



Neutrino CP Phase & New Physics

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vSTEP @ HIAS

李政道研究所

Tsung-Dao Lee Institute

- **CP Violation in the Precision Era**
- **Dirac CP Phase & New Physics**
 1. Non-Standard Interactions (NSI)
 2. Scalar NSI
 3. Dark NSI
 4. Non-Unitary Mixing (NUM)
 5. RG Running
- **Accelerator + μ DAR for Better CP Measurement**
 1. TNT2K
 2. μ THEIA

Georg G. Raffelt

Stars as Laboratories for Fundamental Physics

The Astrophysics of Neutrinos, Axions, and Other
Weakly Interacting Particles

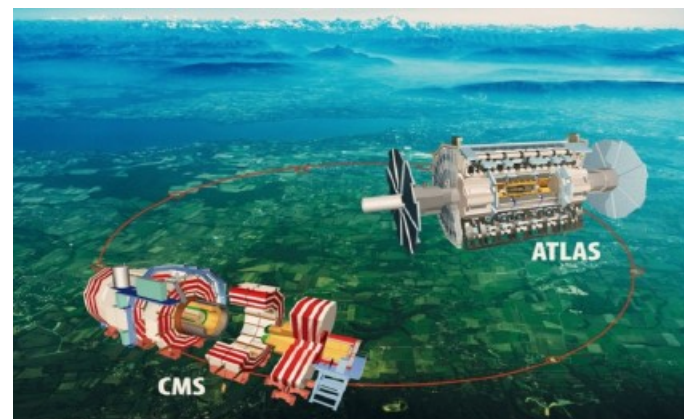
In the standard model, neutrinos have been assigned the most minimal properties compatible with experimental data: zero mass, zero charge, zero dipole moments, zero decay rate, zero almost everything.

Neutrino vs Higgs

- **Higgs boson** $\Rightarrow$ electroweak symmetry breaking & mass. $\sim O(100)\text{GeV}$
- **Chiral symmetry breaking** $\Rightarrow$ majority of mass.
- The world seems not affected by the tiny neutrino mass?
 - Neutrino mass $\Rightarrow$ Mixing
 - 3 Neutrino $\Rightarrow$ possible **CP violation**
 - CP violation $\Rightarrow$ **Leptogenesis**
 - $\Rightarrow$ **Matter-Antimatter Asymmetry**
 - There is something left in the Universe.
 - **EW Baryogenesis** is not enough.



Daya Bay @ **March 8, 2012**



LHC @ **July 4, 2012**

Seesaw & Leptogenesis

With decreasing temperature, heavy N decays to light SM particles.

$$N_k \rightarrow \begin{cases} \ell_j + \bar{\phi} \\ \bar{\ell}_j + \phi \end{cases}$$



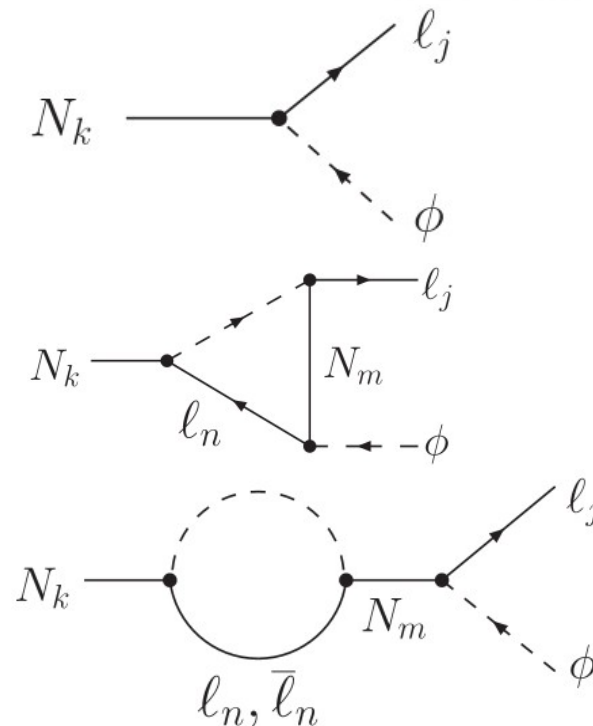
Matter-Antimatter Asymmetry

- Interference between tree & loop diagrams

$$\Gamma = \Gamma_{\text{tree}} + \Gamma_{\text{loop}}(+\delta_D, +\delta_M)$$

$$\bar{\Gamma} = \Gamma_{\text{tree}} + \Gamma_{\text{loop}}(-\delta_D, -\delta_M)$$

The matter-antimatter asymmetry needs Dirac/Majorana CP phases.



Yanagida



Fukugita

Current Status of ν Oscillation

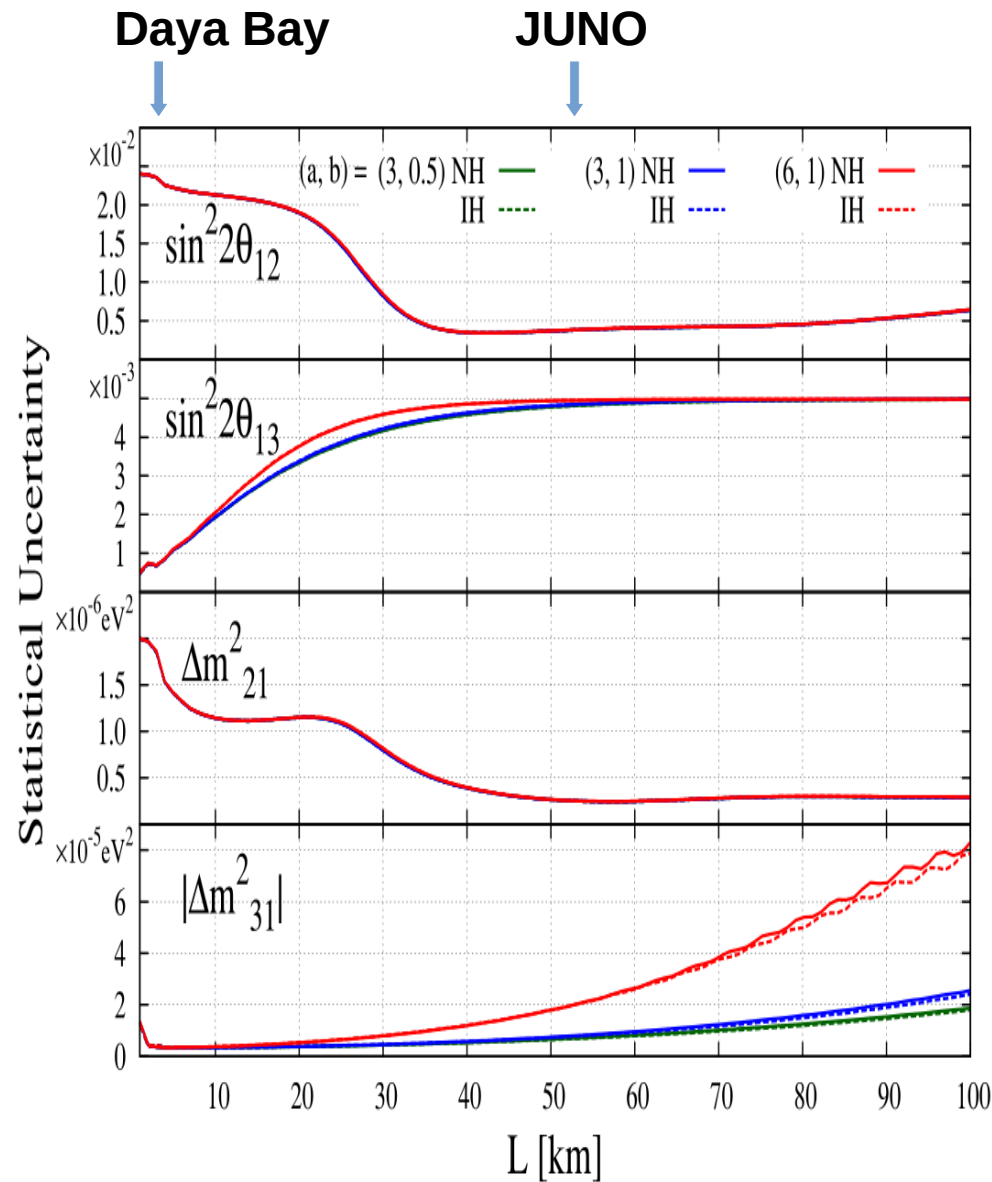
		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 7.0$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^\circ$	$33.45^{+0.77}_{-0.75}$	$31.27 \rightarrow 35.87$	$33.45^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.450^{+0.019}_{-0.016}$	$0.408 \rightarrow 0.603$	$0.570^{+0.016}_{-0.022}$	$0.410 \rightarrow 0.613$
	$\theta_{23}/^\circ$	$42.1^{+1.1}_{-0.9}$	$39.7 \rightarrow 50.9$	$49.0^{+0.9}_{-1.3}$	$39.8 \rightarrow 51.6$
	$\sin^2 \theta_{13}$	$0.02246^{+0.00062}_{-0.00062}$	$0.02060 \rightarrow 0.02435$	$0.02241^{+0.00074}_{-0.00062}$	$0.02055 \rightarrow 0.02457$
	$\theta_{13}/^\circ$	$8.62^{+0.12}_{-0.12}$	$8.25 \rightarrow 8.98$	$8.61^{+0.14}_{-0.12}$	$8.24 \rightarrow 9.02$
	$\delta_{CP}/^\circ$	230^{+36}_{-25}	$144 \rightarrow 350$	278^{+22}_{-30}	$194 \rightarrow 345$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.510^{+0.027}_{-0.027}$	$+2.430 \rightarrow +2.593$	$-2.490^{+0.026}_{-0.028}$	$-2.574 \rightarrow -2.410$

Gonzalez-Garcia, Maltoni & Schwetz [2111.03086]

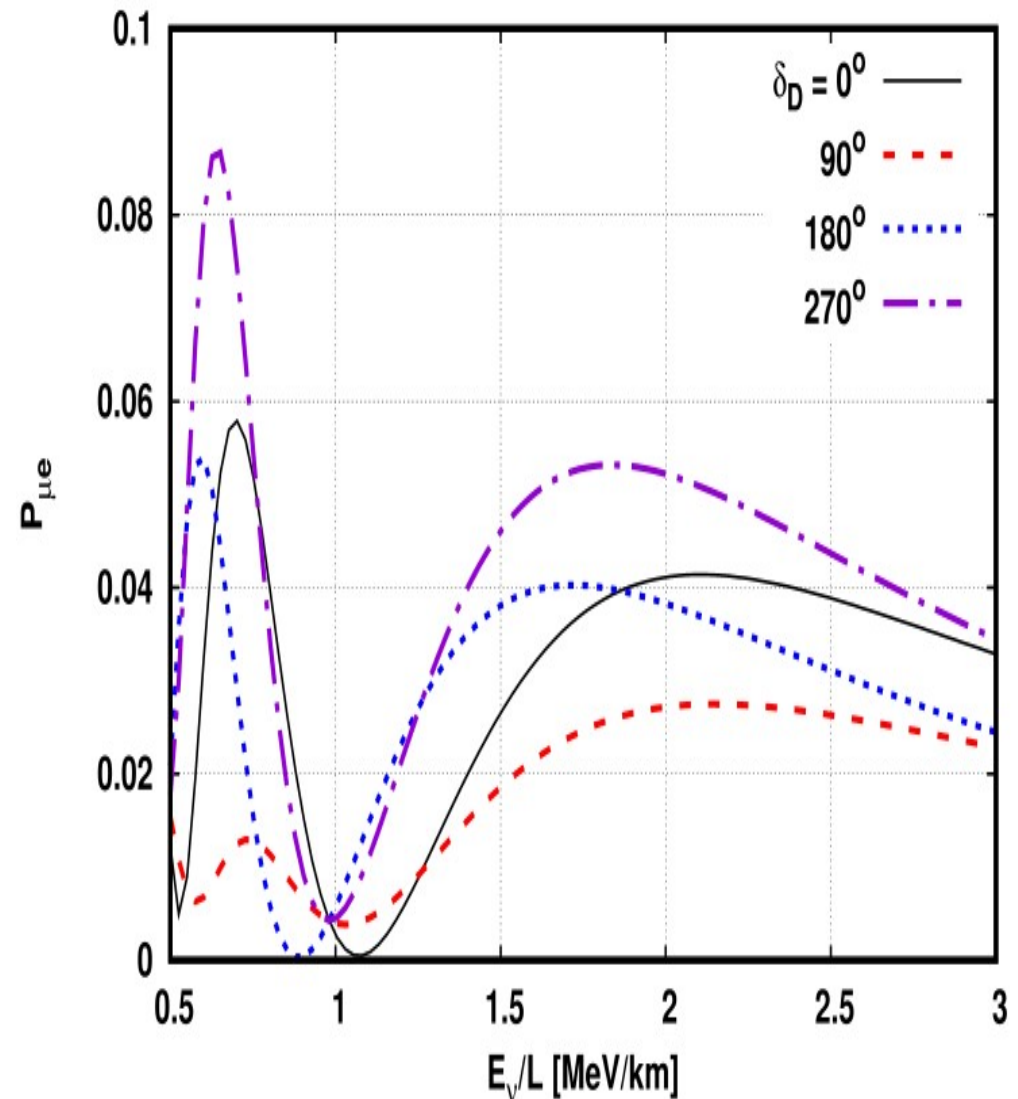
Daya Bay heralded a new era of precision measurement in 2012!

Kam-Biu Luk @ Neutrino 2022

Precision Era of ν Oscillation



SFG, Hagiwara, Okamura & Takaesu [1210.8141]



SFG & Smirnov [1607.08513]

Current Status of CP Measurement

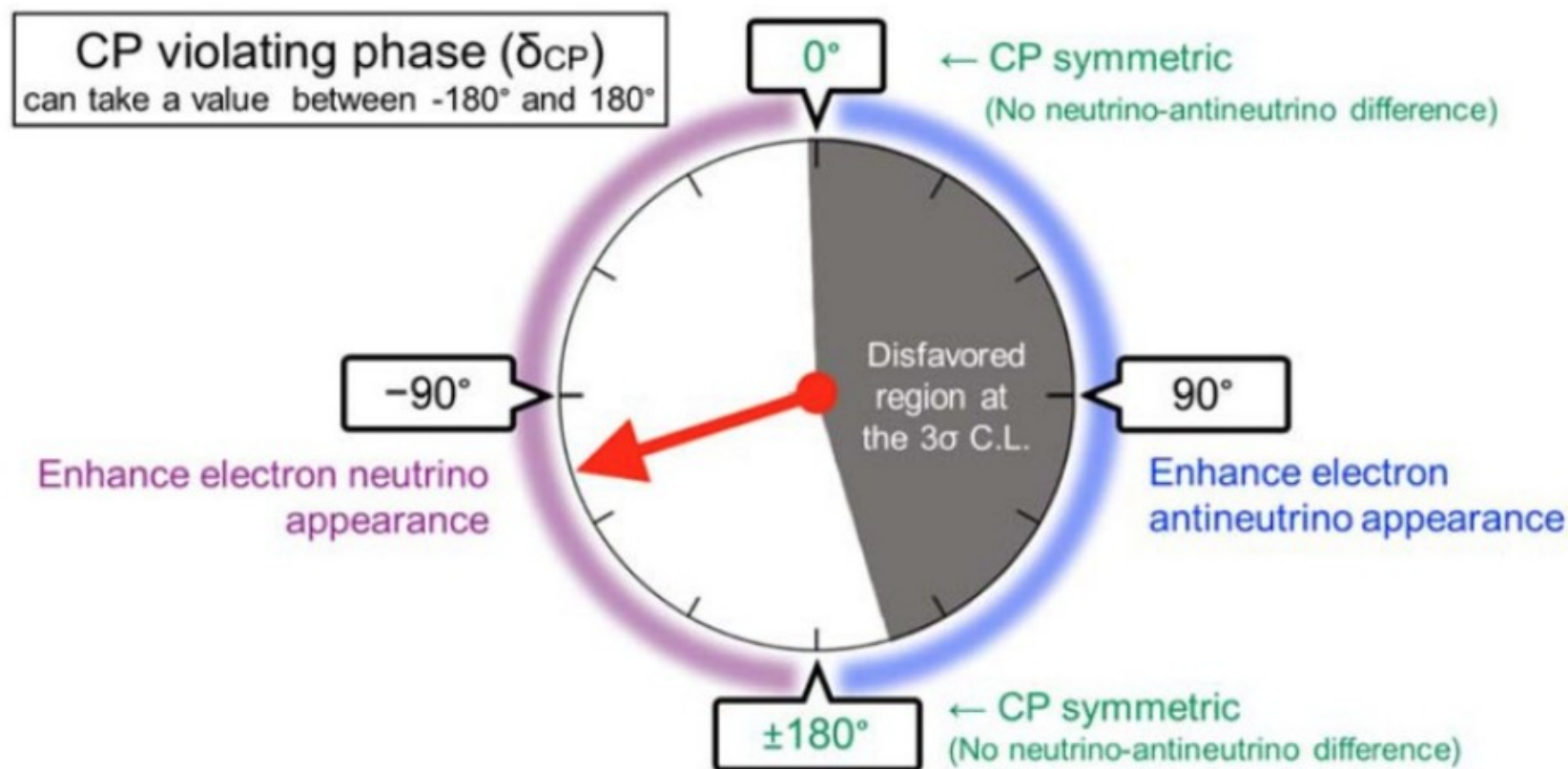
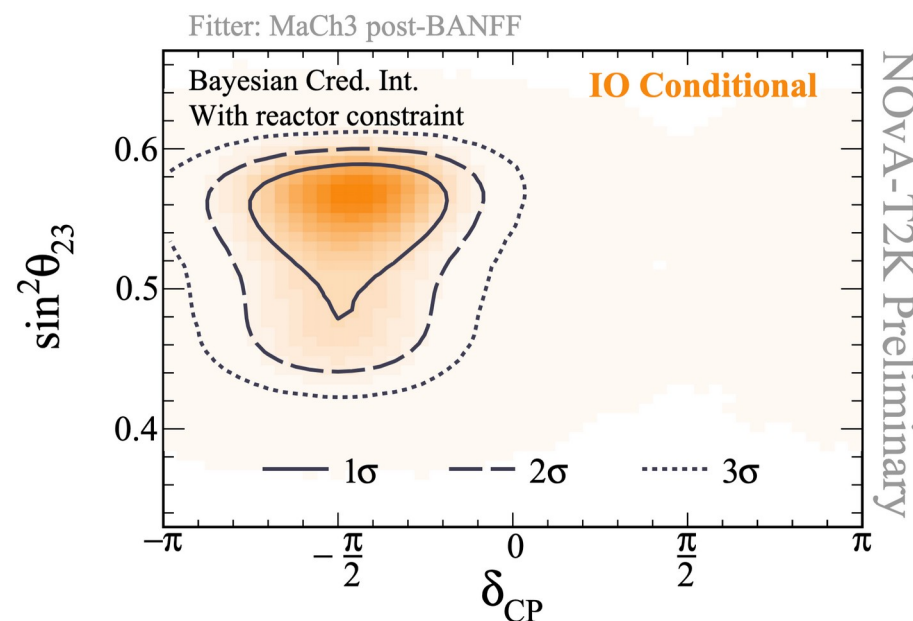
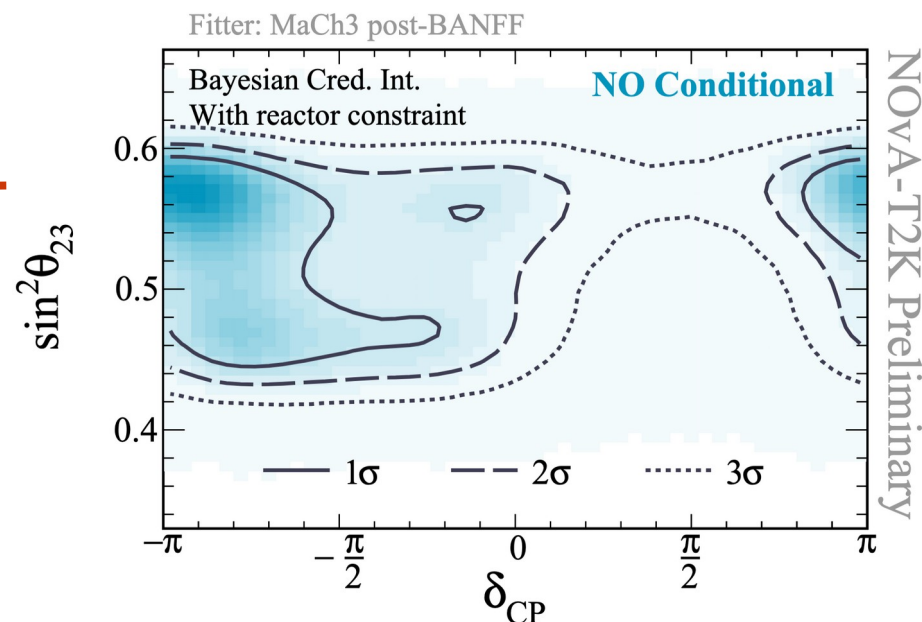
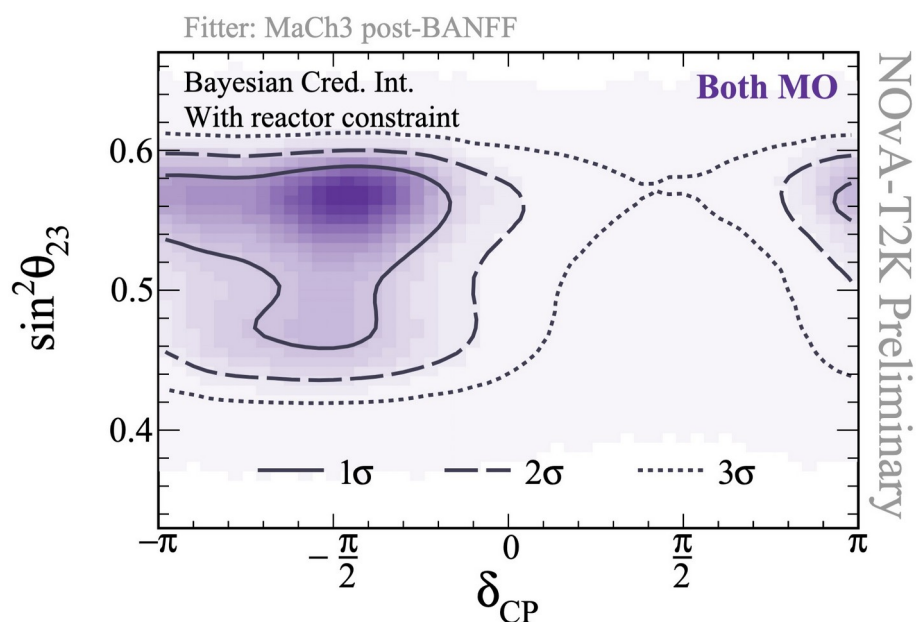


