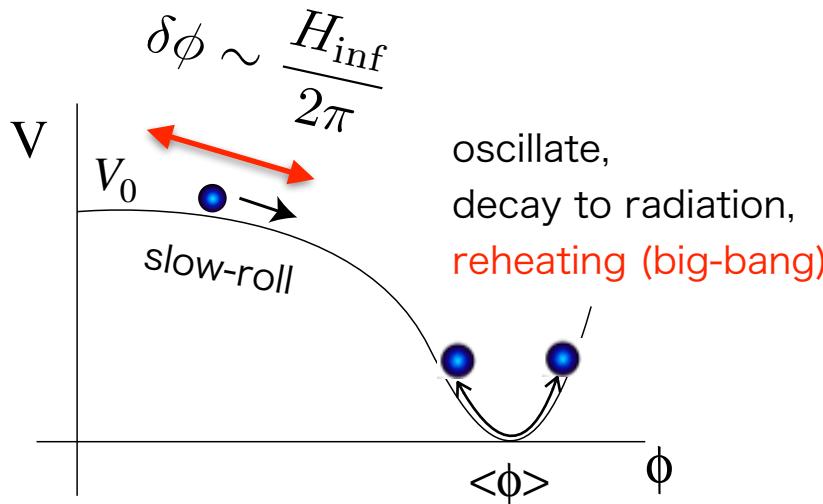
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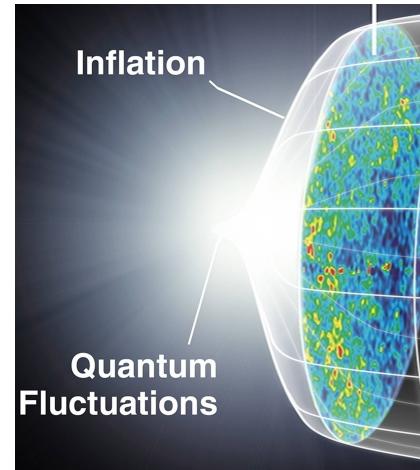
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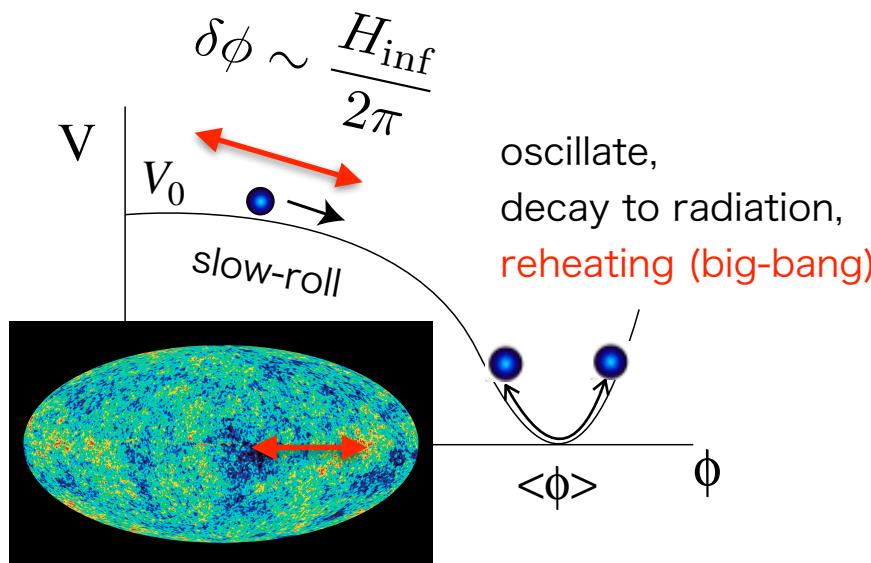
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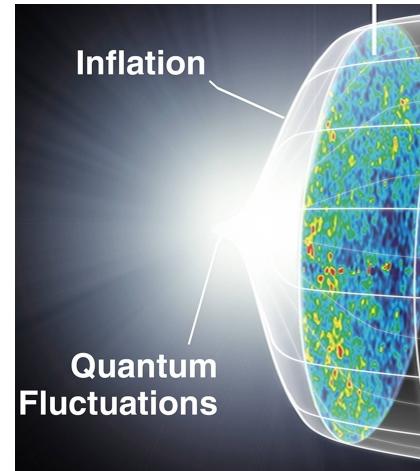
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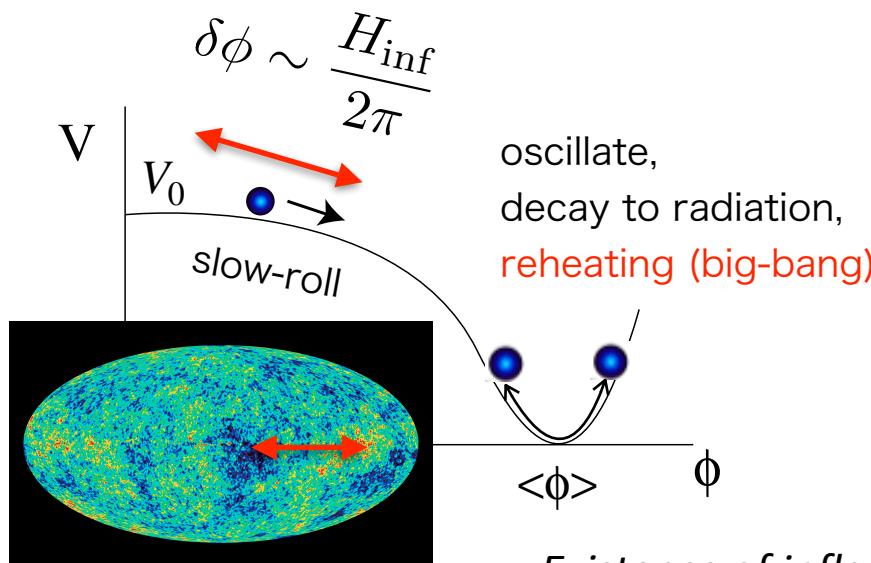
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oscillate,  
decay to radiation,  
reheating (big-bang)

Inflaton  $\phi$ :

Quantum fluctuation for  
anisotropy of the Universe  
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*Existence of inflaton and inflation is very rigid!*

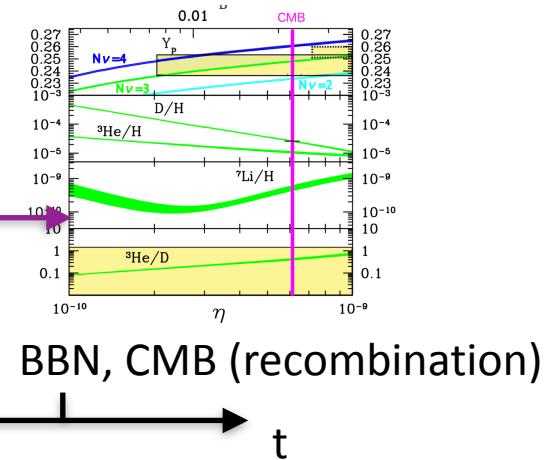
# New physics: baryogenesis

$$\frac{\Delta n_B}{S} \simeq 0$$

*Baryogenesis happens*

Inflation ends

*reheating  
(big bang)*



BBN, CMB (recombination)

t

To generate the baryon asymmetry of our universe  
Sakharov's conditions should be satisfied:

- \*Baryon/Lepton number violation with sphaleron
- \*C and CP violation
- \*Out of thermal equilibrium

Unfortunately, the SM of the particle theory does not sufficiently satisfy them... **New physics is needed for baryogenesis!**

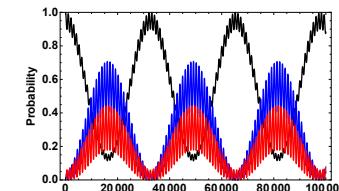
# New physics: neutrino oscillation

A simple explanation:

the SM is a non-renormalizable effective theory  
i.e. Majorana neutrino

$$\mathcal{L}_{SM} = \mathcal{L}_{SM}^{d \leq 4} - \frac{\kappa_{ij}}{2} \bar{L}_i^c \hat{P}_L L_j H H + h.c. + \dots$$

$\Downarrow \frac{m_{\nu ij}}{2} \bar{\nu}_i^c \hat{P}_L \nu_j$



Possible origins of the LLHH term

UV completed by heavy particles.  
e.g.

*seesaw mechanism*

Yanagida 79; Gell-Mann, et al 79; Minkowski, 77;

High scale R-parity violating SUSY?  
See Prof Liu's talk slide,  
See also WY, 1808.00440 in the context of  
charge quantization.

Just exist as it is valid  
up to  $10^{17}$  GeV

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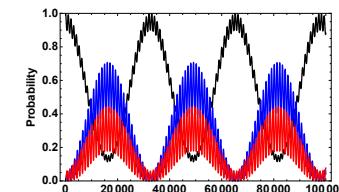
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Lepton # violating

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# Baryon asymmetry of universe with Majorana neutrino

- Baryogenesis with right-handed neutrinos

M. Fukugita, T. Yanagida 1986; Pilaftsis 1997; Buchmuller Plumacher, 1998;  
Akhmedov et al, 1998; Asaka, Shaposhnikov, 2005; Eijima, Kitano, WY, 2019 (See Eijima's talk).

- Baryogenesis with the LLHH interaction term Hamada, Kitano, WY, 2018;

See also Hamada, Kawana 2015; Takahashi, Yamada 2015; Hamada Kitano 2016,  
with LLHH + other higher dimensional terms.

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Hamada, Kitano, WY, 2018;

Today's topic

See also Hamada, Kawana 2015; Takahashi, Yamada 2015; Hamada Kitano 2016,  
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# I will be talking about

Setup:

$$\mathcal{L} = \mathcal{L}_{SM}^{d \leq 4} - \frac{\kappa_{ij}}{2} \bar{L}^c{}_i \hat{P}_L L_j H H + h.c.$$

At ***around the reheating  
(big-bang), neutrino flavor  
oscillation*** can generate  
baryon asymmetry with  
***LLHH scattering process.***

Sakharov's conditions

- \*Baryon/Lepton # violation
- \*C and CP violation
- \*Out of equilibrium

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*Neutrino oscillation!* CP-violation is favored at  $2\sigma$  [T2K,1701.00432](#)
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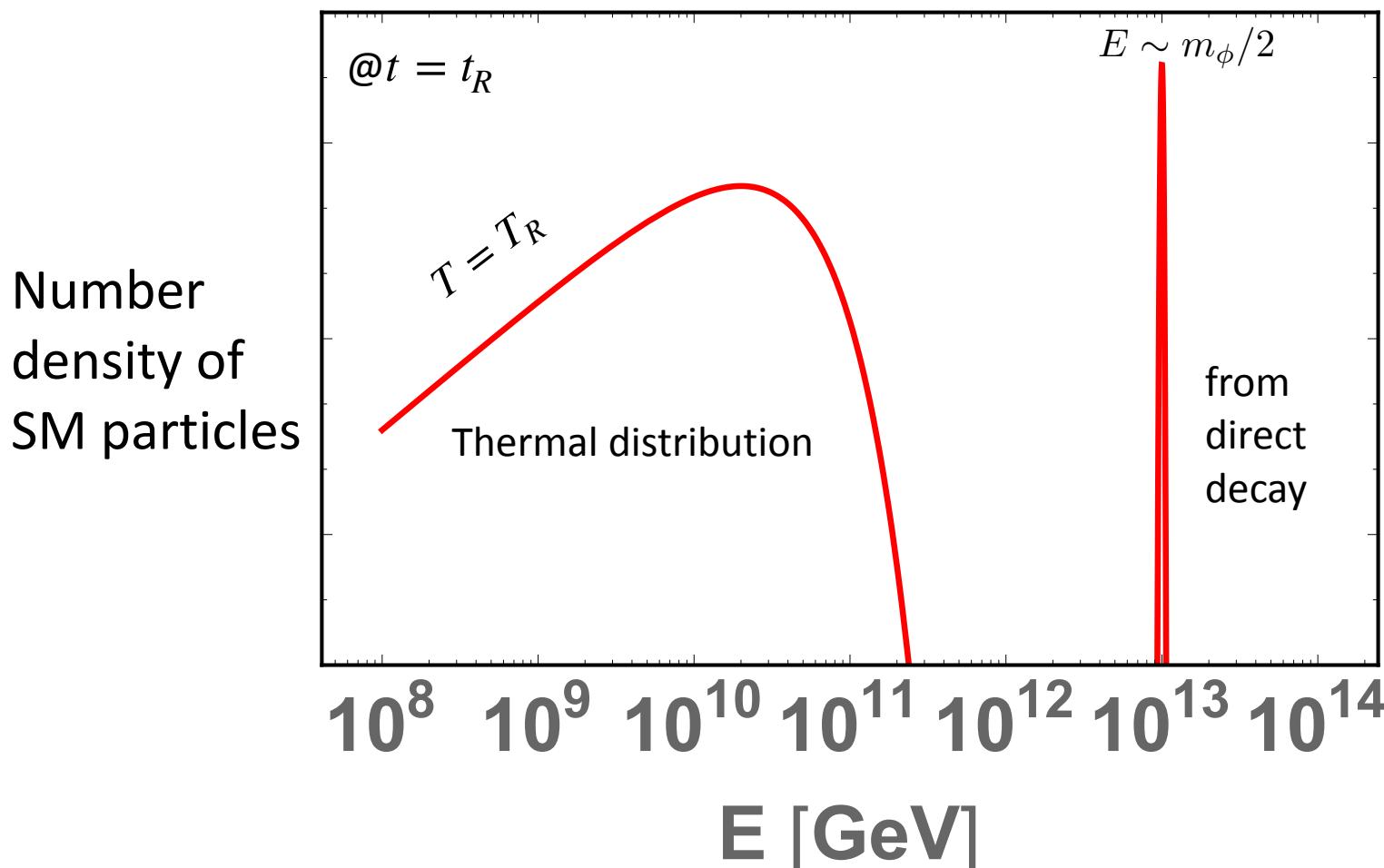
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- \*C and CP violation ✓  
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- \*Out of equilibrium ✓  
*Thermalization around reheating*

## 2. Baryogenesis via active neutrino oscillation

Kitano, Hamada, WY 1807.06582

Inflaton decay:  $\phi \rightarrow \text{SM particles}$  (2 body)

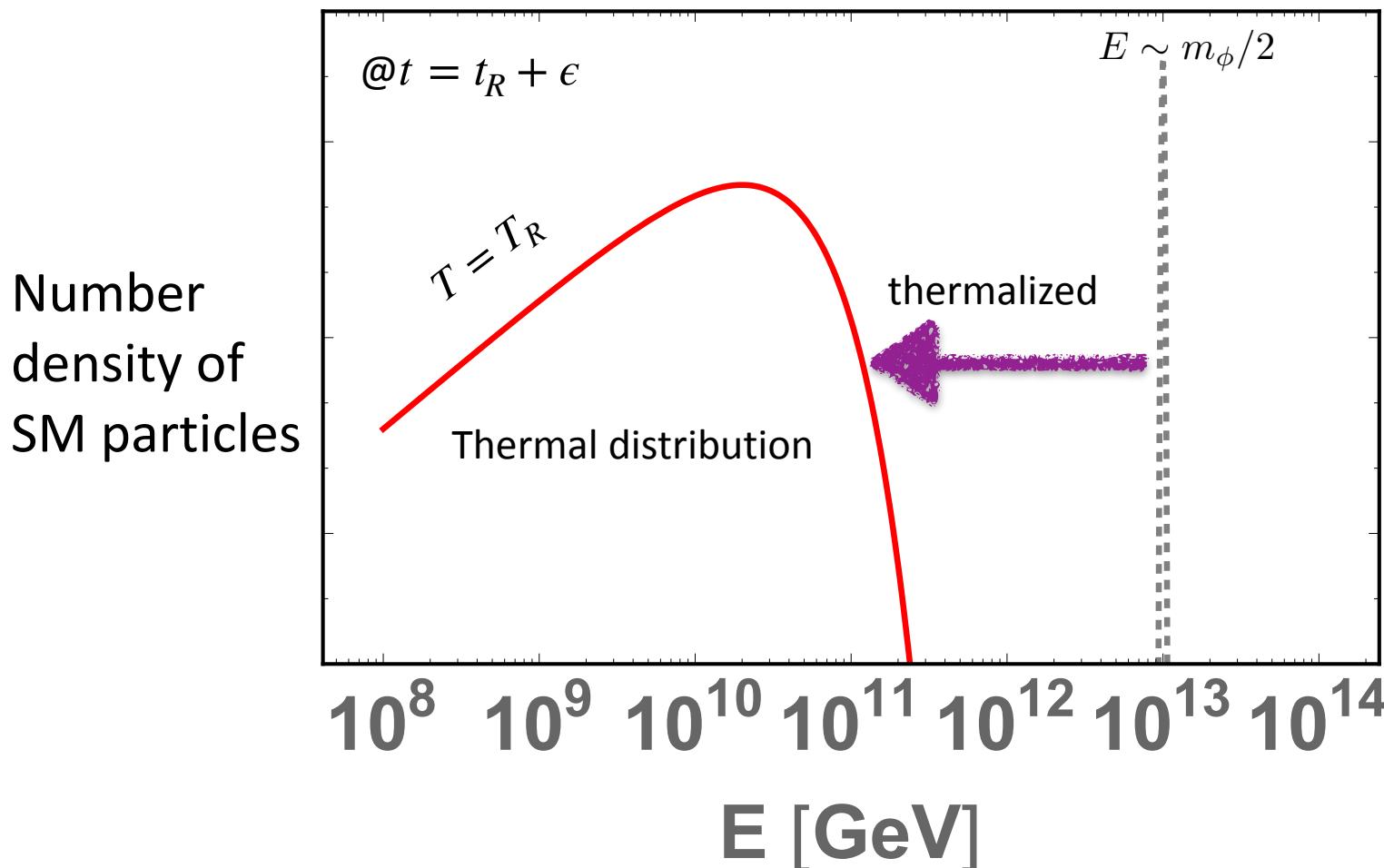
at the moment of an inflaton decay



# Thermalization during reheating

Inflaton decay:

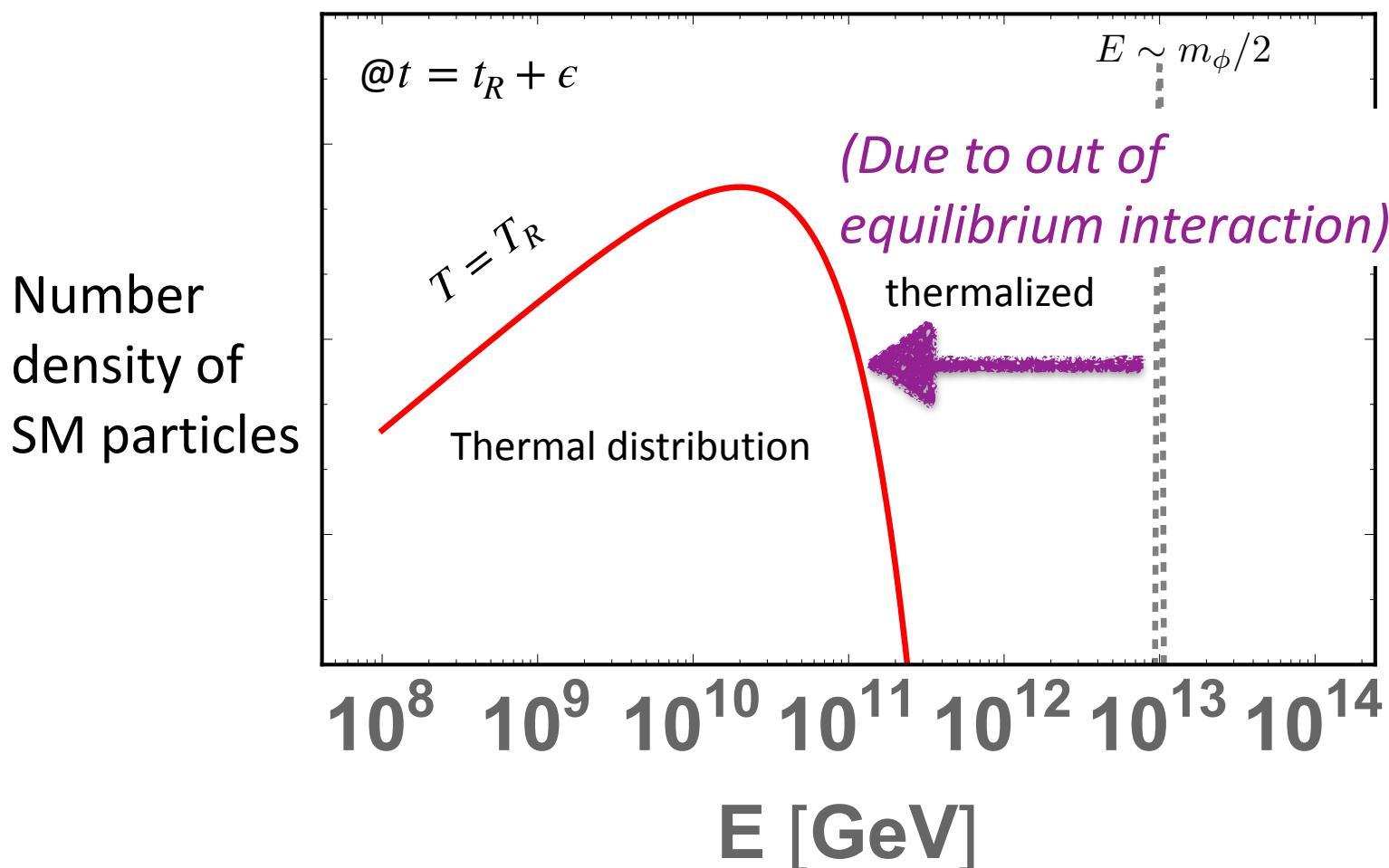
$$\phi \rightarrow \text{SM particles}$$



