



# BESIII上超子绝对分支比的测量

第二届强子物理新发展研讨会

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(On behalf of BESIII)  
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# Outline

01

**Hyperon weak radiative decays**

02

**Hyperon semi-leptonic decays**

03

**Hyperon nonleptonic decays**

# /// Study hyperons at BESIII

## Electromagnetic Calorimeter

CsI(Tl): L=28 cm

Barrel  $\sigma_E = 2.5\%$

Endcap  $\sigma_E = 5.0\%$

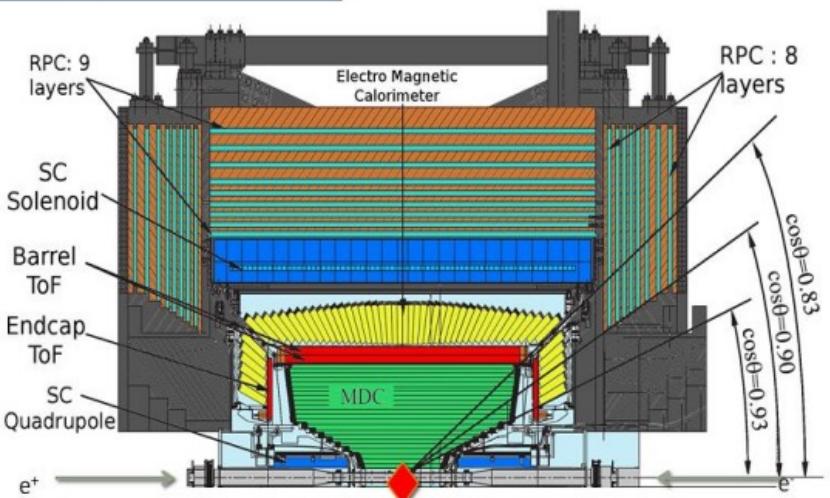
## Muon Counter

### RPC

Barrel: 9 layers

Endcap: 8 layers

$\sigma_{\text{spatial}} = 1.48 \text{ cm}$



## Main Drift Chamber

Small cell, 43 layer

$\sigma_{xy} = 130 \mu\text{m}$

$dE/dx \sim 6\%$

$\sigma_p/p = 0.5\% \text{ at } 1 \text{ GeV}$

## Time Of Flight

Plastic scintillator

$\sigma_T(\text{barrel}) = 80 \text{ ps}$

$\sigma_T(\text{endcap}) = 110 \text{ ps}$

(update to 65 ps with MRPC)

With 10 billion  $J/\psi$  and 2.7 billion  $\psi(3686)$  collected at BESIII,  $\sim 10^7$  entangled hyperon pairs can be produced, which enables precise measurements of the hyperon absolute BFs.

Front. Phys. 12(5), 121301 (2017)

Decay mode	$B(\times 10^{-3})$	$N_B(\times 10^6)$
$J/\psi \rightarrow \Lambda \bar{\Lambda}$	$1.89 \pm 0.09$	$\sim 18.9$
$J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$	$1.172 \pm 0.032$	$\sim 11.7$
$J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$	$1.07 \pm 0.04$	$\sim 10.7$
$J/\psi \rightarrow \Xi^0 \bar{\Xi}^0$	$1.17 \pm 0.04$	$\sim 11.7$
$J/\psi \rightarrow \Xi^- \bar{\Xi}^+$	$0.97 \pm 0.08$	$\sim 9.7$
$\psi(2S) \rightarrow \Omega^- \bar{\Omega}^+$	$0.057 \pm 0.003$	$\sim 0.17$

# Hyperon weak radiative decays

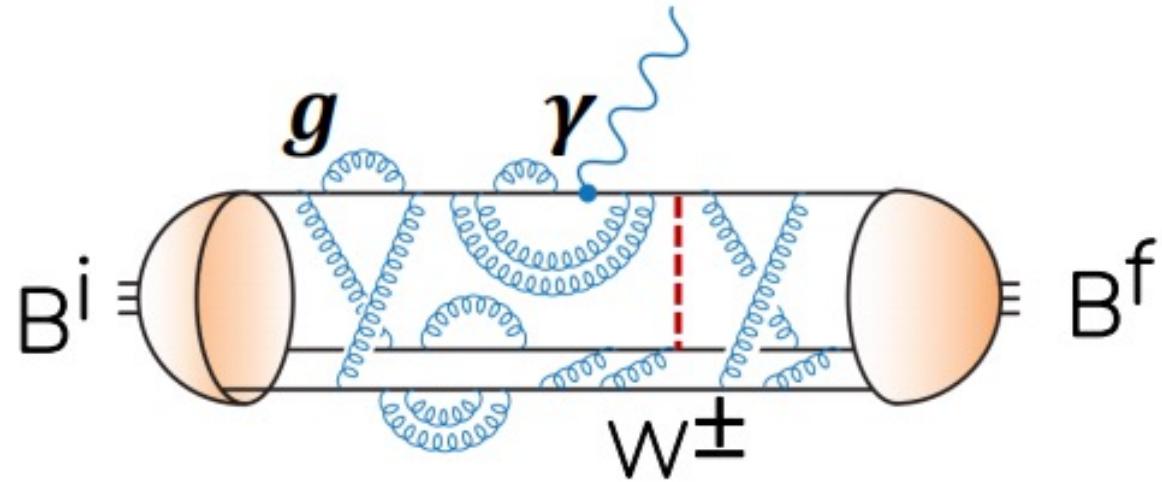
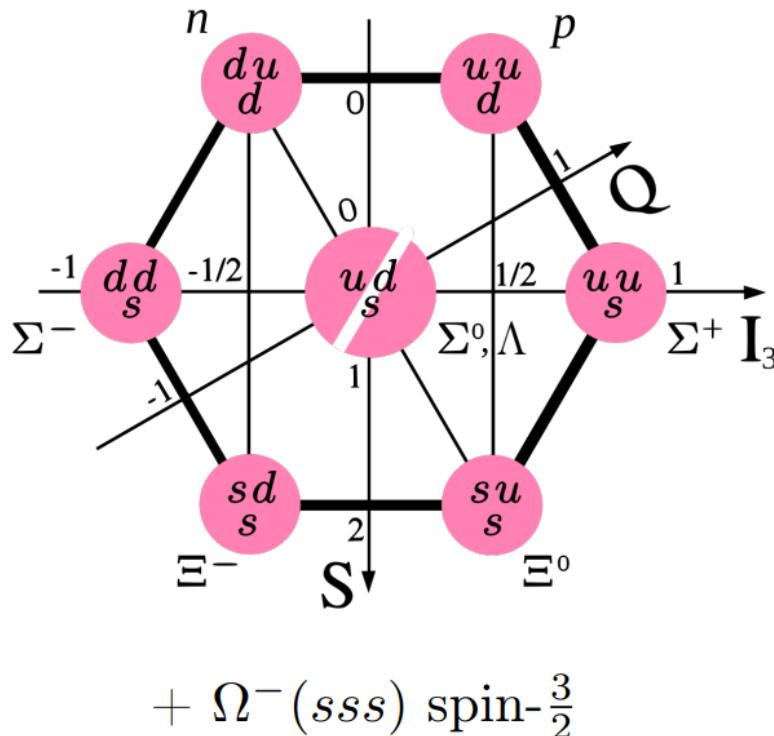
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# /// Physics Motivation

## Hyperon weak radiative decays (WRHDs)

- flavor changing neutral current (FCNC) process ( $s \rightarrow d\gamma$  transition)
- significant non-perturbative QCD effects
- A symphony of **strong**, **weak**, and **EM** interaction



Prog. Part. Nucl. Phys. **91** (2016) 1-100  
Int. J. Mod. Phys. A **10** (1995) 3817-3876

# /// Physics Motivation

Phys. Rev. Lett. 12 (1964) 378-379

- Hara's theorem predicts the parity-violating decay amplitudes for the  $\Sigma^+ \rightarrow p\gamma$  and  $\Xi^- \rightarrow \Sigma^-\gamma$  decays vanish in the SU(3) limit.
- The experimentally measured asymmetry decay parameter for  $\Sigma^+ \rightarrow p\gamma$  is surprisingly large.

$-0.720 \pm 0.086 \pm 0.045$	35k	<sup>2</sup> FOUCHER	1992	SPEC	$\Sigma^+ 375 \text{ GeV}$
$-0.86 \pm 0.13 \pm 0.04$	190	KOBAYASHI	1987	CNTR	$\pi^+ p \rightarrow \Sigma^+ K^+$
$-0.53^{+0.38}_{-0.36}$	46	MANZ	1980	HBC	$K^- p \rightarrow \Sigma^+ \pi^-$
$-1.03^{+0.52}_{-0.42}$	61	GERSHWIN	1969B	HBC	$K^- p \rightarrow \Sigma^+ \pi^-$

$\alpha_\gamma$

- In the SM, the branching fraction of  $\Omega^- \rightarrow \Xi^-\gamma$  is very small, there are many new physics models can enhance it so that this decay can serve as a probe for the physics beyond SM.