Fig.1 The arrow indicates the value most compatible with the data. The gray region is disfavored at 99.7% (3σ) confidence level. Nearly half of the possible values are excluded.

Nature vol. 580, pages 339-344(2020)

https://www.kek.jp/en/newsroom/attic/PR20200416_T2K_E.pdf

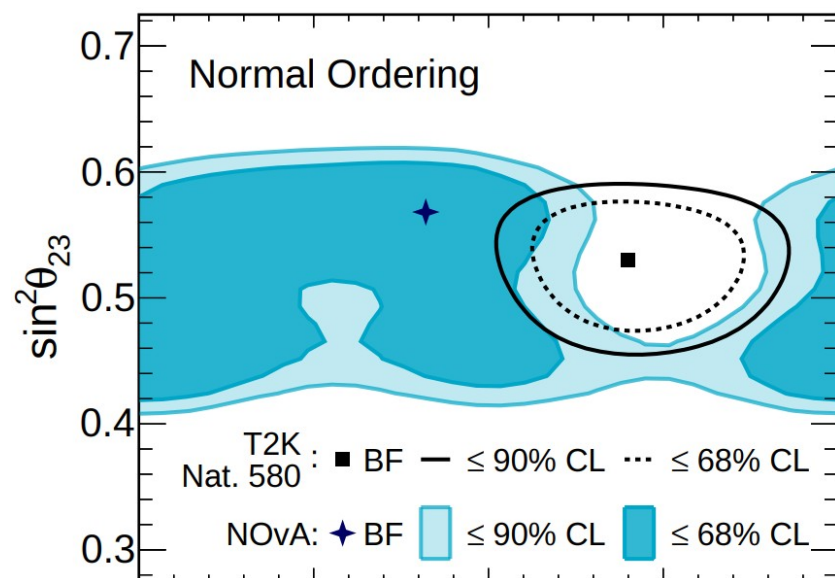
T2K+NOvA Joint Analysis



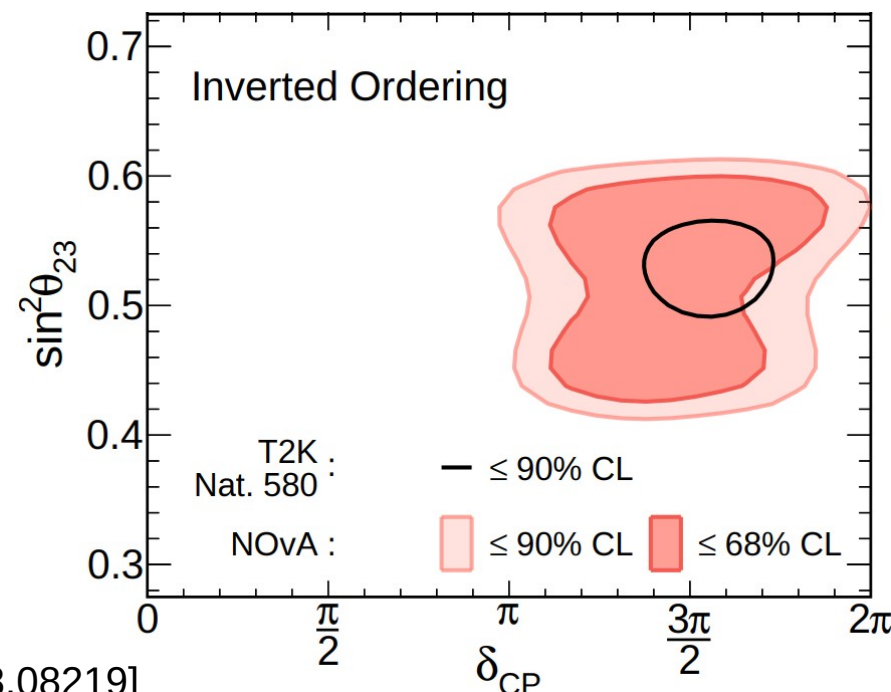
Zoya Vallari [On behalf of NOvA & T2K Collaborations], Feb/16, 2024
Joint Experimental-Theoretical Physics Seminar, Fermilab

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Tension between T2K & NOvA



NovA, Phys.Rev.D 106 (2022) 3, 032004 [arXiv:2108.08219]



- Non-Standard Interactions
- Non-Unitary Mixing
- Lorentz Violation
- Sterile Neutrinos

Denton, Gehrlein & Pestes [2008.01110]

Rahaman, Razzaque & Sankar [2201.03250]

Chatterjee & Palazzo [2005.10338]

1. Non-Standard Interaction (NSI)

$$\mathcal{H} \equiv \frac{1}{2\mathbf{E}_\nu} U \begin{pmatrix} 0 & & \\ & \Delta m_s^2 & \\ & & \Delta m_a^2 \end{pmatrix} U^\dagger + V_{cc} \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu}^* & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau}^* & \epsilon_{\mu\tau}^* & \epsilon_{\tau\tau} \end{pmatrix}$$

- Standard Interaction – V_{cc} (also V_{nc})

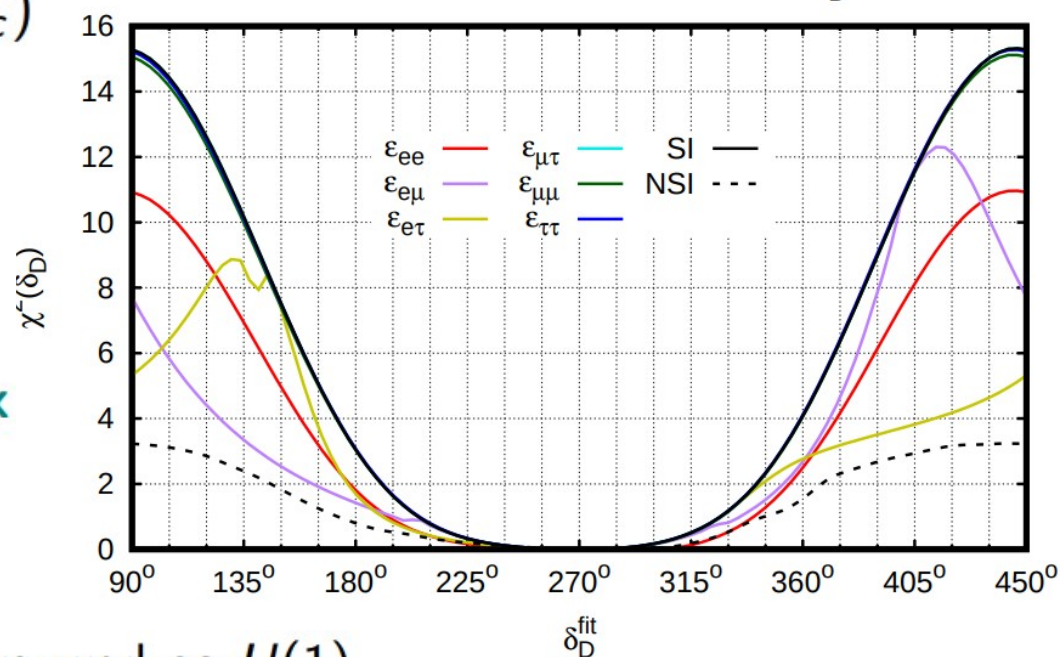
- Non-Standard Interaction – $\epsilon_{\alpha\beta}$

- Diagonal $\epsilon_{\alpha\alpha}$ are real
- Off-diagonal $\epsilon_{\alpha\neq\beta}$ are complex
- Both can fake CP

- Z' in LMA-Dark model with $L_\mu - L_\tau$ gauged as $U(1)$

- $M_{Z'} \sim \mathcal{O}(10)\text{MeV}$
- $g_{Z'} \sim 10^{-5}$

The effect of NSI on the CP sensitivity at T2K [$\delta_D^{\text{true}} = -90^\circ$]



2. Scalar NSI

- Vector NSI

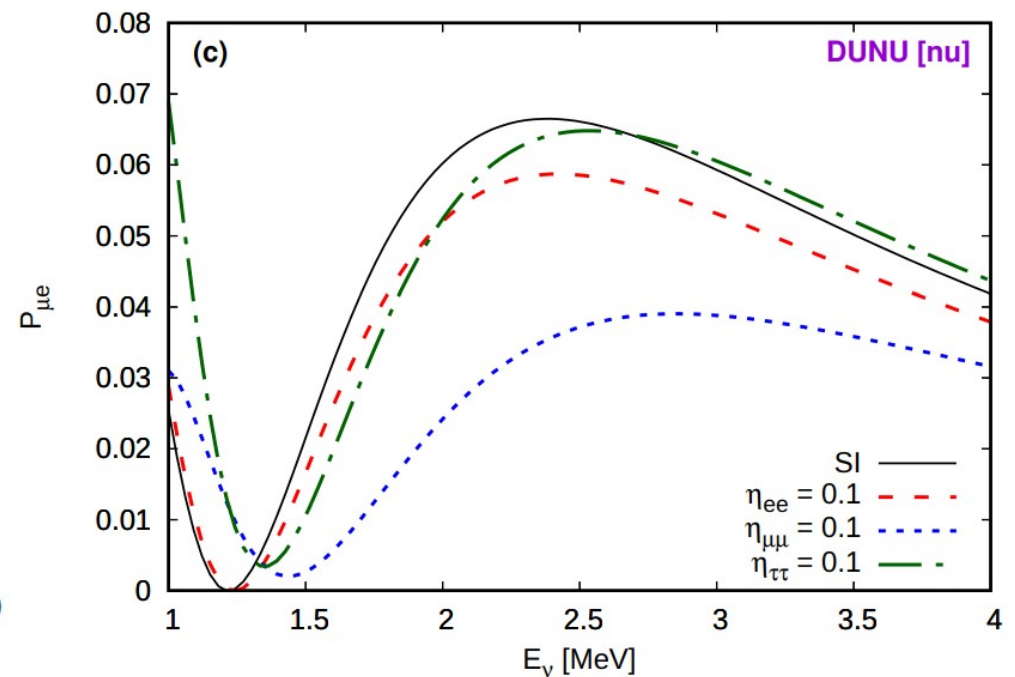
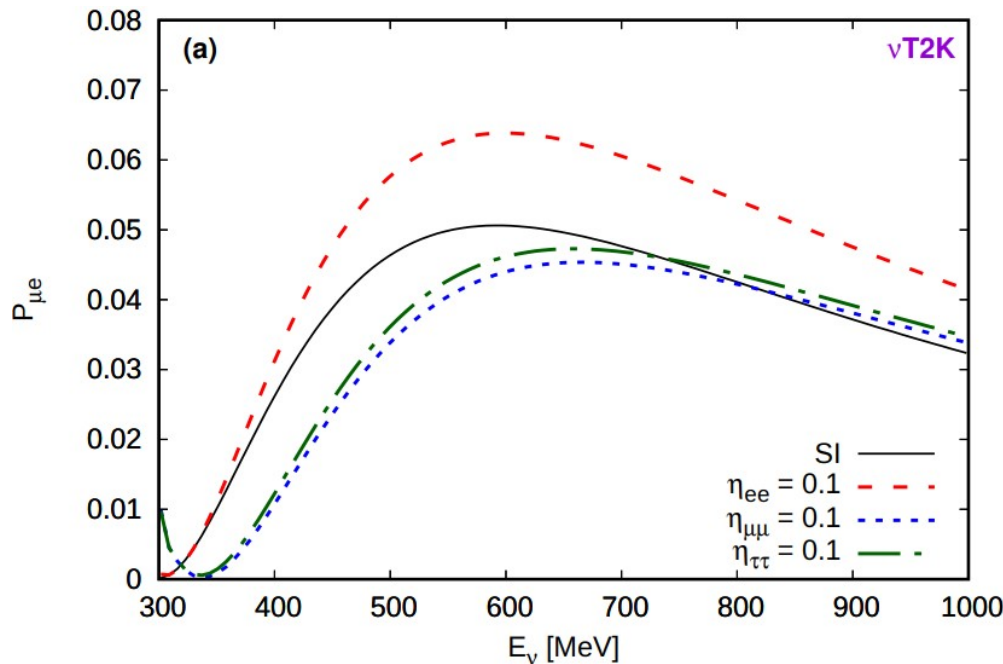
$$\mathcal{L}_{\text{cc}}^{\text{eff}} = \frac{g_{\alpha\rho}g_{\beta\sigma}^*}{2} \frac{1}{-m_V^2} (\bar{\nu}_\alpha \gamma_\mu P_L \nu_\beta) (\bar{\ell}_\sigma \gamma^\mu P_L \ell_\rho)$$

- Scalar NSI

$$\mathcal{L}_{\text{eff}}^s \propto y_{\alpha\beta} Y_{ee} [\bar{\nu}_\alpha(p_3) \nu_\beta(p_2)] [\bar{e}(p_1) e(p_4)]$$

$$\mathcal{H} \approx E_\nu + \frac{(M + \mathbf{M}_S)(M + \mathbf{M}_S)^\dagger}{2E_\nu} \pm V_{\text{SI}}$$

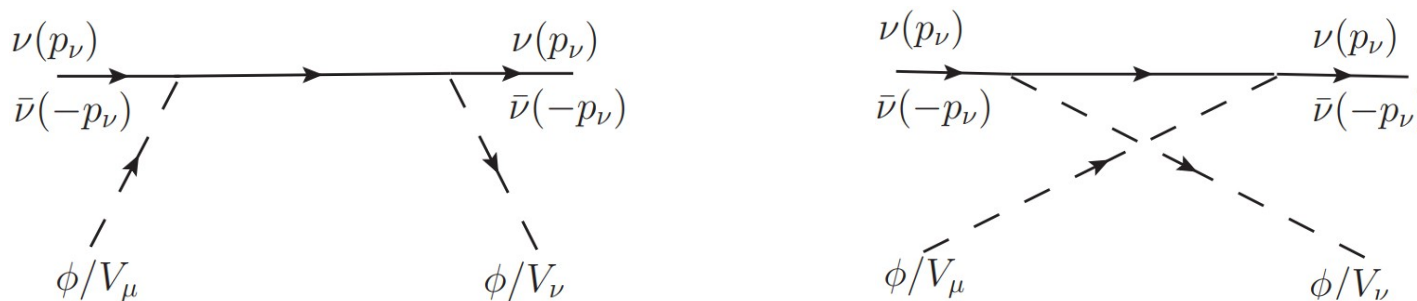
SFG, Stephen Parke, Phys.Rev.Lett. 122 (2019) 21, 211801 [arXiv:1812.08376]



3. Dark NSI with Forward Scattering

$$-\mathcal{L} = \frac{1}{2}m_\phi^2\phi^2 + \frac{1}{2}M_{\alpha\beta}\bar{\nu}_\alpha\nu_\beta + y_{\alpha\beta}\phi\bar{\nu}_\alpha\nu_\beta + h.c.$$

- Forward scattering in DM medium



$$H = \frac{M^2}{2E_\nu} - \frac{1}{\mathbf{E}_\nu} \sum_j y_{\alpha j} y_{j\beta}^* \frac{\rho_\chi}{m_\phi^2} \equiv \frac{M^2 + \delta M^2}{2\mathbf{E}_\nu}$$

- With $1/E_\nu$ dependence, the dark potential is promoted to mass

Dark NSI can fake neutrino mass!