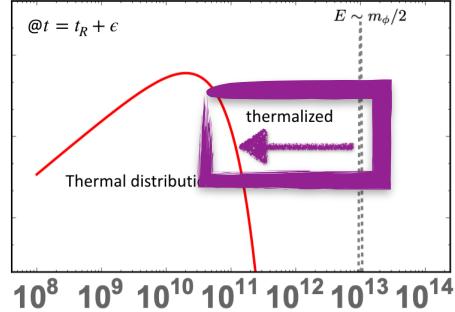
# Thermalization during reheating

Inflaton decay:

$$\phi \rightarrow \text{SM particles}$$



# *Neutrino oscillation during thermalization*



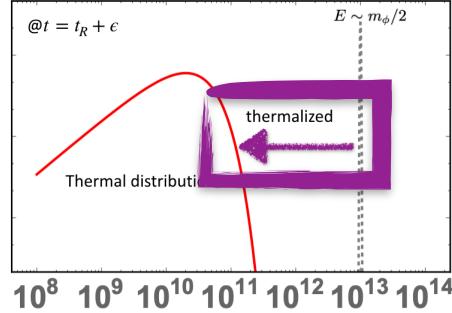
$$\phi \rightarrow \nu_{\text{ini}} + X, \bar{\nu}_{\text{ini}} + \bar{X}$$

$$\langle \nu_{\text{ini}} | \quad \bullet \quad \longrightarrow$$

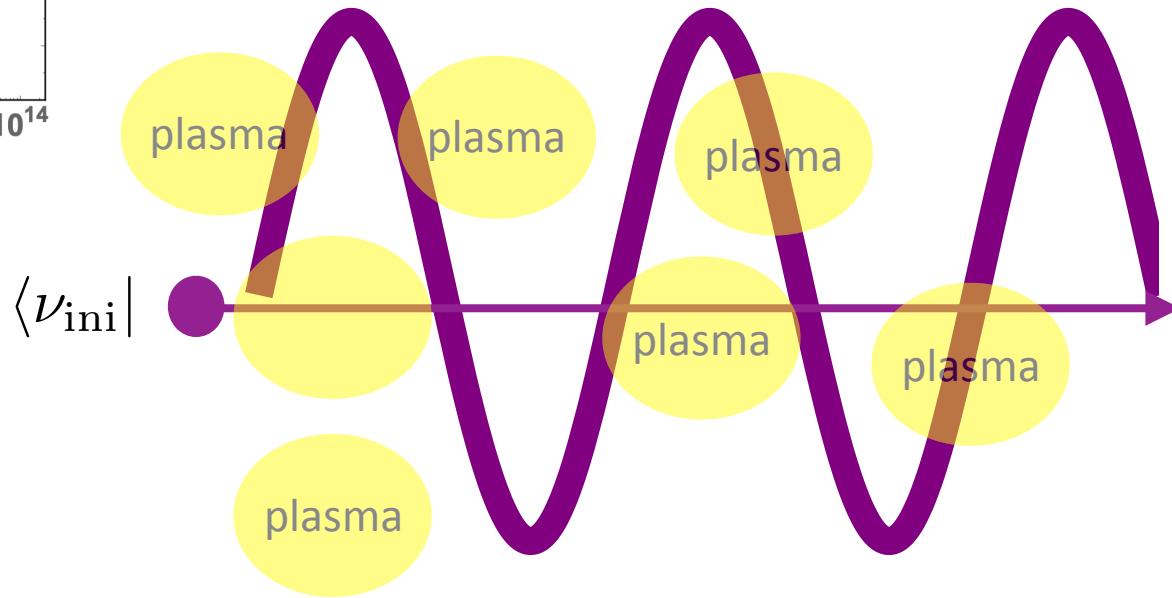
$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

c.f.  $P_{e \rightarrow \mu} \simeq \left| \sum_{\alpha} \langle \nu_e | \nu_{\alpha} \rangle e^{itm_{\nu_{\alpha}}^2 / k} \langle \nu_{\alpha} | \nu_{\mu} \rangle \right|^2$  @ vacuum

# Neutrino oscillation during thermalization



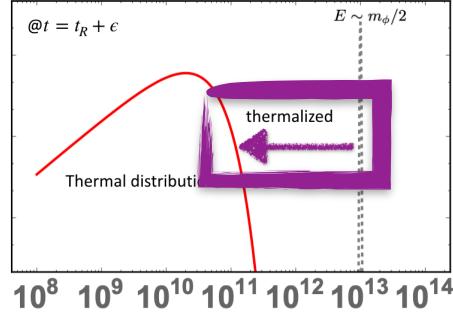
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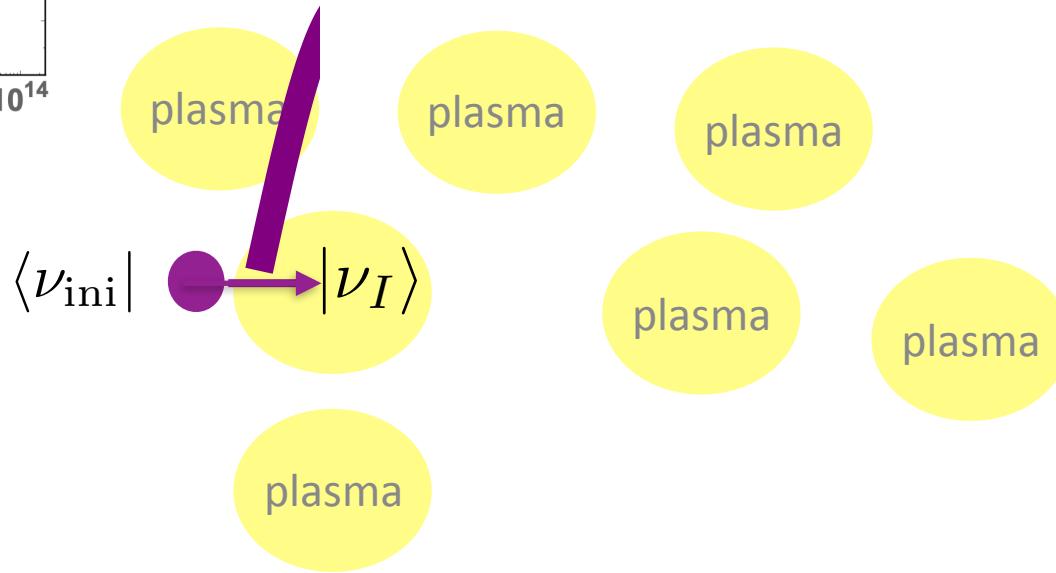
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# Neutrino oscillation during thermalization



$$\phi \rightarrow \nu_{\text{ini}} + X, \bar{\nu}_{\text{ini}} + \bar{X}$$



$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

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$$P_{e \rightarrow \mu} \simeq \left| \sum_{\alpha} \langle \nu_e | \nu_{\alpha} \rangle e^{itm_{\nu_{\alpha}}^2 / k} \langle \nu_{\alpha} | \nu_{\mu} \rangle \right|^2 \quad @ \text{vacuum}$$

# *Neutrino oscillation provides CP violation*

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

$$t_{MFP} \sim \frac{1}{\alpha_2^2 T} \sqrt{\frac{k}{T}} \quad (m_{\nu, \alpha}^{\text{th}})^2 = \text{eigen} \left[ \frac{y_i^2 T^2}{16} \delta_{ij} + 0.046 (\kappa^* \kappa)_{ij} T^4 \right] + C \delta_{ij}$$

$$P_{\text{ini} \rightarrow I} - P_{\overline{\text{ini}} \rightarrow \bar{I}} \propto \frac{\Delta(m_{\nu}^{\text{th}})^2}{k} t_{MFP} \sim 0.01 \sqrt{T/k}$$

c.f.  $P_{e \rightarrow \mu} - P_{\bar{e} \rightarrow \bar{\mu}} \propto \sin[t \Delta m_{\nu}^2 / k]$  @vacuum

Oscillation phase is not too small at thermalization around the reheating.

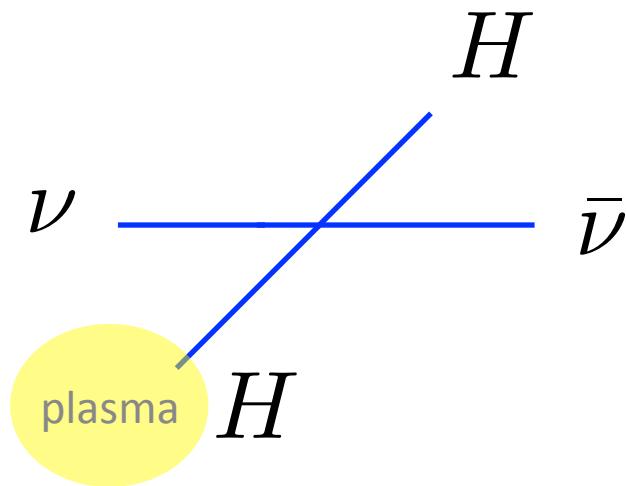
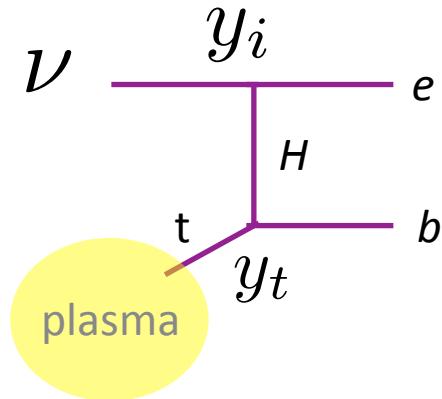
Hamada Kitano 2016

# How to observe “flavor”?

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

Only flavor dependent process can identify the flavor.

“Observation” is made due to the following interaction process.



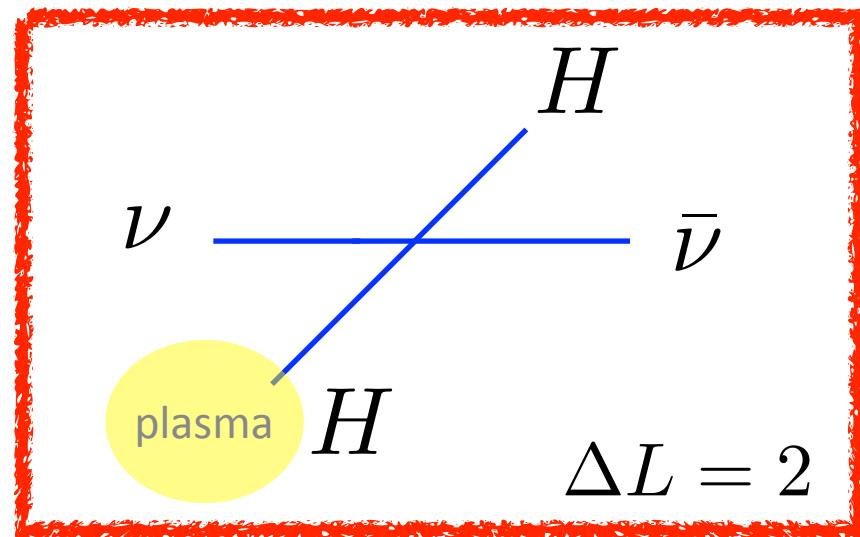
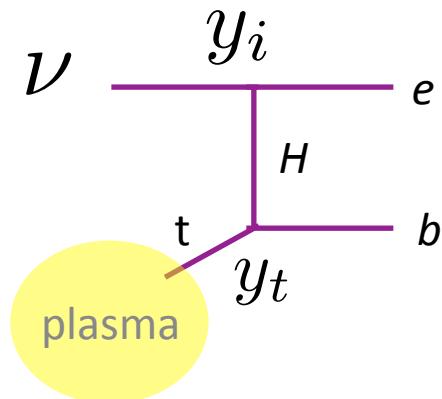
$|\nu_I\rangle$  is the state defined by the interaction.

# *Lepton number violation happens through “observation”.*

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

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**Lepton asymmetry can be made!**

# *The (naive) estimation of lepton asymmetry*

$m_\phi \sim T \ll 10^{12} GeV$  with O(1) CP phase, general flavor structure

$$\frac{\Delta n_L}{s} \propto B_{\phi \rightarrow \nu_{\text{ini}} + X/\bar{\nu}_{\text{ini}} + \bar{X}} \times t_{MFP} \frac{\Delta m_\nu^2}{T} \times \frac{\sigma_{LLHH}^{\text{th}}}{\sigma_{\text{yukawa}}^{\text{th}}}$$

Lepton asymmetry

Branching ratio

CP violation

Lepton # violation

— Flavor dependent asymmetry of order

$$\frac{\Delta m_{\text{th}}^2}{T} \frac{1}{\Gamma_{\text{th}}} \sim 0.01$$

— How frequently the flavor is observed by the llHH interaction.

$$\frac{\sigma_{llHH}^{\text{th}}}{\sigma_{\text{yukawa}}^{\text{th}}} \sim \frac{\Delta m_\nu^2 T^2}{y_\tau^2 y_t^2 v^4}$$

# *The (naive) estimation of lepton asymmetry*

$m_\phi \sim T \ll 10^{12} GeV$  with O(1) CP phase, general flavor structure

$$\frac{\Delta n_L}{s} \propto B_{\phi \rightarrow \nu_{\text{ini}} + X / \bar{\nu}_{\text{ini}} + \bar{X}} \times 10^{-9} \left( \frac{T_R}{10^9 GeV} \right)^2$$

c.f. required asymmetry

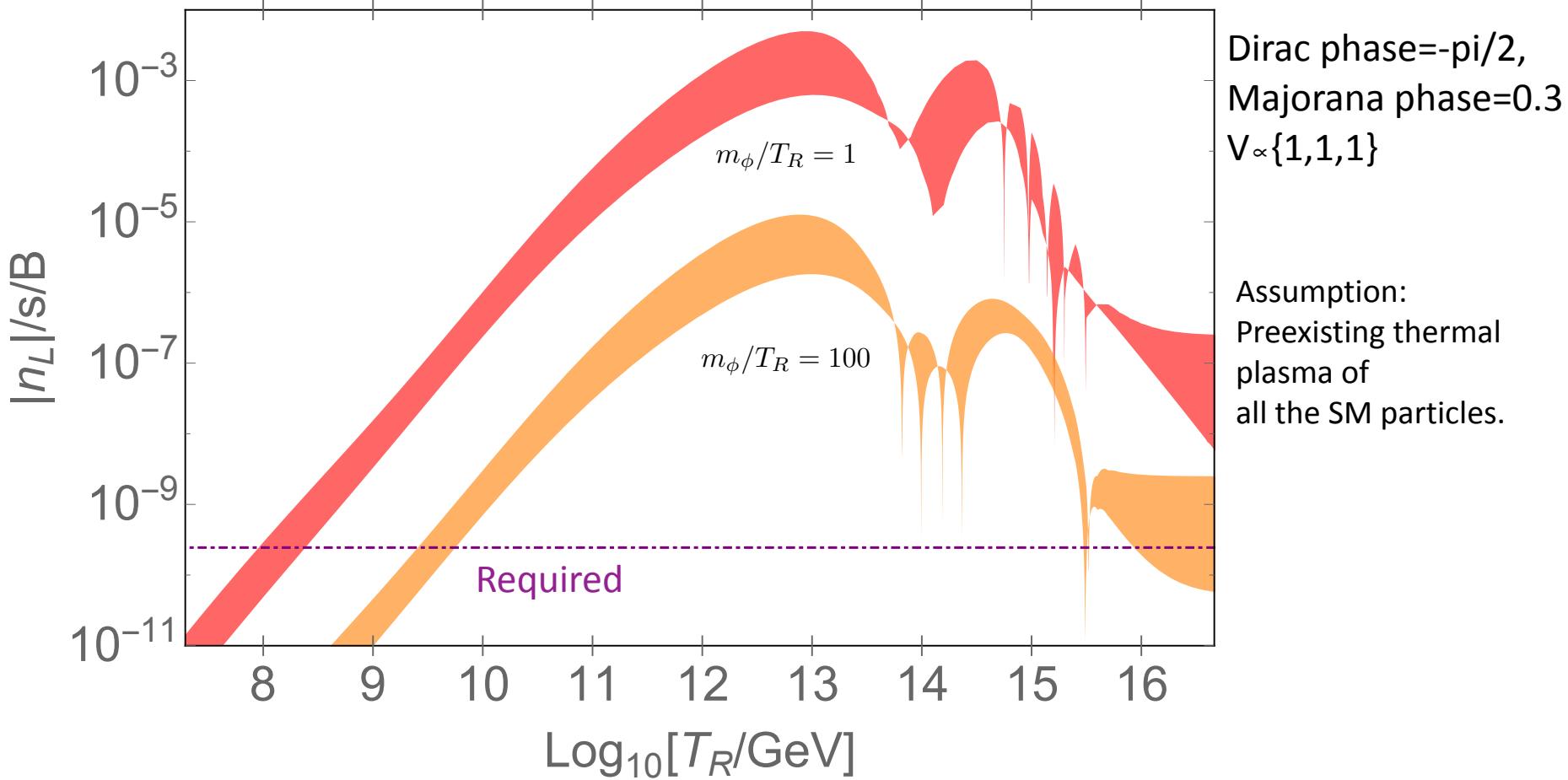
$$|\Delta n_L/s| \sim 10^{-10}$$

**Enough asymmetry can be generated with sufficiently high reheating temperature.**

# Numerical result (Normal Hierarchy)

By solving kinetic equations, [Sigl, Raffelt, 1993](#)

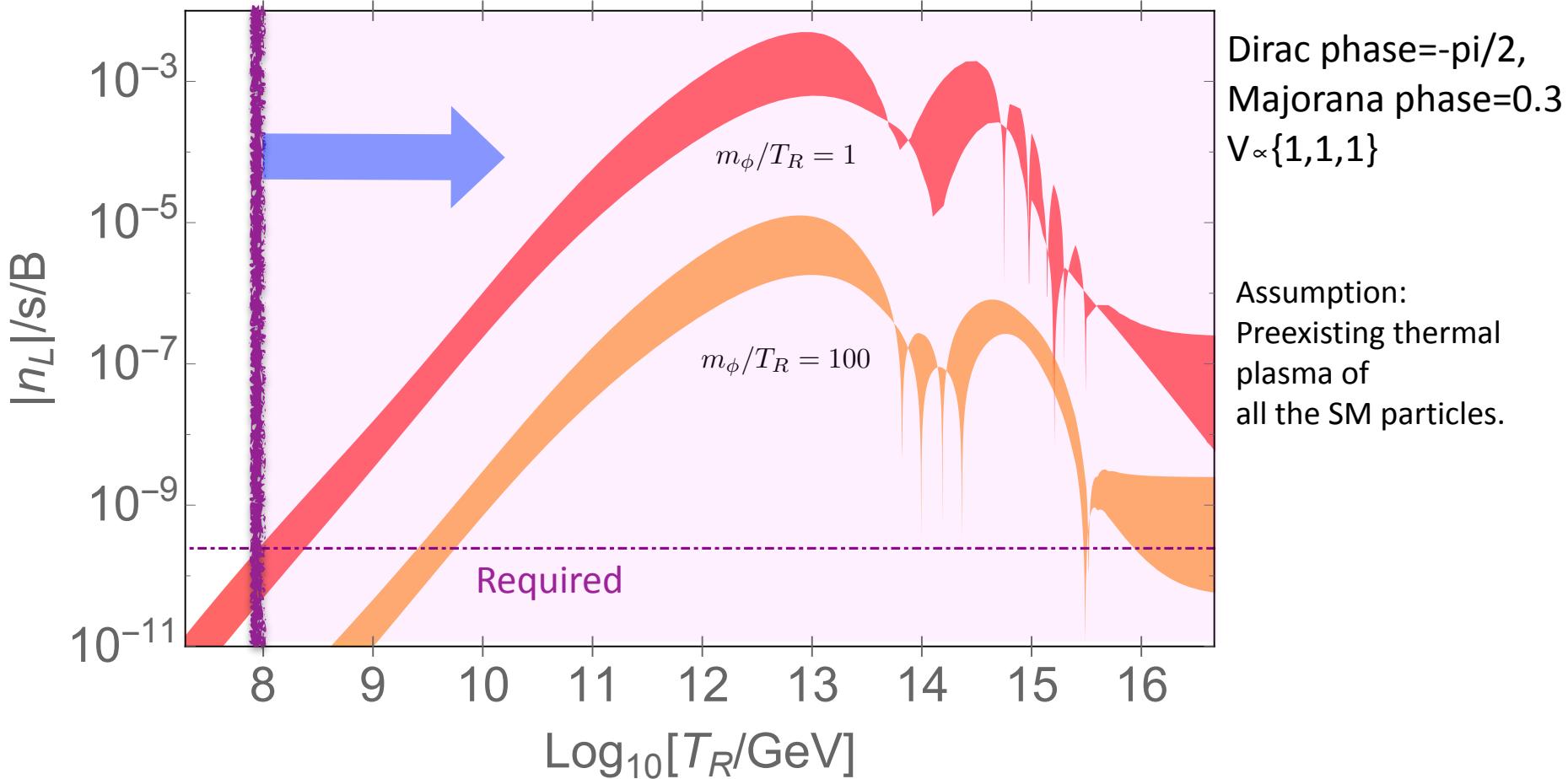
we get



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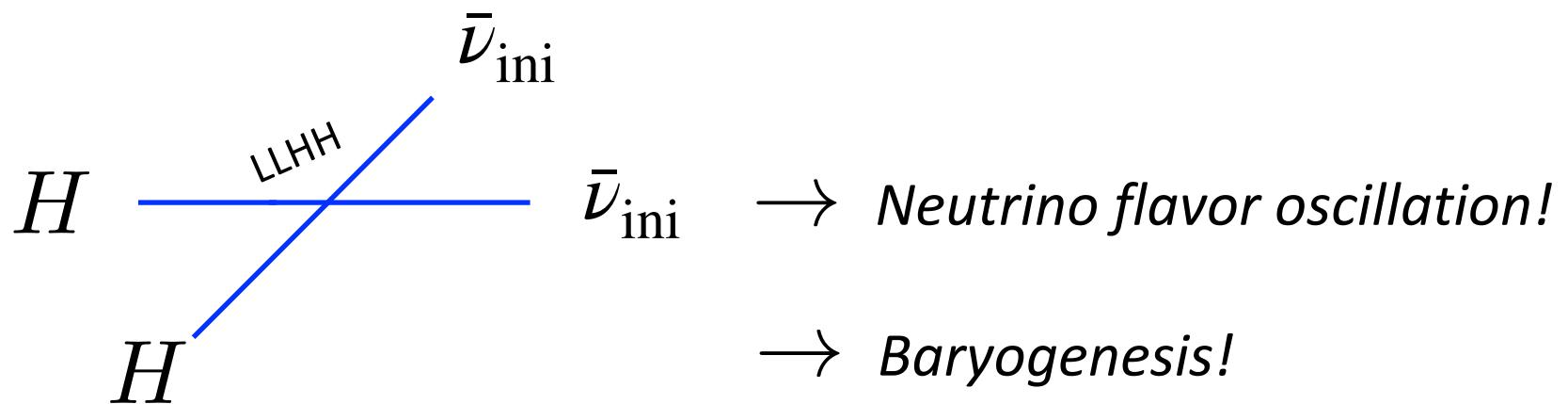
*Baryogenesis can be successful for  $T_R \gtrsim 10^8 \text{ GeV}$  due to active neutrino oscillation during thermalization.*