Phys. Rev. D 53, 3620 (1996)

Phys. Rev. D 61, 114022 (2000)

# Puzzle!

Λ →  $n\gamma$

$J/\psi \rightarrow \Lambda\bar{\Lambda}$ ,  $\Lambda \rightarrow n\gamma$ ,  $\bar{\Lambda} \rightarrow \bar{p}\pi^+ + c.c.$

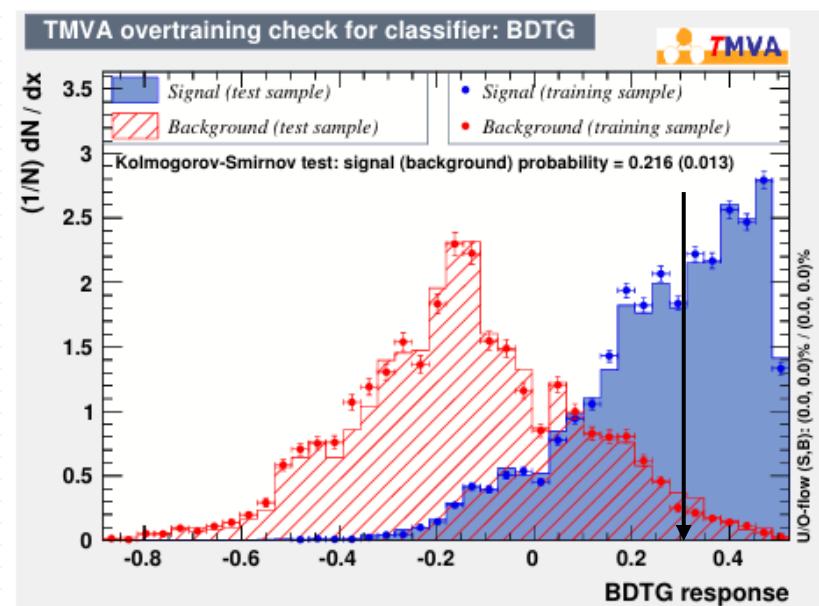
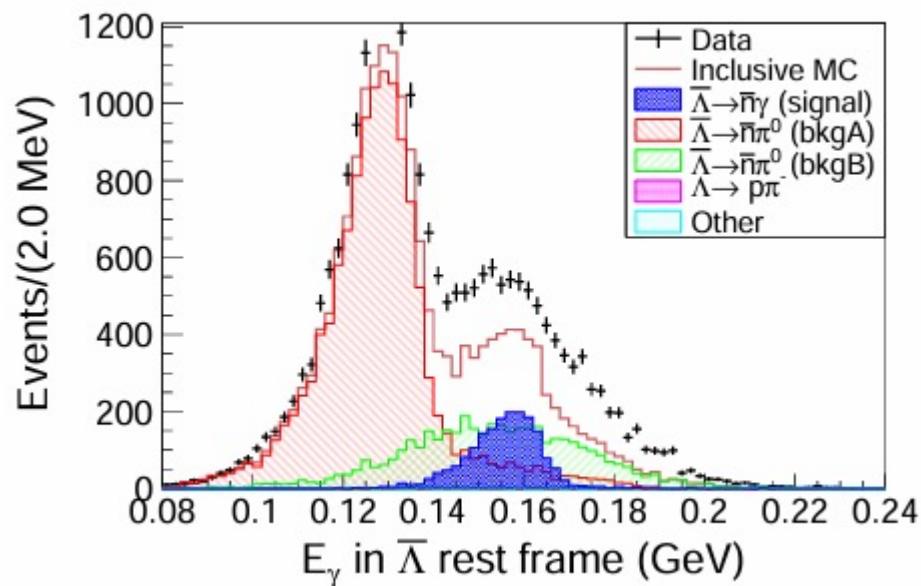
## Analysis Method Highlights

### Kinematic fit with missing particle/energy

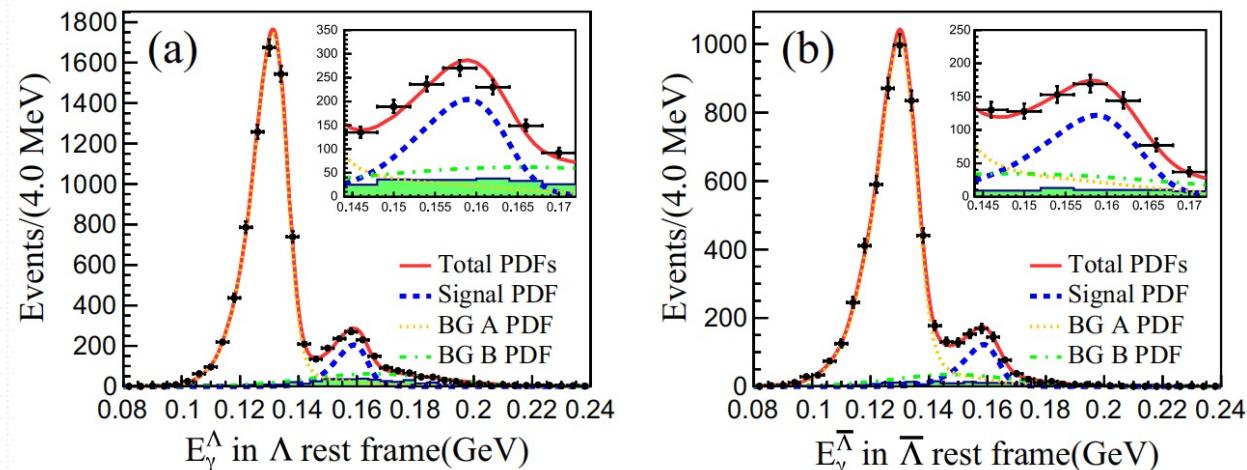
- Hypothesis:  $\bar{\Lambda}(\rightarrow \bar{p}\pi^-)\gamma + n(\text{missing particle})$
- Hypothesis:  $\Lambda(\rightarrow p\pi^+)\gamma + \bar{n}(\text{missing energy, the direction of the anti-neutron is reconstructed})$
- Superiority of well-constrained kinematics

MVA-base background photon suppression

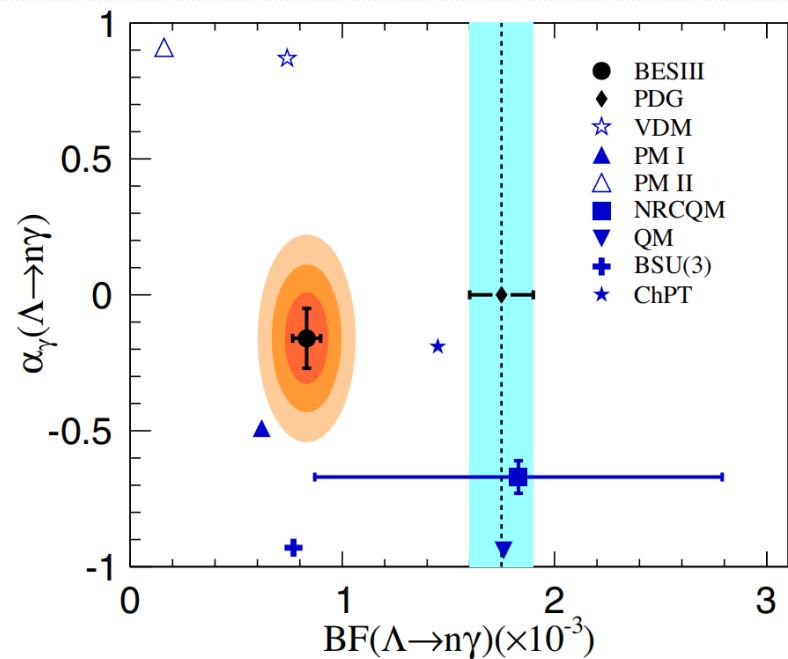
Rejected 96.9% background B with 50.1% signal efficiency



## Analysis results



Decay mode	$\Lambda \rightarrow n\gamma$	$\bar{\Lambda} \rightarrow \bar{n}\gamma$
$N_{ST} (\times 10^3)$	$6853.2 \pm 2.6$	$7036.2 \pm 2.7$
$\varepsilon_{ST} (\%)$	$51.13 \pm 0.01$	$52.53 \pm 0.01$
$N_{DT}$	$723 \pm 40$	$498 \pm 41$
$\varepsilon_{DT} (\%)$	$6.58 \pm 0.04$	$4.32 \pm 0.03$
BF ( $\times 10^{-3}$ )	$0.820 \pm 0.045 \pm 0.066$	$0.862 \pm 0.071 \pm 0.084$
	<b><math>0.832 \pm 0.038 \pm 0.054</math></b>	
$\alpha_\gamma$	$-0.13 \pm 0.13 \pm 0.03$	$0.21 \pm 0.15 \pm 0.06$
	<b><math>-0.16 \pm 0.10 \pm 0.05</math></b>	