SFG, Chui-Fan Kong, Alexei Smirnov [2404.17352]

SFG, Murayama [1904.02518]

SFG, PoS NuFact2019 (2020) 108

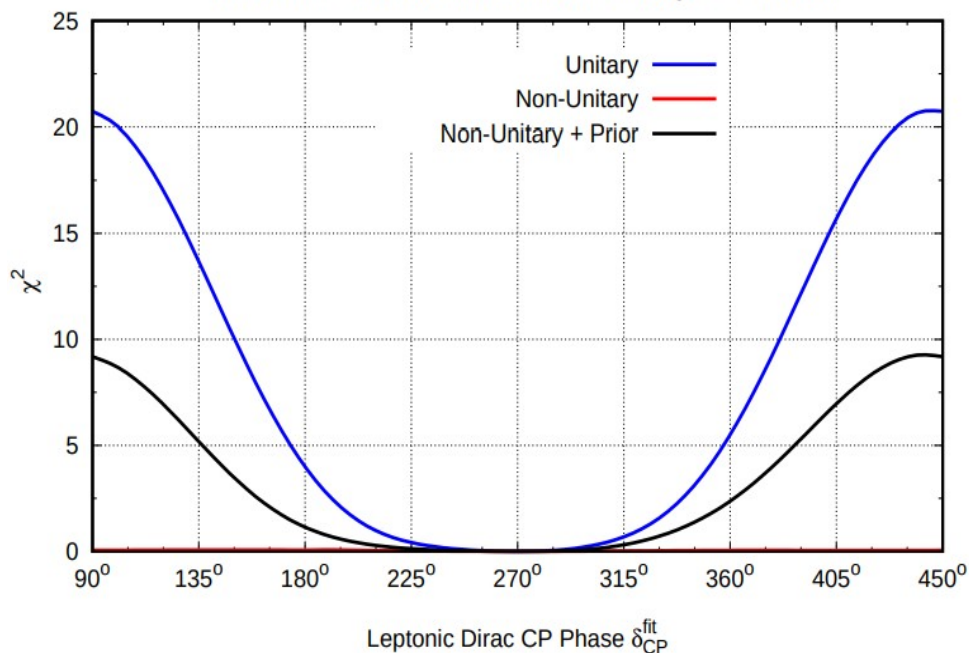
SFG, J.Phys.Conf.Ser. 1468 (2020) 1, 012125

4. Non-Unitarity Mixing (NUM)

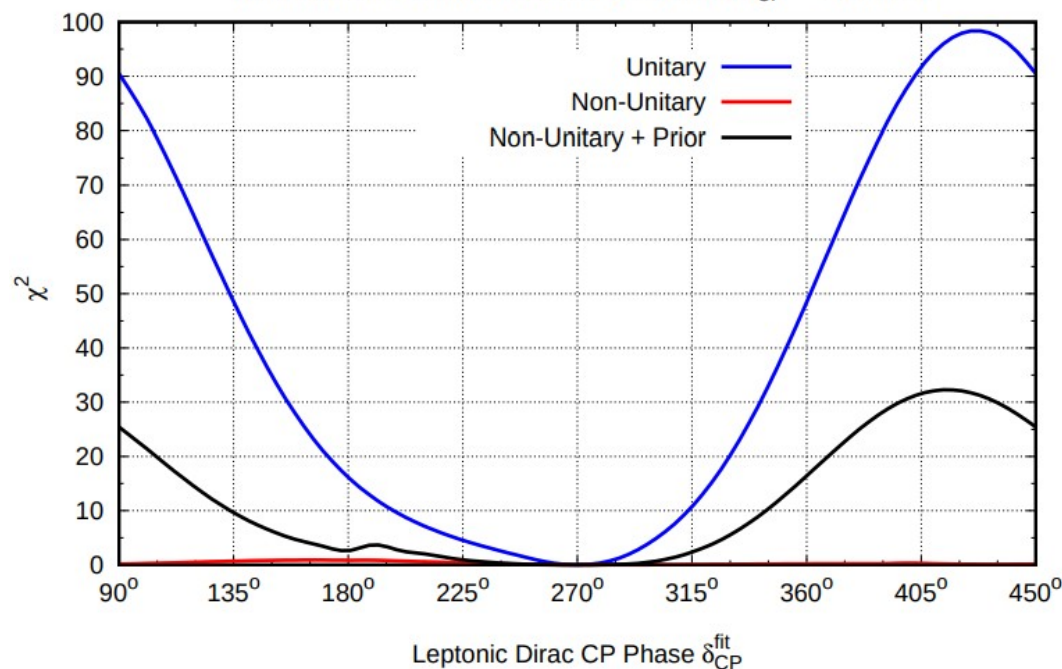
$$N = N^{NP} U = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ |\alpha_{21}| e^{i\phi} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} U$$

$$P_{\mu e}^{NP} = \alpha_{11}^2 \left\{ \alpha_{22}^2 \left[c_a^2 |S'_{12}|^2 + s_a^2 |S'_{13}|^2 + 2c_a s_a (\cos \delta_D \mathbb{R} - \sin \delta_D \mathbb{I})(S'_{12} S'_{13}^*) \right] + |\alpha_{21}|^2 P_{ee} \right. \\ \left. + 2\alpha_{22} |\alpha_{21}| \left[c_a (c_\phi \mathbb{R} - s_\phi \mathbb{I})(S'_{11} S'_{12}^*) + s_a (c_{\phi+\delta_D} \mathbb{R} - s_{\phi+\delta_D} \mathbb{I})(S'_{11} S'_{13}^*) \right] \right\}.$$

The effect of including non-unitarity at T2K [$\delta_{CP}^{\text{true}} = -90^\circ$, NH]



The effect of including non-unitarity at T2HK [$\delta_{CP}^{\text{true}} = -90^\circ$, NH]



SFG, Pasquini, Tortola & Valle [1605.01670]

4. NUM vs Seeaw Mechanism

- Heavy Neutrinos

$$\bar{\nu} M_D \mathcal{N} + h.c. + \bar{\mathcal{N}} M_N \mathcal{N} = \begin{pmatrix} \bar{\nu} & \bar{\mathcal{N}} \end{pmatrix} \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \begin{pmatrix} \nu \\ \mathcal{N} \end{pmatrix}$$

The diagonalization of the full mass matrix

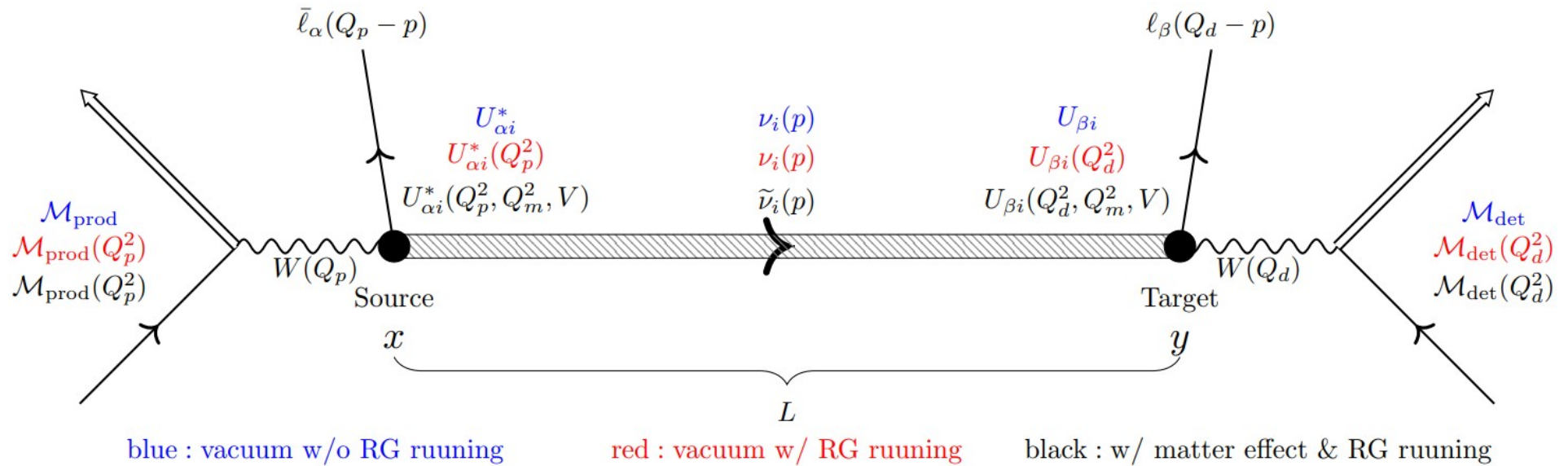
$$\begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \Rightarrow M_\nu = -M_D \frac{1}{M_N} M_D^T$$



$$N = N^{NP} U = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ |\alpha_{21}| e^{i\phi} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} U$$

NUM is not exotic at all!

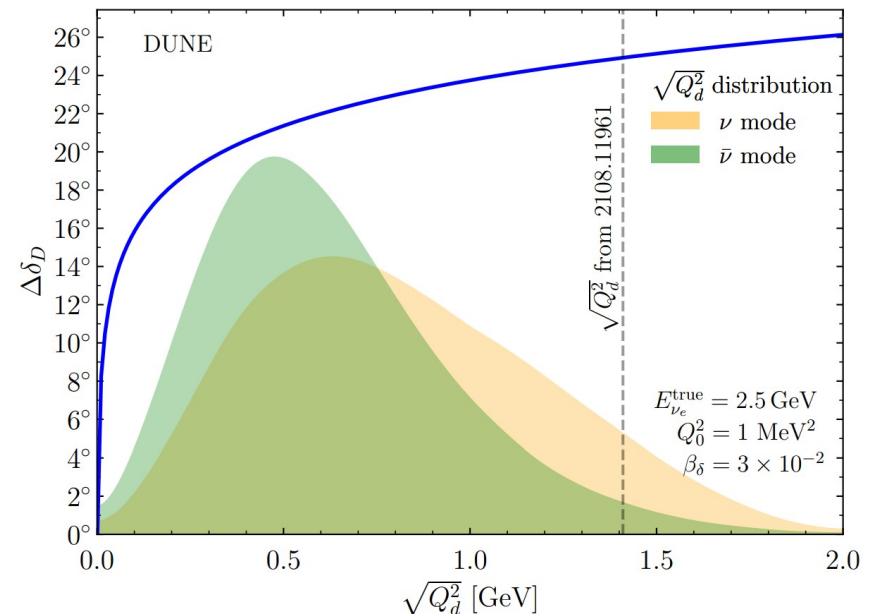
5. RG Running



● Mismatched Momentum

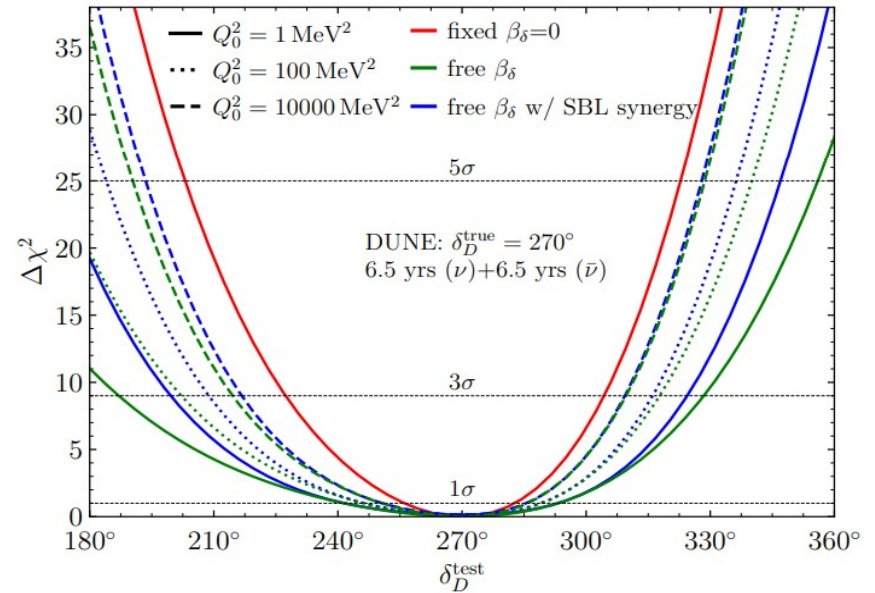
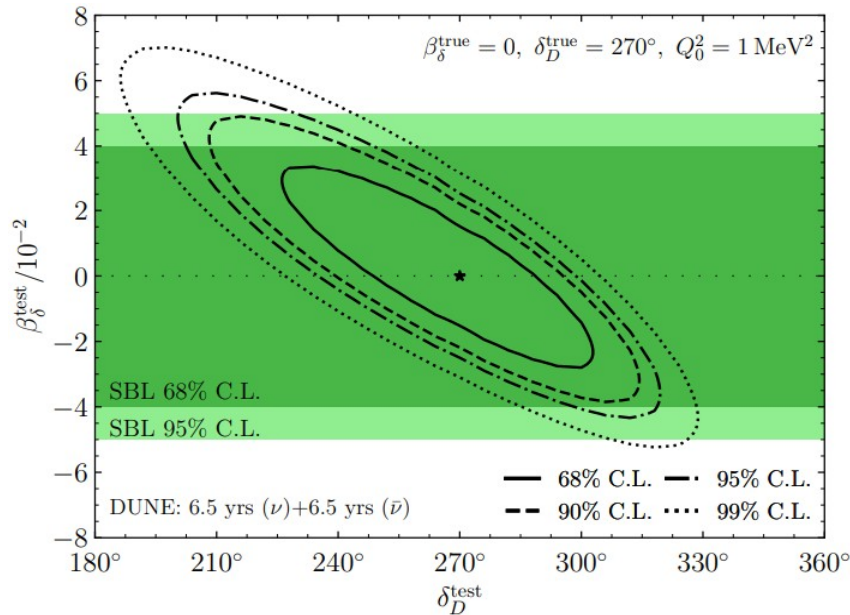
$$\mathcal{A}_{\beta\alpha}^{\text{osc}} = U_{\beta i}(Q_d^2) e^{-iL \frac{m_i^2}{2E_\nu}} U_{\alpha i}^*(Q_p^2)$$

$$P_{\alpha\beta} = \left| [U(Q_d^2) U^\dagger(Q_p^2)]_{\beta\alpha} \right|^2$$



SFG, Chui-Fan Kong, Pedro Pasquini [arXiv:2310.04077]

5. RG Running & CP Measurement



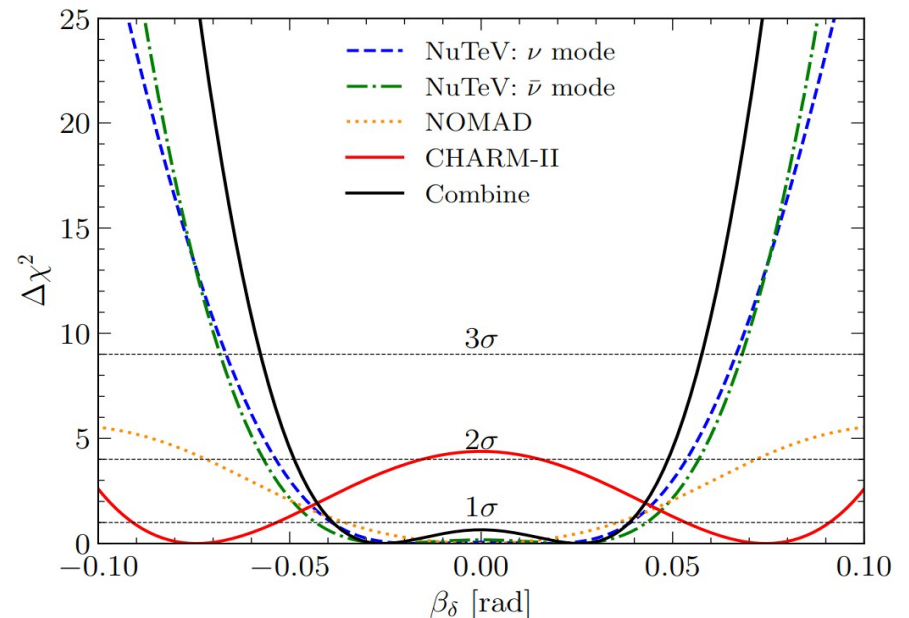
SFG, Chui-Fan Kong, Pedro Pasquini [arXiv:2310.04077]

• Zero Distance Effect

$$P_{ee}(Q_{d,p}^2) = 1 - \sin^2 \left(\frac{\Delta\delta_D}{2} \right) \sin^2 2\theta_{13}$$

$$P_{\mu e}(Q_{d,p}^2) = \sin^2 \left(\frac{\Delta\delta_D}{2} \right) s_{23}^2 \sin^2 2\theta_{13}$$

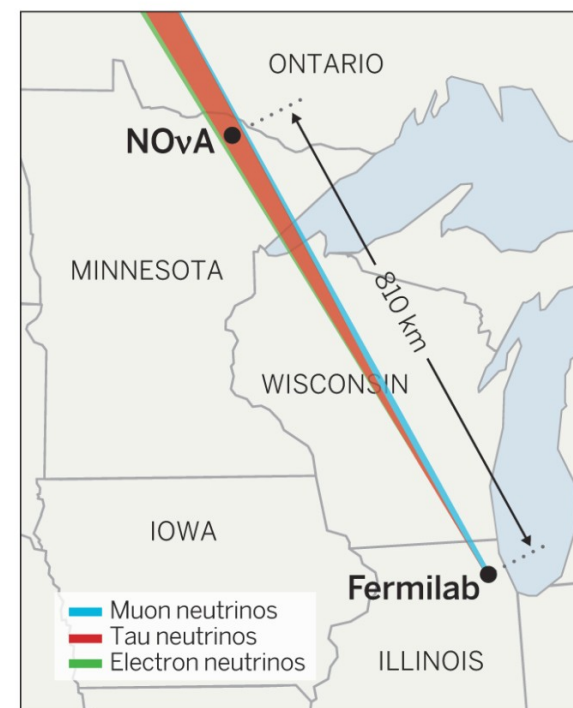
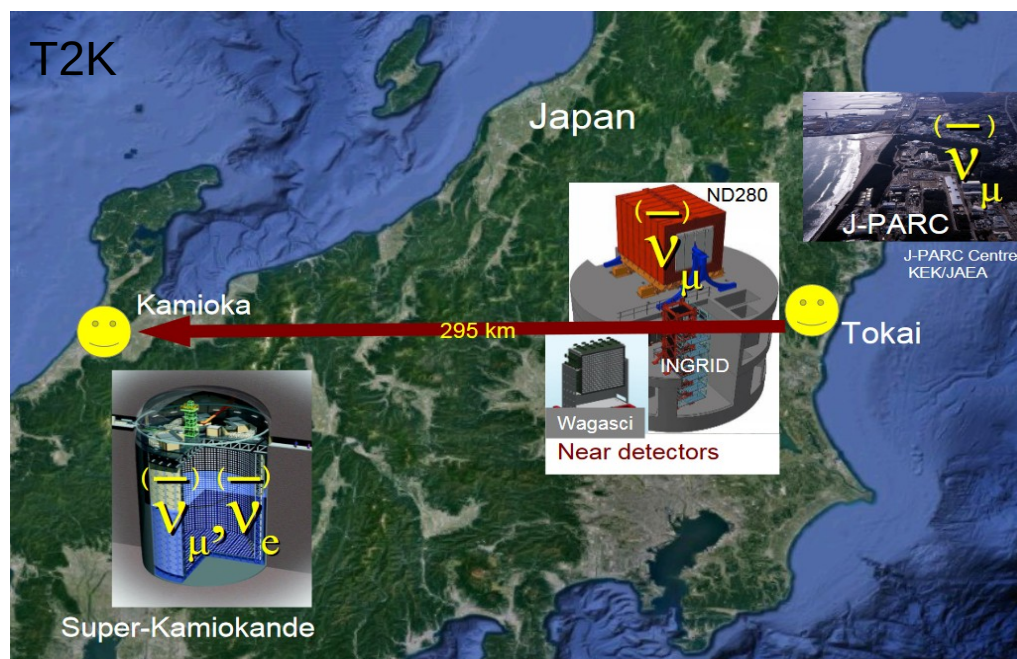
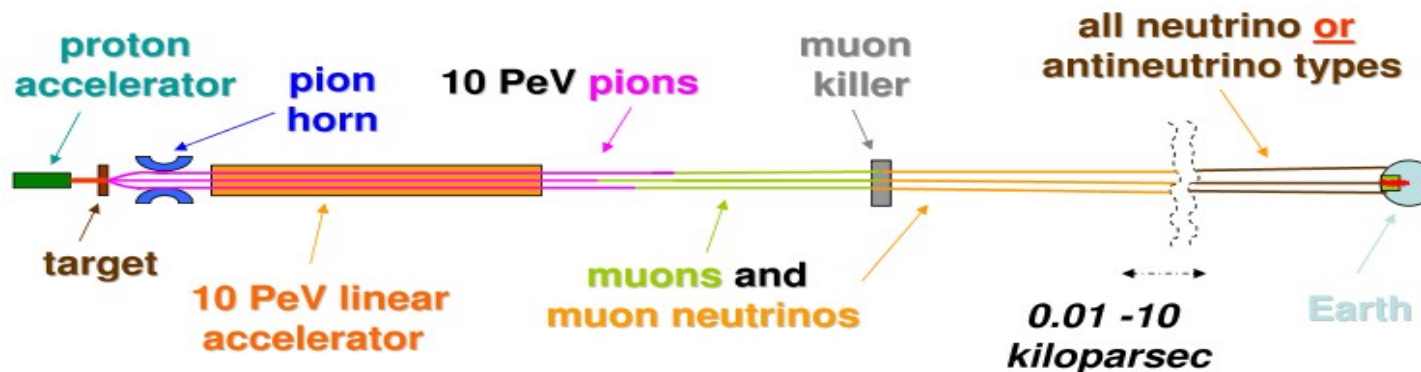
Short-Baseline Experiment (SBL):