### 3. Baryogenesis from PMNS matrix

Let us consider the renormalizable inflaton coupling to the SM

$$\mathcal{L} \supset -A\phi|H|^2 - \lambda_\phi\phi^2|H|^2 \quad A, \lambda_\phi: \text{real parameters}$$

$$\phi \rightarrow HH^*$$

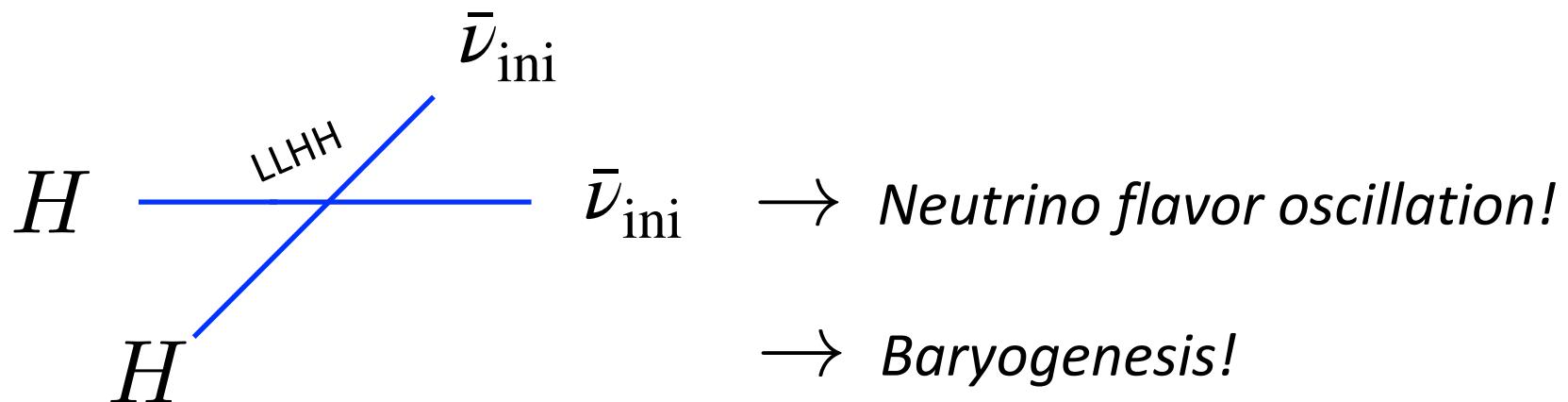


### 3. Baryogenesis from PMNS matrix

Let us consider the renormalizable inflaton coupling to the SM

$$\mathcal{L} \supset -A\phi|H|^2 - \lambda_\phi\phi^2|H|^2 \quad A, \lambda_\phi: \text{real parameters}$$

$$\phi \rightarrow HH^*$$



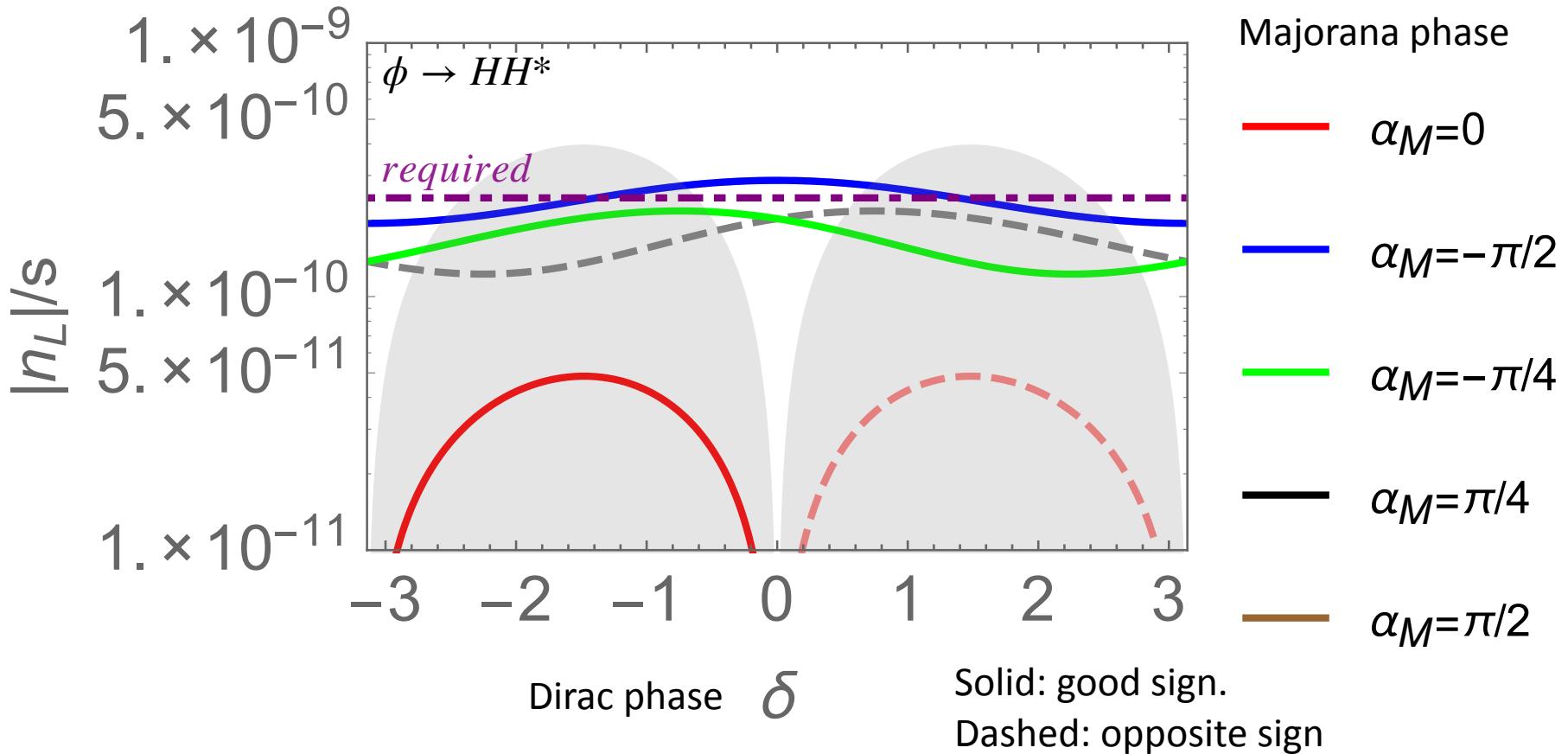
***CP violation can only appear via CP phases in  
LLHH interaction, i.e. the PMNS matrix.***

***The baryon asymmetry is related with the PMNS matrix***

# Numerical result:

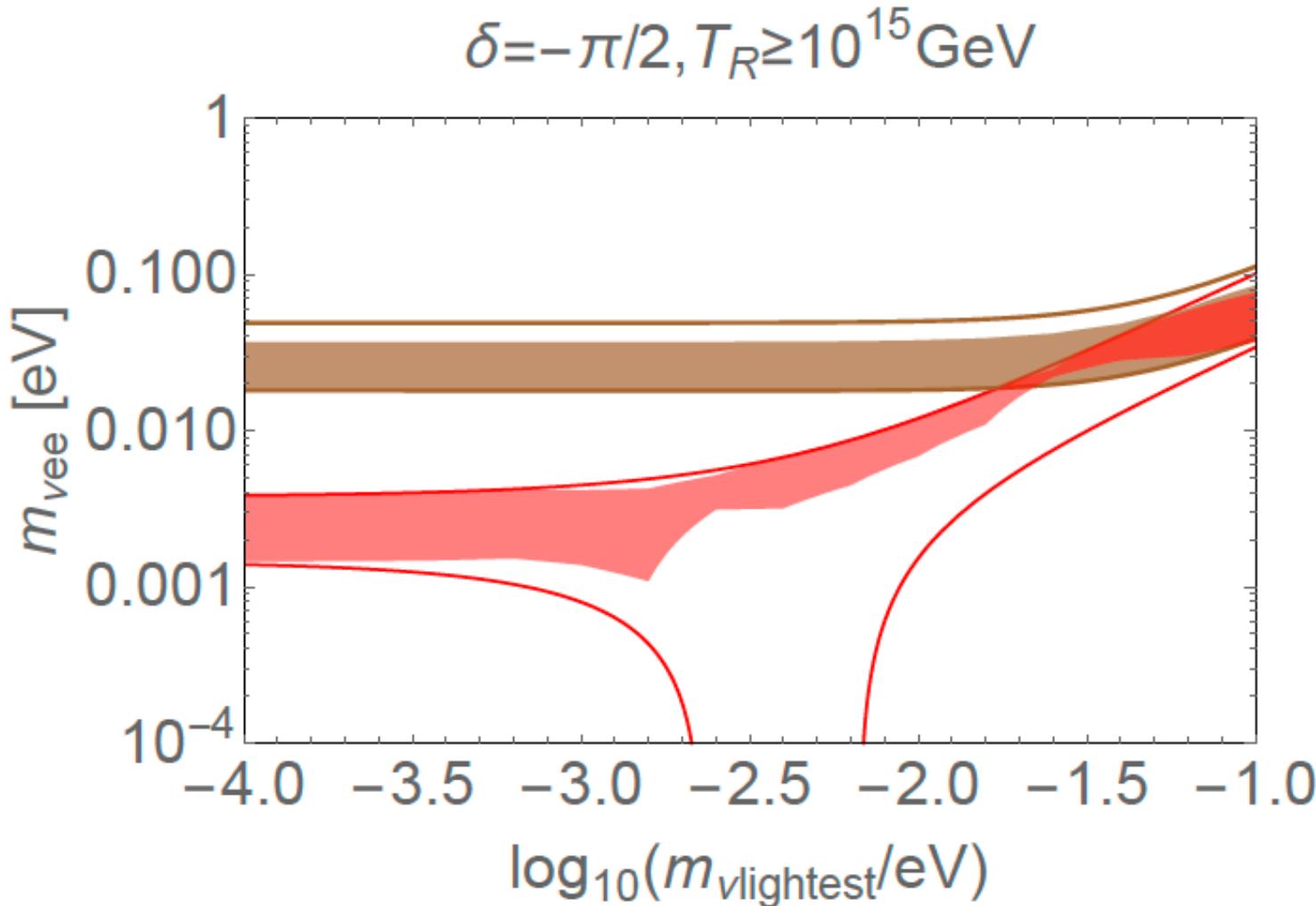
## Dirac phase dependence

Normal,  $T_R = m_\phi / 100 = 2 \times 10^{12} \text{ GeV}$ ,  $m_{\text{lightest}} = 0 \text{ eV}$



# Neutrinoless double beta decay

The CP phase and neutrino mass are related and can be tested from neutrino exps.



# Summary

Baryon asymmetry can be explained due to neutrino oscillation with

$$\mathcal{L} = \mathcal{L}_{SM}^{d \leq 4} - \frac{\kappa_{ij}}{2} \bar{L}^c_i \hat{P}_L L_j H H + h.c \quad \text{at } \textcolor{red}{\underline{\text{around reheating era.}}}$$

- .  $T_R \gtrsim 10^8 GeV$  for  $\phi \rightarrow \nu + X, \bar{\nu} + \bar{X}$
- . If  $\phi \rightarrow HH^*$ , the scenario, can be tested from ground-based experiments.

See also Eijima's talk for baryogenesis via active neutrino oscillation with sterile neutrinos.

# Backups

# *Enhancement by non-trivial reheating dynamics*

Reheating can complete via the scattering process:

$$\phi + H^- \rightarrow \nu_i + e_j$$

Daido, Takahashi, WY, 1710.11107, 1903.00462,

i.e. due to dissipation effect. Yokoyama 0510091 etc.

No thermal blocking process:

$$\frac{n_\phi}{s} \simeq \frac{3T_R}{4m_\phi} \gg 1$$

$T_R/m_\phi \sim 10^{2-3}$  in Refs. 1710.11107, 1903.00462

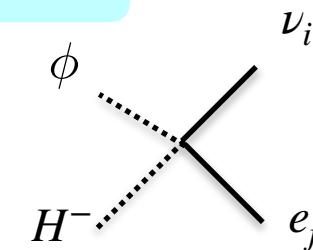
Thus, the asymmetry is enhanced.

LLHH scenario:

$$T_R \gtrsim 10^6 \text{GeV} \times \left( \frac{10^3}{T_R/m_\phi} \right)^{1/2}$$

Inflaton condensate

Thermal Plasma



Thermal Plasma

Thermal Plasma

seesaw scenario:

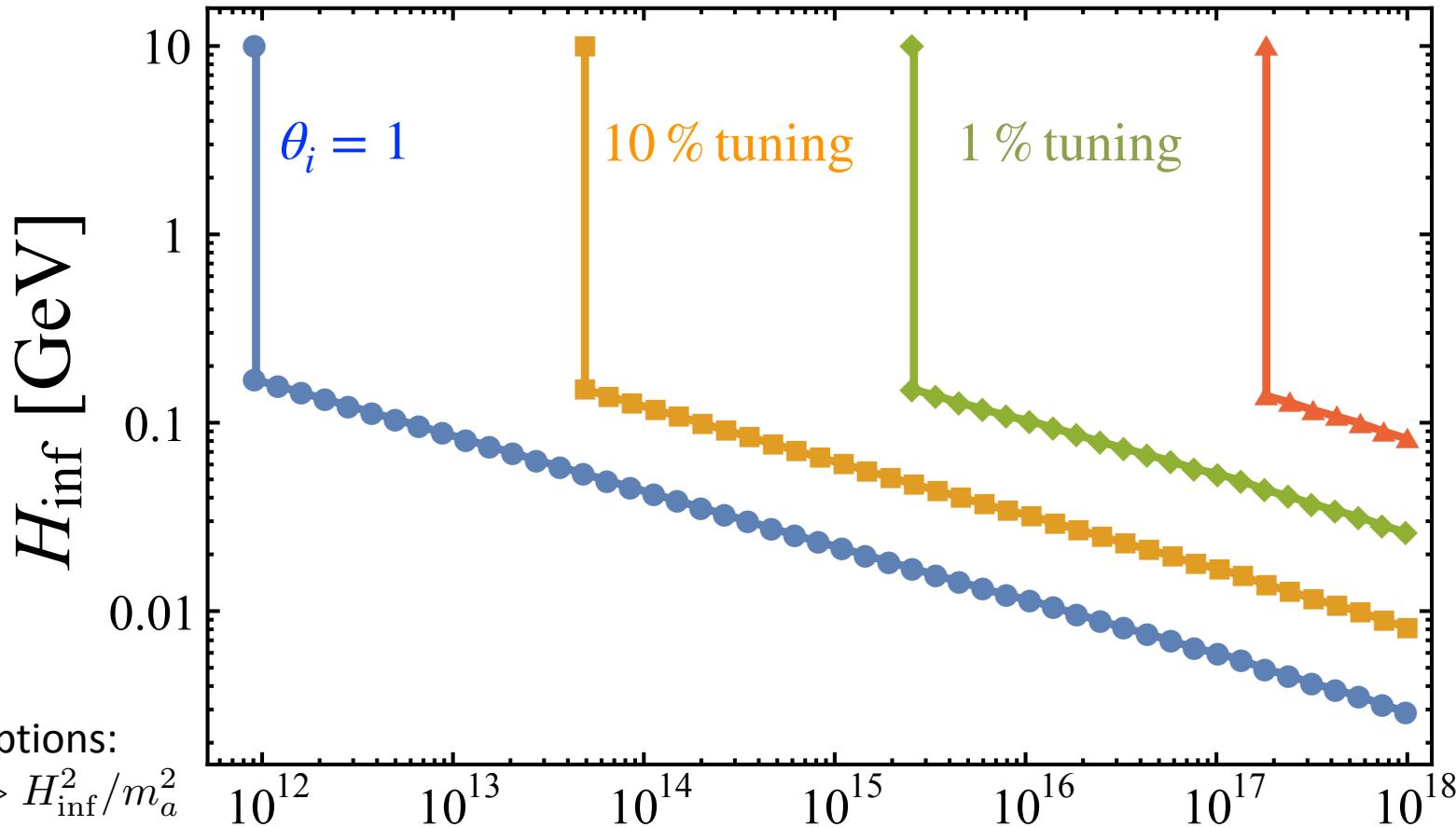
$$T_R \gtrsim 10^2 \text{GeV} \left( \frac{10^2}{T_R/m_\phi} \right)$$

# The upper bound of the QCD axion window can be relaxed

in low-scale inflation with  $H_{\text{inf}} \lesssim \Lambda_{\text{QCD}}$ .

Peter W. Graham, Adam Scherlis, 1805.07362,  
Fuminobu Takahashi, WY, Alan H. Guth, 1805.08763

Fuminobu Takahashi, WY, Alan H. Guth, 1805.08763



$f_a [\text{GeV}]$

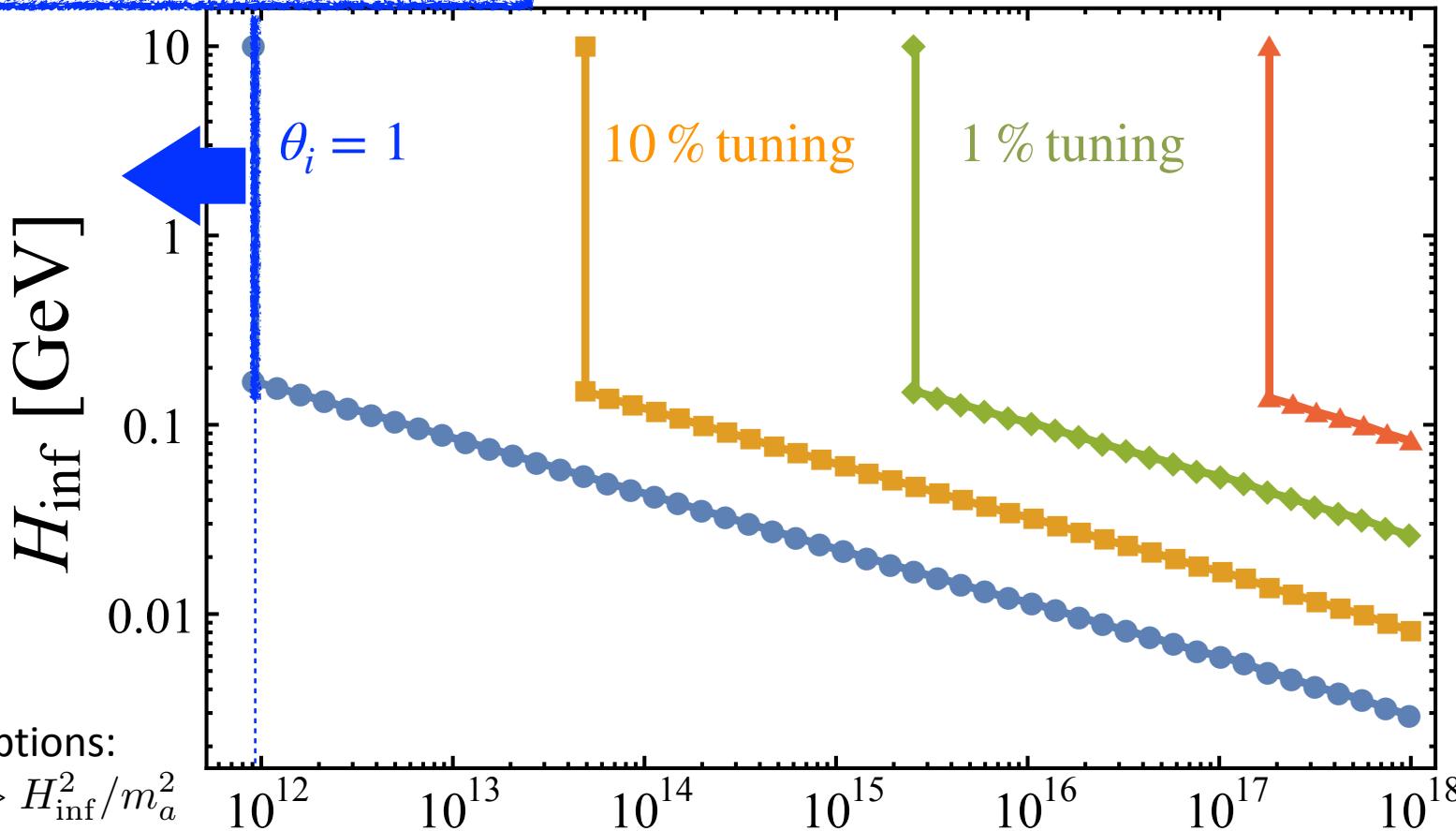
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Peter W. Graham, Adam Scherlis, 1805.07362,  
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Conventional axion  
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Fuminobu Takahashi, WY, Alan H. Guth, 1805.08763