 PDG2022:  $BF = (1.75 \pm 0.15) \times 10^{-3}$ 

 First measurement on  $\alpha_\gamma$ 

 5.6 $\sigma$  deviation of BF

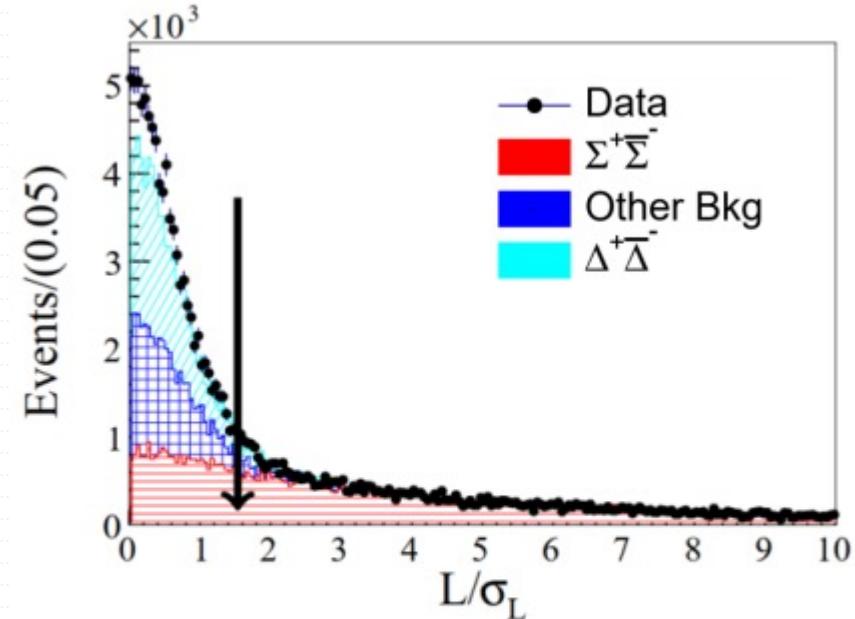
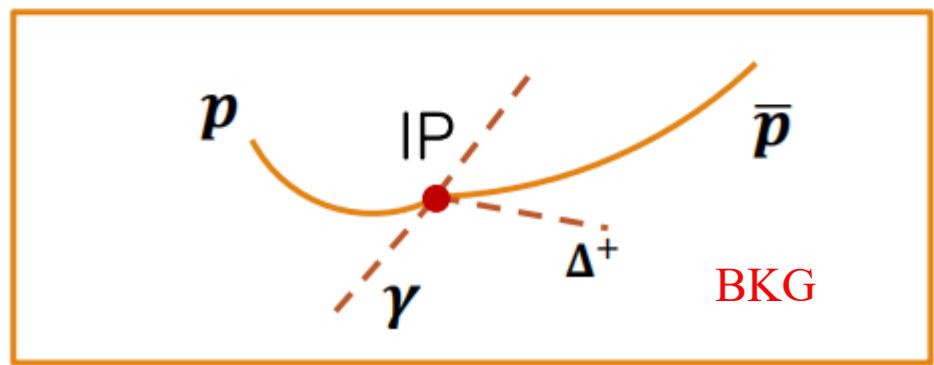
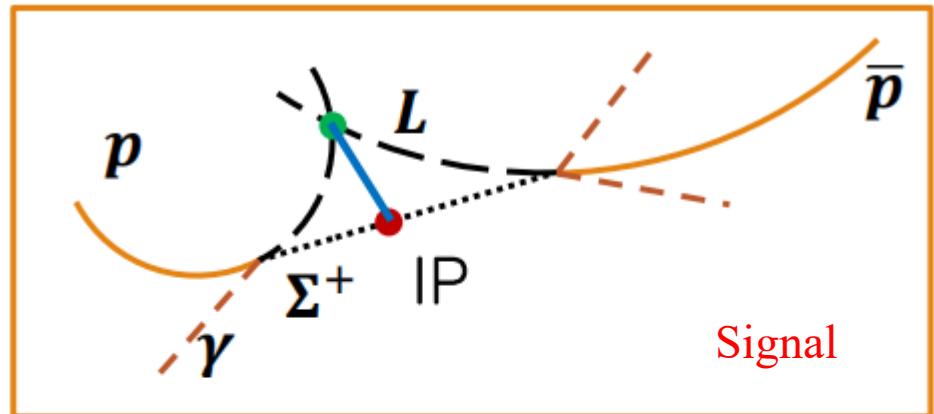
///  $\Sigma^+ \rightarrow p\gamma$

$J/\psi \rightarrow \Sigma^+\bar{\Sigma}^-$ ,  $\Sigma^+ \rightarrow p\gamma$ ,  $\bar{\Sigma}^- \rightarrow \bar{p}\pi^0 + c.c.$

## Analysis Method Highlights

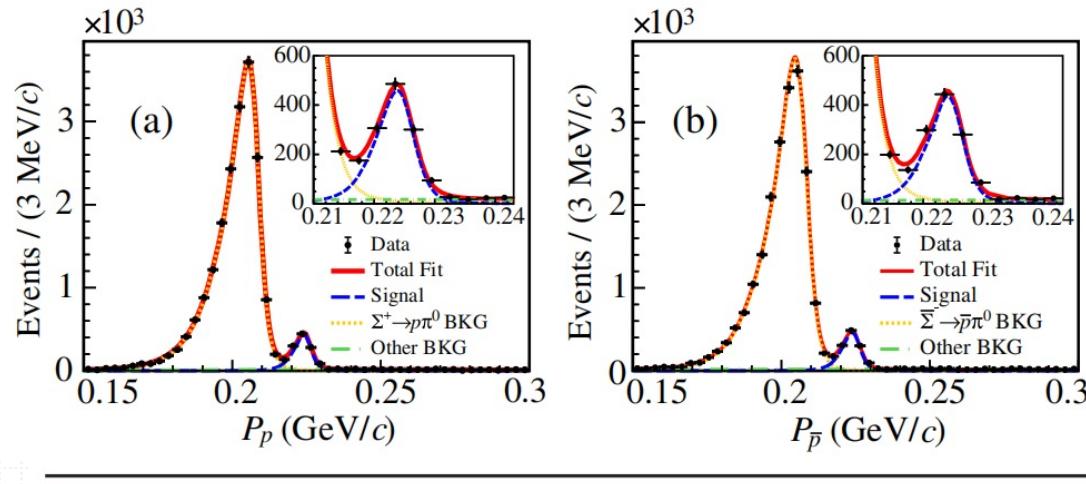
Phys. Rev. Lett. 130 (2023) 21, 211901

Utilize joint decay length to discriminate short-lived baryons from signals



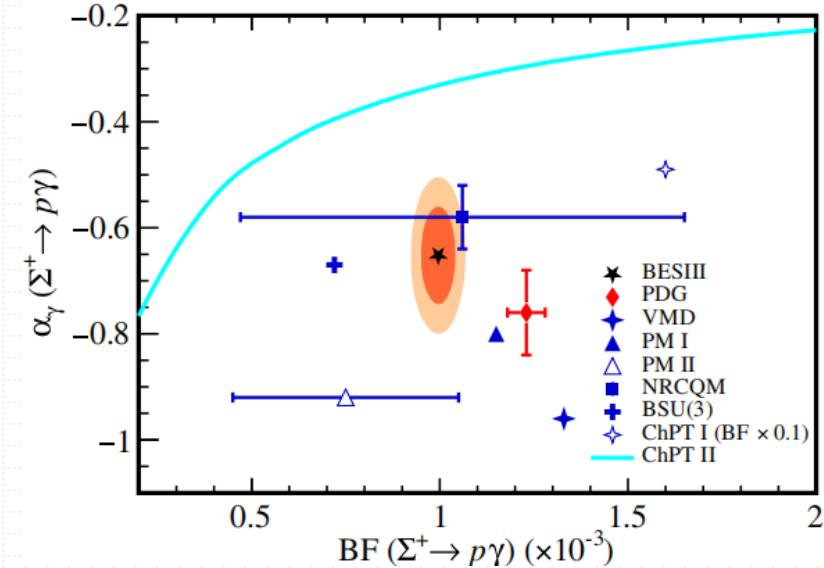
Signal efficiency > 78%  
Background efficiency < 7%

## Analysis results



Mode	$\Sigma^+ \rightarrow p\gamma$	$\bar{\Sigma}^- \rightarrow \bar{p}\gamma$
$N_{ST}^{\text{obs}}$	$2\,177\,771 \pm 2285$	$2\,509\,380 \pm 2301$
$\epsilon_{ST} (\%)$	$39.00 \pm 0.04$	$44.31 \pm 0.04$
$N_{DT}^{\text{obs}}$	$1189 \pm 38$	$1306 \pm 39$
$\epsilon_{DT} (\%)$	$21.16 \pm 0.03$	$23.20 \pm 0.03$
Individual BF ( $10^{-3}$ )	$1.005 \pm 0.032$	$0.993 \pm 0.030$
Simultaneous BF ( $10^{-3}$ )	$0.996 \pm 0.021 \pm 0.018$	
Individual $\alpha_\gamma$	$-0.587 \pm 0.082$	$0.710 \pm 0.076$
Simultaneous $\alpha_\gamma$	$-0.651 \pm 0.056 \pm 0.020$	

Phys. Rev. Lett. **130** (2023) 21, 211901



Significantly improved accuracy

- BF: 78%
- $\alpha_\gamma$ : 34%

PDG:  $\text{BF} = (1.23 \pm 0.05) \times 10^{-3}$

$4.2\sigma$  deviation

# /// Ongoing analysis

In the final internal review stage, the results will be released very soon!

$\Xi^0 \rightarrow \Lambda\gamma$		
Experiment	BF( $10^{-3}$ )	$\alpha_\gamma$
BESIII	$xxx \pm 0.066 \pm 0.054$	$xxx \pm 0.062 \pm 0.019$
PDG	$1.17 \pm 0.07$	$-0.70 \pm 0.07$

$\Xi^0 \rightarrow \Sigma^0\gamma$		
Experiment	BF( $10^{-3}$ )	$\alpha_\gamma$
BESIII	$xxx \pm 0.21 \pm 12$	$xxx \pm 0.095 \pm 0.015$
PDG	$3.33 \pm 0.10$	$-0.69 \pm 0.06$

Competitive precision with PDG.