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Accelerator v Experiments

Pion Accelerator Neutrino Beam Concept



K. Engman, Science 345, 6204

Accelerator v's by Lee & Yang

李政道研究所
Tsung-Dao Lee Institute

PHYSICAL REVIEW LETTERS

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Feasibility of Using High-Energy Neutrinos to Study the Weak Interactions

M. Schwartz

Phys. Rev. Lett. **4**, 306 – Published 15 March 1960

Theoretical Discussions on Possible High-Energy Neutrino Experiments

T. D. Lee and C. N. Yang

Phys. Rev. Lett. **4**, 307 – Published 15 March 1960

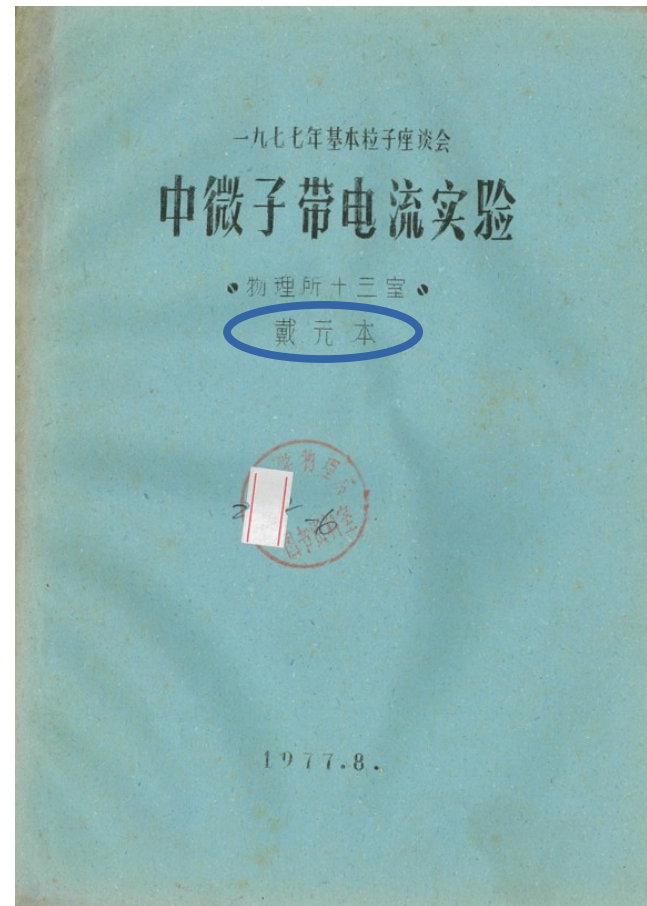
历史印记——60年前高能加速器中微子实验原理诞生

🕒 2021-01-04 👁 50

作者：葛韶锋

这项60年前的工作，今天还在为粒子物理研究指引着前进的方向

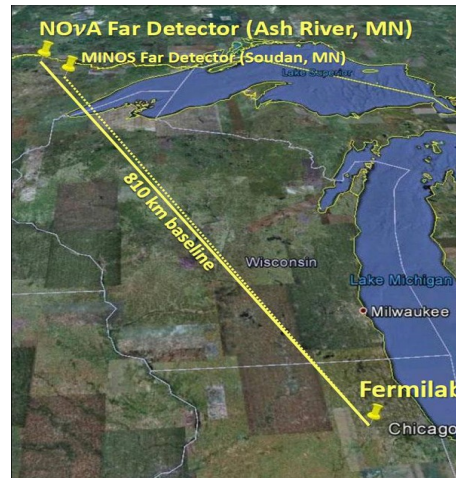
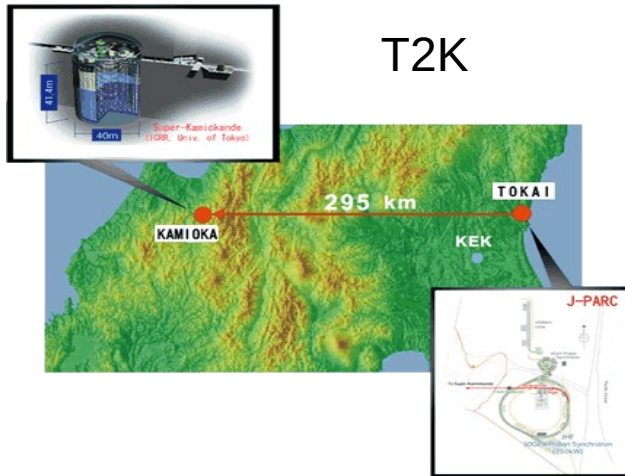
中微子是粒子物理标准模型中非常独特而重要的基本粒子。中微子只参与弱相互作用，能够穿透几光年的铅板，是非常难以探测的鬼魅粒子。然而，恰恰是中微子率先给出了超出标准模型的第一个新物理现象——中微子振荡——这已经得到大量实验的证实，并于2015年获诺贝尔物理学奖，成为指引超出标准模型新物理研究的重要线索。在上世纪五六十年代粒子物理发展的黄金期，施瓦兹、李政道与杨振宁提出的高能加速器中微子实验原理，是一个非常革命性的思想，一直在有力地推动着包括中微子在内的粒子物理不断向前发展。



何小刚，李政道先生和现代中微子物理，《现代物理知识杂志》2021

<https://tdli.sjtu.edu.cn/CN/customize/436?columnId=35>

Future Accelerator Exps



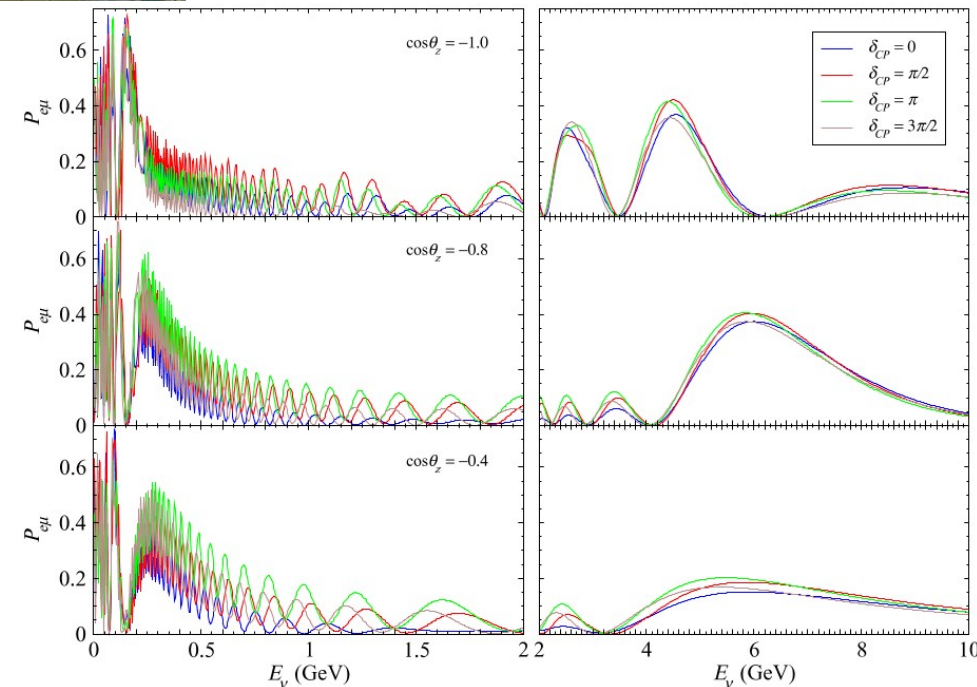
- Flux upgrade: **T2K-II**, **NOvA-II**?
- Detector upgrade: **T2HK**
- Baseline upgrade: **T2KK**, **T2KO**
- MOMENT**
- In China? Tang, Vihonen & Xu [2202.13595]
Li et al [2204.11871, 2205.15350, 2301.02493]
- Atmospheric

Super-PINGU: Razzaque & Smirnov [1406.1407]

JUNO: An et al [1507.05613], 2310.06281

DUNE: Kelly, Machado, Martinez-Soler, Parke & Perez-Gonzalez [1904.02751]

Super-ORCA: Hofestadt, Bruchner & Eberl [1907.12983]



- Oscillation probabilities @ Accelerator Neutrino Exps

$$P_{\nu_\mu \rightarrow \nu_e} \approx 4s_a^2 c_r^2 s_r^2 \sin^2 \phi_{31} - 8c_a s_a c_r^2 s_r c_s s_s \sin \phi_{21} \sin \phi_{31} [\cos \delta_D \cos \phi_{31} \pm \sin \delta_D \sin \phi_{31}]$$

for ν & $\bar{\nu}$, respectively. $[\phi_{ij} \equiv \frac{\delta m_{ij}^2 L}{4E_\nu}]$

- Run both ν & $\bar{\nu}$ modes @ first peak $[\phi_{31} = \frac{\pi}{2}, \phi_{21} = \alpha \frac{\pi}{2}]$, $\alpha = \frac{\delta M_{21}^2}{|\delta M_{31}^2|} \sim 3\%$

$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e} + P_{\nu_\mu \rightarrow \nu_e} = 2s_a^2 c_r^2 s_r^2,$$

$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e} - P_{\nu_\mu \rightarrow \nu_e} = \alpha \pi \sin(2\theta_s) \sin(2\theta_r) \sin(2\theta_a) \cos \theta_r \sin \delta_D.$$

中微子、反中微子的振荡概率之间的差别 $\rightarrow$ 测量 CP 相角 δ_D 。

$$P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e} - P_{\nu_\mu \rightarrow \nu_e} = \alpha\pi \sin(2\theta_s) \sin(2\theta_r) \sin(2\theta_a) \cos\theta_r \sin\delta_D$$

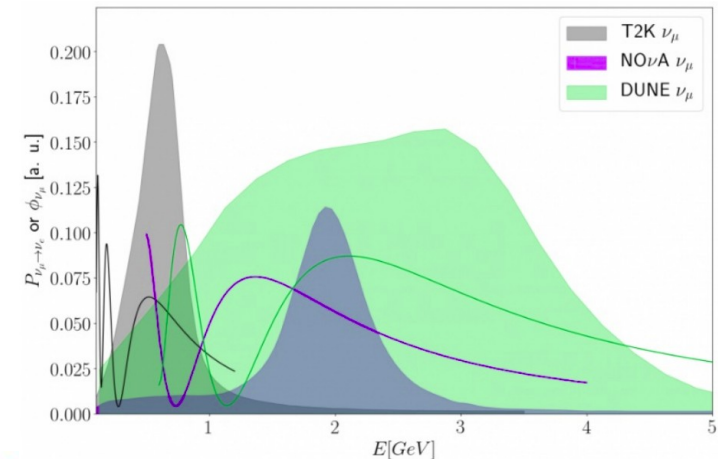
@ 1st oscillation peak

• Efficiency:

- Proton accelerators produce ν more efficiently than $\bar{\nu}$ ($\sigma_\nu > \sigma_{\bar{\nu}}$).
- The $\bar{\nu}$ mode needs more beam time [$\mathbf{T_{\bar{\nu}} : T_\nu = 2 : 1}$].
- Undercut statistics $\Rightarrow$ Difficult to reduce the uncertainty.

• Degeneracy:

- Only $\sin\delta_D$ appears in $P_{\nu_\mu \rightarrow \nu_e}$ & $P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e}$.
- Cannot distinguish δ_D from $\pi - \delta_D$.



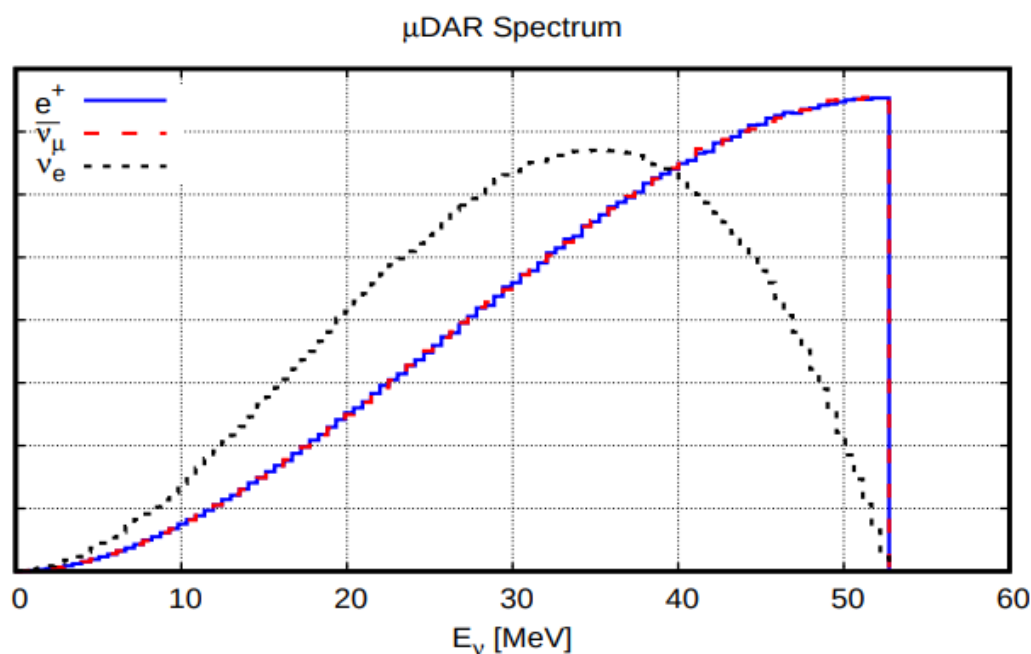
• CP Uncertainty

$$\frac{\partial P_{\mu e}}{\partial \delta_D} \propto \cos\delta_D \Rightarrow \Delta(\delta_D) \propto \mathbf{1/\cos\delta_D}$$

SFG [1704.08518, PoS NuFact2019 (2020) 108]

Solution: Muon Decay at Rest

- A cyclotron produces 800 MeV proton beam @ fixed target.
- Produce $\pi^\pm$ which stops &
 - π^- is absorbed,
 - π^+ decays @ rest: $\pi^+ \rightarrow \mu^+ + \nu_\mu$.
- μ^+ stops & decays @ rest: $\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e$



Well predicted spectrum!

- $\bar{\nu}_\mu$ travel in all directions, oscillating as they go.
- A detector measures the $\bar{\nu}_e$ from $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillation.

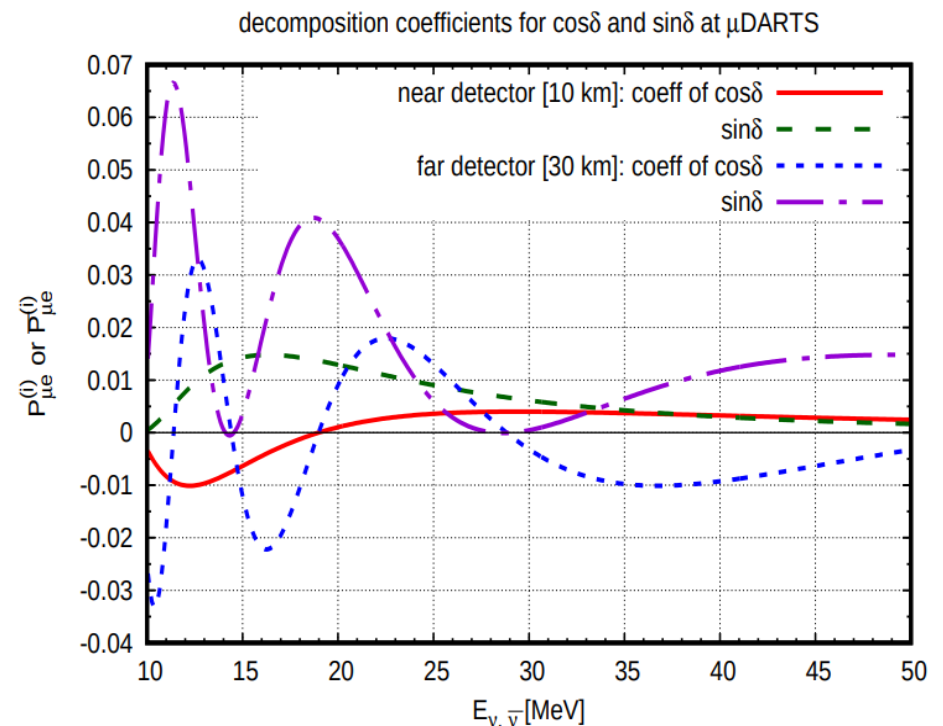
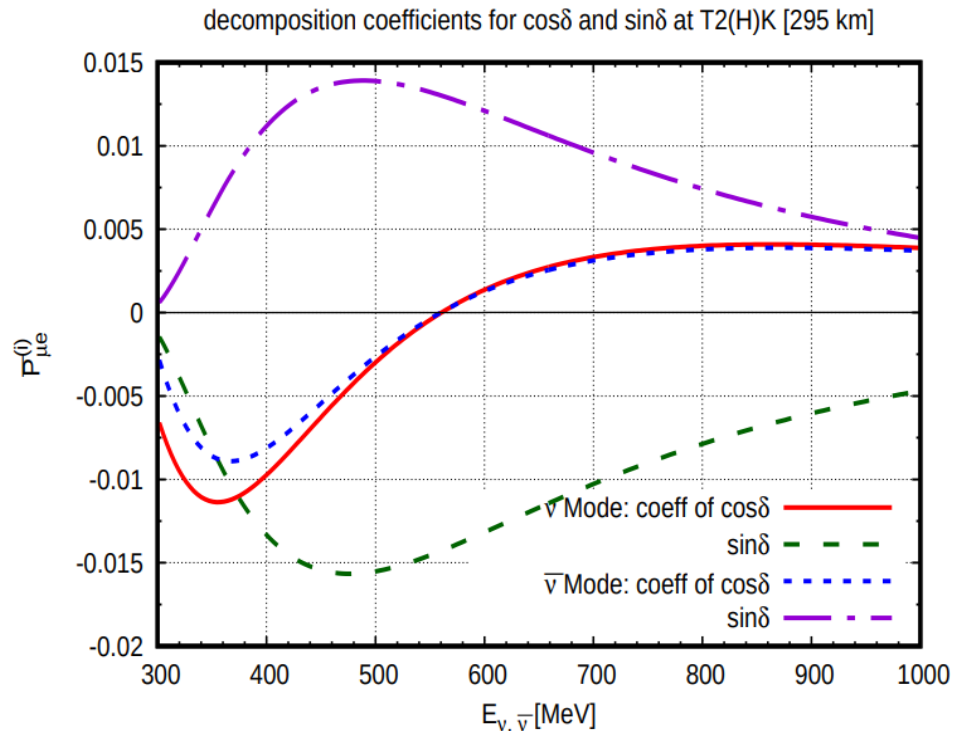
μ DAR & Accelerator ν

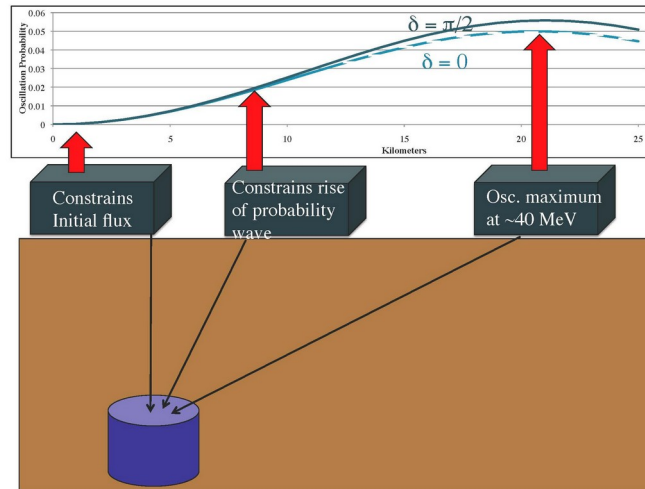
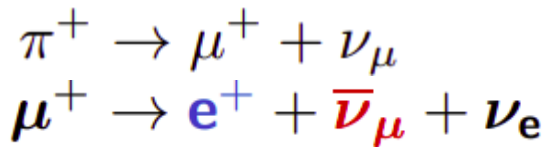
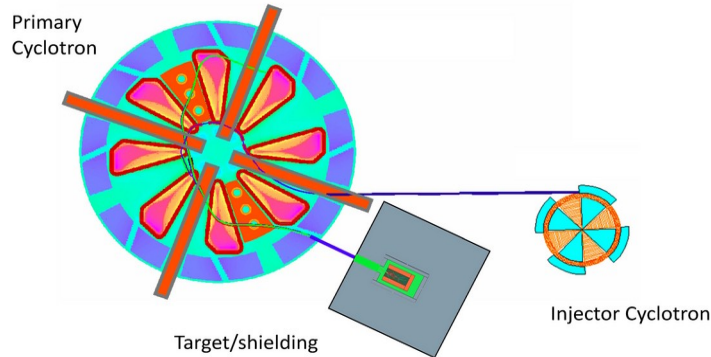
Combining $\nu_\mu \rightarrow \nu_e$ @ accelerator [narrow peak @ 550 MeV] & $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ @ μ DAR [wide peak ~ 45 MeV] solves the 2 problems:

- **Efficiency:**

- $\bar{\nu}$ @ high intensity, μ DAR is plentiful enough.
- Accelerator Exps can devote all run time to the ν mode. With same run time, the statistical uncertainty drops by $\sqrt{3}$.