$f_a$  [GeV]

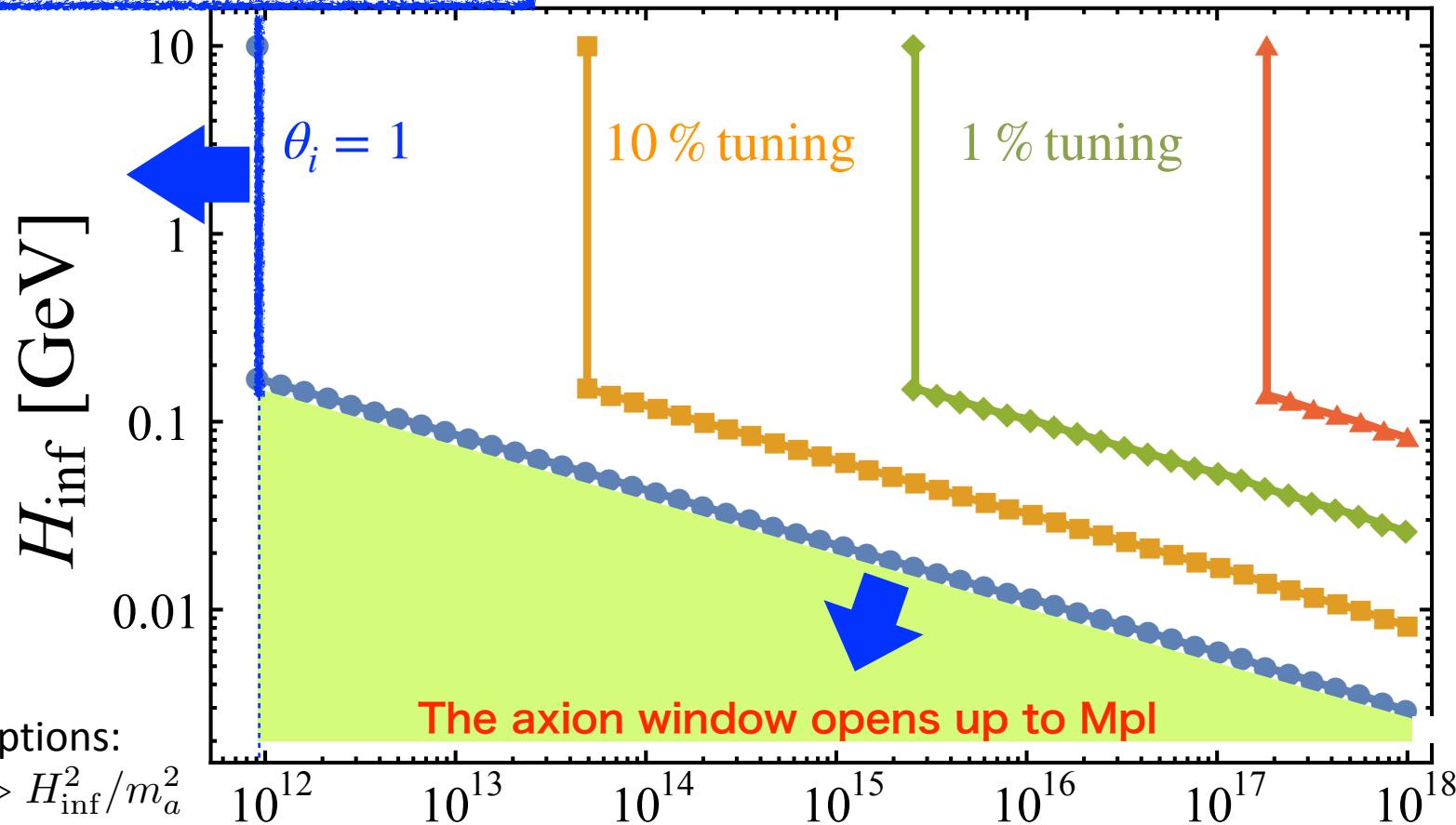
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Fuminobu Takahashi, WY, Alan H. Guth, 1805.08763



$f_a$  [GeV]

# Numerical estimation

density matrix for left-handed leptons  $\rho(\mathbf{p}) \equiv \rho_{ij}(\mathbf{p})$   $i, j = e, \mu, \tau$

## Kinetic Equation (Extended Boltzmann Eqs)

Sigl, Raffelt, 1993

$$i \frac{d\rho(\mathbf{p})}{dt} = [\Omega(\mathbf{p}), \rho(\mathbf{p})] - \frac{i}{2} \{\Gamma_{\mathbf{p}}^d, \rho(\mathbf{p})\} + \frac{i}{2} \{\Gamma_{\mathbf{p}}^p, 1 - \rho(\mathbf{p})\},$$

Oscillation term      Interaction terms (with CP phase)

$$i \frac{d\bar{\rho}(\mathbf{p})}{dt} = -[\Omega(\mathbf{p}), \bar{\rho}(\mathbf{p})] - \frac{i}{2} \{\Gamma_{\mathbf{p}}^d, \bar{\rho}(\mathbf{p})\} + \frac{i}{2} \{\Gamma_{\mathbf{p}}^p, 1 - \bar{\rho}(\mathbf{p})\},$$

Hamiltonian:  $\Omega_{ij}(\mathbf{p}) \simeq \frac{y_i^2 T^2}{16|\mathbf{p}|} \delta_{ij} + 0.046 (\kappa^* \kappa)_{ij} \frac{T^4}{|\mathbf{p}|}$ , for  $|\mathbf{p}| \gtrsim T$ .

*This is absent in ordinary Boltzmann eqs.*

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↑  
Different      Interaction terms (with CP phase)  
↓

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Oscillating phase

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Different

$$i \frac{d\bar{\rho}(\mathbf{p})}{dt} = [[\Omega(\mathbf{p}), \bar{\rho}(\mathbf{p})]] - \frac{i}{2} \{\Gamma_{\mathbf{p}}^d, \bar{\rho}(\mathbf{p})\} + \frac{i}{2} \{\Gamma_{\mathbf{p}}^p, 1 - \bar{\rho}(\mathbf{p})\},$$

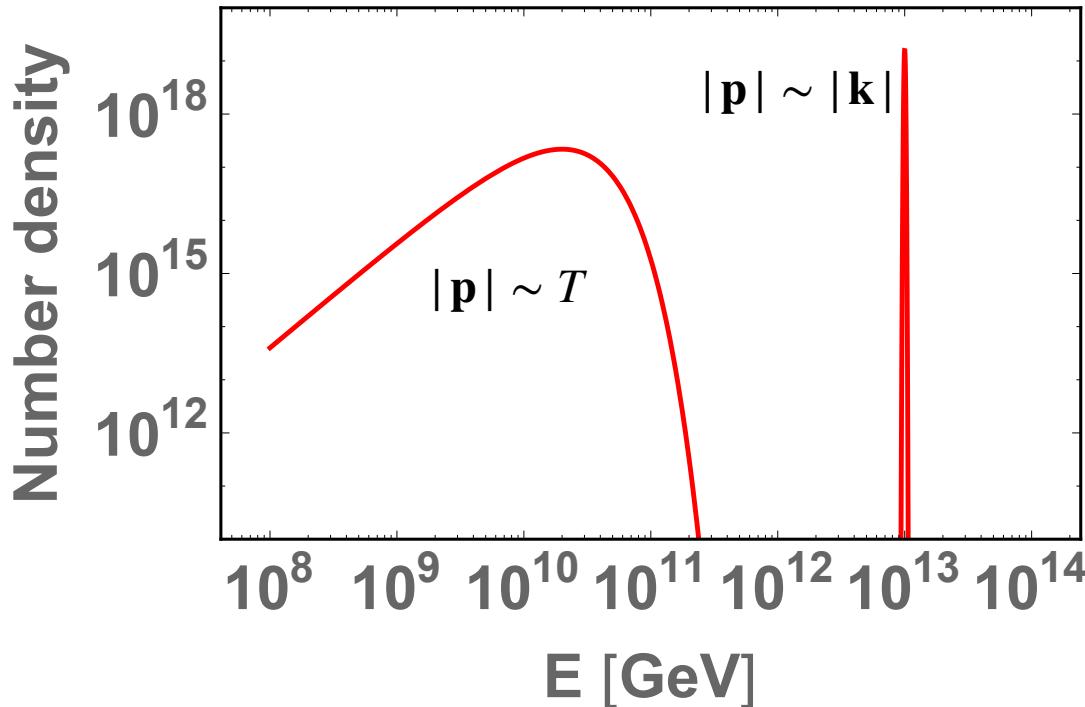
Interaction terms (with CP phase)

Oscillating phase      Thermalization, observation, L # violation

Hamiltonian:  $\Omega_{ij}(\mathbf{p}) \simeq \frac{y_i^2 T^2}{16|\mathbf{p}|} \delta_{ij} + 0.046 (\kappa^* \kappa)_{ij} \frac{T^4}{|\mathbf{p}|}$ , for  $|\mathbf{p}| \gtrsim T$ .

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# Two scale approximation



$$(\rho_{\mathbf{k}})_{ij} = \int_{|\mathbf{p}| \sim |\mathbf{k}|} \frac{d^3 \mathbf{p}}{(2\pi)^3} \frac{\rho_{ij}(\mathbf{p}, t)}{s},$$

$$(\delta\rho_T)_{ij} = \int_{|\mathbf{p}| \sim T} \frac{d^3 \mathbf{p}}{(2\pi)^3} \left( \frac{\rho_{ij}(\mathbf{p})}{s} - \frac{\rho_{ij}^{\text{eq}}(\mathbf{p})}{s} \right),$$

# Equations to be solved

$$i \frac{d\rho_{\mathbf{k}}}{dt} = [\Omega_{\mathbf{k}}, \rho_{\mathbf{k}}] - \frac{i}{2} \{\Gamma_{\mathbf{k}}^d, \rho_{\mathbf{k}}\},$$

+ eqs of right-handed charged/anti leptons

$$i \frac{d\delta\rho_T}{dt} = [\Omega_T, \delta\rho_T] - \frac{i}{2} \{\Gamma_T^d, \delta\rho_T\} + i\delta\Gamma_T^p,$$

$$\Omega_k \simeq \frac{y_i^2 T^2}{16m_\phi} \delta_{ij} + 0.046(\kappa^* \kappa)_{ij} \frac{T^4}{m_\phi} \quad \Omega_T \simeq \frac{y_i^2 T}{16} \delta_{ij} + 0.046(\kappa^* \kappa)_{ij} T^3$$

$$(\Gamma_{\mathbf{k}}^d)_{ij} \simeq C\alpha_2^2 T \sqrt{\frac{T}{|\mathbf{k}|}} \delta_{ij} + \frac{9y_t^2}{64\pi^3 |\mathbf{k}|} T^2 (\delta_{i\tau} \delta_{\tau j} y_\tau^2 + \delta_{i\mu} \delta_{\mu j} y_\mu^2) + \frac{21\zeta(3)}{32\pi^3} (\kappa^* \cdot \kappa)_{ij} T^3,$$

$$(\Gamma_T^d)_{ij} \simeq C'\alpha_2^2 T \delta_{ij} + \frac{9y_t^2}{64\pi^3} T (\delta_{i\tau} \delta_{\tau j} y_\tau^2 + \delta_{i\mu} \delta_{\mu j} y_\mu^2) + \frac{21\zeta(3)}{32\pi^3} (\kappa^* \cdot \kappa)_{ij} T^3,$$

$$(\delta\Gamma_T^p)_{ij} \simeq C\alpha_2^2 T \sqrt{\frac{T}{|\mathbf{k}|}} (\rho_{\mathbf{k}})_{ij} - C'\alpha_2^2 T (\delta\bar{\rho}_T)_{ij} \\ + \frac{3\zeta(3)}{8\pi^3} (\kappa^* \cdot (\bar{\rho}_{\mathbf{k}} - 3/4\rho_{\mathbf{k}})^t \cdot \kappa)_{ij} T^3 + \frac{3\zeta(3)}{8\pi^3} (\kappa^* \cdot (\delta\bar{\rho}_T - 3/4\delta\rho_T)^t \cdot \kappa)_{ij} T^3.$$

Some formula can be also found in [Akhmedov, et al. 9803255](#); [Abada, et al. 0601083.](#); [Asaka, et al. 1112.5565](#).  
 See Refs. [[Landau, Pomeranchuk 1953](#); [Migdal 1956](#)] for LPM effect.

$$\phi \rightarrow \nu_{\text{ini}} + X, \bar{\nu}_{\text{ini}} + \bar{X}$$

## Initial condition

$$\rho_{\mathbf{k}}|_{t=t_R} = \bar{\rho}_{\mathbf{k}}|_{t=t_R} = \mathcal{N} V_i V_j^*, \quad \delta\rho_T|_{t=t_R} = \delta\bar{\rho}_T|_{t=t_R} = 0.$$

$$\mathcal{N} = \frac{3}{4} \frac{T_R}{m_\phi} B,$$

## Free parameters

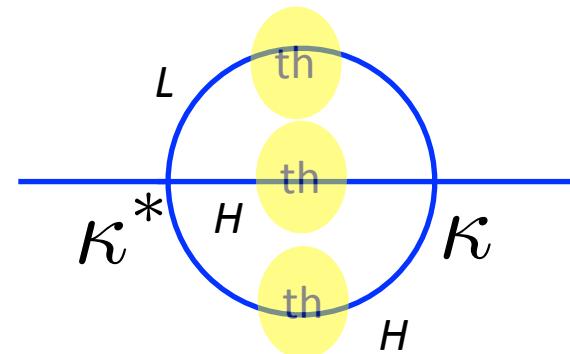
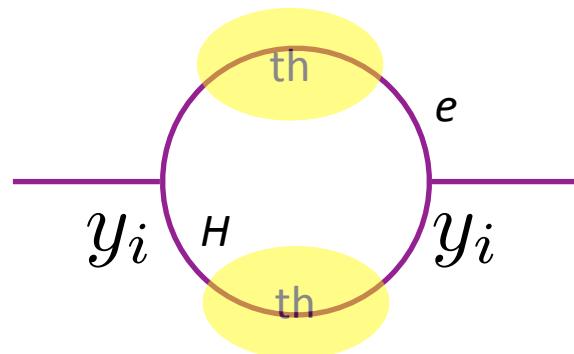
$$T_R, m_\phi, B, V_i$$

+Parameters in neutrino sector.

# *Thermal mass*

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

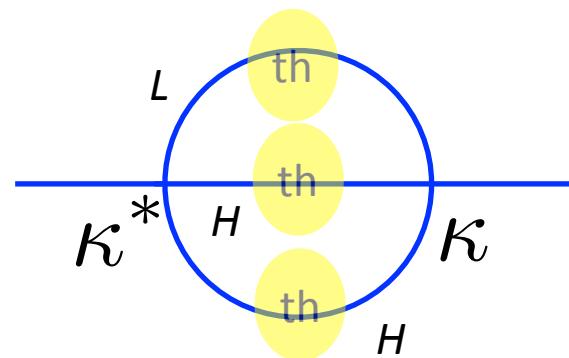
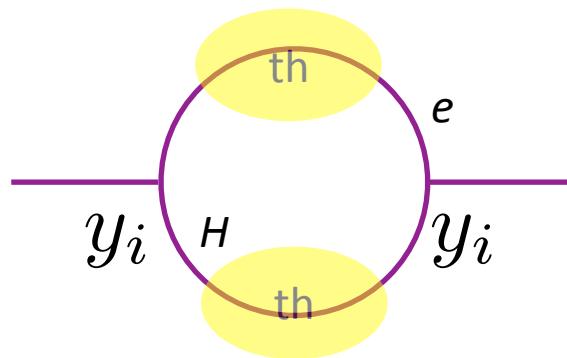
$$(m_{\nu_{\alpha}}^{\text{th}})^2 = \text{eigen} \left[ \frac{y_i^2 T^2}{16} \delta_{ij} + 0.046 (\kappa^* \kappa)_{ij} T^4 \right] + C \delta_{ij}$$



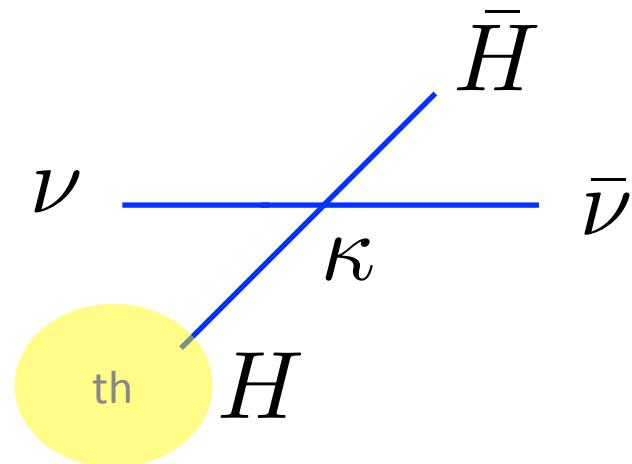
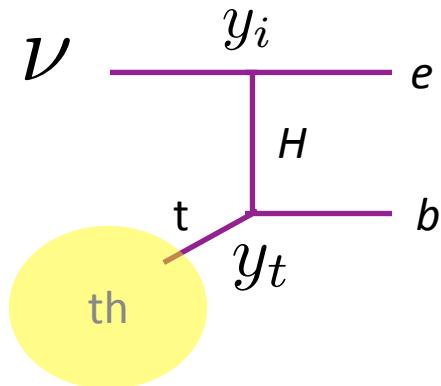
$|\nu_{\alpha}\rangle$  is the mass eigenstate.

# ***Mass basis*** $\neq$ ***interaction basis!***

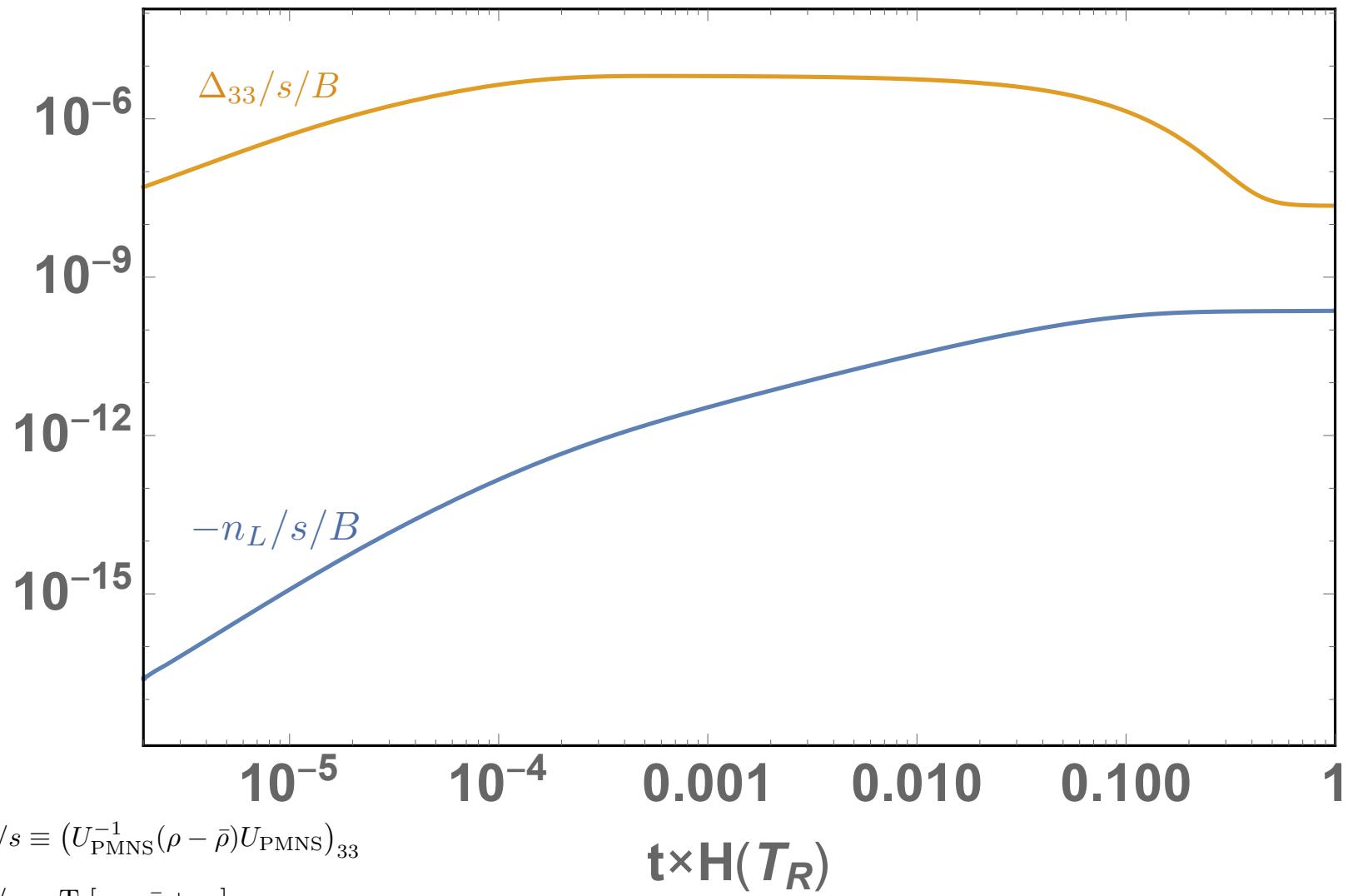
Mass:

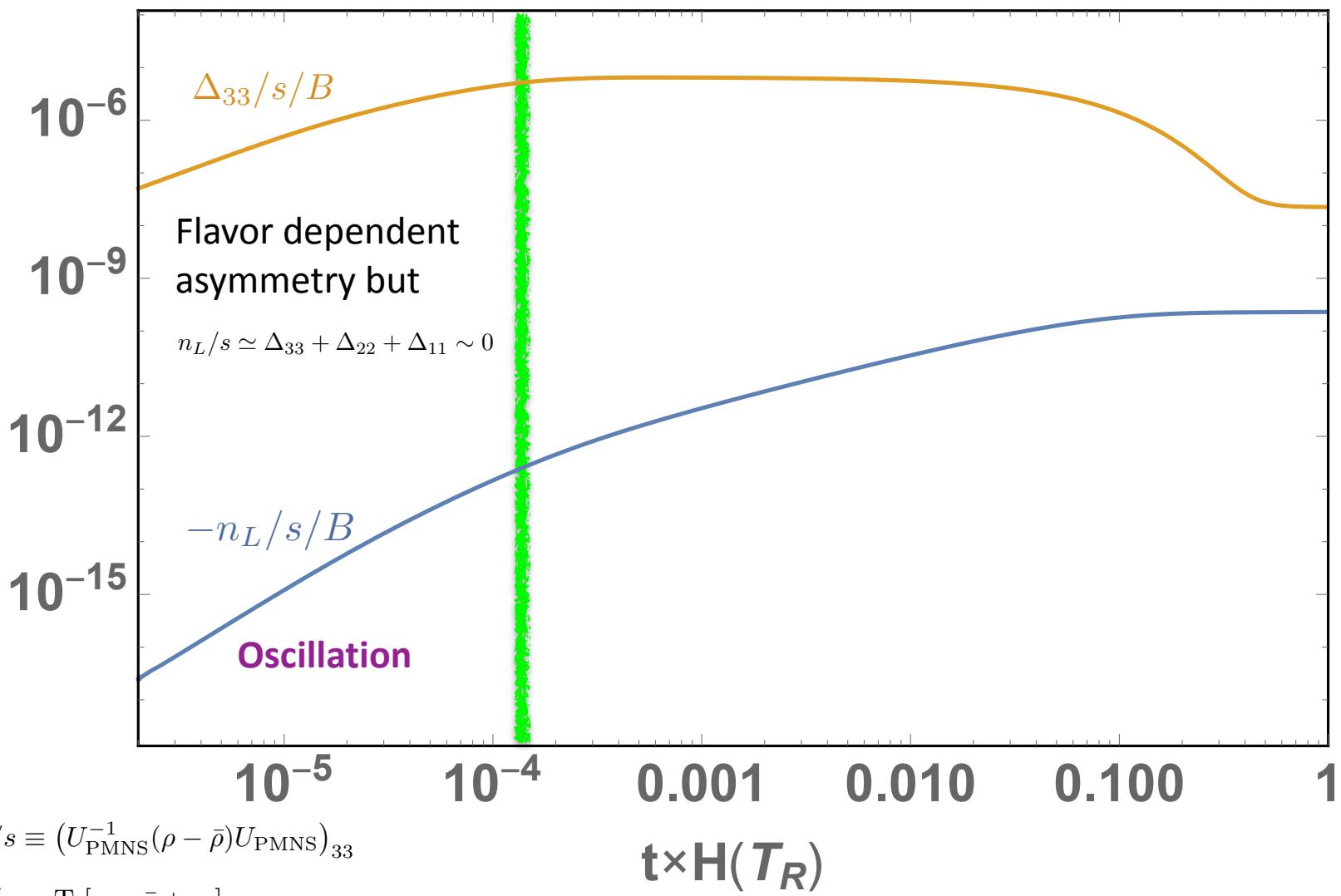


Interaction:



**CP violation can take place!**

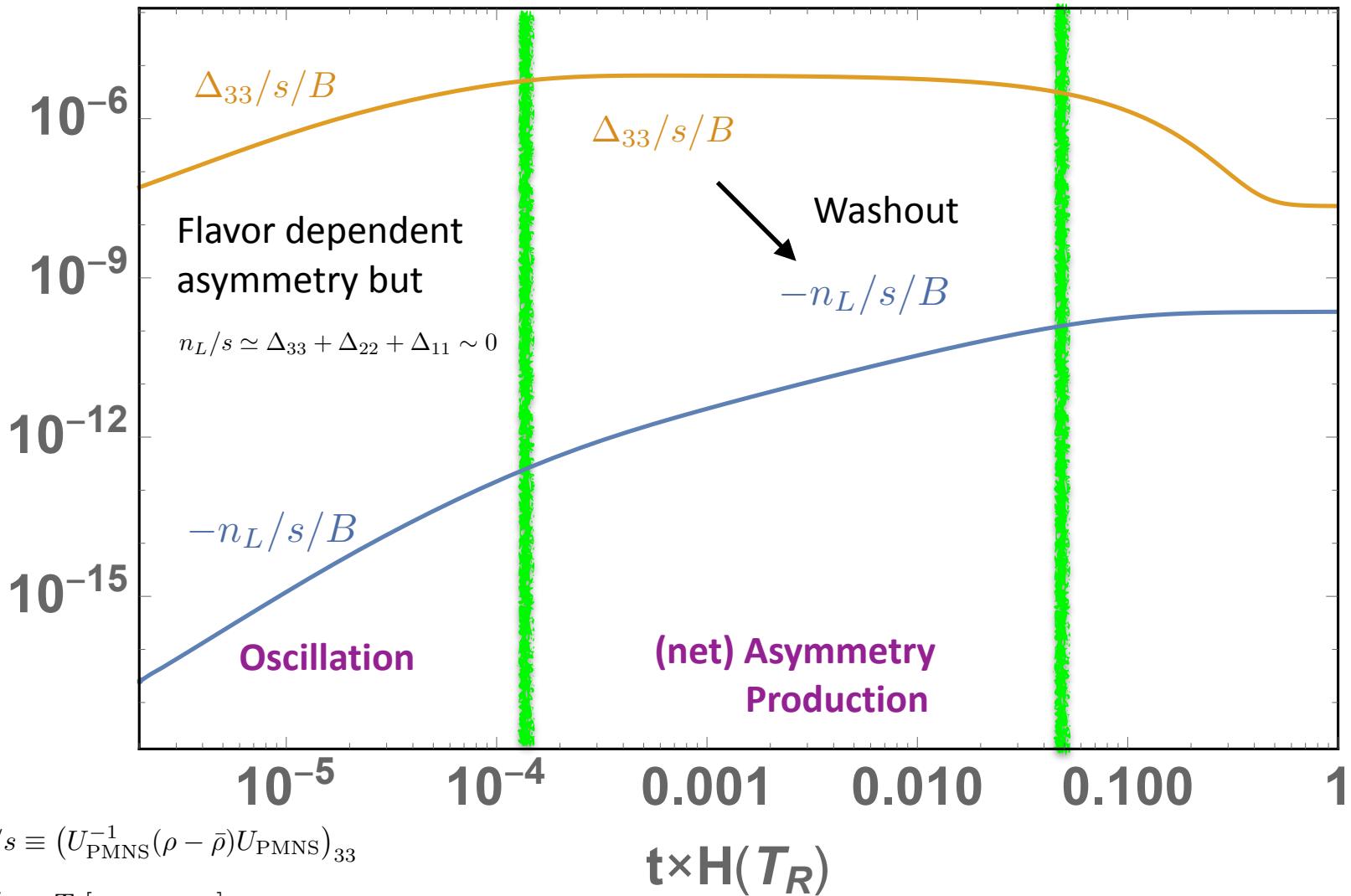






$$(\Gamma_{wo})_\alpha \propto m_{\nu_\alpha}^2$$

Normal hierarchy:  $(\Gamma_{wo})_3$  is largest.



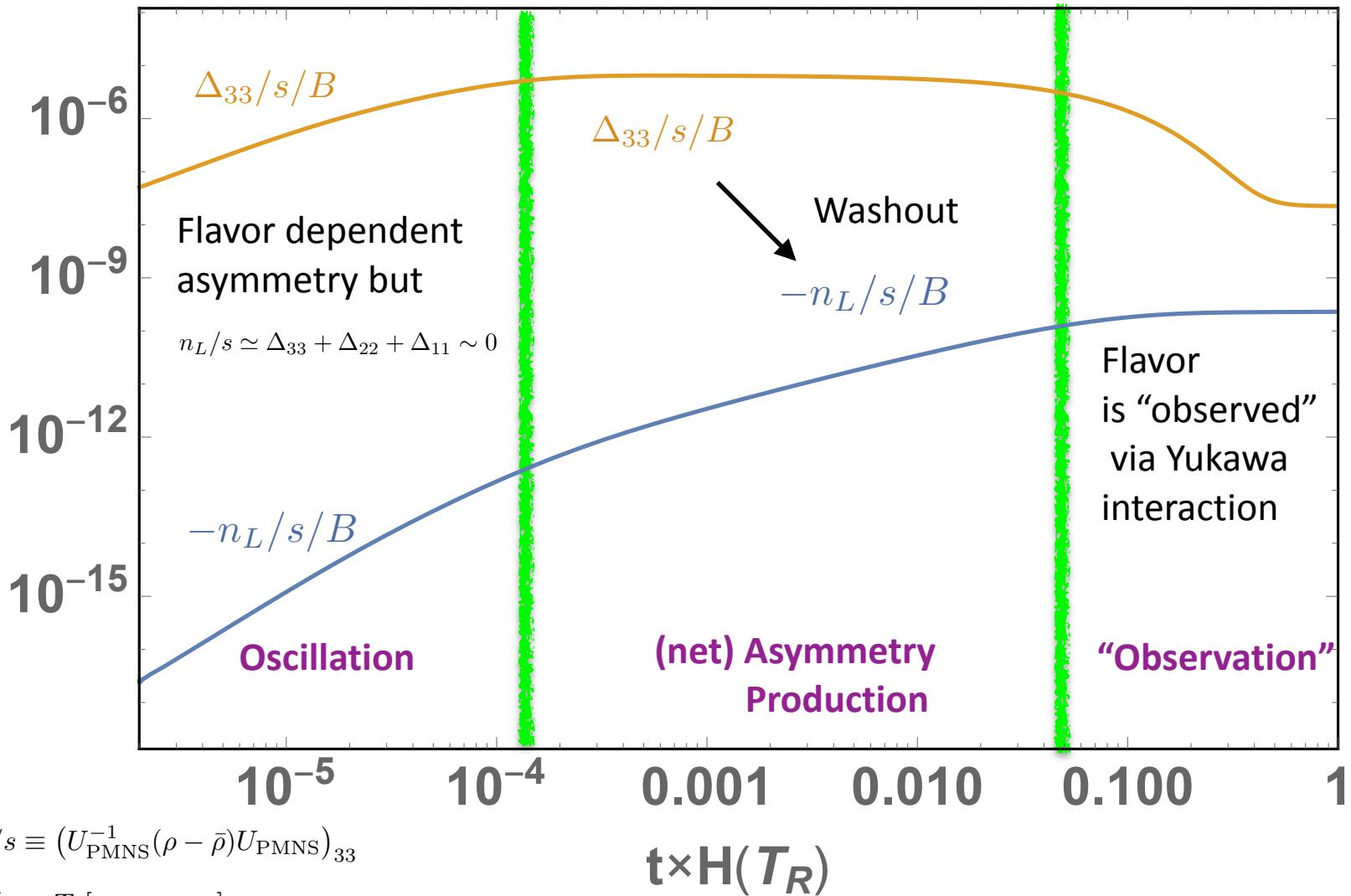
$$\Delta_{33}/s \equiv (U_{\text{PMNS}}^{-1} (\rho - \bar{\rho}) U_{\text{PMNS}})_{33}$$

$$n_L/s \equiv \text{Tr}[\rho - \bar{\rho} + \dots]$$



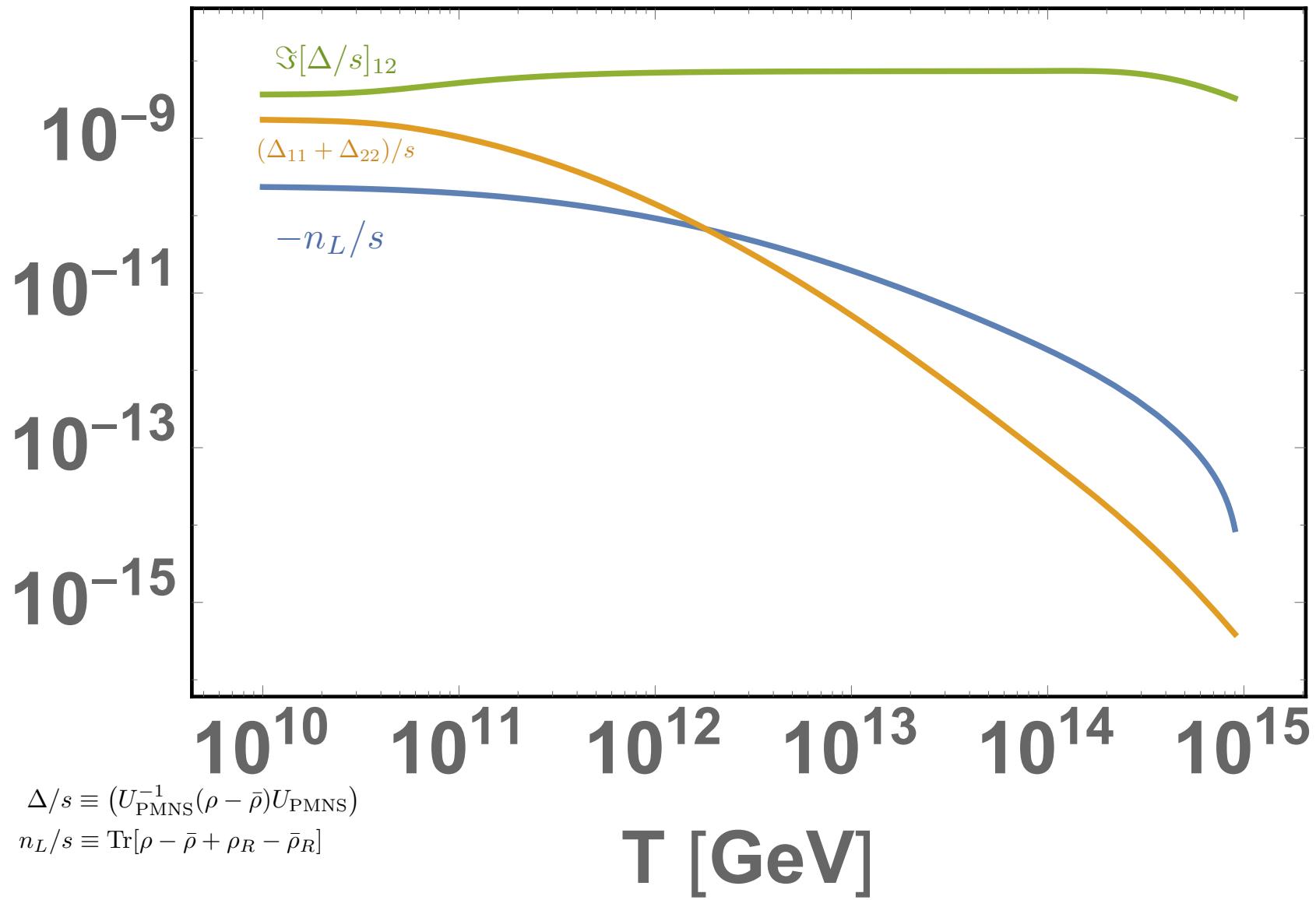
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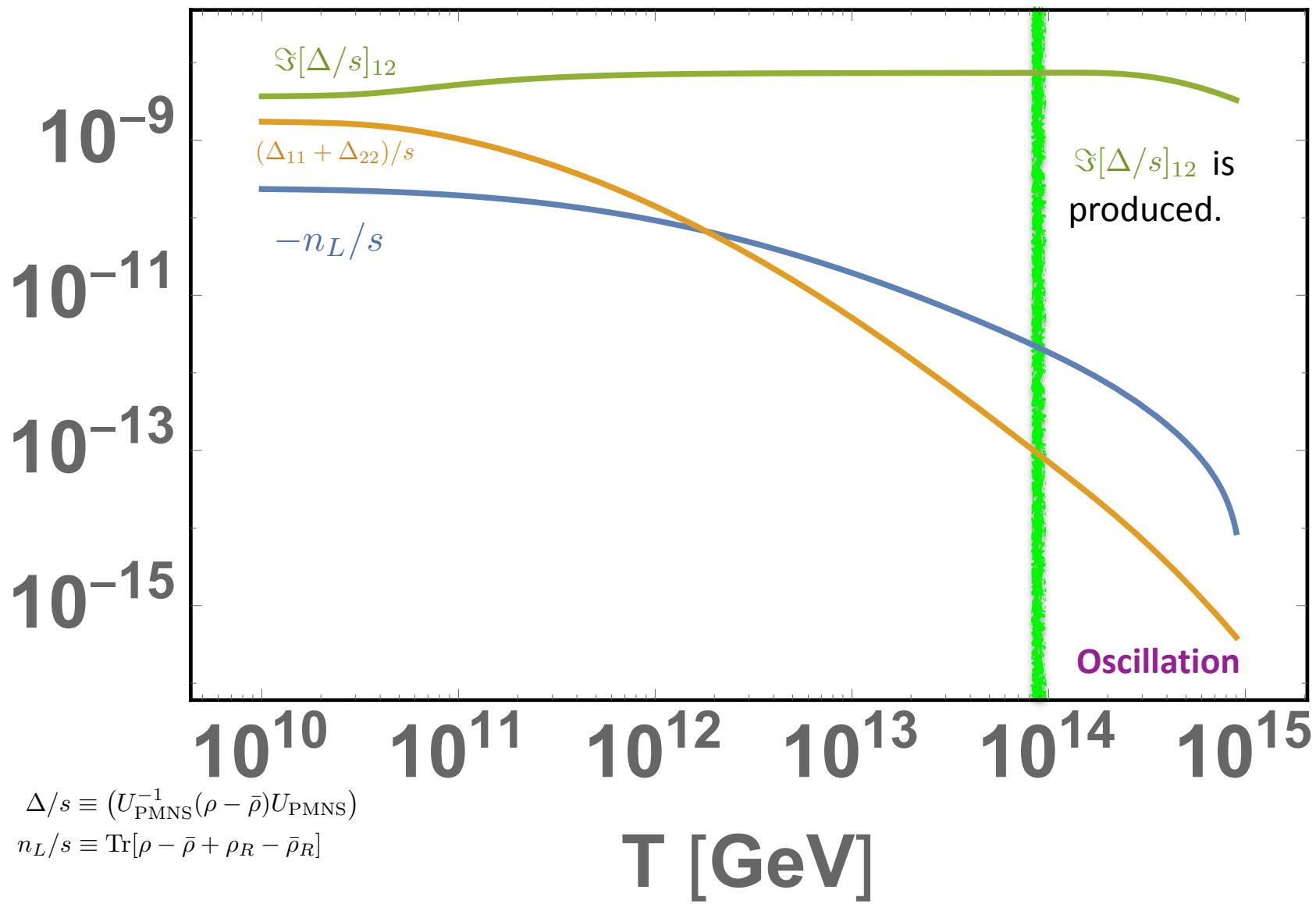
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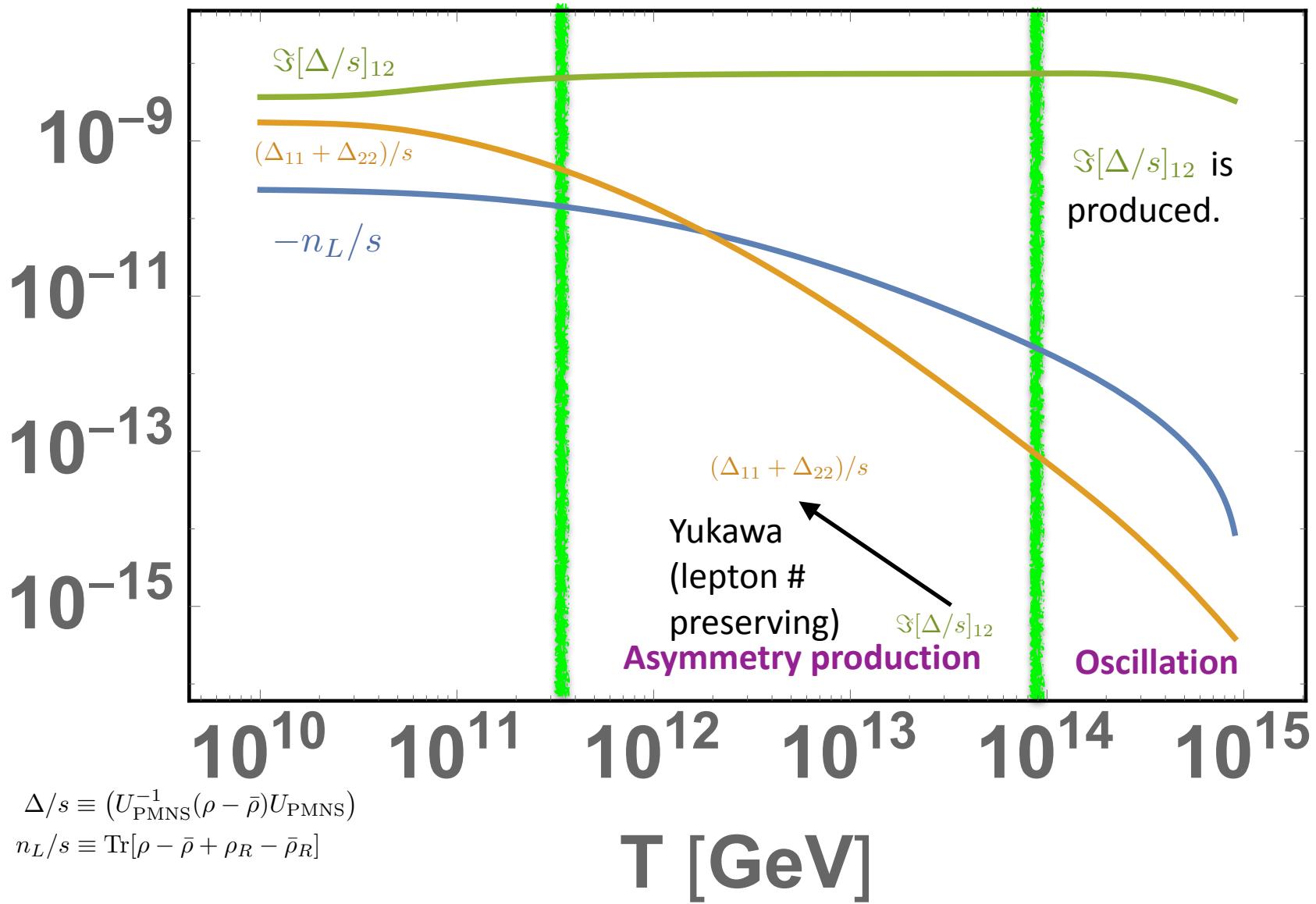
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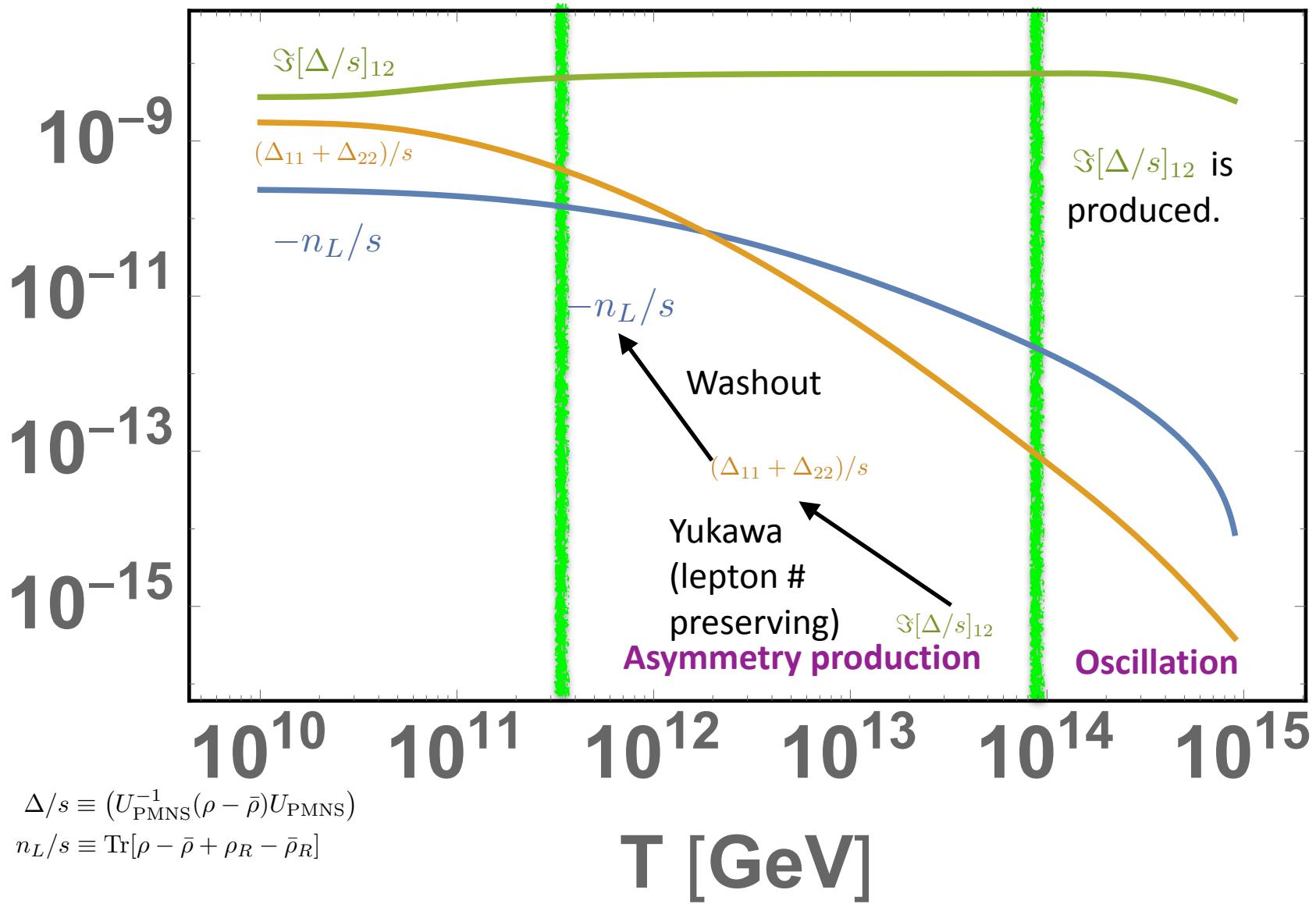