# Hyperon semi-leptonic decays

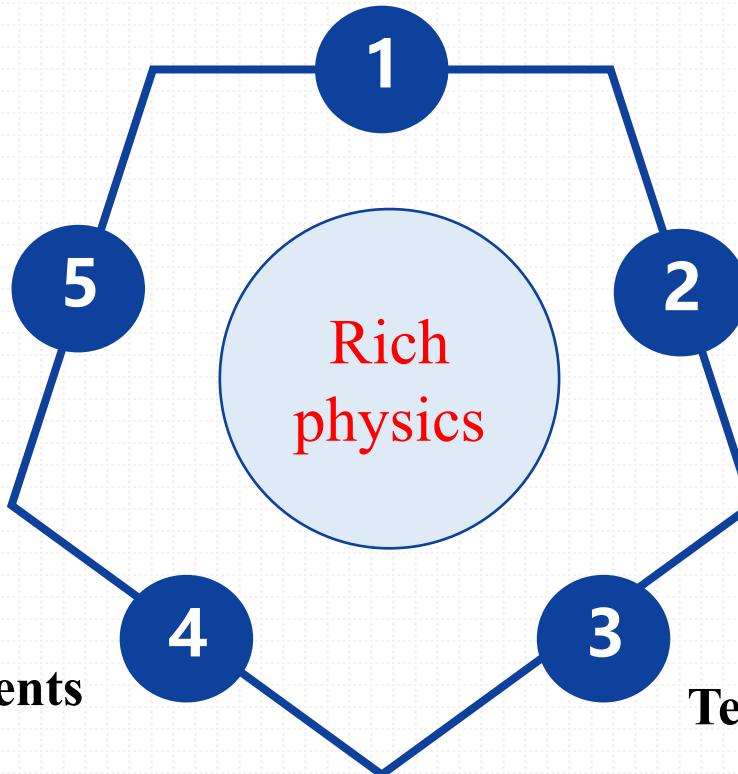
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# /// Physics Motivation

Measure the CKM matrix element  $|V_{us}|$

Search for rare/forbidden decays



Measure the form factors

Search for second-class currents

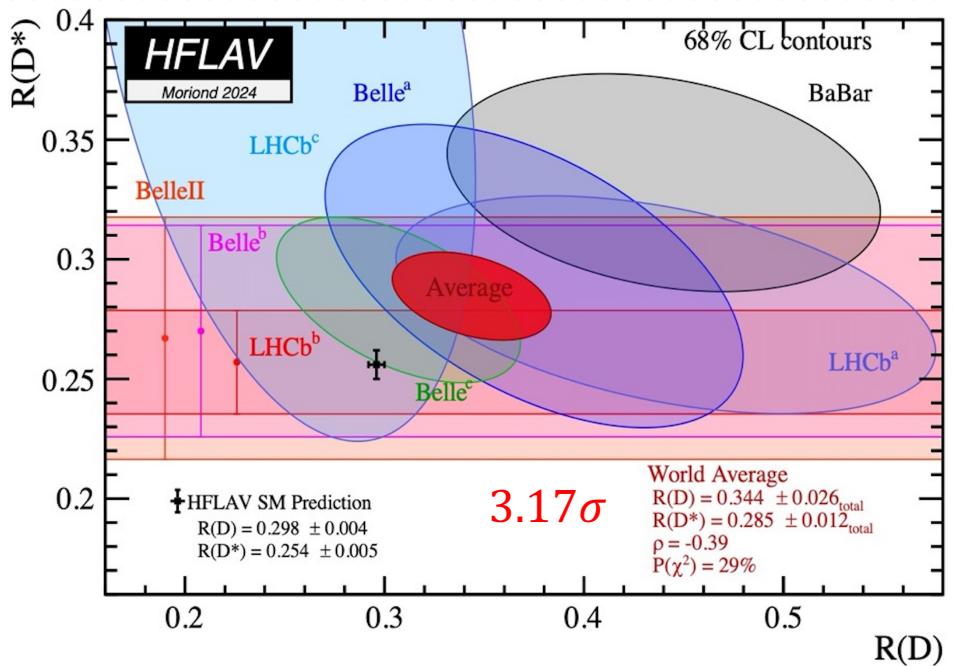
Test lepton flavor universality

# /// Test lepton flavor universality

$$R(D^{(*)}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)}\tau^-\bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)}l^-\bar{\nu}_l)}$$

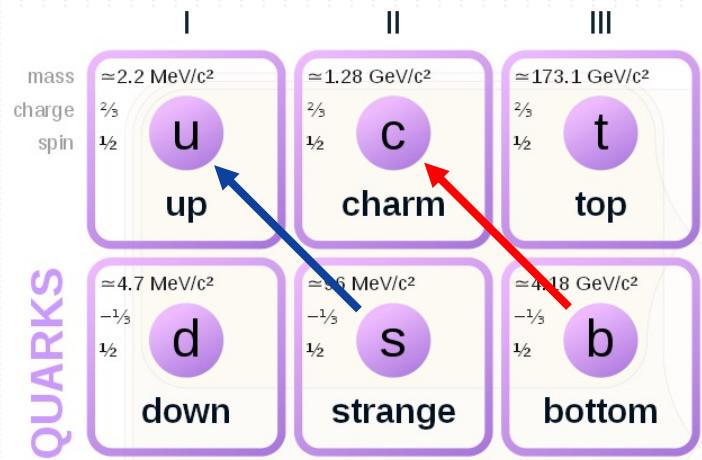
$$R^{\mu e} = \frac{\mathcal{B}(B \rightarrow b\mu^-\bar{\nu}_\mu)}{\mathcal{B}(B \rightarrow be^-\bar{\nu}_e)}$$

Average of  $R(D)$  and  $R(D^*)$  from HFLAV (2024)



Experiment vs. SM NLO for  $R^{\mu e}$  from hyperon semileptonic decays.

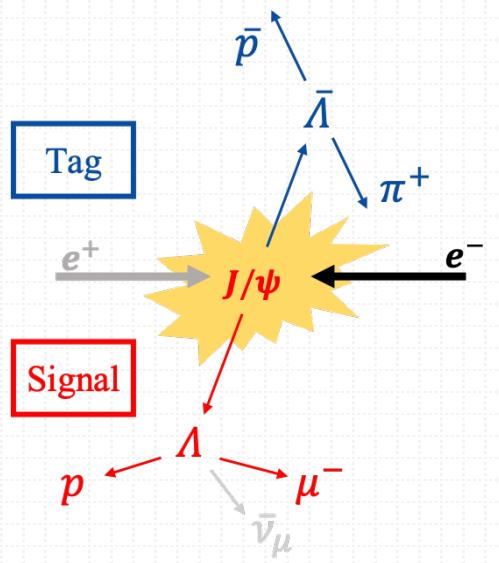
$R^{\mu e}$	$\Lambda \rightarrow pl^-\bar{\nu}_l$	$\Sigma^- \rightarrow nl^-\bar{\nu}_l$	$\Xi^0 \rightarrow \Sigma^+ l^-\bar{\nu}_l$	$\Xi^- \rightarrow \Lambda l^-\bar{\nu}_l$
Experiment	$0.189 \pm 0.041$	$0.442 \pm 0.039$	$0.0092 \pm 0.0014$	$0.6 \pm 0.5$
SM NLO	$0.153 \pm 0.008$	$0.444 \pm 0.022$	$0.0084 \pm 0.0004$	$0.275 \pm 0.014$



Phys. Rev. Lett. 114, 161802 (2015)

# Λ → $p\mu^-\bar{\nu}_\mu$

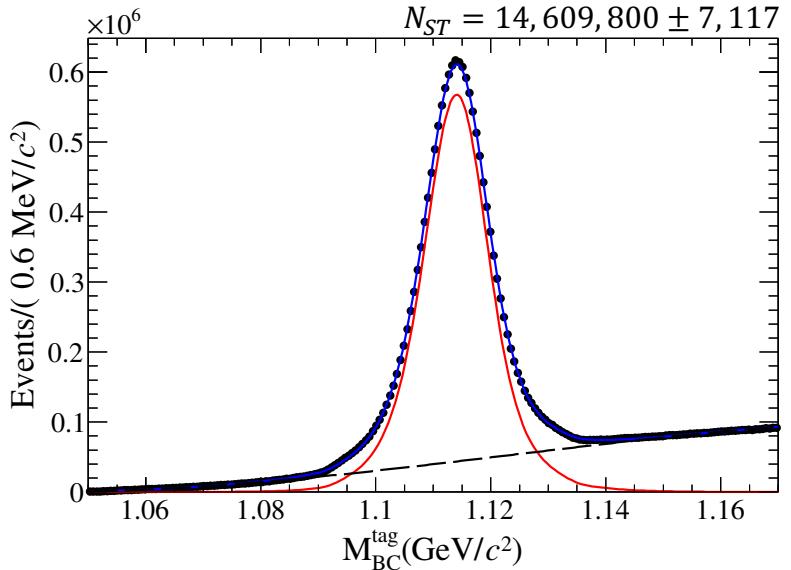
PRL 127, 121802 (2021)



First absolute BF measurement

$$\mathcal{B}(\Lambda \rightarrow p\mu^-\bar{\nu}_\mu) = (1.48 \pm 0.21 \pm 0.08) \times 10^{-4}$$