- **Degeneracy:** (decomposition in propagation basis [1309.3176])





戴达罗斯（希腊神话中的建筑师、工匠）

Disadvantages:

- The scattering lepton from IBD @ low energy is **isotropic**.
- **Cannot** distinguish $\bar{\nu}_e$ from different sources $\bar{\nu}_e + p \rightarrow e^+ n$
- Baseline **cannot be measured**.
- Cyclotrons **cannot** run simultaneously (20~25% duty factor).
- **Large** statistical uncertainty.
- **Higher intensity** is necessary.
- **Expensive** & Technically **challenging**.

Conrad & Shaevitz [0912.4079]

Agarwalla, Huber, Link & Mohapatra [1005.4055]

DAEdALUS [1006.0260, 1307.2949]

New Proposal

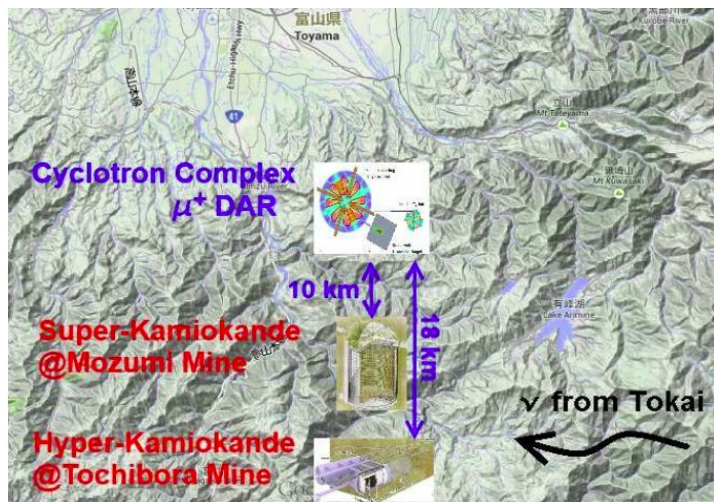
1 μ DAR source + **2** detectors

Advantages

- Full (**100%**) duty factor!
- **Lower** intensity: $\sim 9\text{mA}$ [$\sim 4\times$ lower than DAE δ ALUS]
- Not far beyond the current state-of-art technology of cyclotron [**2.2mA** @ Paul Scherrer Institute]
- MUCH **cheaper** & technically **easier**.
 - Only one cyclotron.
 - Lower intensity.

Disadvantage: A second detector!

- μ **DAR** with **Two Scintillators** (μ **DARTS**) [Ciuffoli, Evslin & Zhang, 1401.3977] also Smirnov, Hu, Li & Ling [1802.03677, 1808.03795]
- **Tokai 'N Toyama to(2) Kamioka** (**TNT2K**) [Evslin, Ge & Hagiwara, 1506.05023]



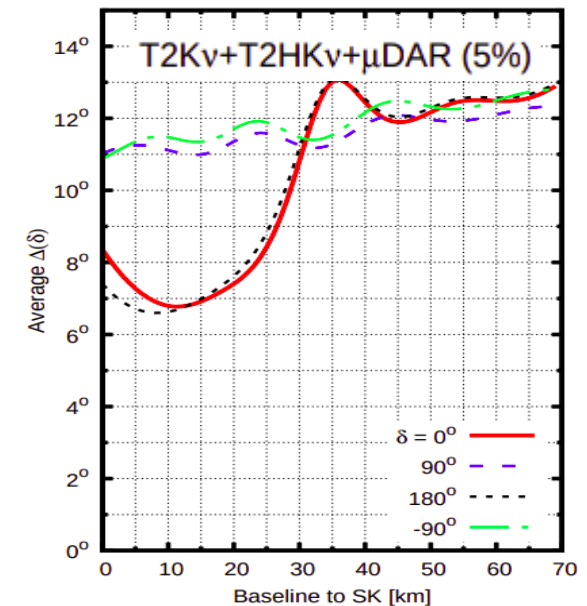
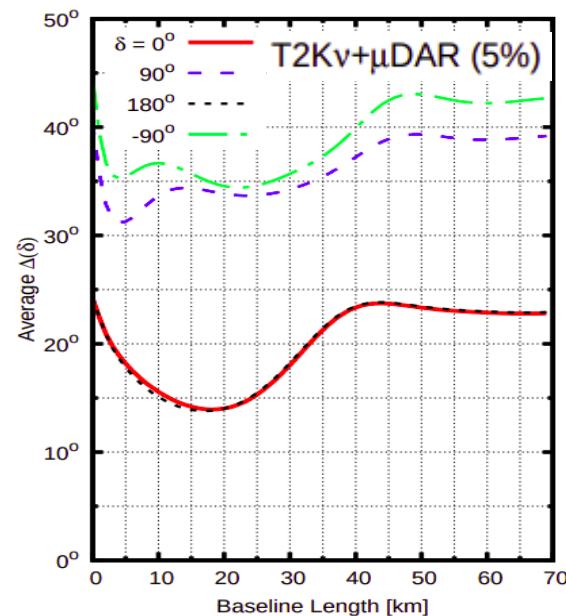
1 μ DAR source + 2 detectors

Advantages

- Full (**100%**) duty factor!
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- MUCH **cheaper** & technically **easier**.
 - Only one cyclotron.
 - Lower intensity.

Disadvantage: A second detector!

Harnik, Kelly & Machado [1911.05088]

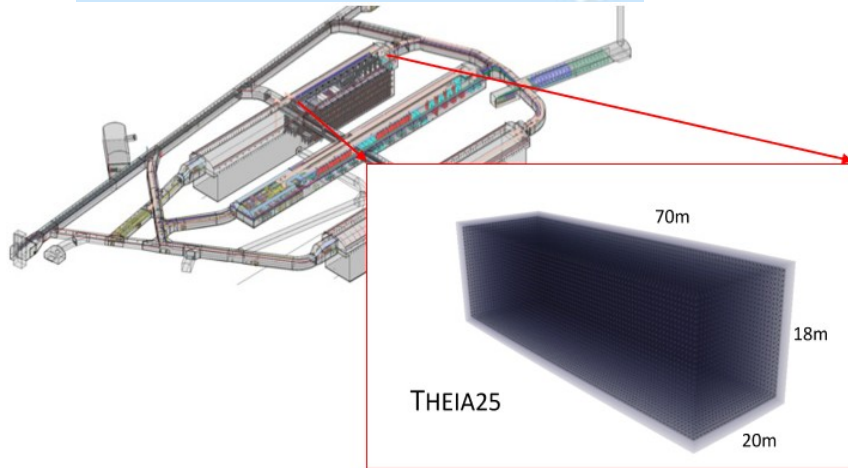


Evslin, SFG, Hagiwara [1506.05023]

SFG, Pasquini, Tortola, Valle [1605.01670]

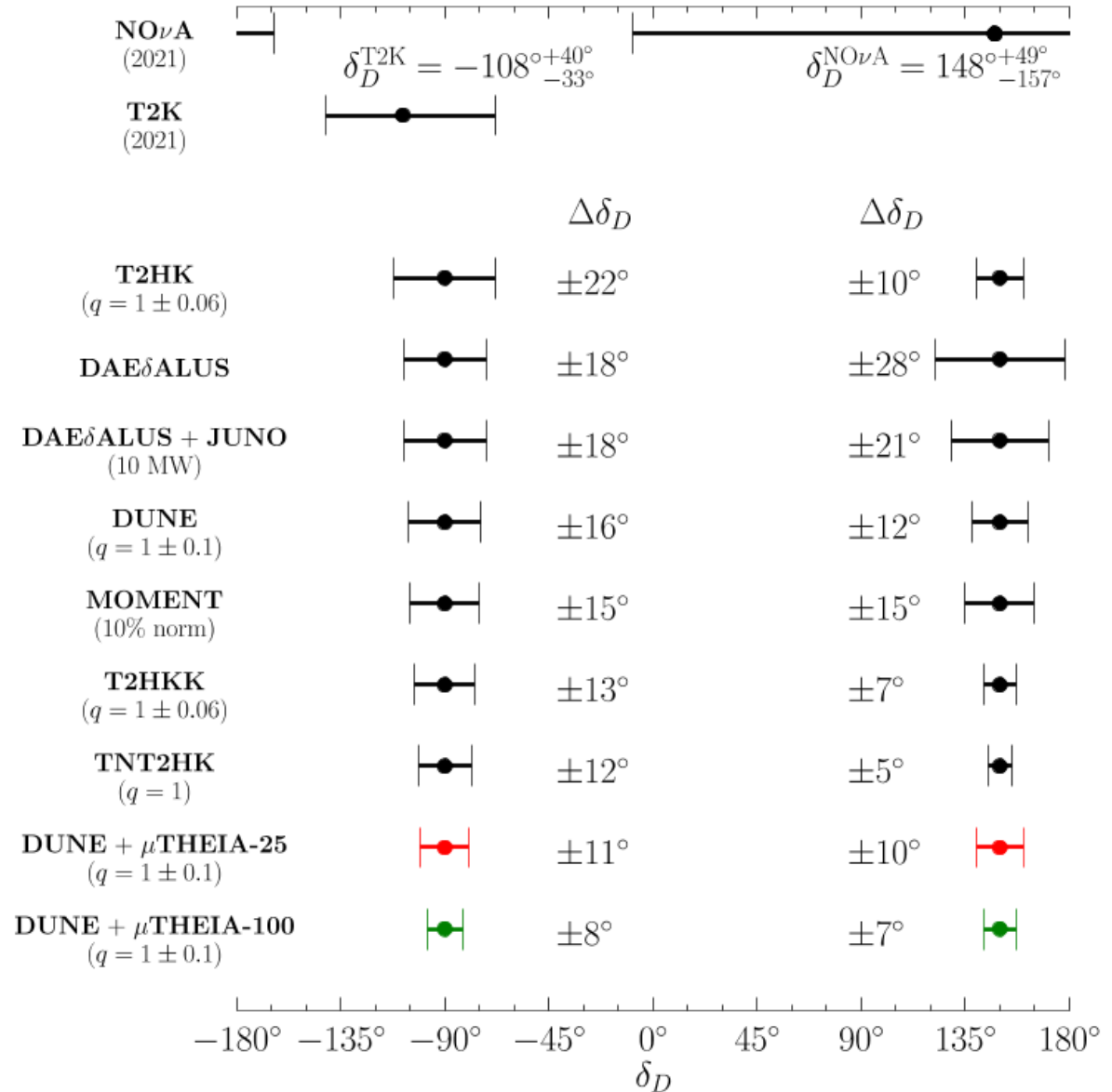
SFG, Smirnov [1607.08513]

μ THEIA+DUNE



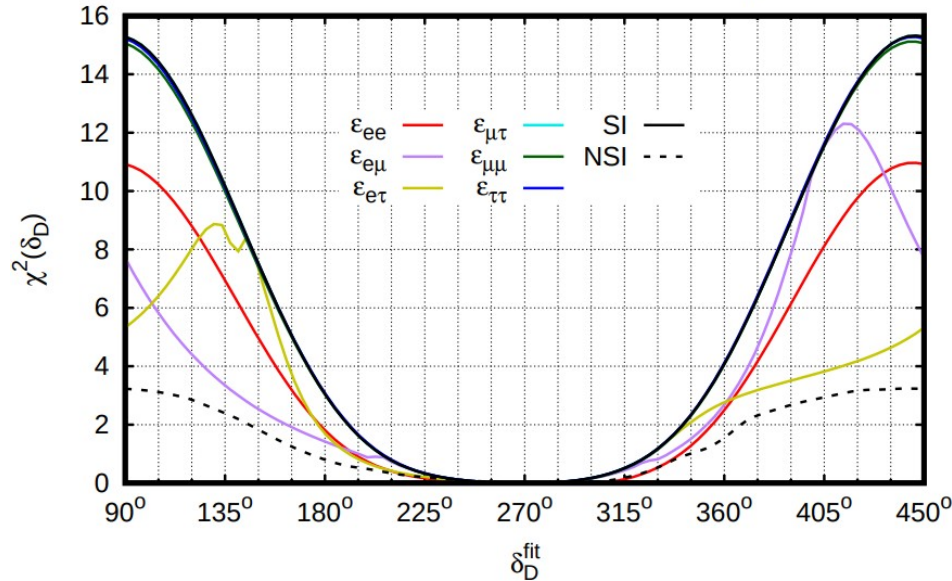
THEIA [1911.03501, 2202.12839]

SFG, Kong, Pasquini, Eur.Phys.J.C
82 (2022) 6, 572 [2202.05038]

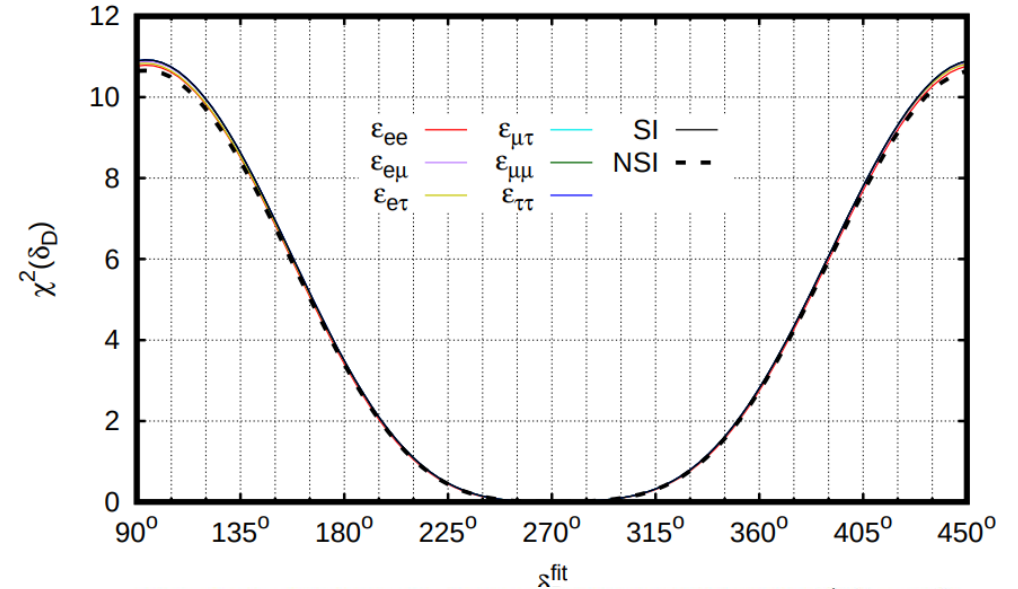


Guarantee CP against NSI

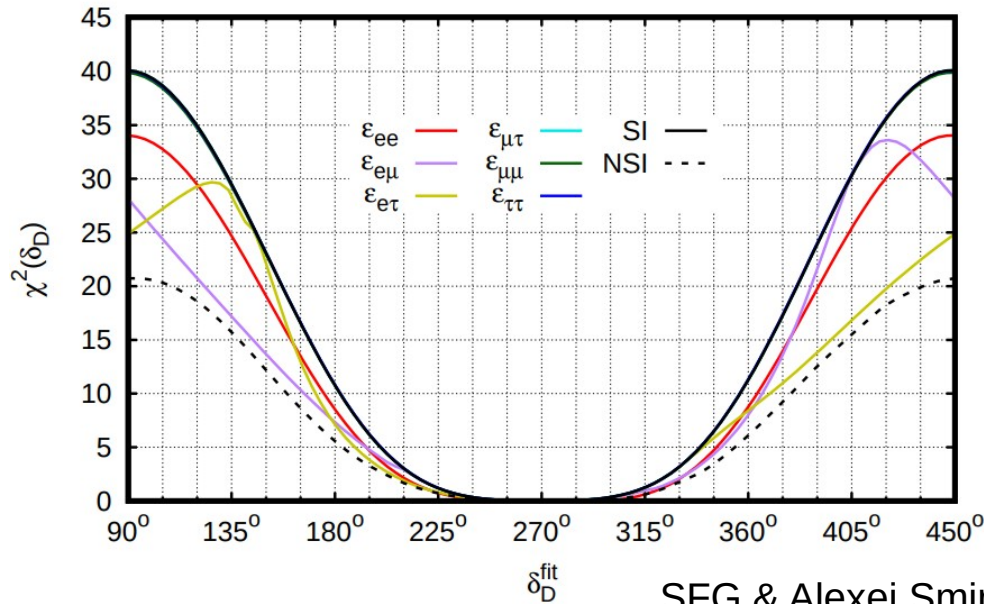
The effect of NSI on the CP sensitivity at T2K [$\delta_D^{\text{true}} = -90^\circ$]



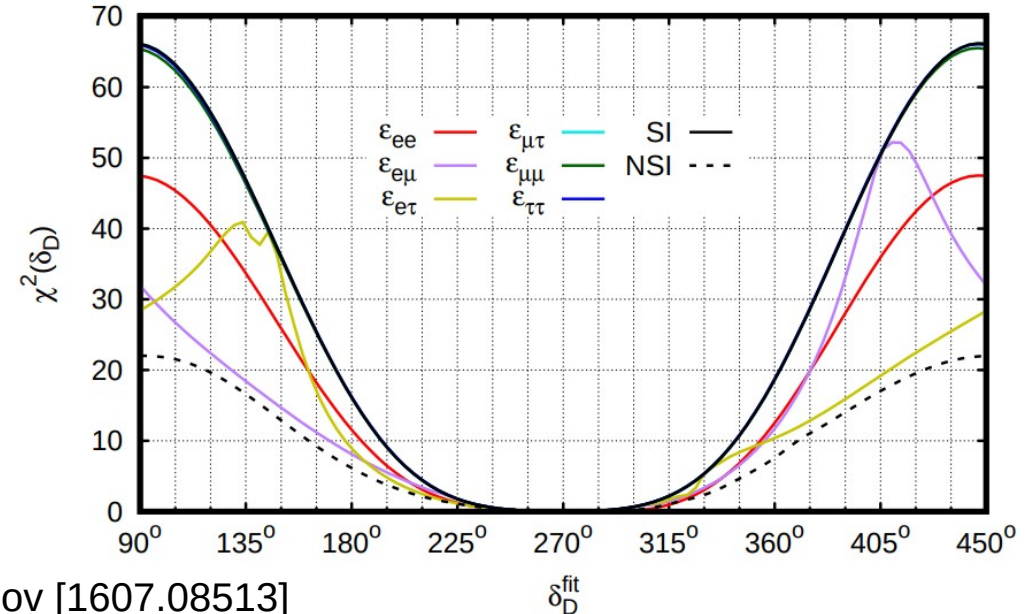
The effect of NSI on the CP sensitivity at μ SK [$\delta_D^{\text{true}} = -90^\circ$]



