



Neutrinoless double beta decay in minimal type-I seesaw mechanism

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Based on the work with Fang, Li and Zhang, [arXiv:2404.12316](#)

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➤ **Brief background**

➤ **Theoretical framework**

$0\nu 2\beta$ process in minimal Type-I seesaw mechanism

➤ **Numerical results**

Constraints (sensitivities) of minimal Type-I seesaw from current (future) $0\nu 2\beta$ experiments

➤ **Conclusions**

About neutrinos

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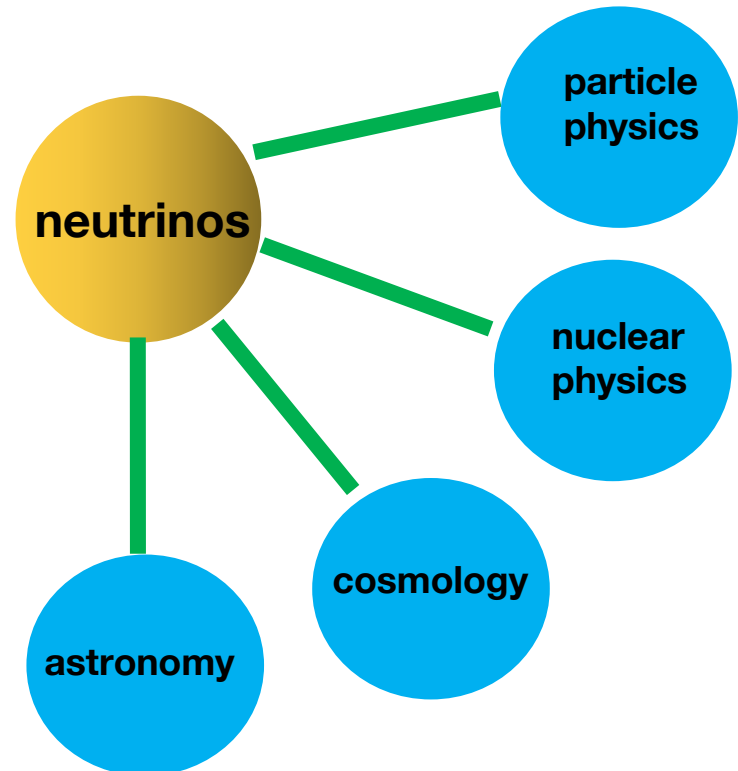


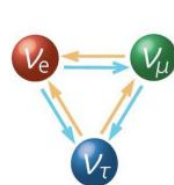
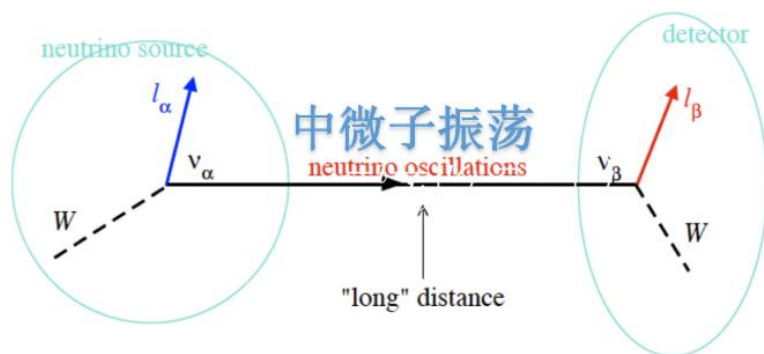
Neutrinos oscillate (only proven new physics in particle physics)
1998 (SuperK)

Precise neutrino oscillation parameters?
Absolute neutrino mass?
Neutrino mass origin?
Dirac or Majorana nature?
Relation to matter-antimatter asymmetry?
more unknowns...

Good portal to more new physics

SM is definitely not the end story





$$\begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

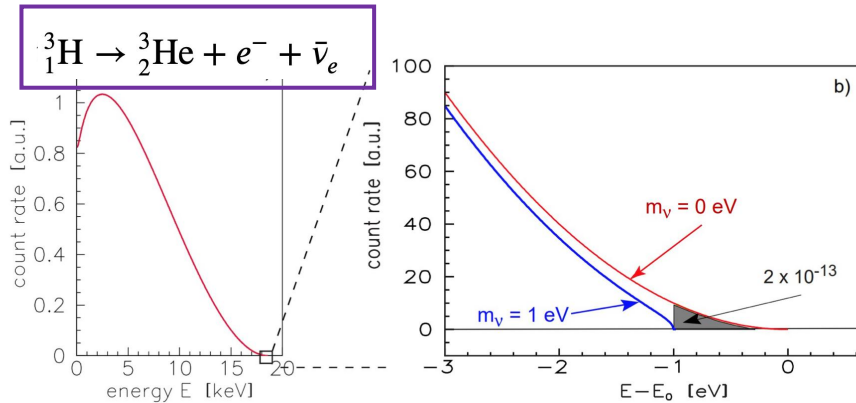
I. Esteban, M. C. Gonzalez-Garcia, A. Hernandez-Cabezudo, et al.,