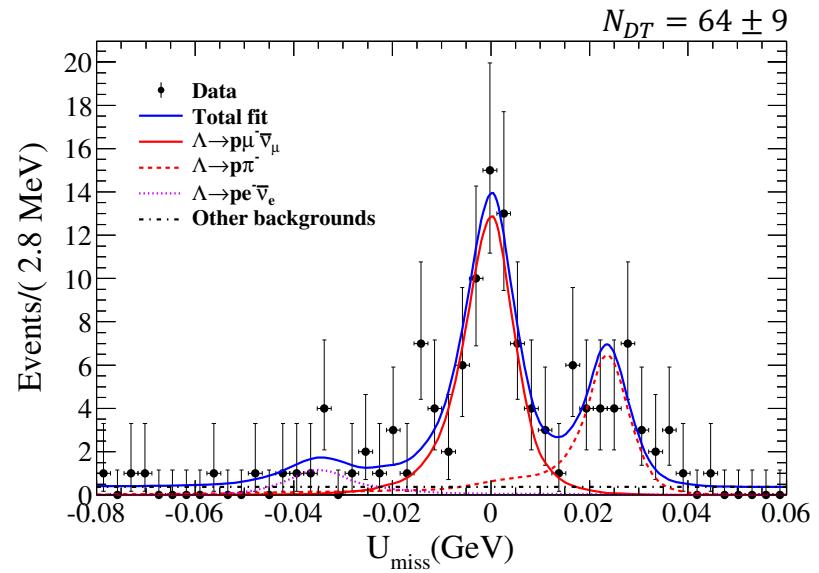
- ✓ Update measurement after about 50 years of break
- ✓ The first study at a collider experiment
- ✓ The most precise result to date



Test lepton flavor universality

$$R^{\mu e} = \frac{\mathcal{B}(\Lambda \rightarrow p\mu^-\bar{\nu}_\mu)}{\mathcal{B}(\Lambda \rightarrow pe^-\bar{\nu}_e)_{PDG}} = 0.178 \pm 0.028$$

Consistent  
with LFU



Search for CP violation

$$\mathcal{A}_{CP} = \frac{\mathcal{B}_{\Lambda \rightarrow p\mu^-\bar{\nu}_\mu} - \mathcal{B}_{\bar{\Lambda} \rightarrow \bar{p}\mu^+\nu_\mu}}{\mathcal{B}_{\Lambda \rightarrow p\mu^-\bar{\nu}_\mu} + \mathcal{B}_{\bar{\Lambda} \rightarrow \bar{p}\mu^+\nu_\mu}} = 0.02 \pm 0.14 \pm 0.02$$

Consistent  
with CP symmetry

# /// Search for second-class currents

- About second-class currents, previous nuclear  $\beta$  decay experiments gave contradictory conclusions.
  - ✓ Refs. [1-4] are in favor of the existence of the second-class currents
  - ✓ Refs. [5-8] reported the absence of second-class currents.
- In hyperon  $\beta$  decay, axial-vector form factor  $g_2$  is related to second-class currents, but the flavor-SU(3)-symmetry-breaking effects [9-10] or second-class currents [11] can cause a nonzero axial-vector form factor  $g_2$ , and some of the experiments suggest a large  $g_2$  [12].

[1] Phys. Rev. Lett. **35**, 1566 (1975).  
[2] Phys. Rev. Lett. **34**, 1533 (1975).  
[3] Phys. Rev. C **59**, 1113 (1999).  
[4] Phys. Rev. C **95**, 035501 (2017).

[5] Phys. Rev. Lett. **26**, 1127 (1971).  
[6] Phys. Rev. Lett. **32**, 314 (1974).  
[7] Eur. Phys. J. A **7**, 307 (2000).  
[8] Phys. Rev. C **84**, 055501 (2011).

[9] Phys. Rev. D **8**, 2963 (1973).  
[10] Phys. Rev. D **79**, 074508 (2009).  
[11] Annu. Rev. Nucl. Part. Sci. **53**, 39 (2003).  
[12] Phys. Rev. D **3**, 2638 (1971).

///  $\Sigma^+ \rightarrow \Lambda e^+ \nu_e$

- To search for the second-class currents, a unique observable ( $R$ ) was first proposed by S. Weinberg [1] in 1958.

$$R \equiv \frac{\Gamma(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)}{\Gamma(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)}$$

- If there are no second-class currents,  $R$  value should be just the phase-space ratio for these two decays, no matter flavor-SU(3)-symmetry-breaking effects exist or not, so any experimental deviation from this deduction would be decisive evidence for the existence of second-class currents.

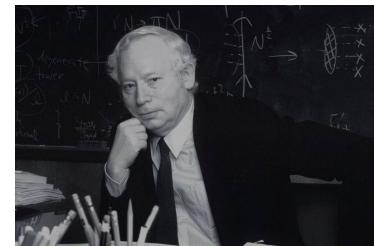
PHYSICAL REVIEW

VOLUME 112, NUMBER 4

NOVEMBER 15, 1958

## Charge Symmetry of Weak Interactions\*

STEVEN WEINBERG  
*Columbia University, New York, New York*  
 (Received June 25, 1958)



Phys. Rev. 112, 1375 (1958)

$$\Sigma^+ \rightarrow \Lambda e^+ \nu_e$$

- T. D. Lee and C. N. Yang calculate  $R$  based on no second-class currents.

$$R = 1.57$$

PHYSICAL REVIEW

VOLUME 119, NUMBER 4

AUGUST 15, 1960

Implications of the Intermediate Boson Basis of the Weak Interactions:  
Existence of a Quartet of Intermediate Bosons and Their  
Dual Isotopic Spin Transformation Properties

T. D. LEE

*Columbia University, New York, New York*

AND

C. N. YANG

*Institute for Advanced Study, Princeton, New Jersey*

(Received April 11, 1960)



Chen Ning Yang



Tsung-Dao Lee

Phys. Rev. 119, 1410 (1960)

# /// $\Sigma^+ \rightarrow \Lambda e^+ \nu_e$

$$R \equiv \frac{\Gamma(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)}{\Gamma(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)} = \frac{\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e) \cdot \tau_{\Sigma^+}}{\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \nu_e) \cdot \tau_{\Sigma^-}}$$

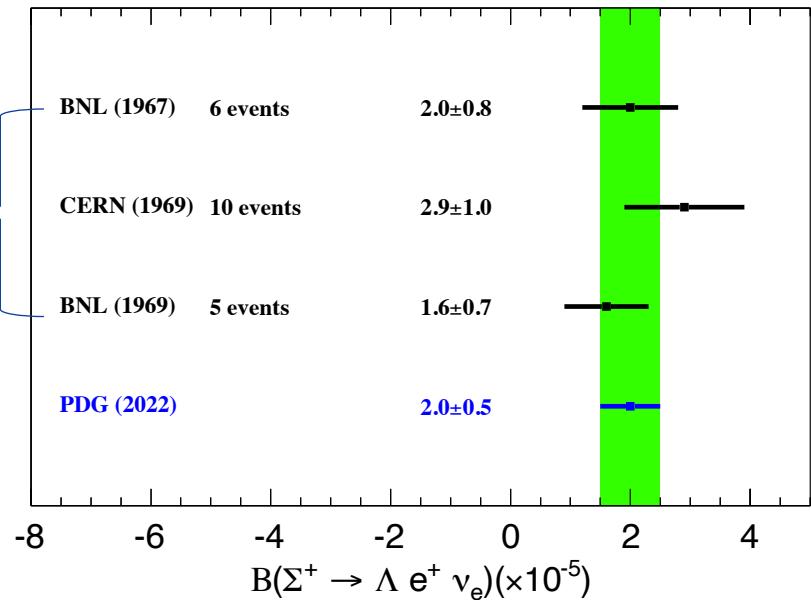
From PDG2022 :

$$\sigma[\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)] \sim 4.7\%$$

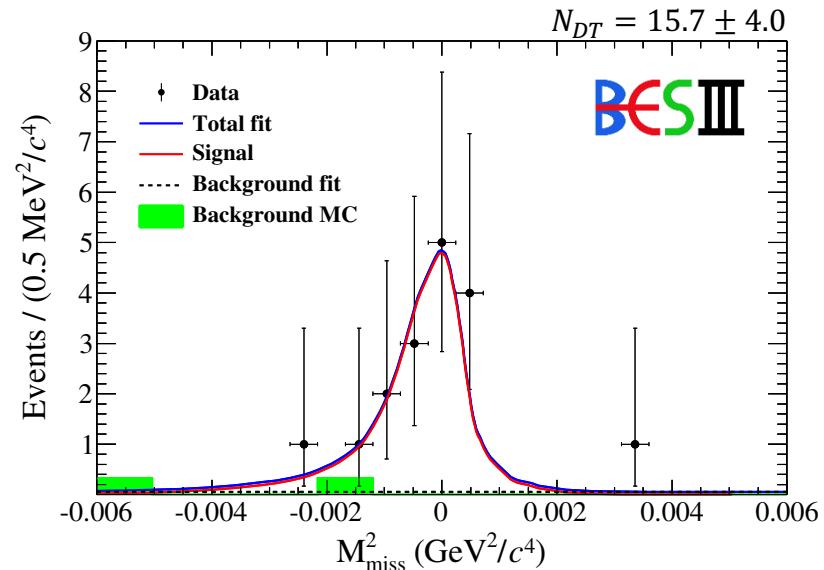
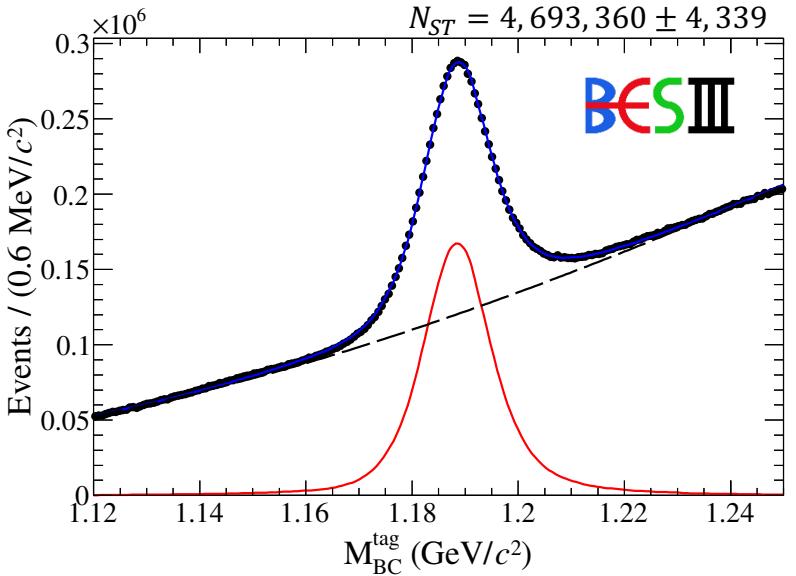
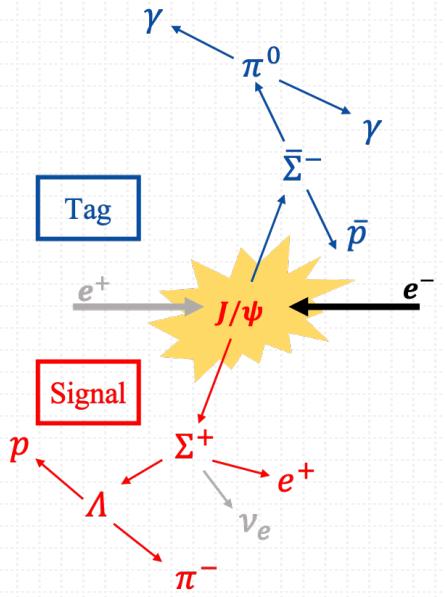
$$\sigma[\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)] \sim 25\%$$