The effect of NSI on the CP sensitivity at T2K+ μ SK [$\delta_D^{\text{true}} = -90^\circ$]



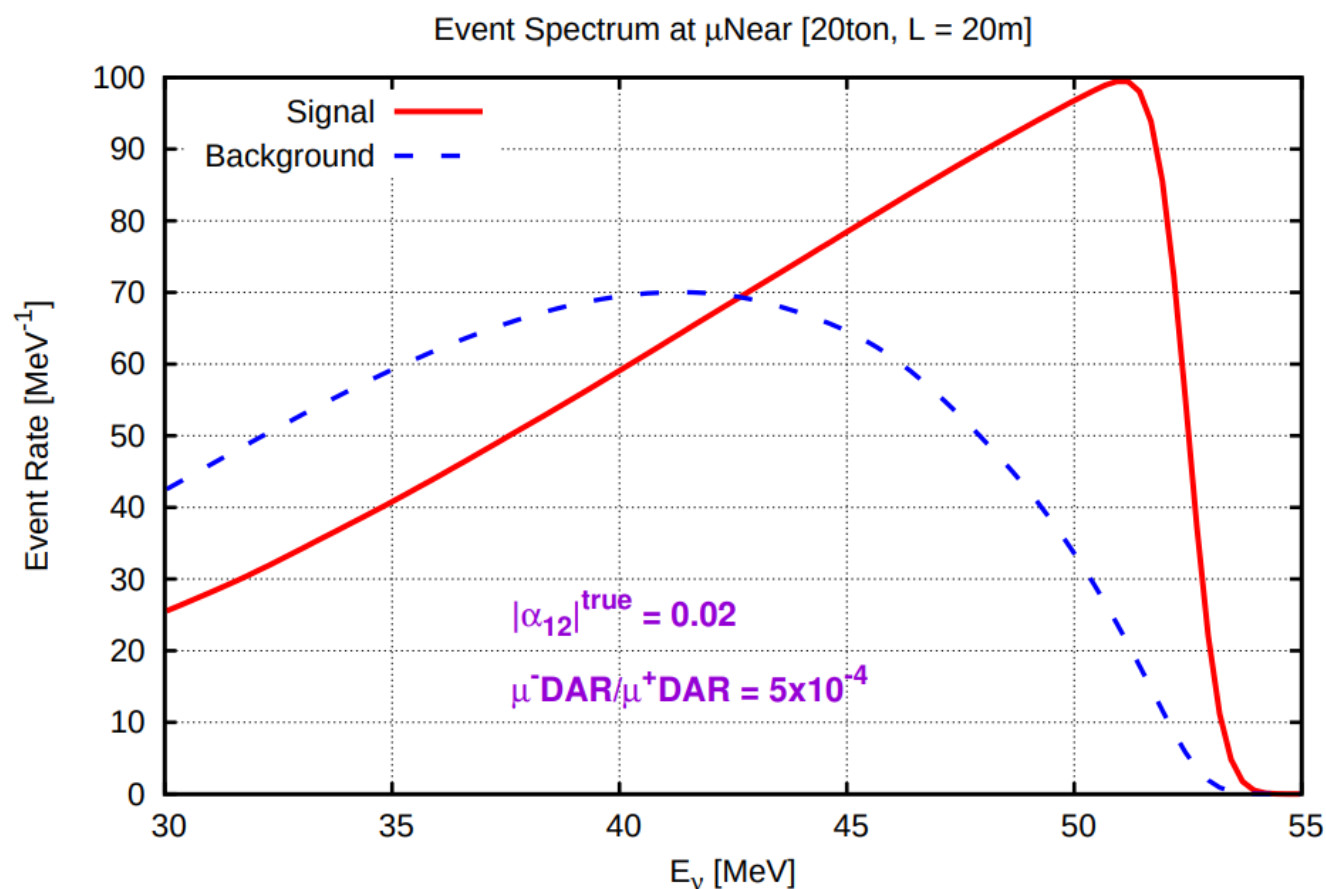
The effect of NSI on the CP sensitivity at ν T2K+ μ SK [$\delta_D^{\text{true}} = -90^\circ$]



SFG & Alexei Smirnov [1607.08513]

NUM Zero Distance Effect

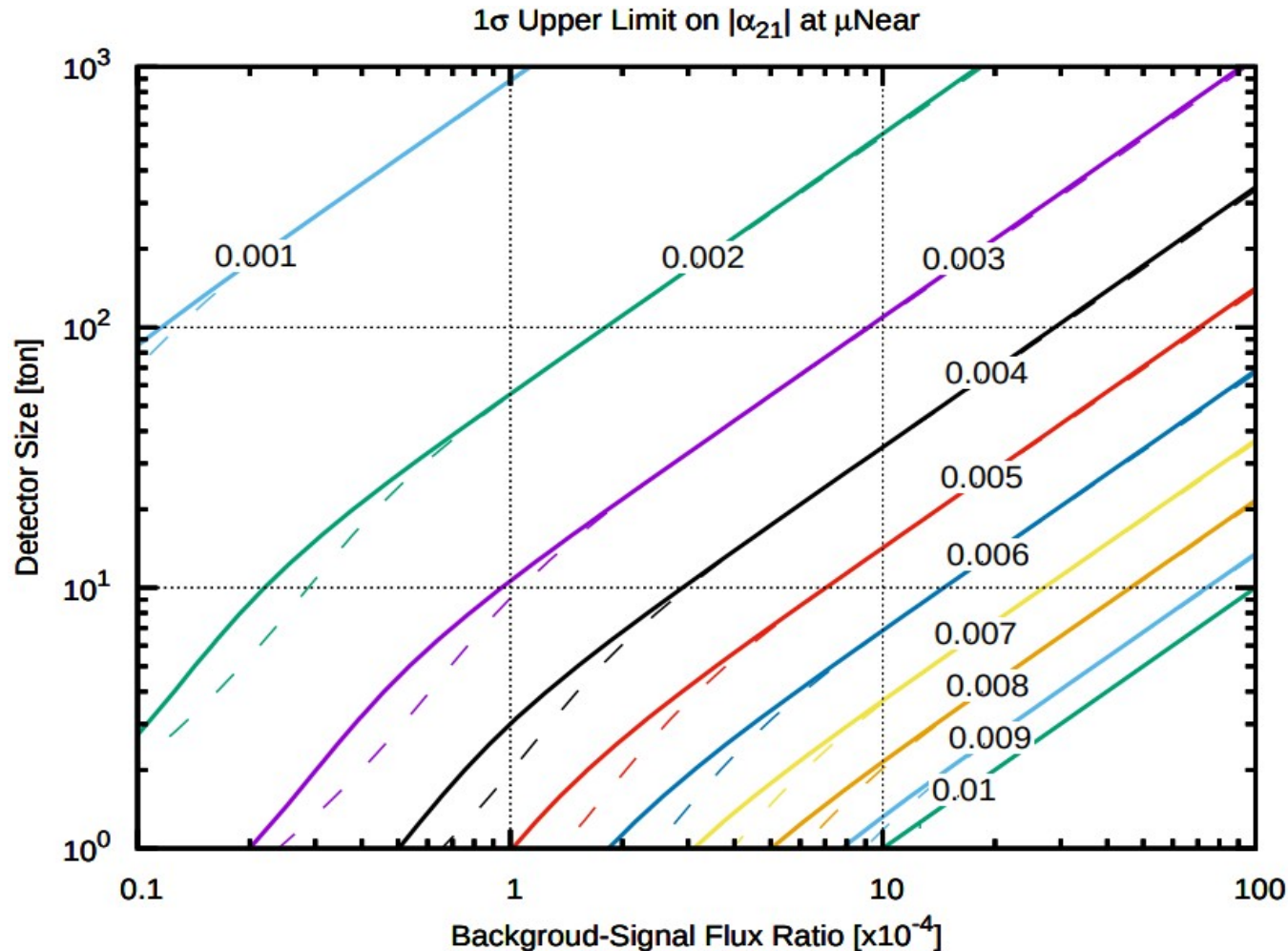
$$N = N^{NP} U = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ |\alpha_{21}| e^{i\phi} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} U \quad P_{\mu e}^{NP}(L \rightarrow 0) = \alpha_{11}^2 |\alpha_{21}|^2 P_{ee} \\ \approx \alpha_{11}^2 |\alpha_{21}|^2 \approx |\alpha_{21}|^2$$



Transition @ $L \rightarrow 0$

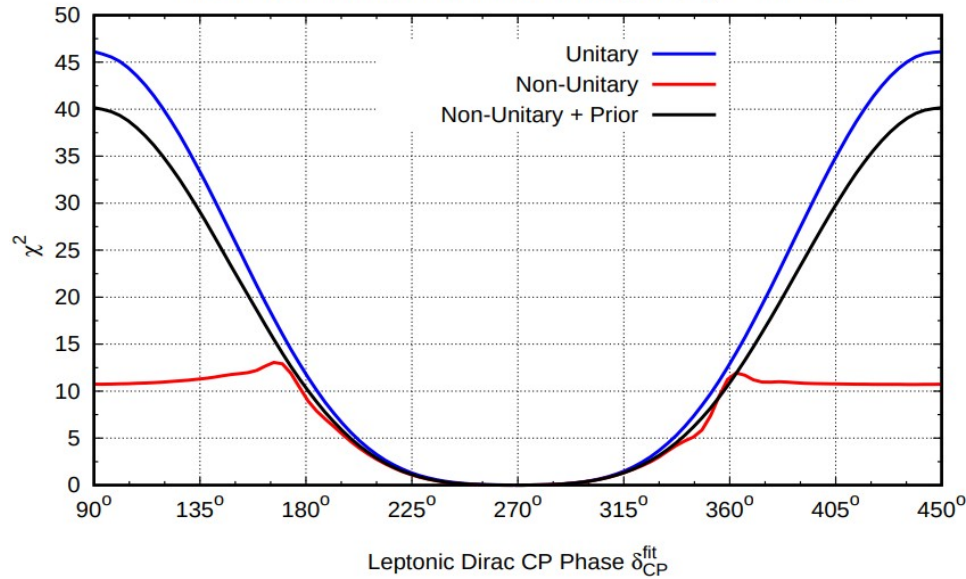
SFG, Pasquini, Tortola
& Valle [1605.01670]

$$P_{\mu e}^{NP}(L \rightarrow 0) = \alpha_{11}^2 |\alpha_{21}|^2 P_{ee} \approx \alpha_{11}^2 |\alpha_{21}|^2 \approx |\alpha_{21}|^2$$

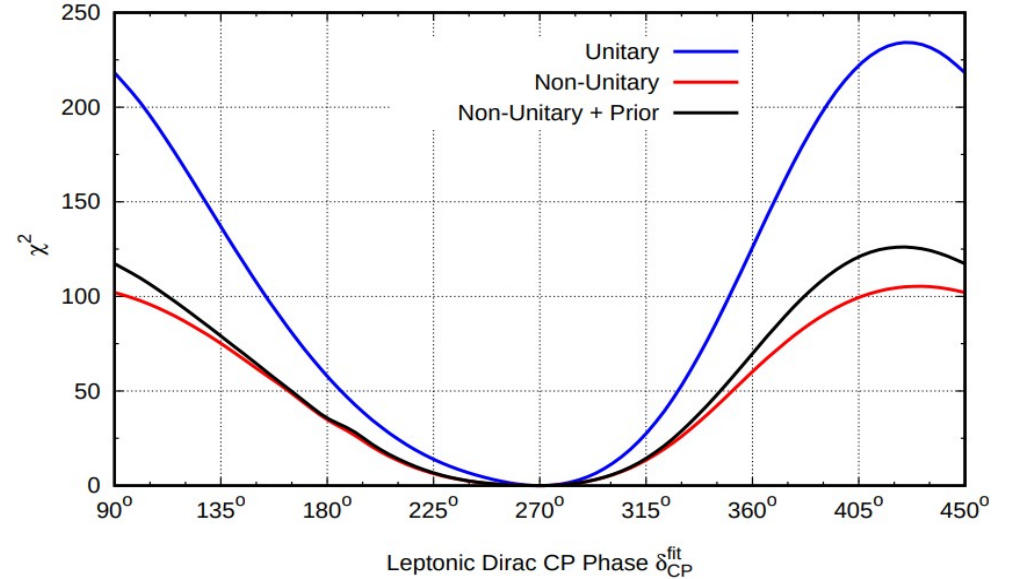


SFG, Pasquini, Tortola & Valle [1605.01670]

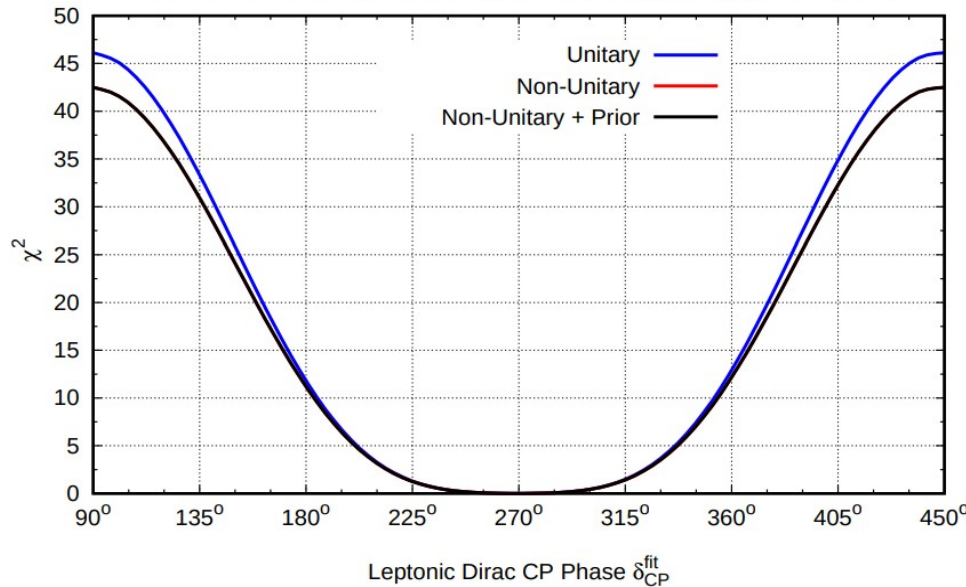
The effect of including non-unitarity at T2K+ μ SK [$\delta_{CP}^{true} = -90^\circ$, NH]



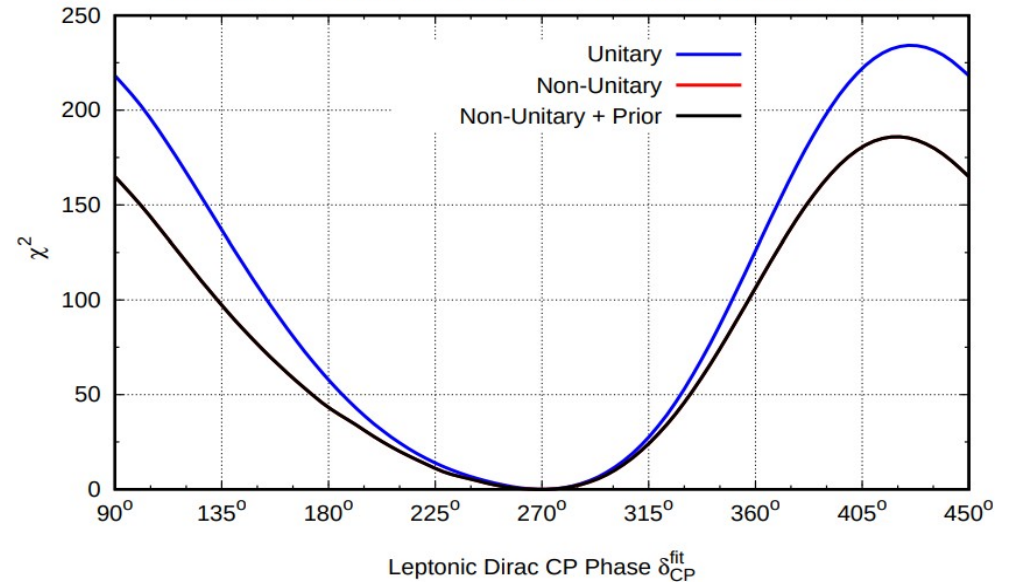
The effect of including non-unitarity at T2HK+ μ HK [$\delta_{CP}^{true} = -90^\circ$, NH]



The effect of including non-unitarity at T2K+ μ SK+ μ Near [$\delta_{CP}^{true} = -90^\circ$, NH]



The effect of including non-unitarity at T2HK+ μ HK+ μ Near [$\delta_{CP}^{true} = -90^\circ$, NH]



SFG, Pasquini, Tortola & Valle [1605.01670]

- **CP Violation in the Precision Era**
- **Dirac CP Phase & New Physics**
 1. Non-Standard Interactions (NSI)
 2. Scalar NSI
 3. Dark NSI
 4. Non-Unitary Mixing (NUM)
 5. RG Running
- **Accelerator + μ DAR for better CP measurement**
 1. TNT2K
 2. μ THEIA