Inverted Hierarchy:  $(\Gamma_{wo})_1 \sim (\Gamma_{wo})_2 \gg (\Gamma_{wo})_3$



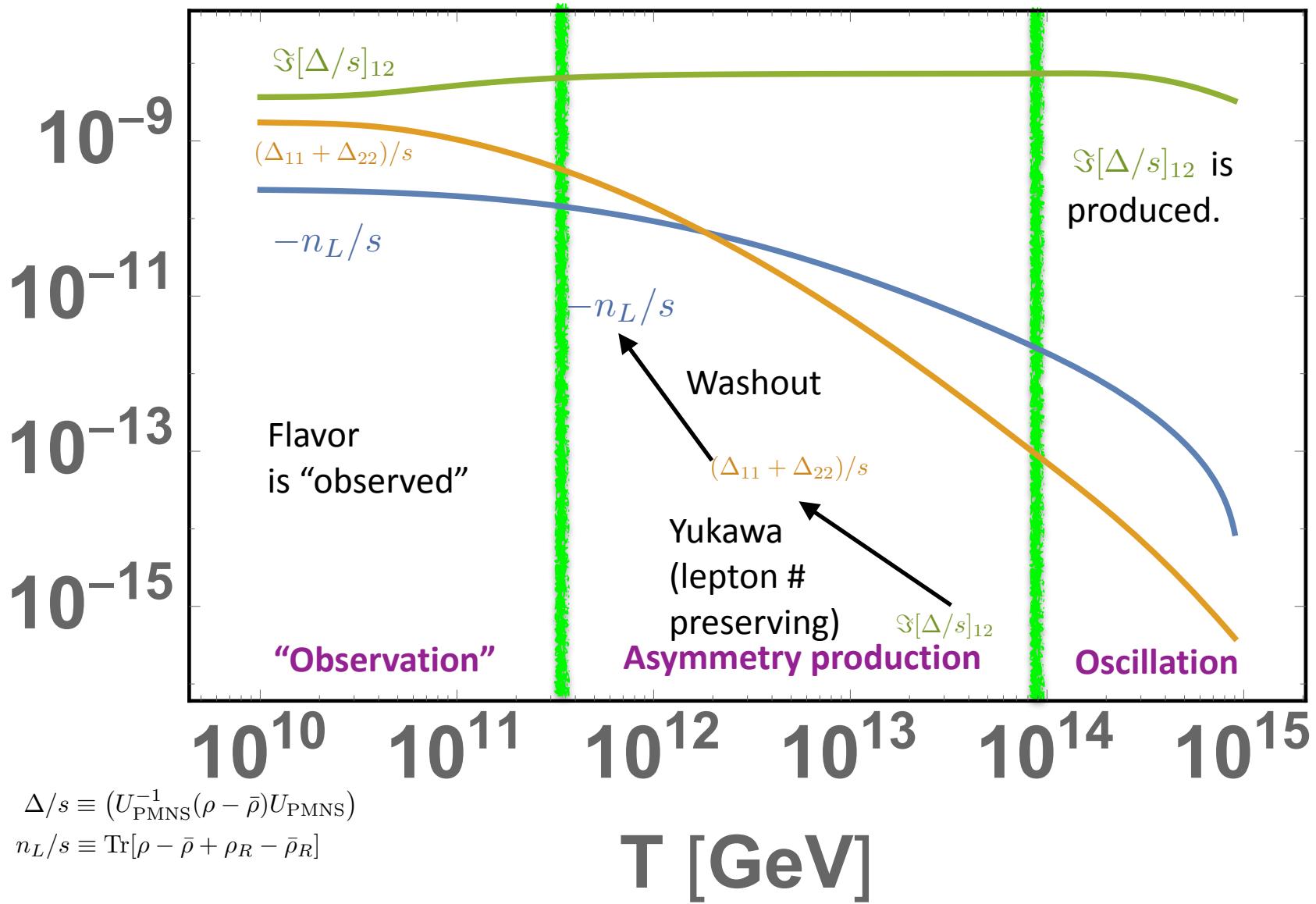


Inverted Hierarchy:  $(\Gamma_{wo})_1 \sim (\Gamma_{wo})_2 \gg (\Gamma_{wo})_3$



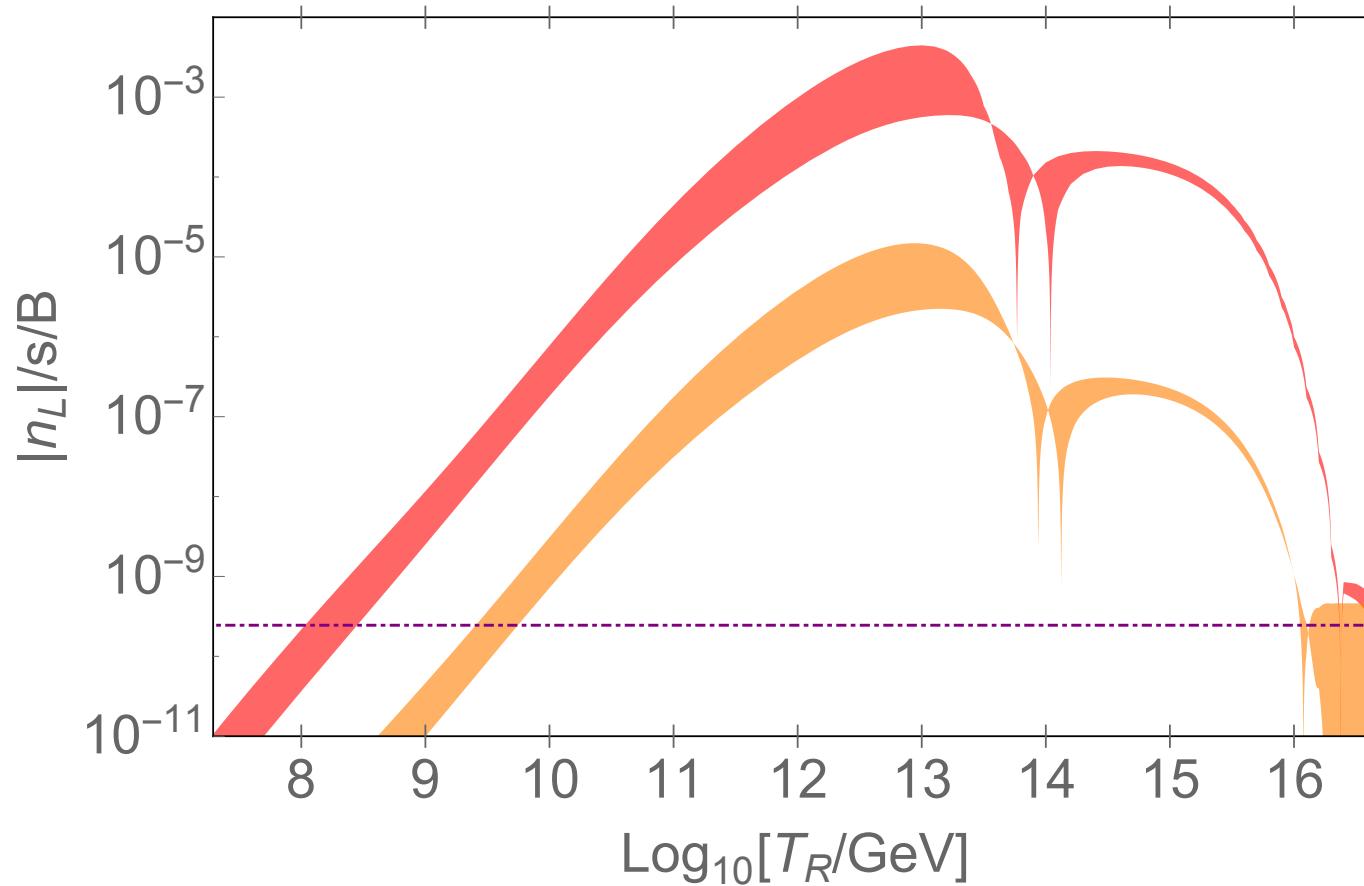


Inverted Hierarchy:  $(\Gamma_{wo})_1 \sim (\Gamma_{wo})_2 \gg (\Gamma_{wo})_3$

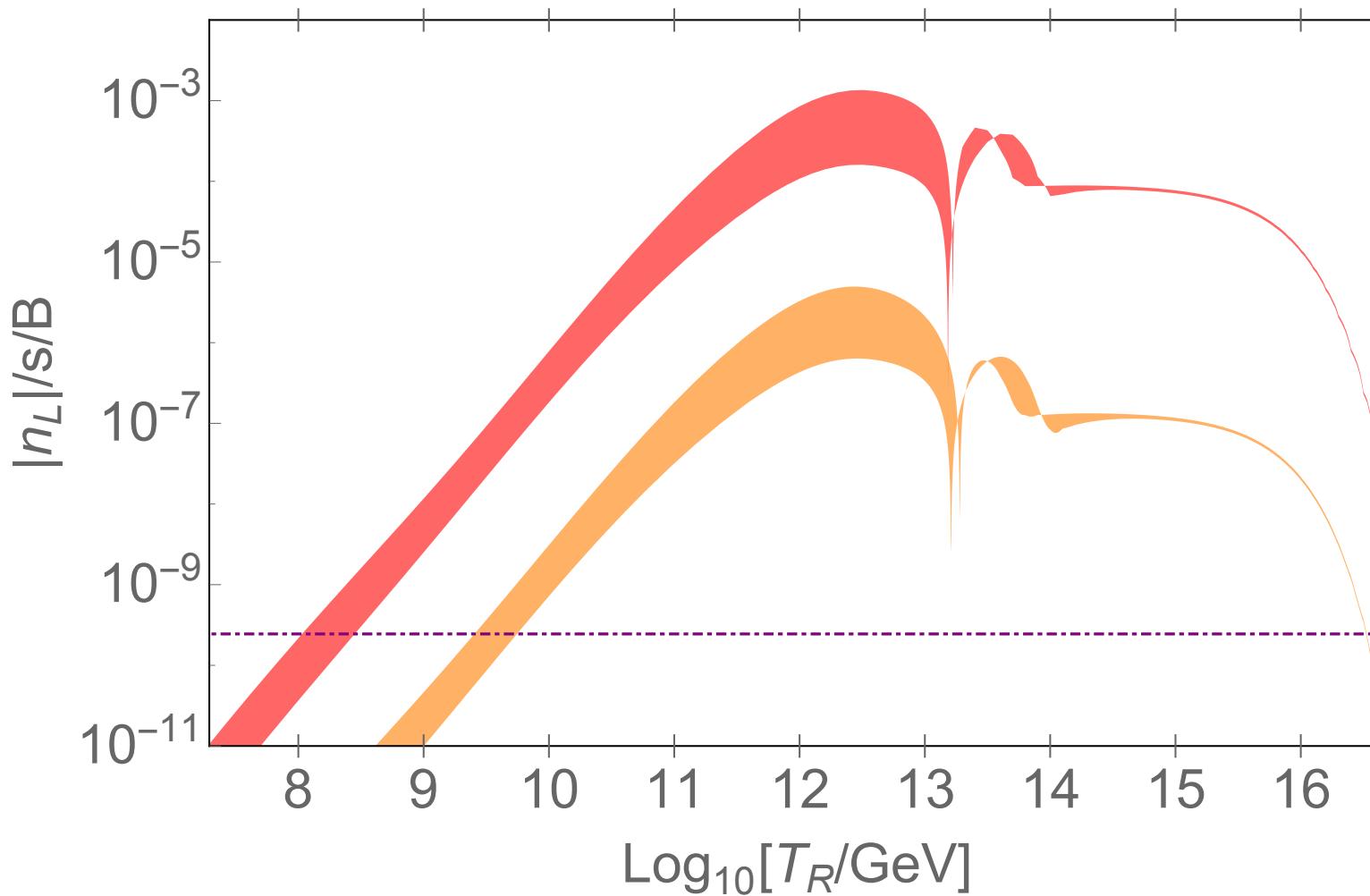


# **FIGURES FOR INFLATON->LEPTON**

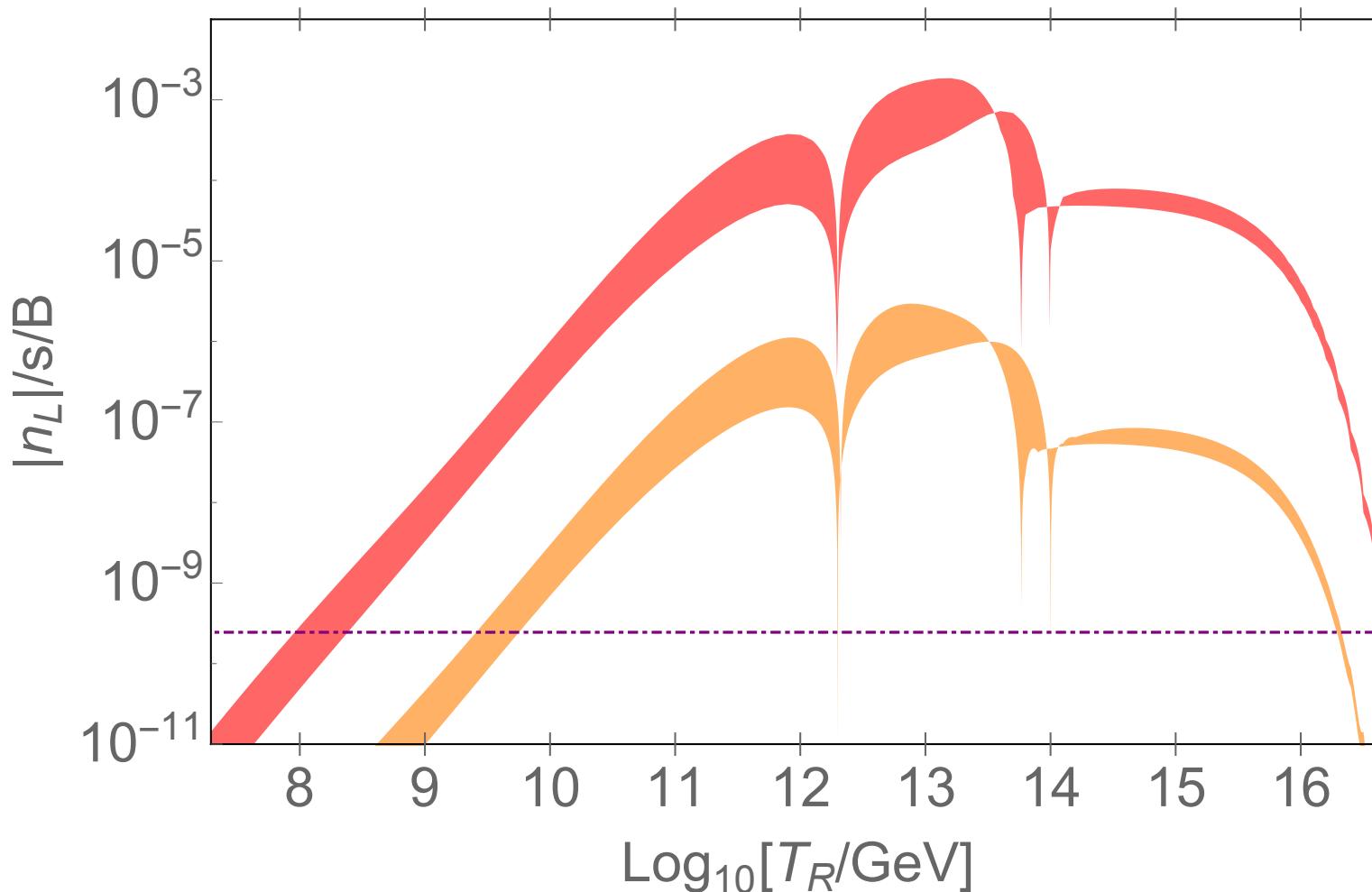
Inverted hierarchy one massless neutrino.  
Other parameters are same as the main part one.



normal order degenerate mass.  $m_{\text{nullightest}}=0.07\text{eV}$   
Other parameters are same as the main part one.