1. Fixed-target experiments
2. Bubble chamber pictures
3. Indirect measurement



///  $\Sigma^+ \rightarrow \Lambda e^+ \bar{\nu}_e$



First direct measurement of absolute BF

$$\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \bar{\nu}_e) = (2.93 \pm 0.74 \pm 0.13) \times 10^{-5}$$

Search for second-class currents

$$R \equiv \frac{\Gamma(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)}{\Gamma(\Sigma^+ \rightarrow \Lambda e^+ \bar{\nu}_e)} = \frac{\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)_{PDG} \cdot \tau_{\Sigma^+ PDG}}{\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \bar{\nu}_e) \cdot \tau_{\Sigma^- PDG}} = 1.06 \pm 0.28$$

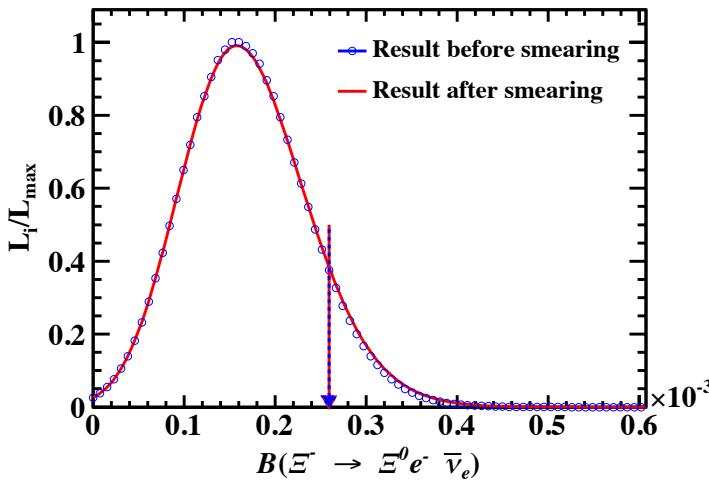
- ✓ Update measurement after about 50 years break
- ✓ The first study at a collider experiment
- ✓ The most precise result in a single experiment

NO evidence for second-class currents

# /// Rare/forbidden decays

Search for the hyperon semi-leptonic decay  $\Xi^- \rightarrow \Xi^0 e^- \bar{\nu}_e$

[BESIII, PRD 104, 072007 \(2021\)](#)

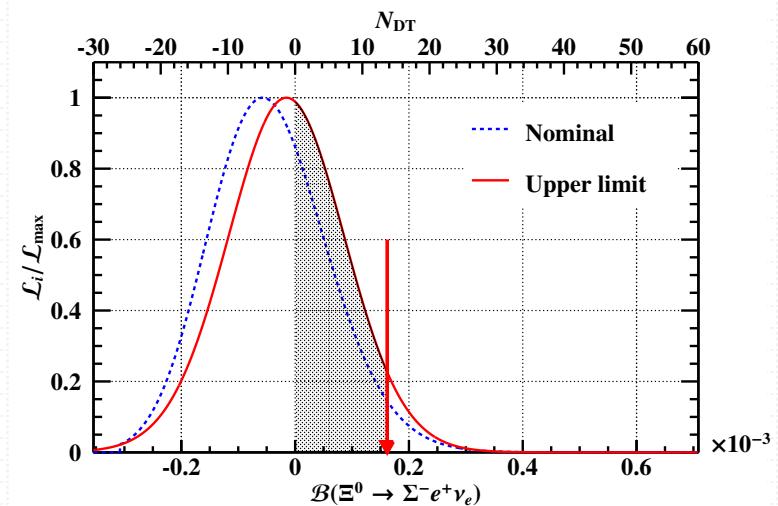


$$\mathcal{B}(\Xi^- \rightarrow \Xi^0 e^- \bar{\nu}_e) < 2.59 \times 10^{-4} \text{ @90\%CL}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Sigma^- e^+ \nu_e) < 1.6 \times 10^{-4} \text{ @90\%CL}$$

Search for hyperon  $\Delta S = \Delta Q$  violating decay  $\Xi^0 \rightarrow \Sigma^- e^+ \nu_e$

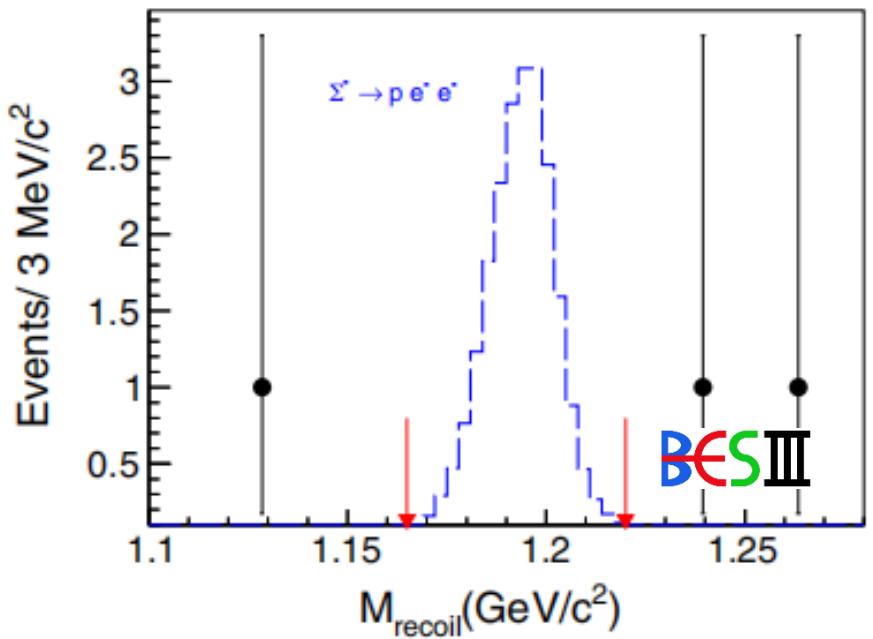
[BESIII, PRD 107, 012002 \(2023\)](#)



# /// Rare/forbidden decays

Search for the hyperon lepton number violating decay  $\Sigma^- \rightarrow p e^- e^-$

PHYS. REV. D 103, 052011 (2021)



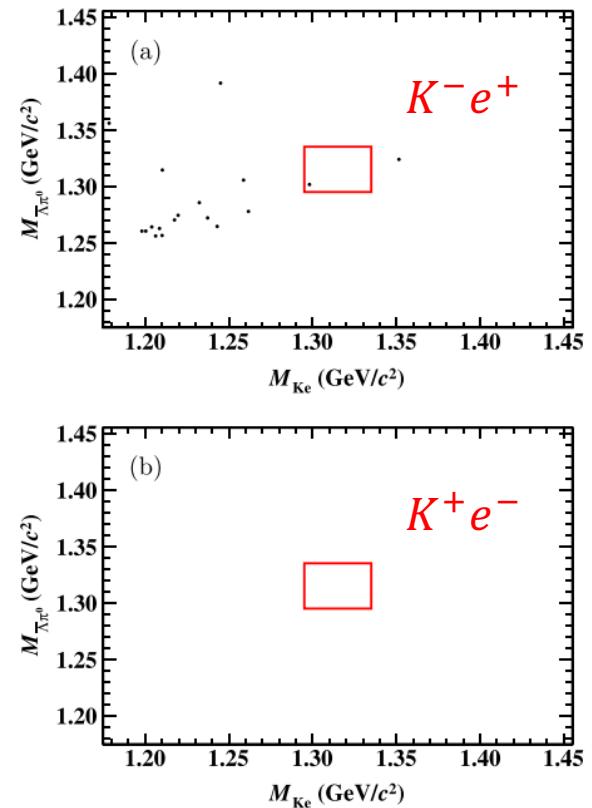
$$\mathcal{B}(\Sigma^- \rightarrow p e^- e^-) < 6.7 \times 10^{-5} \text{ @90\%CL}$$

$$\mathcal{B}(\Xi^0 \rightarrow K^- e^+) < 3.6 \times 10^{-6} \text{ @90\%CL}$$

$$\mathcal{B}(\Xi^0 \rightarrow K^+ e^-) < 1.9 \times 10^{-6} \text{ @90\%CL}$$

Search for hyperon baryon and lepton number violating decay  $\Xi^0 \rightarrow K e$