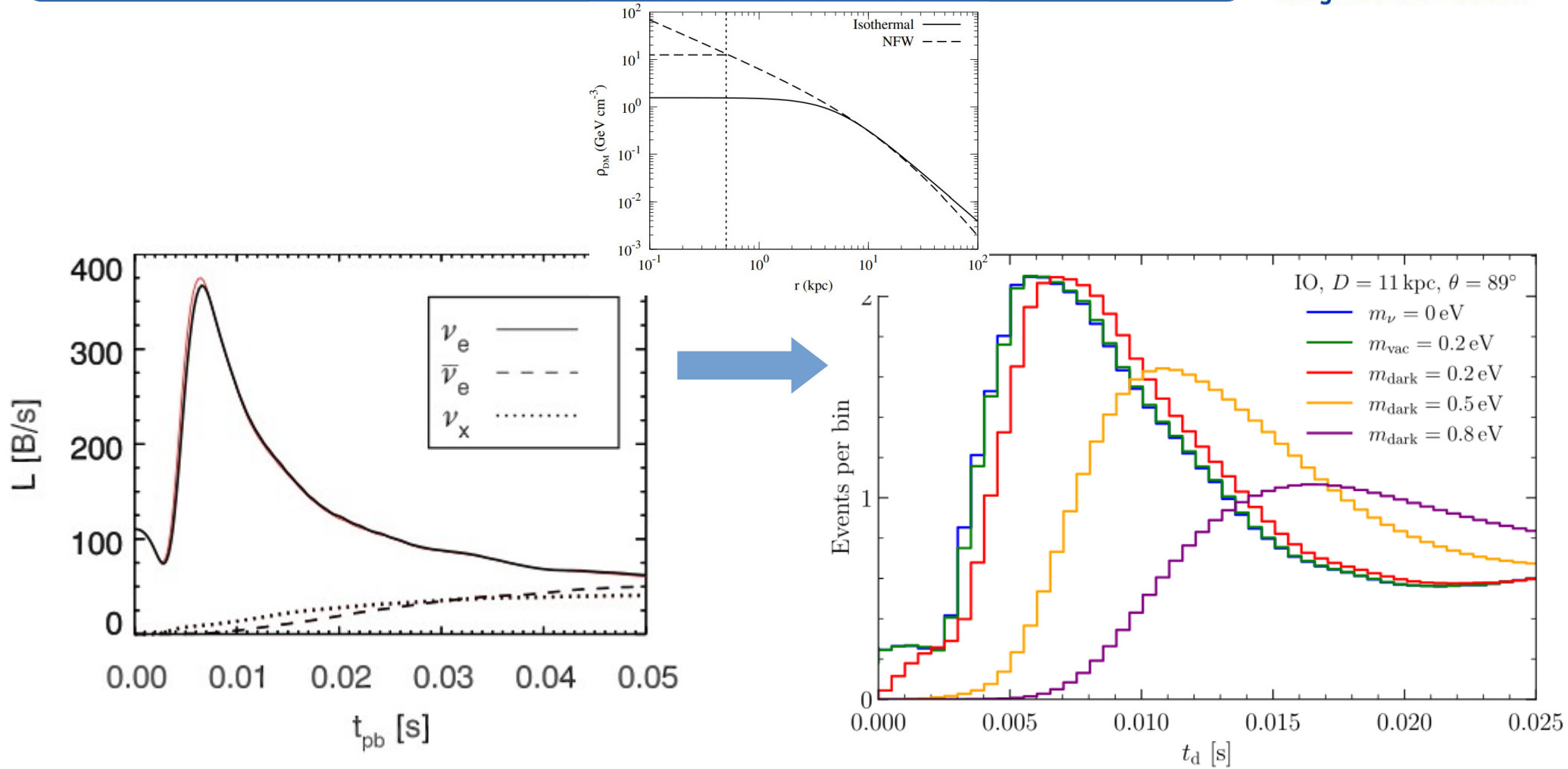
Thank You



李政道研究所
Tsung-Dao Lee Institute

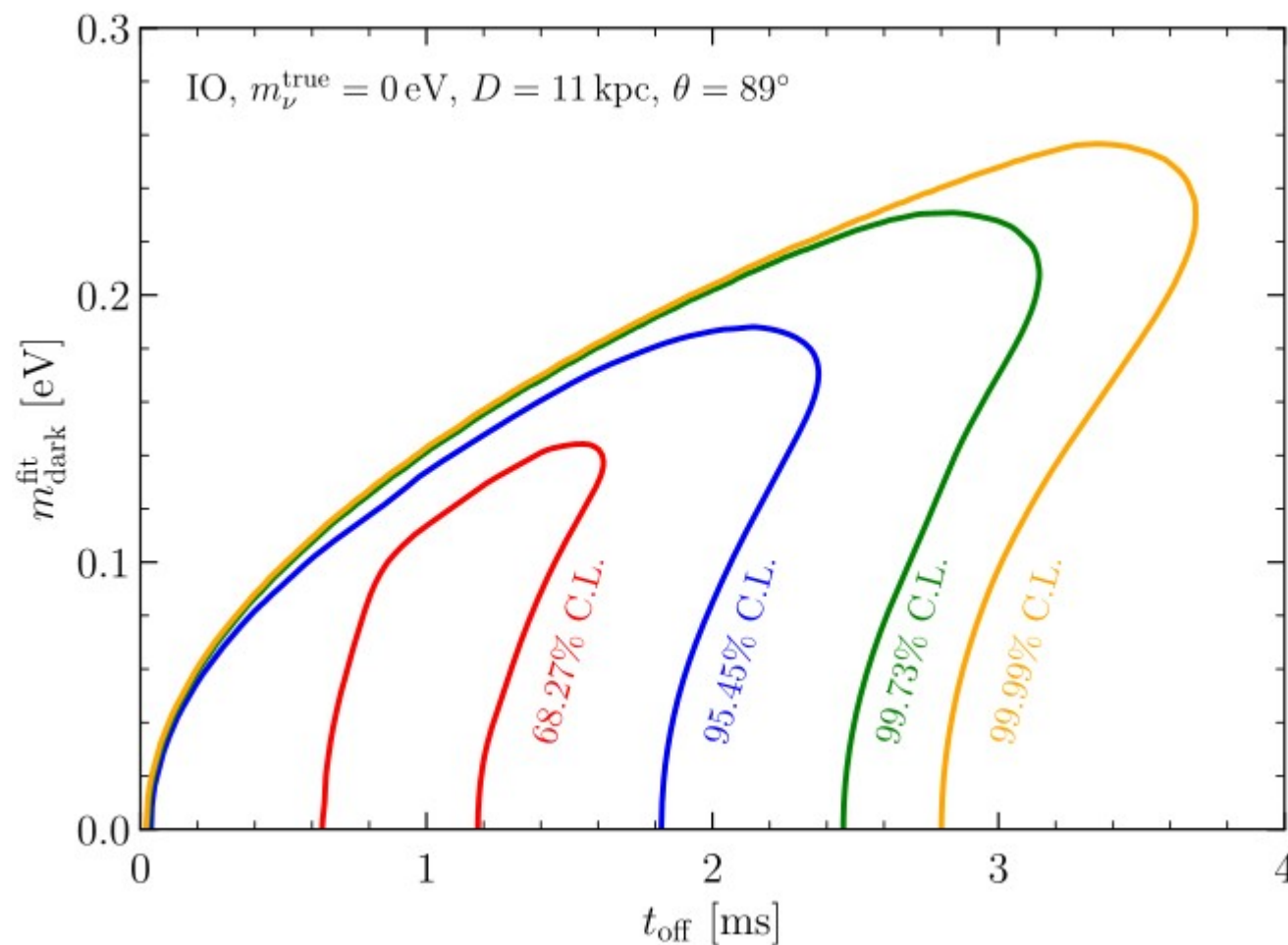
Backup Slides

Dark Mass with SN



$$\Delta t_{\text{dark}} = \frac{m_{\text{dark}}^2(\mathbf{x}_\odot) D \int_{\mathbf{x}_*}^{\mathbf{x}_\odot} \rho_\phi(\mathbf{x}) |d\mathbf{x}|}{2E_\nu^2 D \rho_\phi(\mathbf{x}_\odot)} \equiv \Delta t_\odot \frac{\overline{\rho_\phi}(\mathbf{x}_*)}{\rho_\phi(\mathbf{x}_\odot)}$$

SFG, Chui-Fan Kong, Alexei Smirnov [2404.17352]

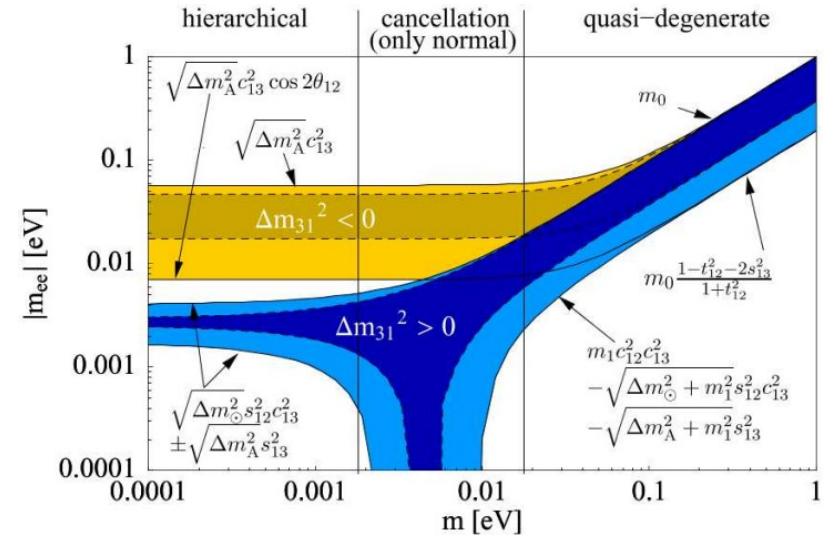
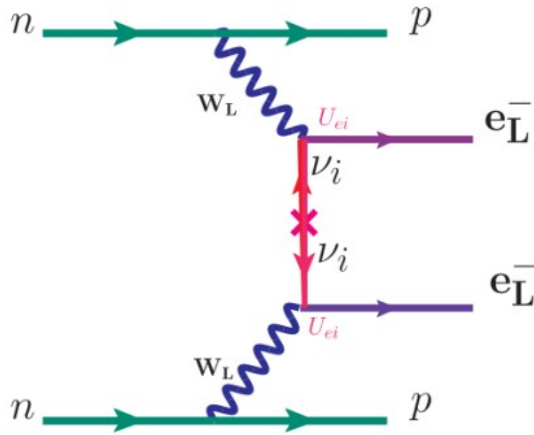


$$\Delta t_{\text{dark}} = \frac{m_{\text{dark}}^2(\mathbf{x}_\odot) D}{2E_\nu^2} \frac{\int_{\mathbf{x}_\star}^{\mathbf{x}_\odot} \rho_\phi(\mathbf{x}) |d\mathbf{x}|}{D \rho_\phi(\mathbf{x}_\odot)} \equiv \Delta t_\odot \frac{\overline{\rho}_\phi(\mathbf{x}_\star)}{\rho_\phi(\mathbf{x}_\odot)}$$

SFG, Chui-Fan Kong, Alexei Smirnov [2404.17352]

Neutrinoless Double Beta Decay

- Mediated by **Majorana Neutrino** + **Lepton # Violation**



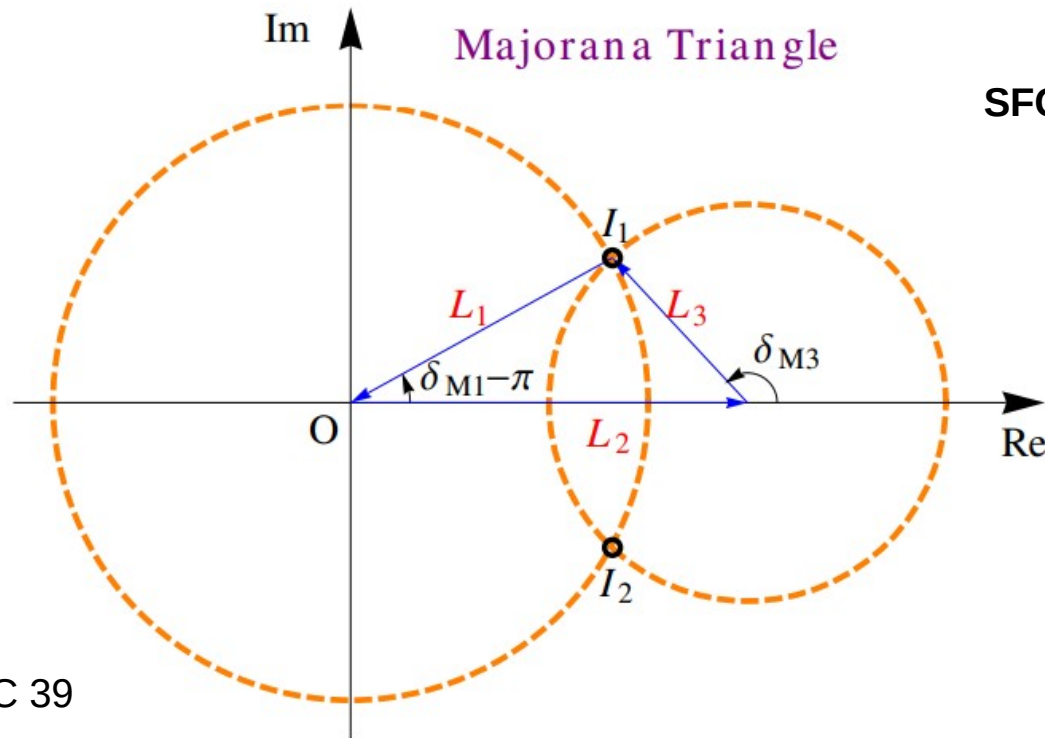
- Mass Suppression**

$$\mathcal{M} \propto \sum_i U_{ei} \frac{i}{p - m_i} U_{ei} \approx \sum_i U_{ei} \frac{m_i}{p^2} U_{ei}$$

- Effective Mass**

$$\langle m \rangle_{ee} \equiv \left| \sum_i m_i U_{ei}^2 \right| = \left| c_s^2 c_r^2 m_1 e^{i\delta_{M1}} + s_s^2 c_r^2 m_2 + s_r^2 m_3 e^{i\delta_{M3}} \right|$$

Majorana Triangle



SFG & Manfred Lindner, PRD
95 (2017) No.3, 033003
[arXiv:1608.01618]

Xing & Zhou, Chin.Phys.C 39
(2015) [arXiv:1404.7001]

$$\langle m \rangle_{ee} \equiv \vec{L}_1 + \vec{L}_2 + \vec{L}_3$$

$$\vec{L}_1 \equiv m_1 U_{e1}^2 = m_1 c_r^2 c_s^2 e^{i\delta_{M1}},$$

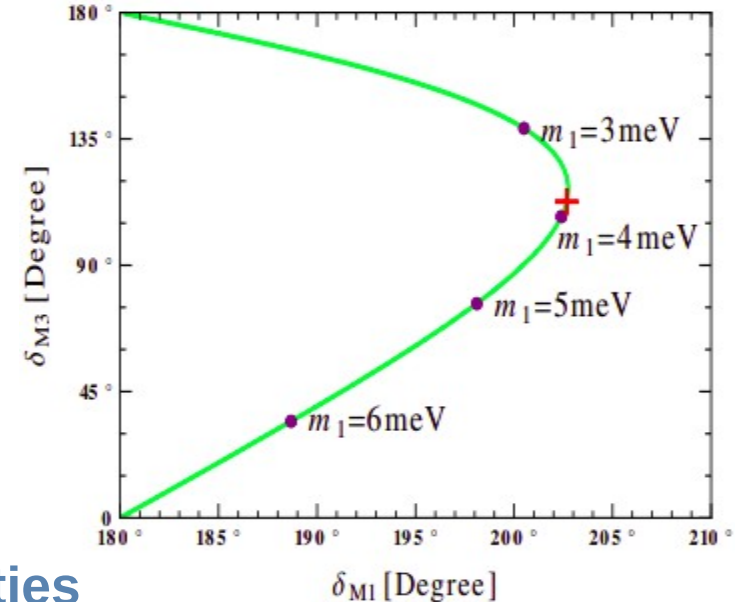
$$\vec{L}_2 \equiv m_2 U_{e2}^2 = \sqrt{m_1^2 + \Delta m_s^2} c_r^2 s_s^2,$$

$$\vec{L}_3 \equiv m_3 U_{e3}^2 = \sqrt{m_1^2 + \Delta m_a^2} s_r^2 e^{i\delta_{M3}}.$$

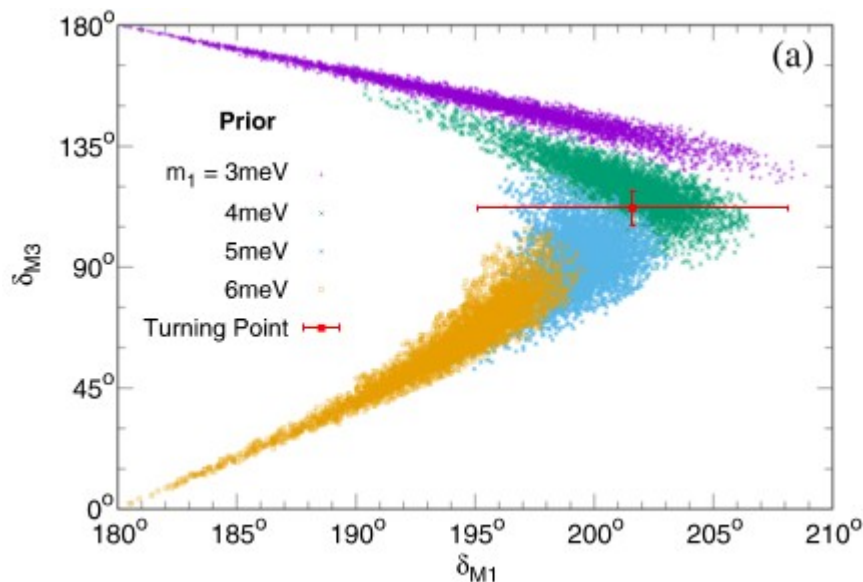
Catching 2 Majorana CP Phases

$$\cos \delta_{M1} = -\frac{m_1^2 c_r^4 c_s^4 + m_2^2 c_r^4 s_s^4 - m_3^2 s_r^4}{2m_1 m_2 c_r^4 c_s^2 s_s^2}$$

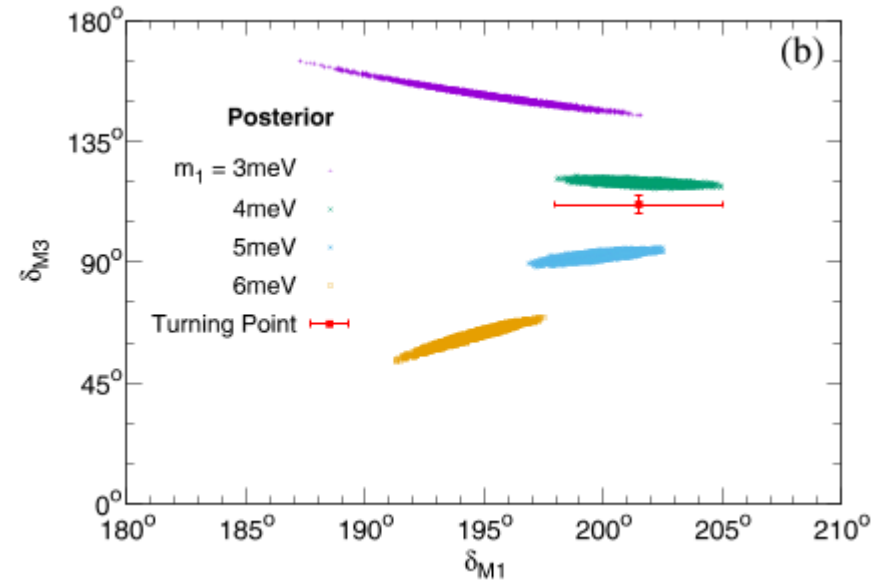
$$\cos \delta_{M3} = +\frac{m_1^2 c_r^4 c_s^4 - m_2^2 c_r^4 s_s^4 - m_3^2 s_r^4}{2m_2 m_3 c_r^2 s_r^2 s_s^2}$$