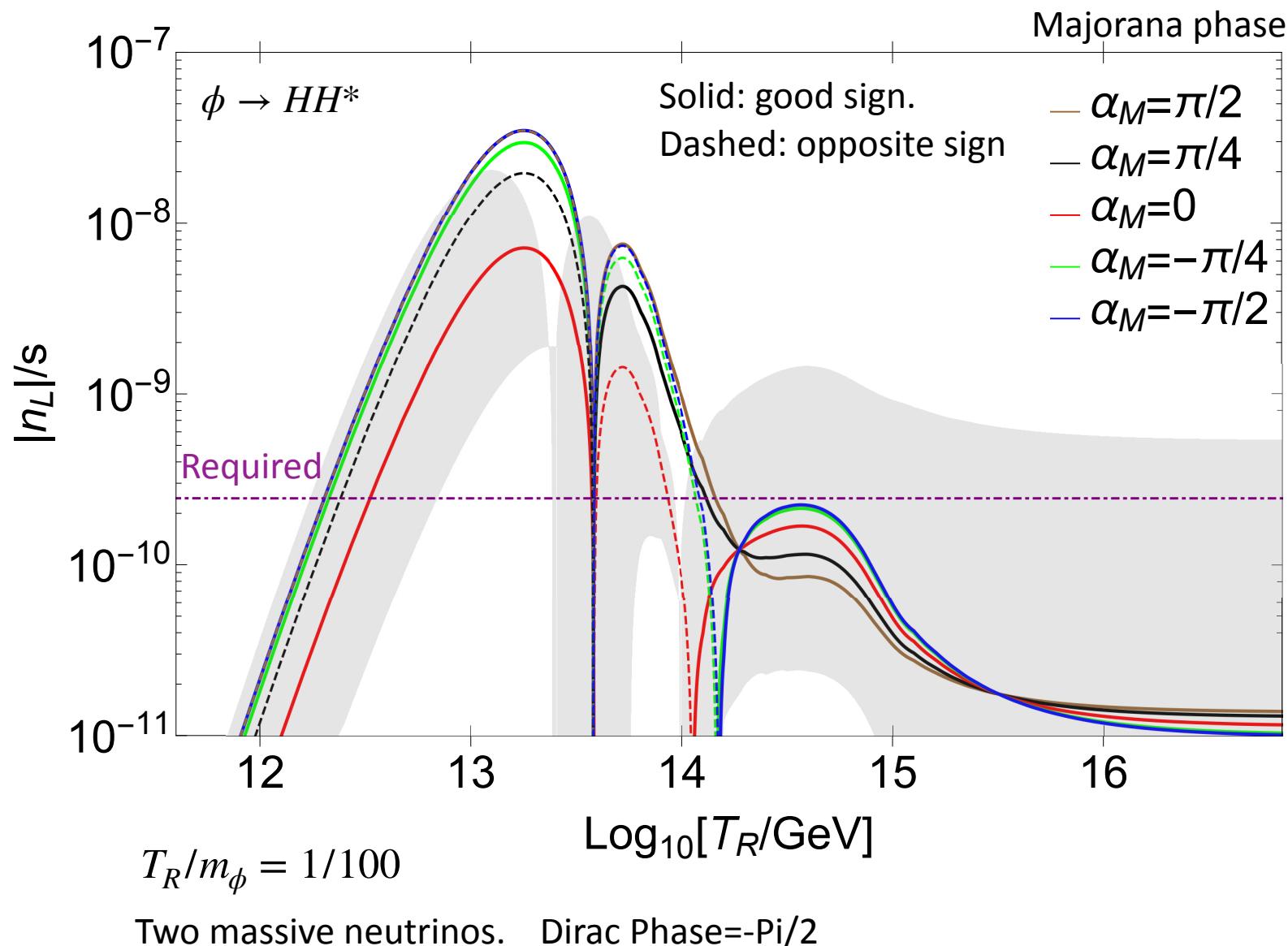


inverted order degenerate mass.  $m_{\text{lightest}}=0.07\text{eV}$   
Other parameters are same as the main part one.

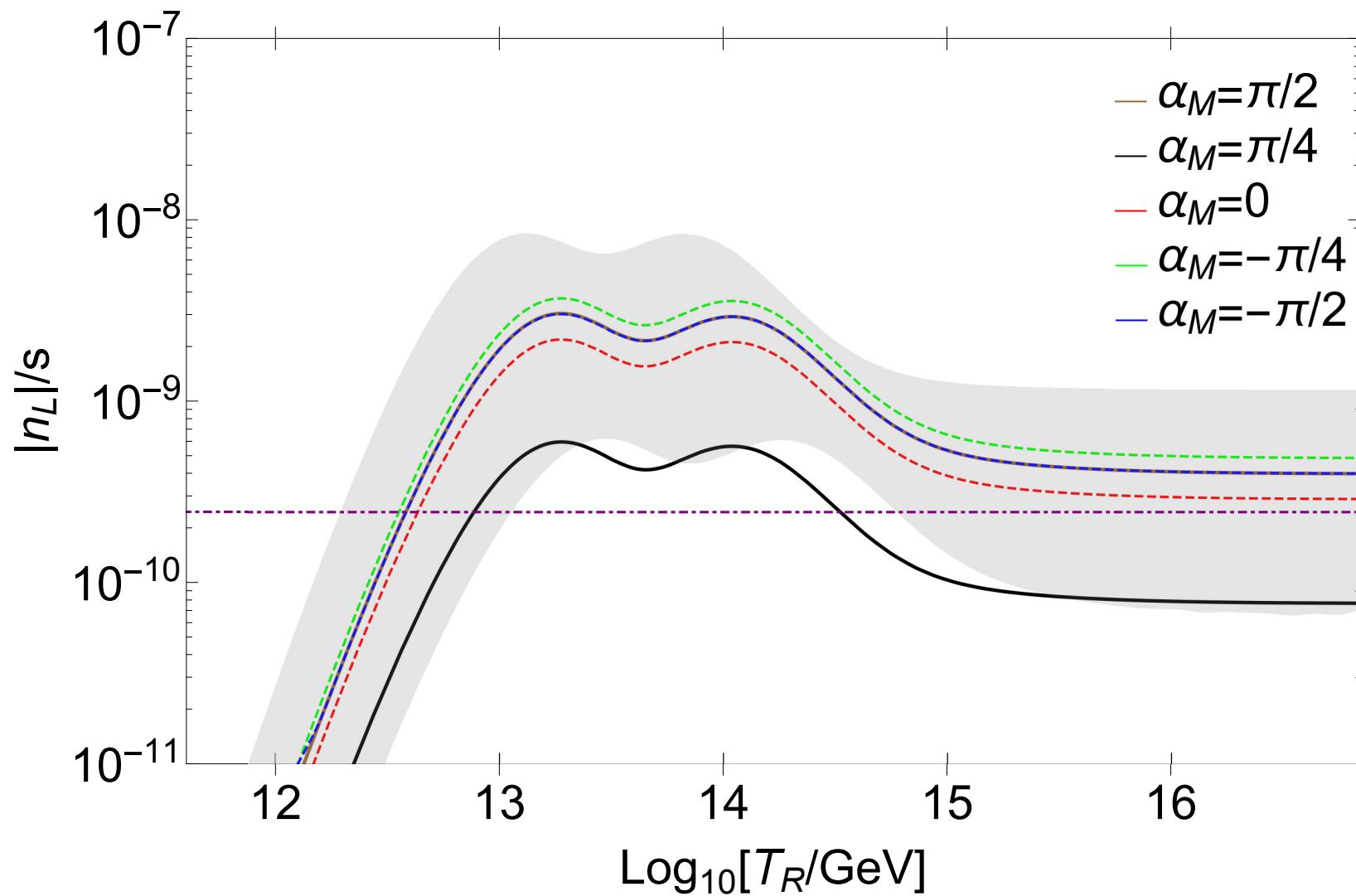


# **FIGURES FOR INFLATON->HIGGS**

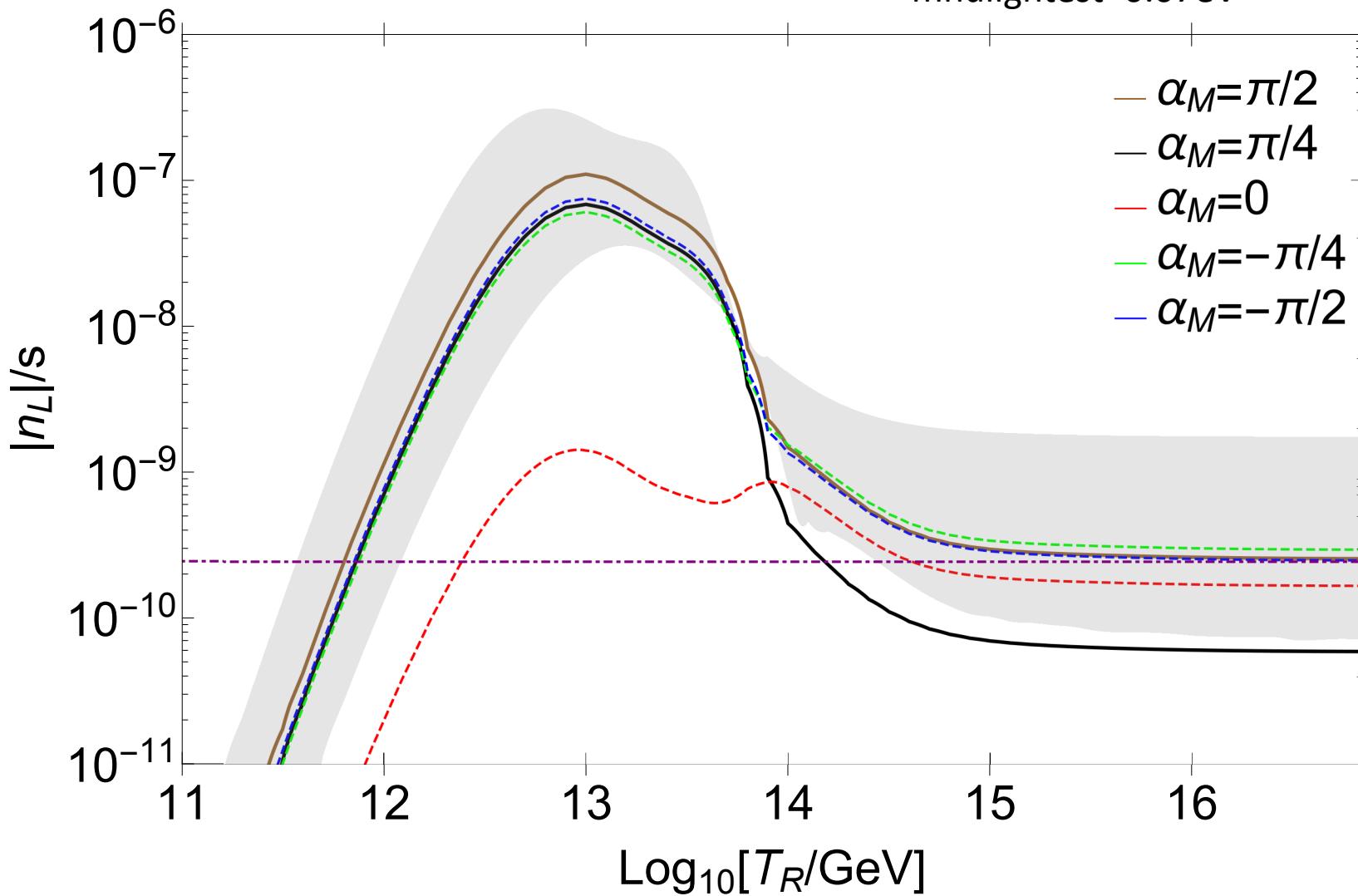
# Numerical result (Normal Hierarchy)



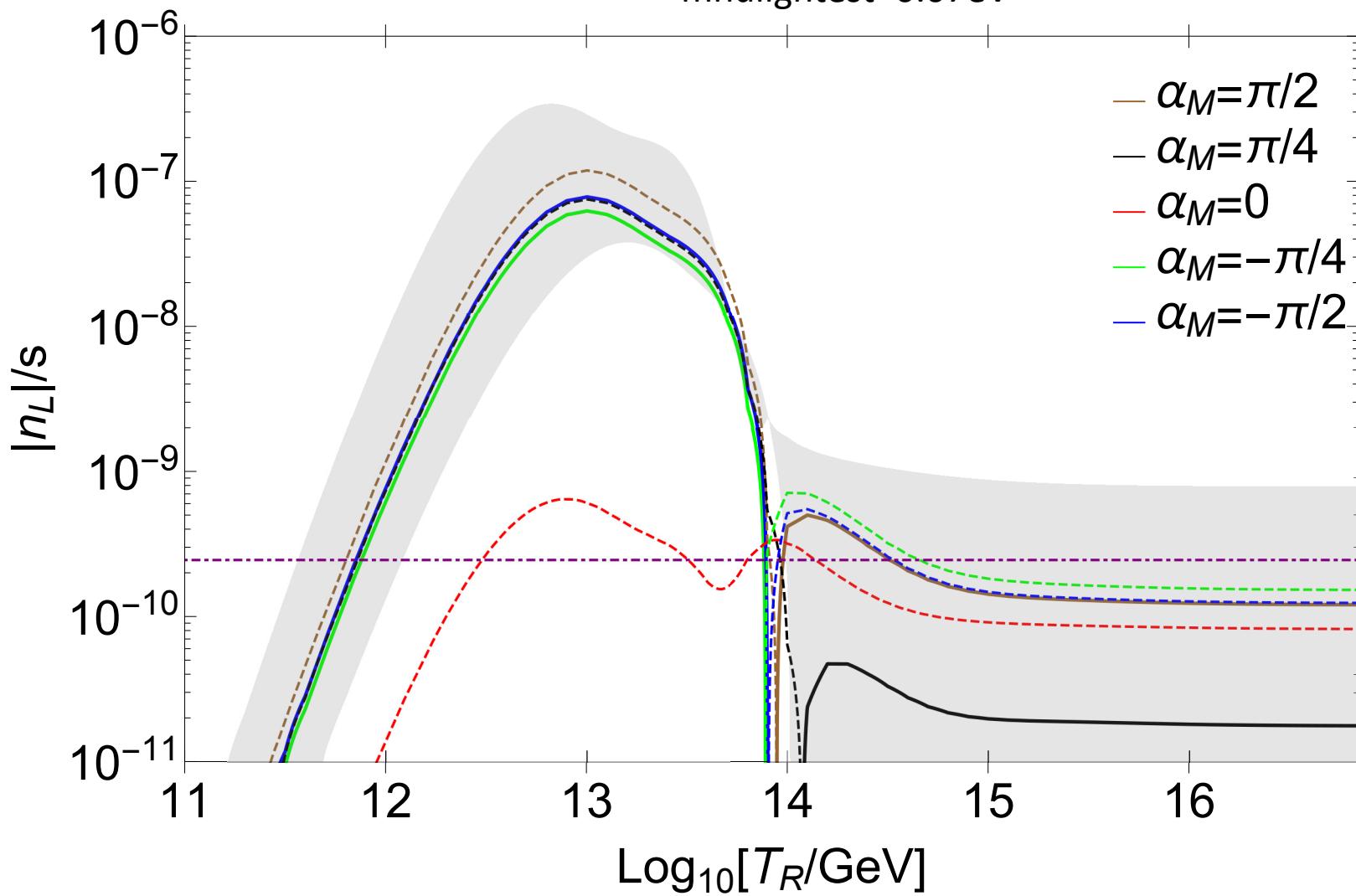
Inverted hierarchy



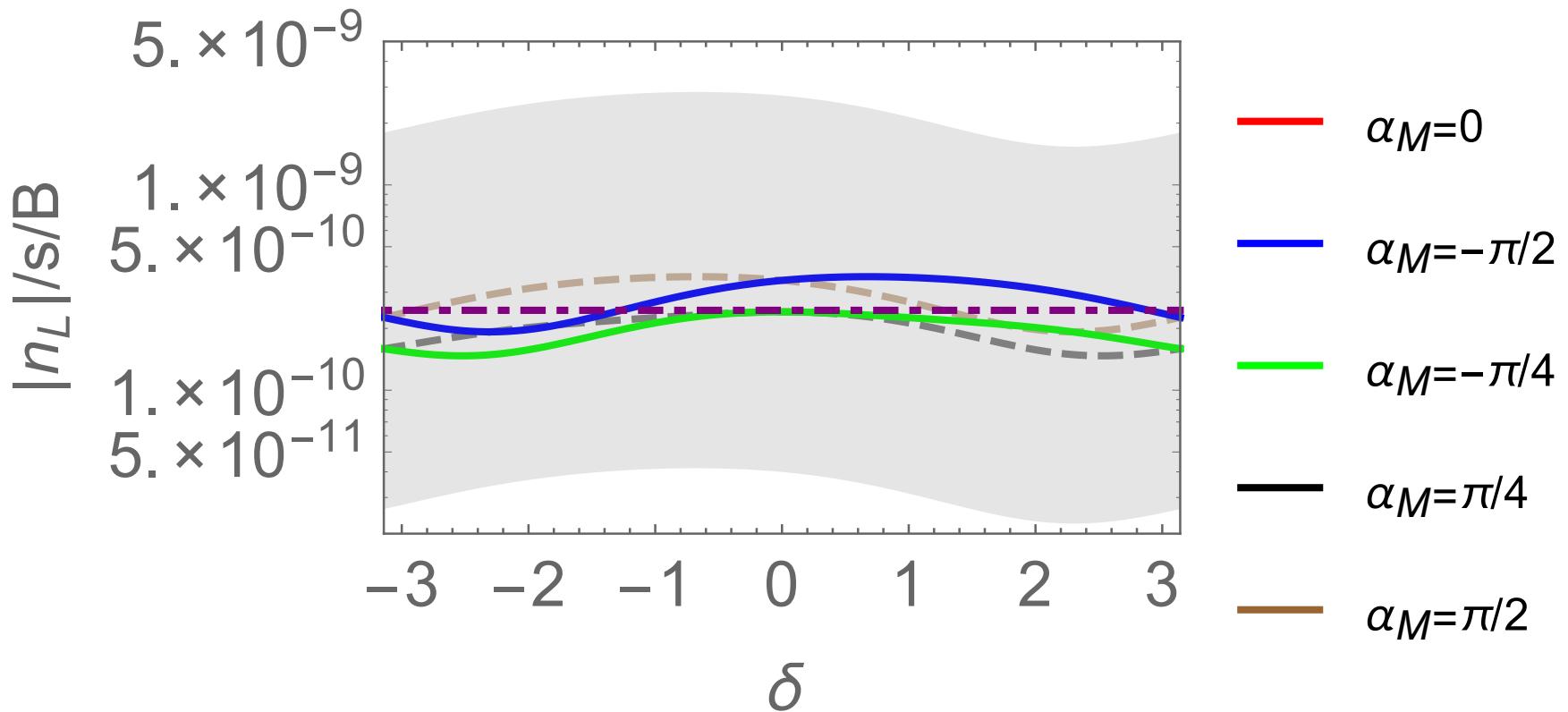
Inverted degenerate case.  
 $m_{\text{lightest}} = 0.07 \text{ eV}$



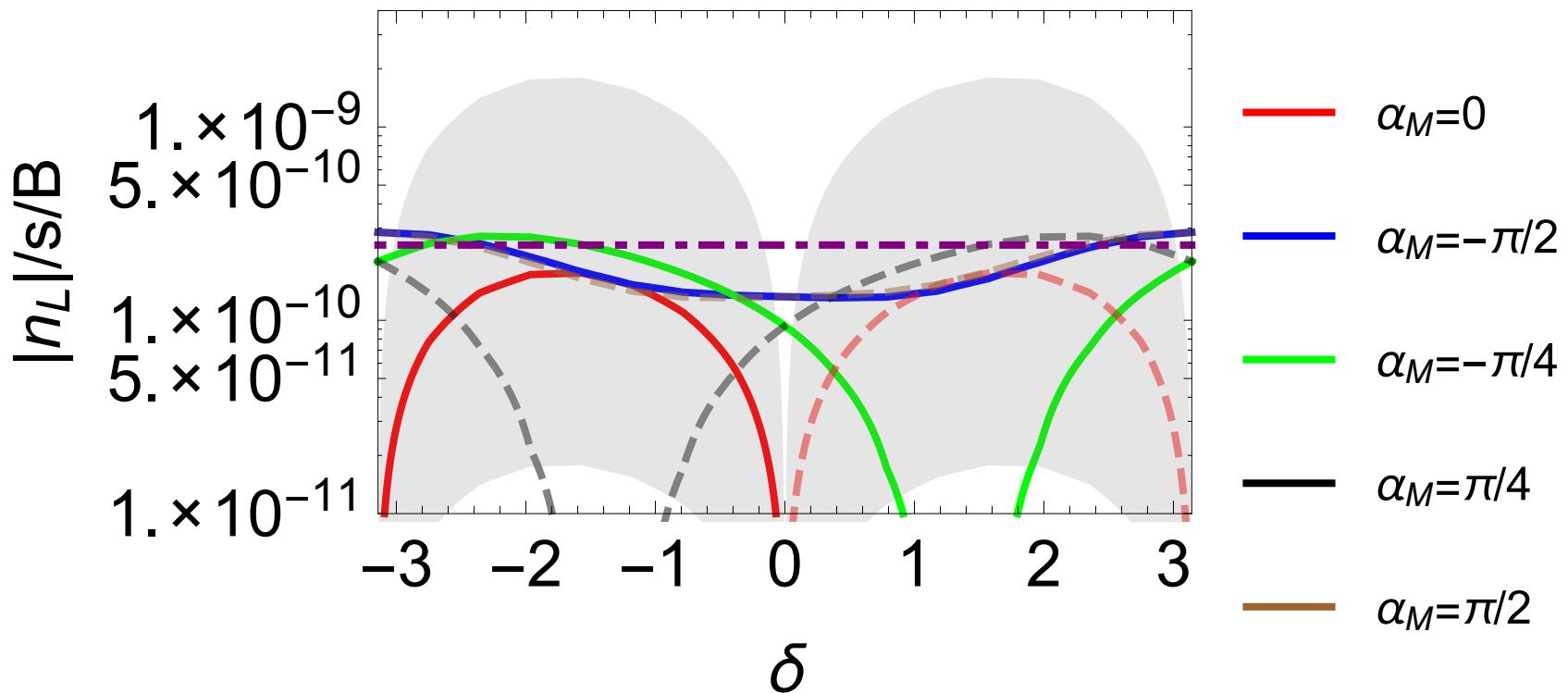
Normal hierarchy degenerate case.  
 $m_{\text{lightest}}=0.07\text{eV}$