PHYS. REV. D 108, 012006 (2023)



# /// Ongoing analysis

$$g_{av} \equiv \frac{g_1(0)}{f_1(0)}, g_w \equiv \frac{f_2(0)}{f_1(0)}$$

$|V_{us}|$

CERN [PLB37\(1971\)535](#)  $0.89 \pm 0.61$



Experiment	BF( $10^{-4}$ )	$g_{av}$	$g_w$
BESIII	$xxx \pm 0.22 \pm 0.15$	$xxx \pm 0.048 \pm 0.007$	$xxx \pm 0.35 \pm 0.14$
PDG	$8.34 \pm 0.14$	$-0.718 \pm 0.015$	

CERN [PLB43\(1973\)237](#)  $0.80 \pm 0.90$

$g_w$

CERN [Z.Phys.C21\(1983\)1](#)  $1.32 \pm 0.81$

Very large  
uncertainties



Experiment	BF( $10^{-4}$ )	$g_{av}$
BESIII	$xxx \pm 0.40 \pm 0.10$	$xxx \pm 0.068 \pm 0.019$
PDG	$5.63 \pm 0.31$	$-0.25 \pm 0.05$

Fermilab [PRD41\(1990\)780](#)  $0.15 \pm 0.30$



Experiment	BF( $10^{-3}$ )
BESIII	$xxx \pm 1.3(stat)$
PDG	$5.6 \pm 2.8$

First observation

# Hyperon nonleptonic decays

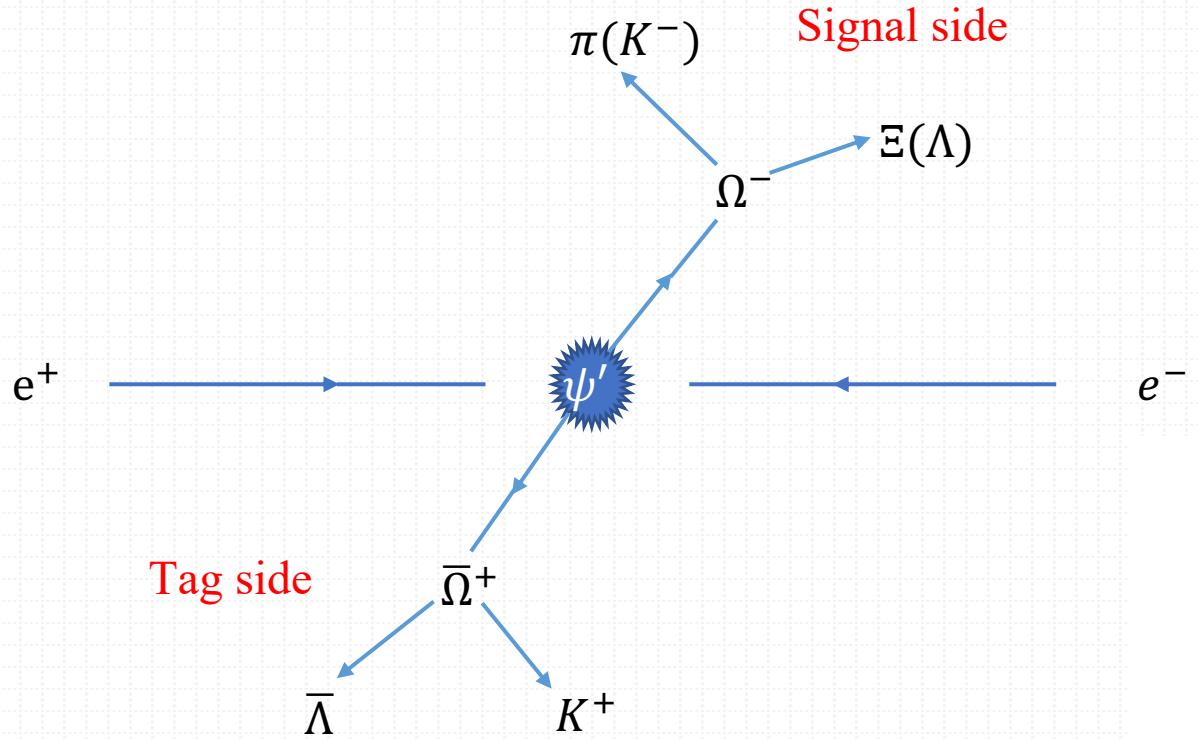
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# Physics Motivation

- Dominant decay models of the hyperons, many studies will benefit from precise measurements of BFs of the hyperon nonleptonic decays.
- All the previous results of the hyperon nonleptonic decays are relative BFs, no absolute BFs are measured.

# /// Absolute BF measurement of the $\Omega^-$ and test of the $\Delta I = 1/2$ rule



Partial reconstruction to improve the efficiencies, only a  $\pi^-$ , a  $\pi^0$  and a  $K^-$  in the signal side for the decay channels  $\Omega^- \rightarrow \Xi^0\pi^-$ ,  $\Omega^- \rightarrow \Xi^-\pi^0$ , and  $\Omega^- \rightarrow \Lambda K^-$ , respectively.

BFs	$\mathcal{B}_{\Omega^- \rightarrow \Xi^0\pi^-}$	$\mathcal{B}_{\Omega^- \rightarrow \Xi^-\pi^0}$	$\mathcal{B}_{\Omega^- \rightarrow \Lambda K^-}$
This work	$25.03 \pm 0.44 \pm 0.53$	$8.43 \pm 0.52 \pm 0.28$	$66.3 \pm 0.8 \pm 2.0$
PDG	$23.6 \pm 0.7$	$8.6 \pm 0.4$	$67.8 \pm 0.7$

Phys. Rev. D 108 (2023) 9, L091101

If  $\Delta I=1/2$  rule is valid in  $\Omega^-$  decay, the BF ratio between two decay channels  $\Omega^- \rightarrow \Xi^0\pi^-$ ,  $\Omega^- \rightarrow \Xi^-\pi^0$  should be 2. This ratio in PDG is  $2.74 \pm 0.15$ , inconsistent with the prediction of the  $\Delta I=1/2$  rule.

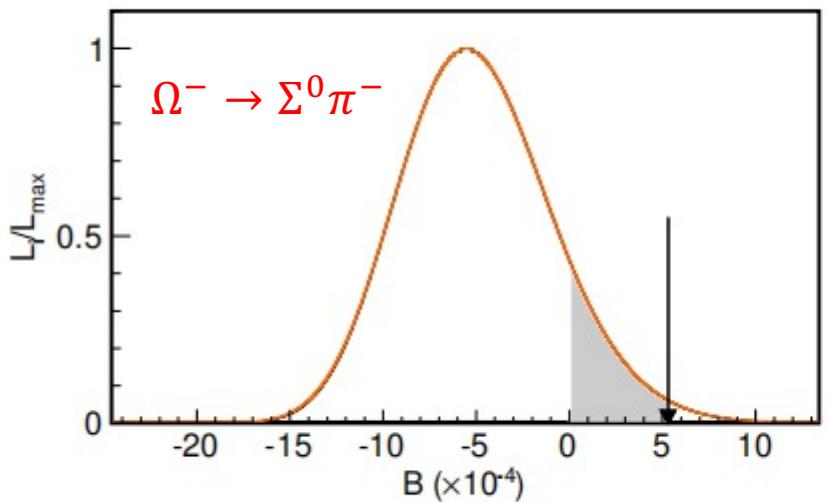
The result was only measured by one experiment, and therefore, received some skepticism!

Our result:  $R = 2.97 \pm 0.19 \pm 0.11$ , consistent with the PDG value, confirms the  $\Delta I=1/2$  rule is not suitable for describing the decays of the  $\Omega^-$  hyperon.

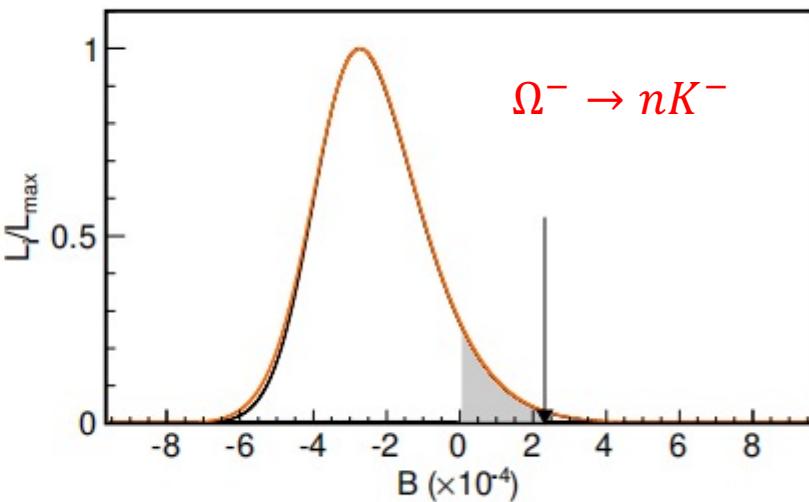
# /// Search for $\Delta S = 2$ $\Omega^-$ nonleptonic

PHYS. REV. D 108, 055012 (2023)

In the SM,  $\Delta S = 2$  nonleptonic hyperon decays are highly suppressed, however, there are new physics models that can enhance the BF of such decays, the  $\Delta S = 2$  nonleptonic hyperon decays could be used as probes for new physics.