- JUNO can significantly reduce uncertainties

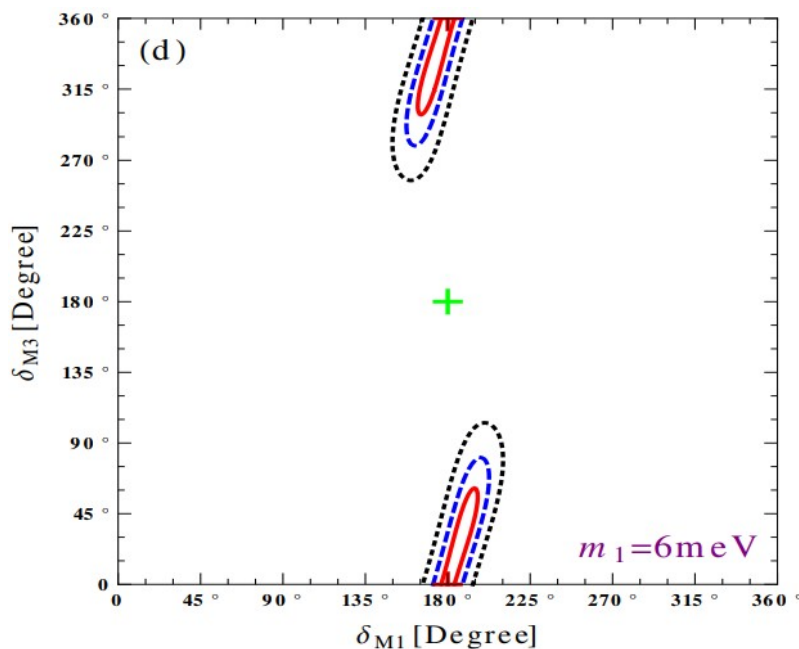
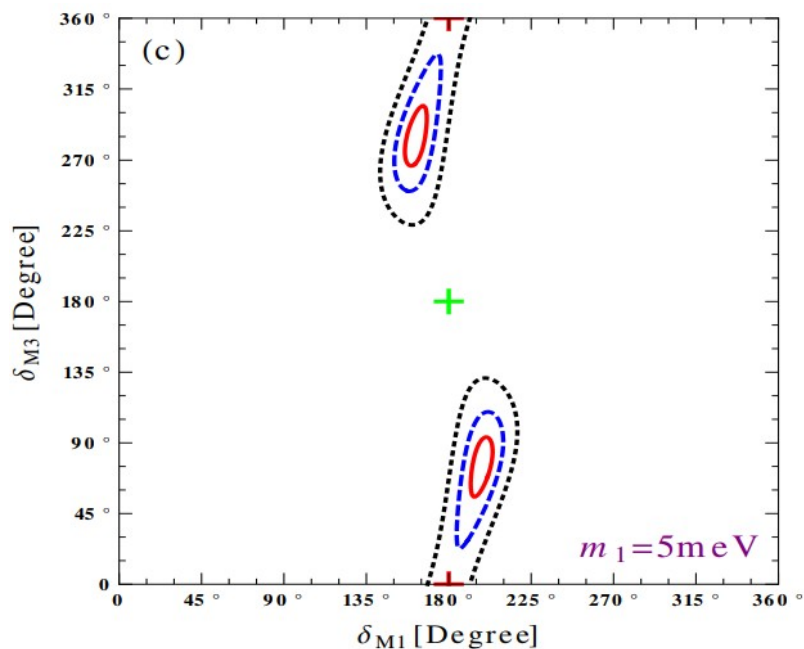
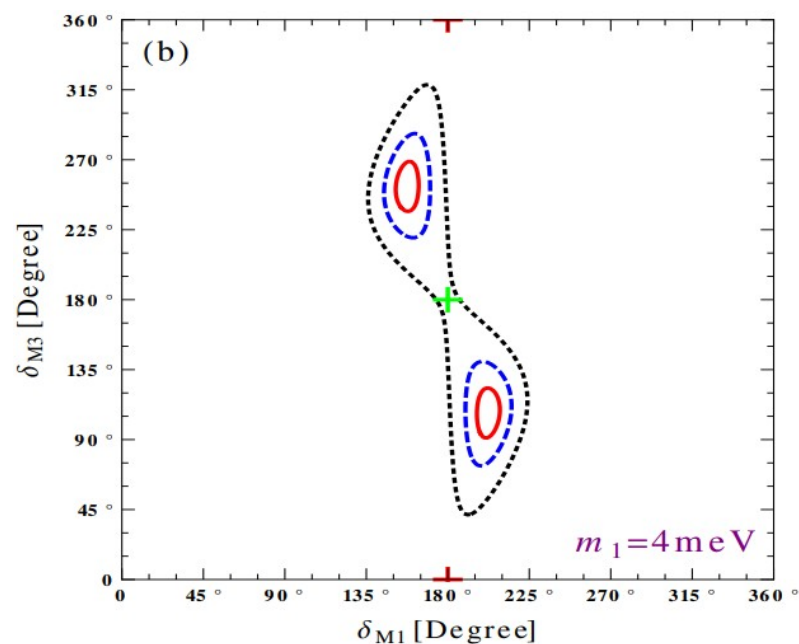
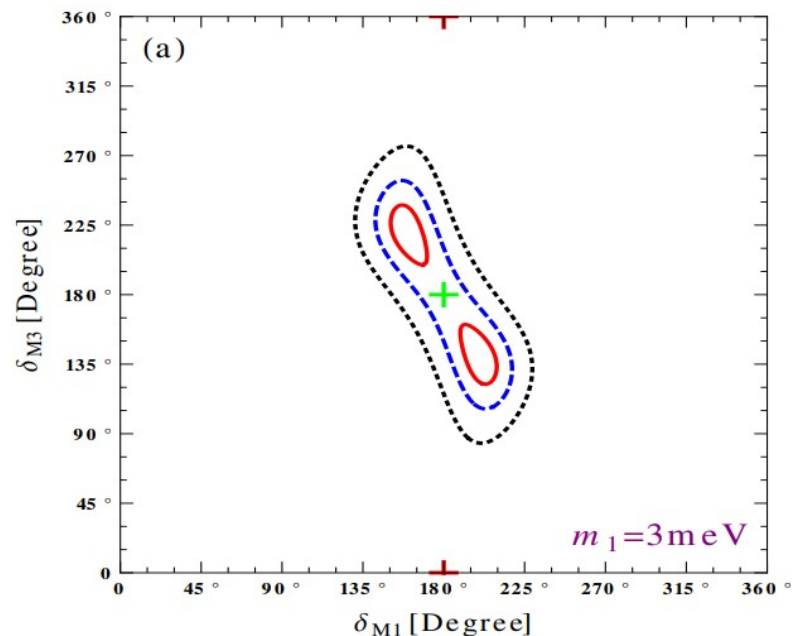


SFG & Manfred Lindner, [1608.01618]

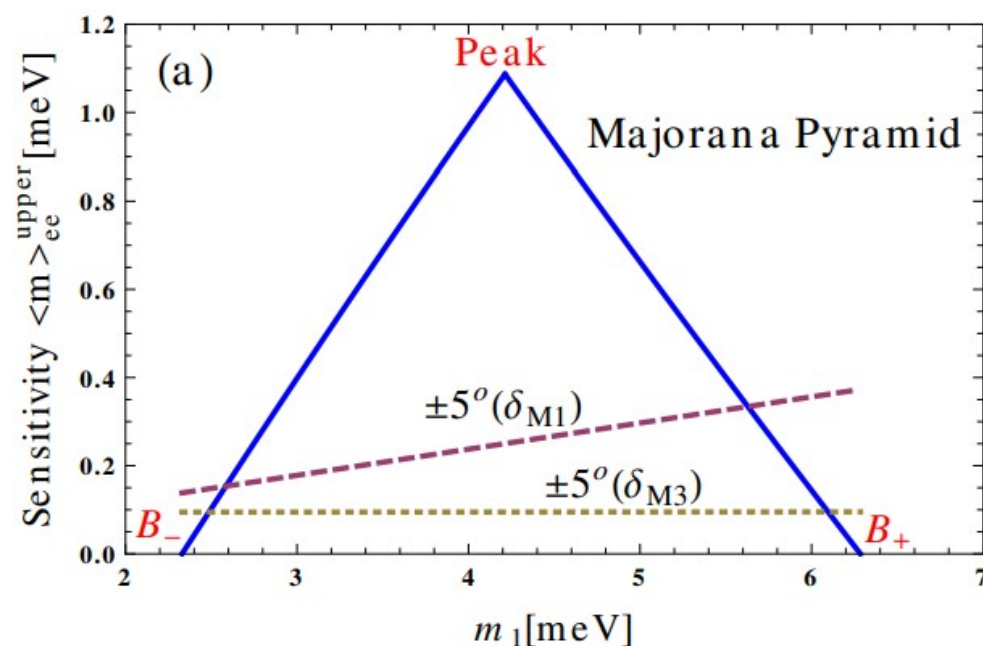
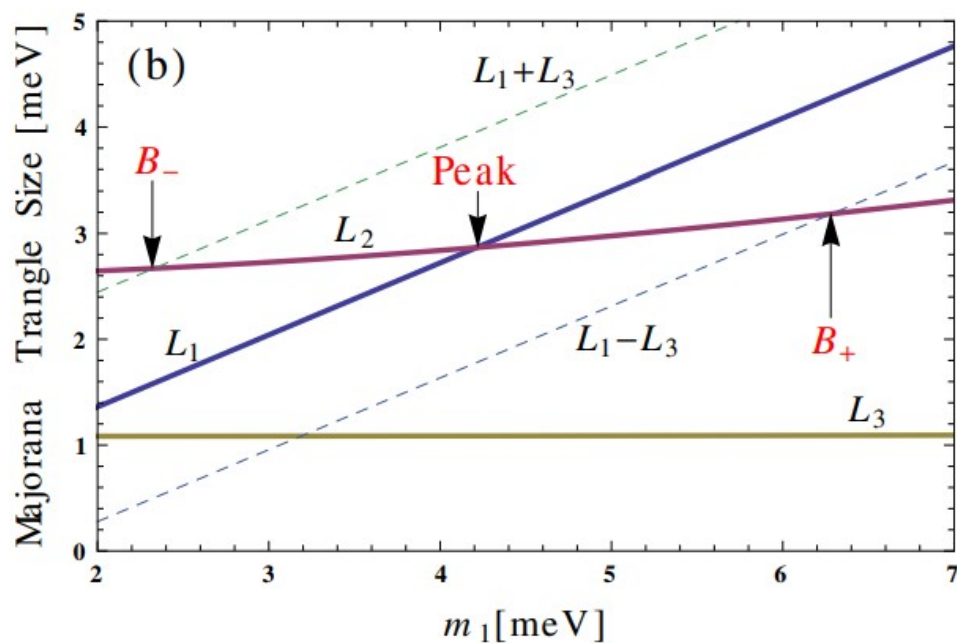
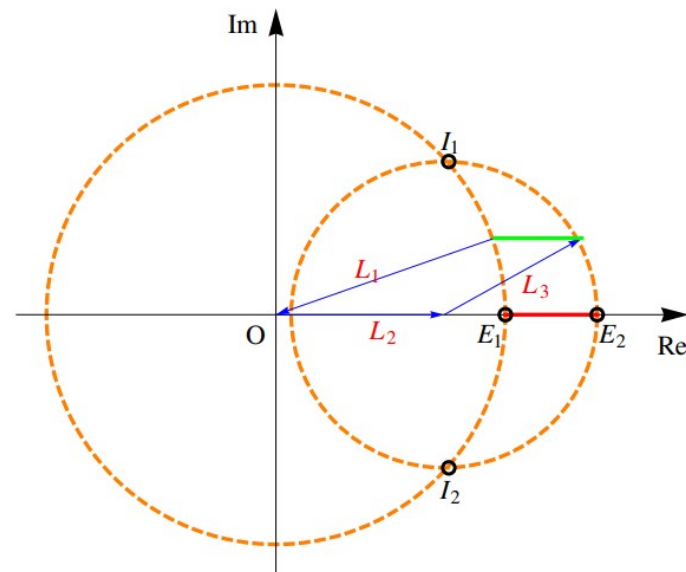
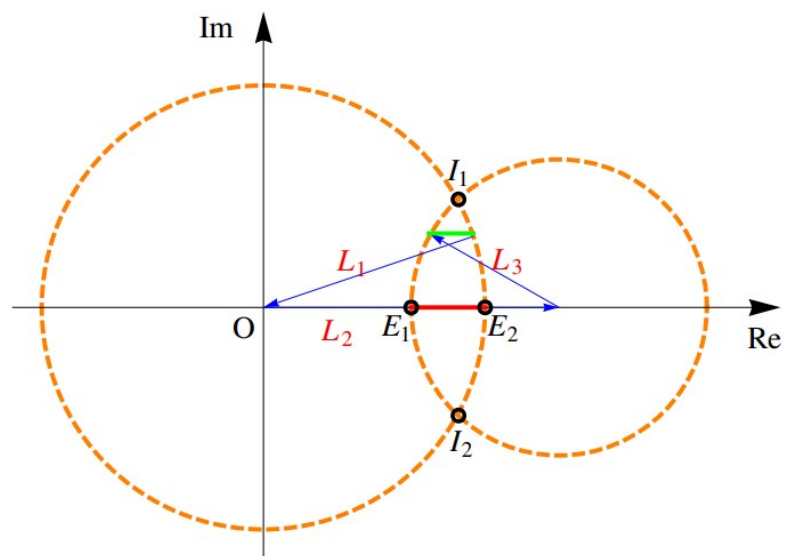


see also SFG & Rodejohann [1507.05514]

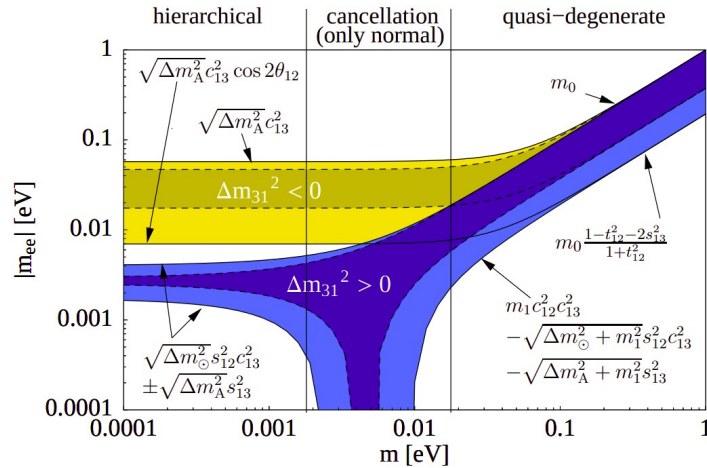
Uncertainty from m_{ee}



Majorana Pyramid



1meV frontier of $0\nu 2\beta$



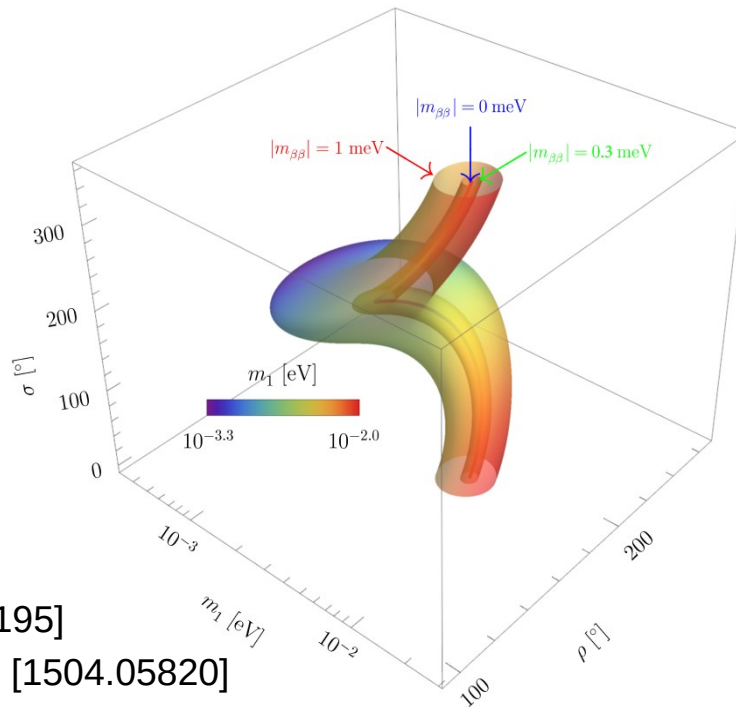
- Nonzero $\rightarrow$ only 1 Majorana CP

$$|m_{ee}| = f$$

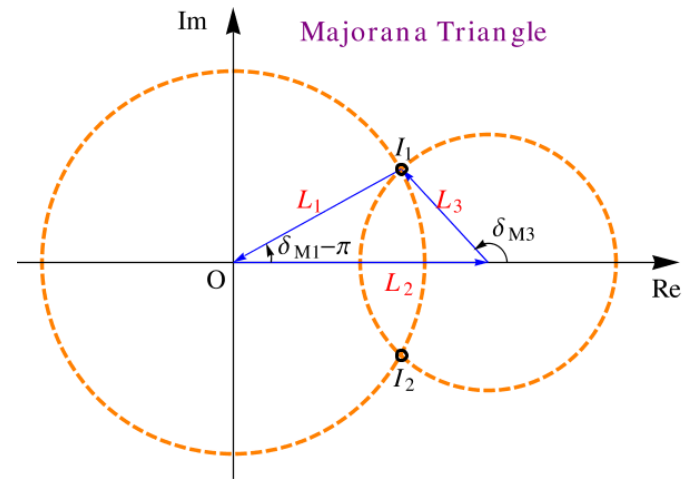
- Zero $\rightarrow$ 2 Majorana CP phases

$$|m_{ee}| = 0 \Rightarrow \mathbb{R}(m_{ee}) = \mathbb{I}(m_{ee}) = 0$$

$$|m_{ee}| < f \Rightarrow \mathbb{R}(m_{ee}) < f \quad \mathbb{I}(m_{ee}) < f$$



$$m_{ee} = c_r^2 c_s^2 m_1 e^{i\tilde{\delta}_{M1}} + c_r^2 s_s^2 m_2 + s_r^2 m_3 e^{i\tilde{\delta}_{M3}}$$



SFG & Manfred Lindner, [1608.01618]

Xing [hep-ph/0305195]

Xing, Zhao & Zhou [1504.05820]

Xing & Zhao [1612.08538]

Cao, Huang, Li, Wang, Wen, Xing, Zhao & Zhou [1908.08355]

Prey of Leptonic CP Phases



• Non-Standard Interactions

$$\mathcal{H} \equiv \frac{1}{2\mathbf{E}_\nu} U \begin{pmatrix} 0 & & \\ & \Delta m_s^2 & \\ & & \Delta m_a^2 \end{pmatrix} U^\dagger + V_{cc} \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu}^* & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau}^* & \epsilon_{\mu\tau}^* & \epsilon_{\tau\tau} \end{pmatrix}$$

Du, Li, Tang, Vihonen & Yu [2011.14292, 2106.15800]

Tang & Zhang [1705.09500]

Du, Li, Tang, Vihonen & Yu [2106.15800]

Scalar NSI: SFG & Parke [1812.08376] Smirnov & Xu [1909.07505]

• Non-Unitary Mixing

$$N = N^{NP} U = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ |\alpha_{21}|e^{i\phi} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} U$$

SFG, Pasquini, Tortola & Valle [1605.01670]

Tang, Zhang & Li [1708.04909]

Hu, Ling, Tang & Wang [2008.09730]

• Sterile neutrinos

Chatterjee & Palazzo [2005.10338]

• Lorentz violation

Rahaman, Razzaque & Sankar [2201.03250]

• Dark NSI

Berlin [1608.01307]

Zhao [1701.02735]

Brdar, Kopp, Liu, Prass & Wang [1705.09455]

Liao, Marfatia & Whisnant [1803.01773]

Chao, Hu, Jiang & Jin [2009.14703]

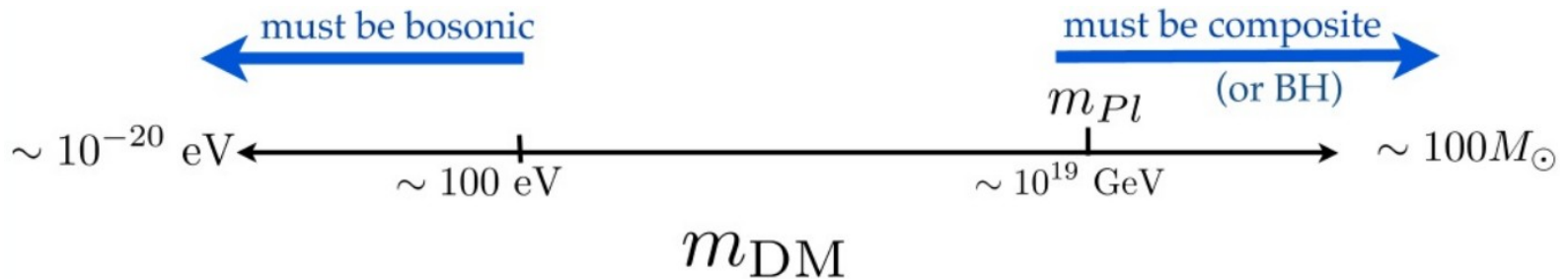
SFG, Murayama [1904.02518]

SFG, PoS NuFact2019 (2020) 108

SFG, J.Phys.Conf.Ser. 1468 (2020) 1, 012125

3. Dark NSI

- Wave DM can be as light as 10^{-22} eV



$$-\mathcal{L} = \frac{1}{2}m_{\phi}^2\phi^2 + \frac{1}{2}M_{\alpha\beta}\bar{\nu}_{\alpha}\nu_{\beta} + y_{\alpha\beta}\phi\bar{\nu}_{\alpha}\nu_{\beta} + h.c.$$

- Bose-Einstein Condensation** $\langle\phi\rangle \neq 0$

$$\phi(x) \simeq \frac{\sqrt{2\rho_{\text{DM}}(x)}}{m_{\phi}} \cos [m_{\phi}(t - \vec{v} \cdot \vec{x})]$$

Berlin [1608.01307]

Zhao [1701.02735]

Brdar, Kopp, Liu, Prass & Wang [1705.09455]

Time-Varying oscillation probabilities!