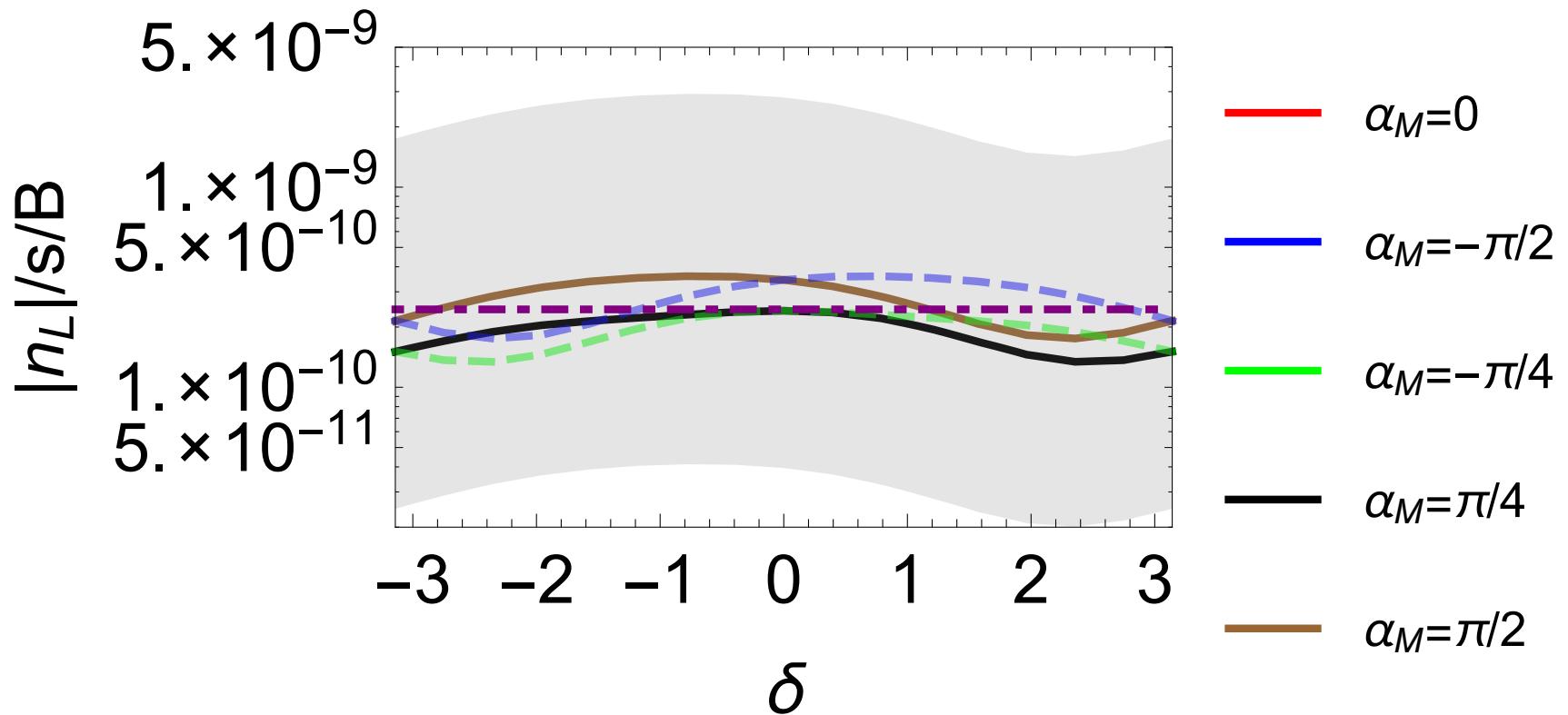
Normal,  $T_R = m_\phi / 100 = 7 \times 10^{11}$  GeV,  $m_{\nu\text{lightest}} = 0.07$  eV



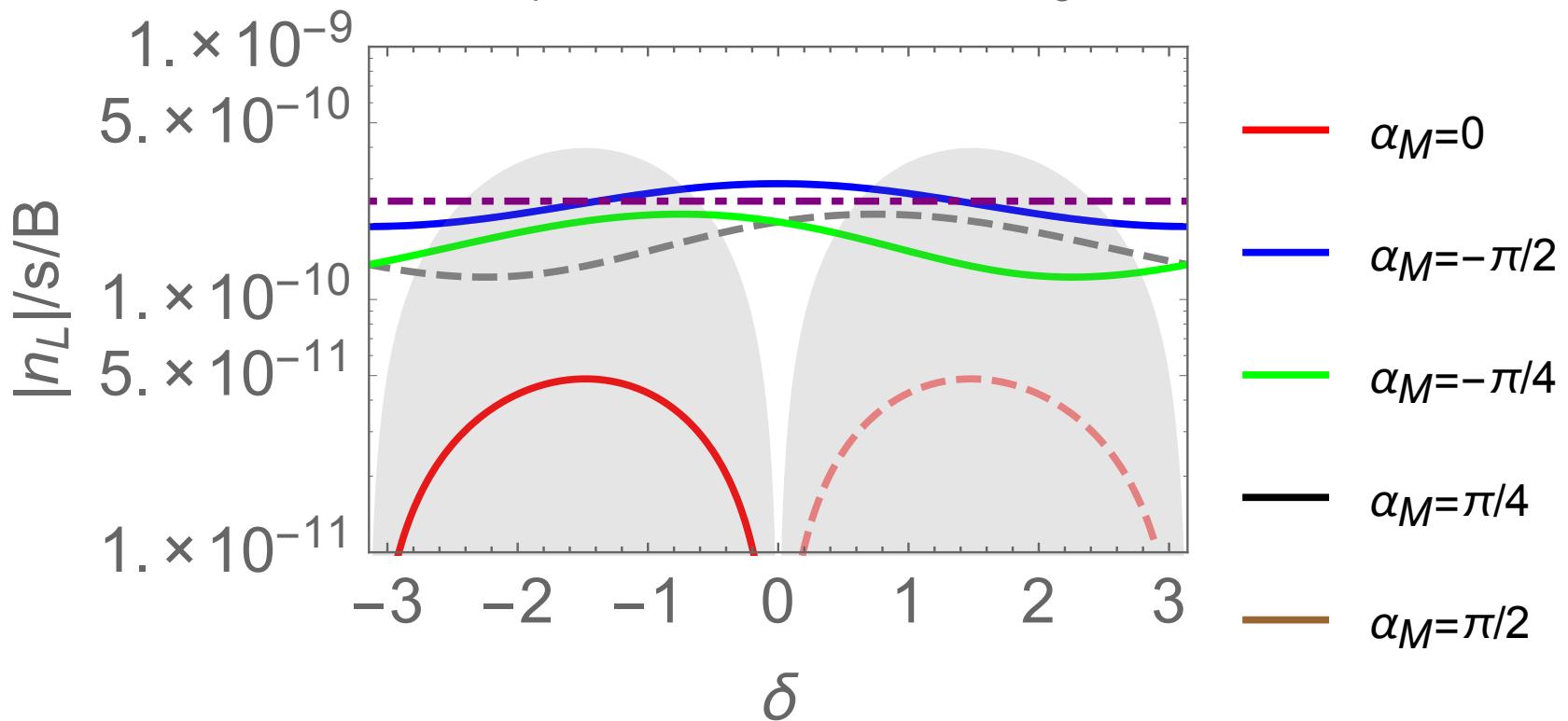
Inverted,  $T_R = m_\phi / 100 = 4 \times 10^{12} \text{ GeV}$ ,  $m_{\nu \text{lightest}} = 0 \text{ eV}$

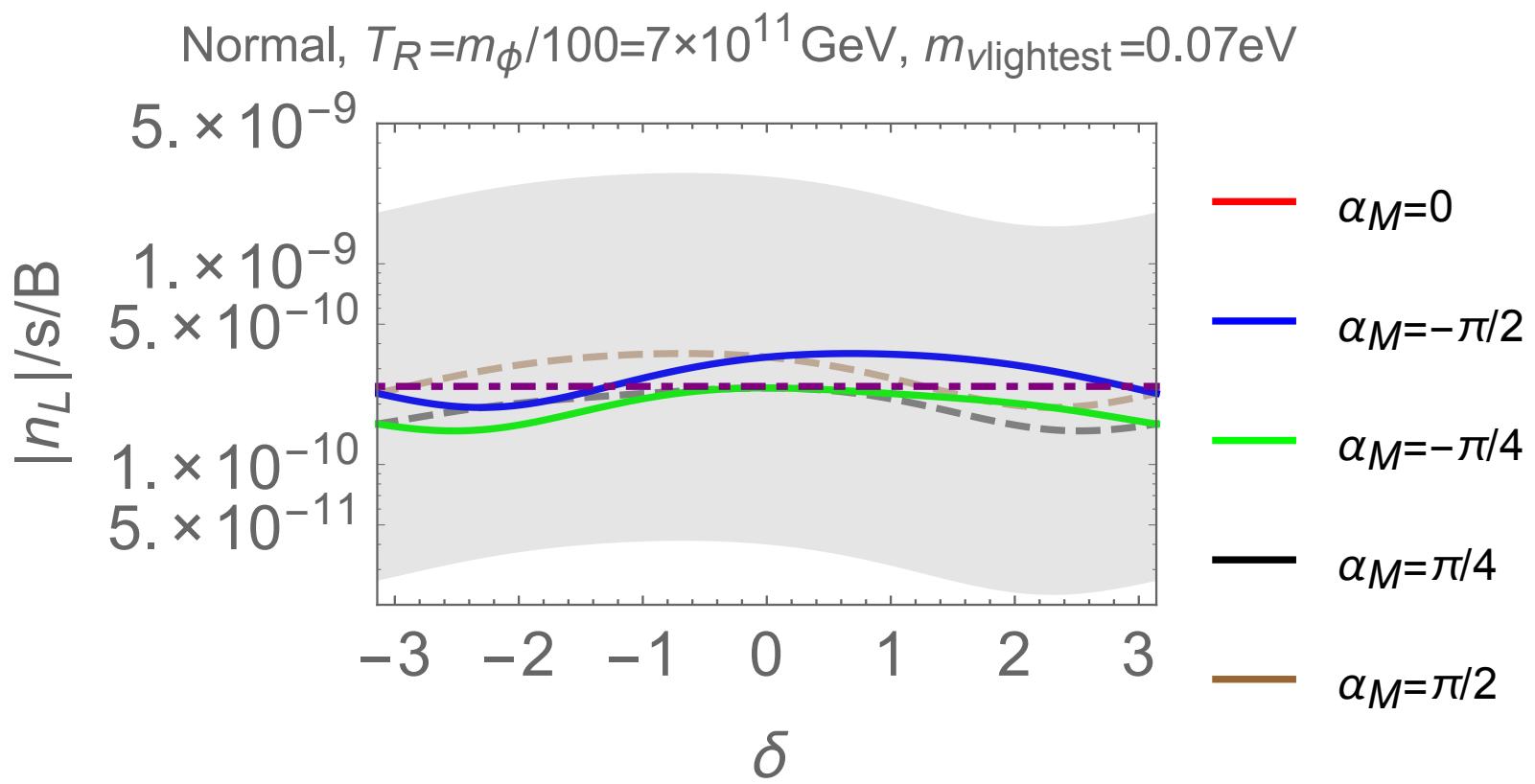


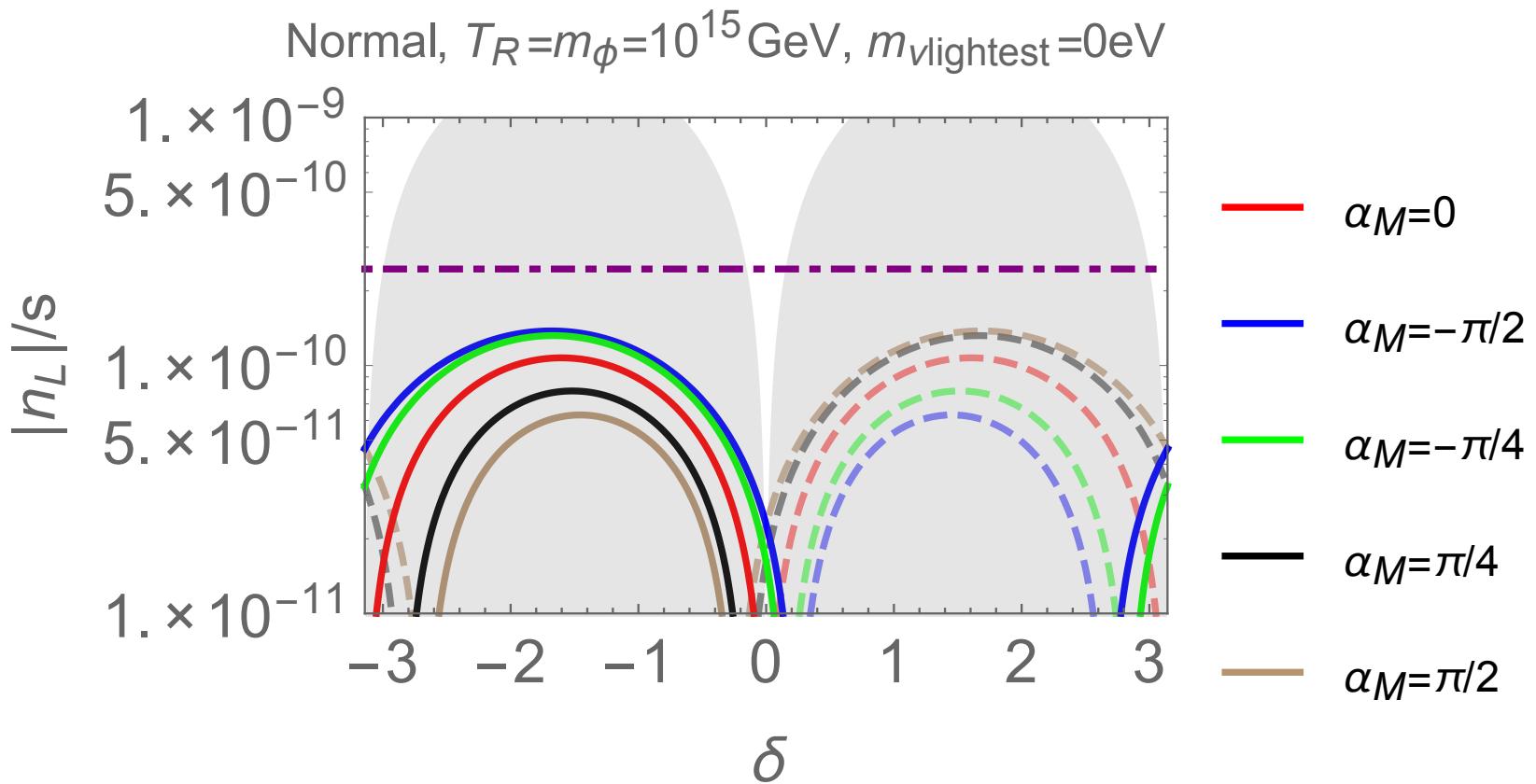
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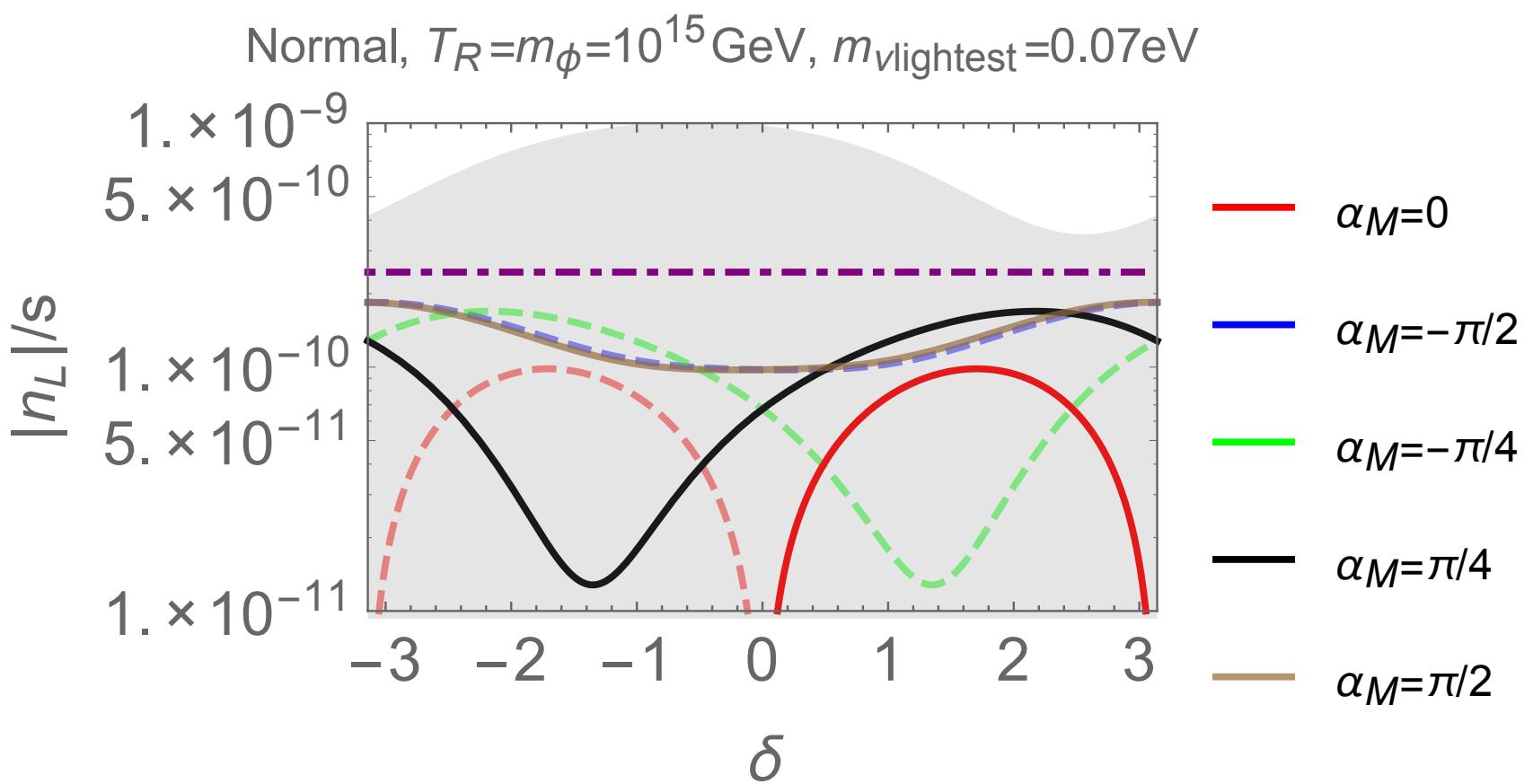


Normal,  $T_R = m_\phi / 100 = 2 \times 10^{12} \text{ GeV}$ ,  $m_{\nu \text{lightest}} = 0 \text{ eV}$

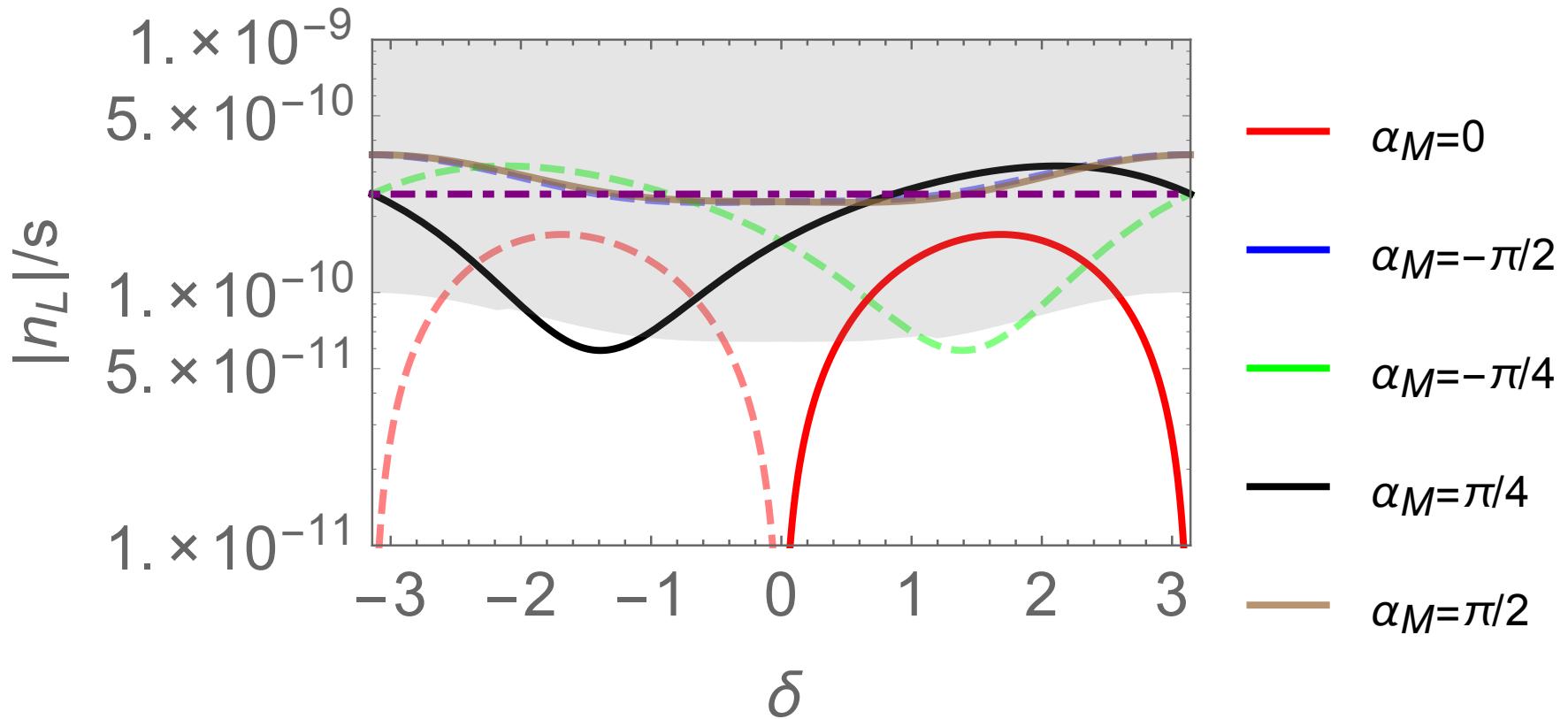








Inverted,  $T_R = m_\phi = 10^{15} \text{ GeV}$ ,  $m_{\nu \text{lightest}} = 0.07 \text{ eV}$



$\delta = -3\pi/4$ ,  $T_R \leq 10^{13}$  GeV