(a)



(b)

$$\mathcal{B}(\Omega^- \rightarrow \Sigma^0 \pi^-) < 5.4 \times 10^{-4} \text{ @90%CL}$$

$$\mathcal{B}(\Omega^- \rightarrow n K^-) < 2.4 \times 10^{-4} \text{ @90%CL}$$

JHEP 05 (2024) 141

# /// Ongoing analysis

$\Sigma^+ \rightarrow p\pi^0$		$\Sigma^+ \rightarrow n\pi^+$	
Experiment	BF(%)	Experiment	BF(%)
BESIII	$xxx \pm 0.06 \pm 0.16$	BESIII	$xxx \pm 0.06 \pm 0.12$
PDG	$51.57 \pm 0.30$	PDG	$48.31 \pm 0.30$

# Summary

P A R T . 0 5

强子物理论坛

# Summary

- ✓ BESIII has made fruitful achievements in the studies of hyperon absolute decay BFs:
  - ✓ Hyperon weak radiative decays
  - ✓ Hyperon semi-leptonic decays
  - ✓ Hyperon nonleptonic decays
- ✓ More exciting hyperon results are expected in the next several years.

**THANKS!**

# Backup

# /// Measure the CKM matrix element $|V_{us}|$

In the SM: First-row unitarity relation

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

$2.2\sigma$  tension  
A hint of new physics?

PDG 2022: Independent measurements

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.99848 \pm 0.00070$$



$|V_{ub}|$ : Small ( $|V_{ub}|^2 \cong 1.7 \times 10^{-5}$ ) → The effect could be ignored in current precision



$|V_{ud}|$ : Most precise; results from different decays are consistent at  $\mathcal{O}(10^{-4})$  → Precise and reliable



$|V_{us}|$ :  $\sigma(|V_{us}|) = 2.6 \times \sigma(|V_{ud}|)$ ; inconsistency between results from different decays



Most precise

Kaon:  $2.2\sigma$  tension from CKM unitarity

$$|V_{us}| = 0.2243 \pm 0.0008$$

PDG 2022

Second most precise

Tau:  $3.6\sigma$  deviation from CKM unitarity

$$|V_{us}| = 0.2207 \pm 0.0014$$

HFLAV 2022

$2.2\sigma$  tension

Largest uncertainty

Hyperon: consistent with CKM unitarity

$$|V_{us}| = 0.2250 \pm 0.0027$$

Dominated by the  $\Lambda \rightarrow p e^- \bar{\nu}_e$

# /// Measure the CKM matrix element $|V_{us}|$

Decay width of  $\Lambda \rightarrow p e^- \bar{\nu}_e$  in the SM

$$\Gamma_{\text{SM}} = \frac{\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}}{\tau_\Lambda} = \frac{G_F^2 |V_{us}|^2 f_1(0)^2 \Delta^5}{60\pi^3} \left[ \left(1 - \frac{3}{2}\delta + \frac{6}{7}\delta^2\right) + \frac{4}{7}\delta^2 g_w^2 \right.$$

[PRD 70, 114036 \(2004\)](#)

$$\left. + \left(3 - \frac{9}{2}\delta + \frac{12}{7}\delta^2\right) g_{av}^2 + \frac{12}{7}\delta^2 g_{av2}^2 + \frac{6}{7}\delta^2 g_w + (-4\delta + 6\delta^2) g_{av} g_{av2} \right]$$

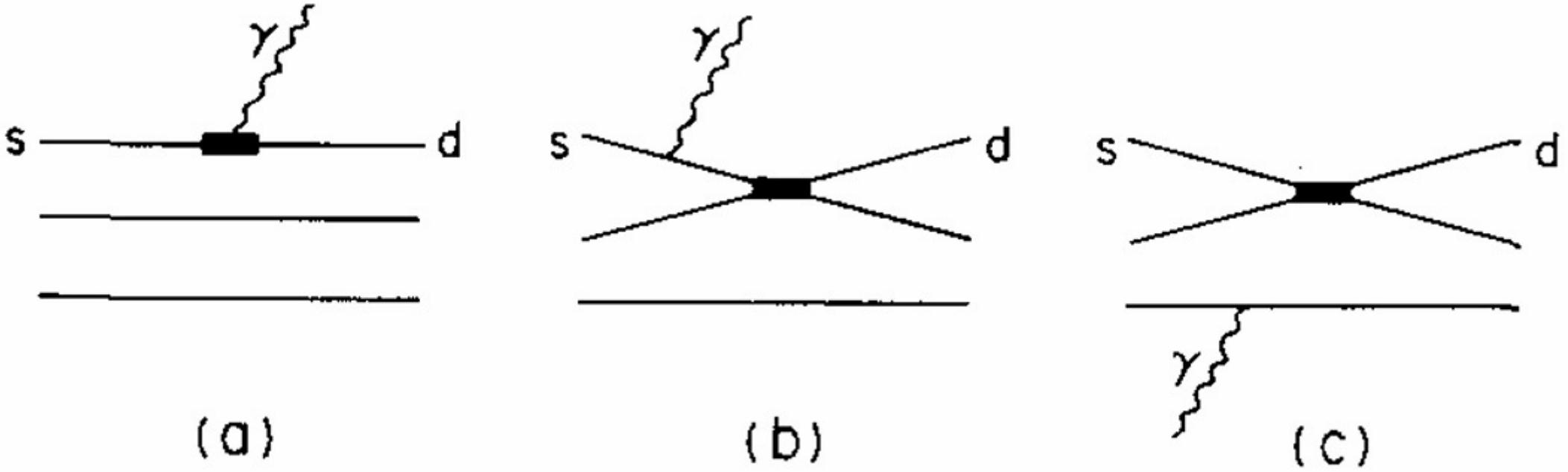
$$\Delta \equiv M_\Lambda - M_p$$

$$\delta \equiv \frac{M_\Lambda - M_p}{M_\Lambda}$$

➤ Extracting  $|V_{us}|$ , requires  $\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}$ ,  $f_1(0)$ ,  $g_{av} \equiv \frac{g_1(0)}{f_1(0)}$ ,  $g_w \equiv \frac{f_2(0)}{f_1(0)}$ , and  $g_{av2} \equiv \frac{g_2(0)}{f_1(0)}$ ,

□  $f_1(0)$ : From LQCD

□  $\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}$ ,  $g_{av}$ ,  $g_w$ , and  $g_{av2}$ : From experimental measurement



# /// Physics Motivation

Fixed target experiments govern the results in 1965-2010 (~23 papers from over 5 experiments)

## $\Sigma^+ \rightarrow p\gamma$

时间	实验名或实验方案	分支比 ( $\times 10^{-3}$ )	$\alpha_\gamma$
2023	BESIII	$0.996 \pm 0.021 \pm 0.018$	$-0.652 \pm 0.056 \pm 0.020$
1995	E761	$1.20 \pm 0.08$	-
1992	SPEC	-	$-0.720 \pm 0.086$
1989	CNTR	$1.45 \pm 0.31$	-
1987	CNTR	$1.23 \pm 0.20$	-
1985	CNTR	$1.27 \pm 0.18$	-
1980	HBC	$1.09 \pm 0.20$	$-0.53 \pm 0.36$
1969	HBC	$1.1 \pm 0.2$	-
1969	HBC	$1.42 \pm 0.26$	$-1.03 \pm 0.52$
1965	HBC	$1.9 \pm 0.4$	-

## $\Lambda \rightarrow n\gamma$

时间	实验名或实验方案	分支比 ( $\times 10^{-3}$ )	$\alpha_\gamma$
2022	BESIII	$0.846 \pm 0.039 \pm 0.052$	$-0.160 \pm 0.101 \pm 0.046$
1994	E761	$1.75 \pm 0.15$	-
1992	SPEC	$1.78 \pm 0.24$	-

$\Xi^0 \rightarrow \Lambda\gamma$			
时间	实验名或实验方案	分支比 ( $\times 10^{-3}$ )	$\alpha_\gamma$
2010	NA48	-	$-0.704 \pm 0.064$
2004	NA48	$1.17 \pm 0.09$	$-0.78 \pm 0.18$
2000	NA48	$1.91 \pm 0.34$	-
1990	SPEC	$1.06 \pm 0.18$	$-0.43 \pm 0.44$

$\Xi^0 \rightarrow \Sigma^0\gamma$			
时间	实验名或实验方案	分支比 ( $\times 10^{-3}$ )	$\alpha_\gamma$
2010	NA48	-	$-0.729 \pm 0.076$
2001	KTEV	$3.34 \pm 0.09$	$-0.63 \pm 0.09$
2000	NA48	$3.16 \pm 0.76$	-
1989	SPEC	$3.56 \pm 0.42$	$0.20 \pm 0.32$

$\Xi^- \rightarrow \Sigma^-\gamma$			
时间	实验名或实验方案	分支比 ( $\times 10^{-3}$ )	$\alpha_\gamma$
1994	E761	$0.122 \pm 0.023$	-
1987	SPEC	$0.227 \pm 0.102$	-

$\Omega^- \rightarrow \Xi^-\gamma$			
时间	实验名或实验方案	分支比 ( $\times 10^{-3}$ )	$\alpha_\gamma$
1994	E761	$<0.46$	-
1984	SPEC	$<0.22$	-
1979	SPEC	$<0.31$	-