相对精度 (1 σ /bf)		NuFIT 5.2	正质量顺序		?	倒质量顺序 ($\Delta\chi^2 = 6.4$)	
			最佳拟合 $\pm 1\sigma$	3 σ 范围		最佳拟合 $\pm 1\sigma$	3 σ 范围
2%	✓	$\theta_{12}/^\circ$	$33.41^{+0.75}_{-0.72}$	$31.31 \rightarrow 35.74$		$33.41^{+0.75}_{-0.72}$	$31.31 \rightarrow 35.74$
2%	✓	$\theta_{23}/^\circ$	$42.2^{+1.1}_{-0.9}$	$39.7 \rightarrow 51.0$		$49.0^{+1.0}_{-1.2}$	$39.9 \rightarrow 51.5$
1%	✓	$\theta_{13}/^\circ$	$8.58^{+0.11}_{-0.11}$	$8.23 \rightarrow 8.91$		$8.57^{+0.11}_{-0.11}$	$8.23 \rightarrow 8.94$
13%	?	$\delta/^\circ$	232^{+36}_{-26}	$144 \rightarrow 350$		276^{+22}_{-29}	$194 \rightarrow 344$
3%	✓	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.41^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.03$		$7.41^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.03$
1%	✓	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.507^{+0.026}_{-0.027}$	$+2.427 \rightarrow +2.590$		$-2.486^{+0.025}_{-0.028}$	$-2.570 \rightarrow -2.406$

Not sensitive to
absolute neutrino
mass

Precise measurement era

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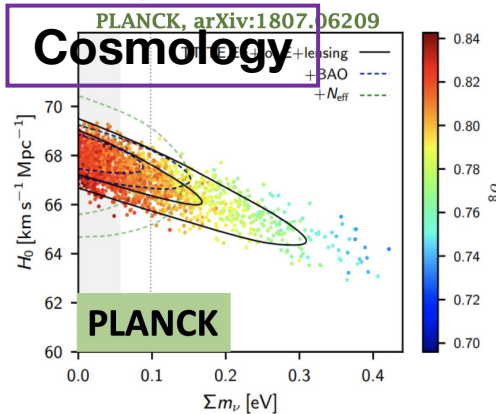


$m_\beta < 0.8 \text{ eV (90\% CL)}$

KATRIN 最终的灵敏度

$m_\beta < 0.2 \text{ eV (90\% CL)}$

$m_1 < 0.2 \text{ eV (90\% CL)}$



Planck TT, TE, EE + lowE + lensing + BAO

$\Sigma < 0.12 \text{ eV (95\% CL)}$

$m_1 < 0.03 \text{ eV (95\% CL, NO)}$

Future:

JUNO, DUNE

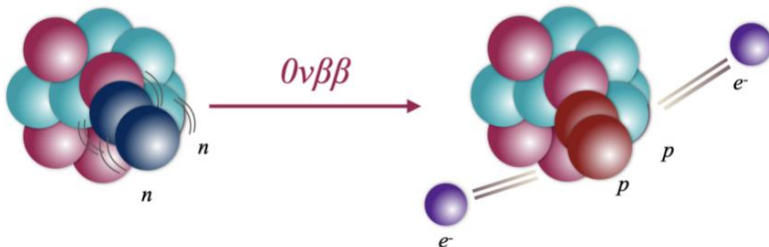
CDEX, PandaX-III,

NuDEX, CUPID,

TRIDENT,

PTOLEMY...

$0\nu 2\beta$



Nuclear physics
Particle physics
Matter antimatter asymmetry

Formulas (minimal type-I seesaw)

6

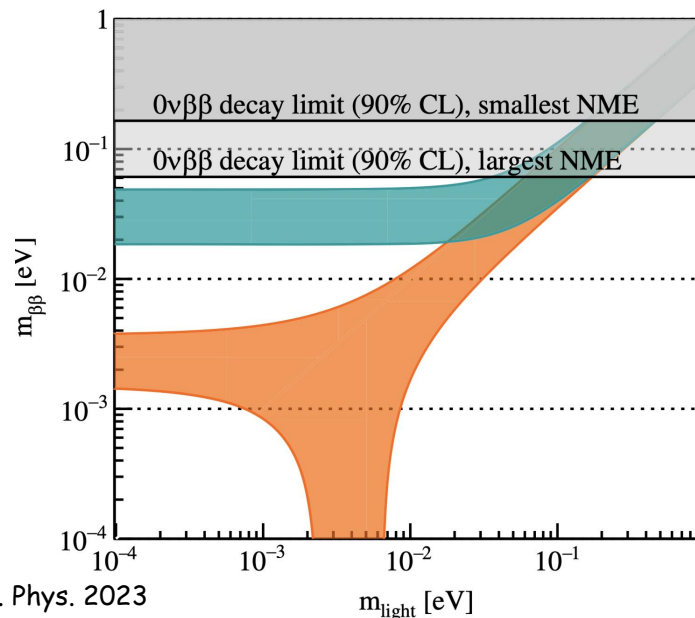
$$\mathcal{L}_{\text{mass}} = -\frac{1}{2} \overline{(\nu_L, N_R^c)} \begin{pmatrix} 0 & M_D \\ M_D^T & M_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix} + \text{h.c.}$$



$$1/T_{1/2}^{0\nu} = G |M_{0\nu}(0) \cdot m_{\text{eff}}|^2$$

$$|m_{\text{eff}}| = \left| |m_{\text{eff}}^\nu| - |m_{\text{eff}}^\nu| f_\beta(M_2) + |R_{e1}^2| e^{2i\delta_{14}} M_1 [f_\beta(M_1) - f_\beta(M_2)] \right|$$

$$f_\beta(M_N) = M_{0\nu}(M_N)/M_{0\nu}(0) \quad \text{Mass dependent nuclear matrix element (NME)}$$



minimal Type-I seesaw
NMO, [1,4] meV
IMO, [15, 50] meV

NME of light neutrinos

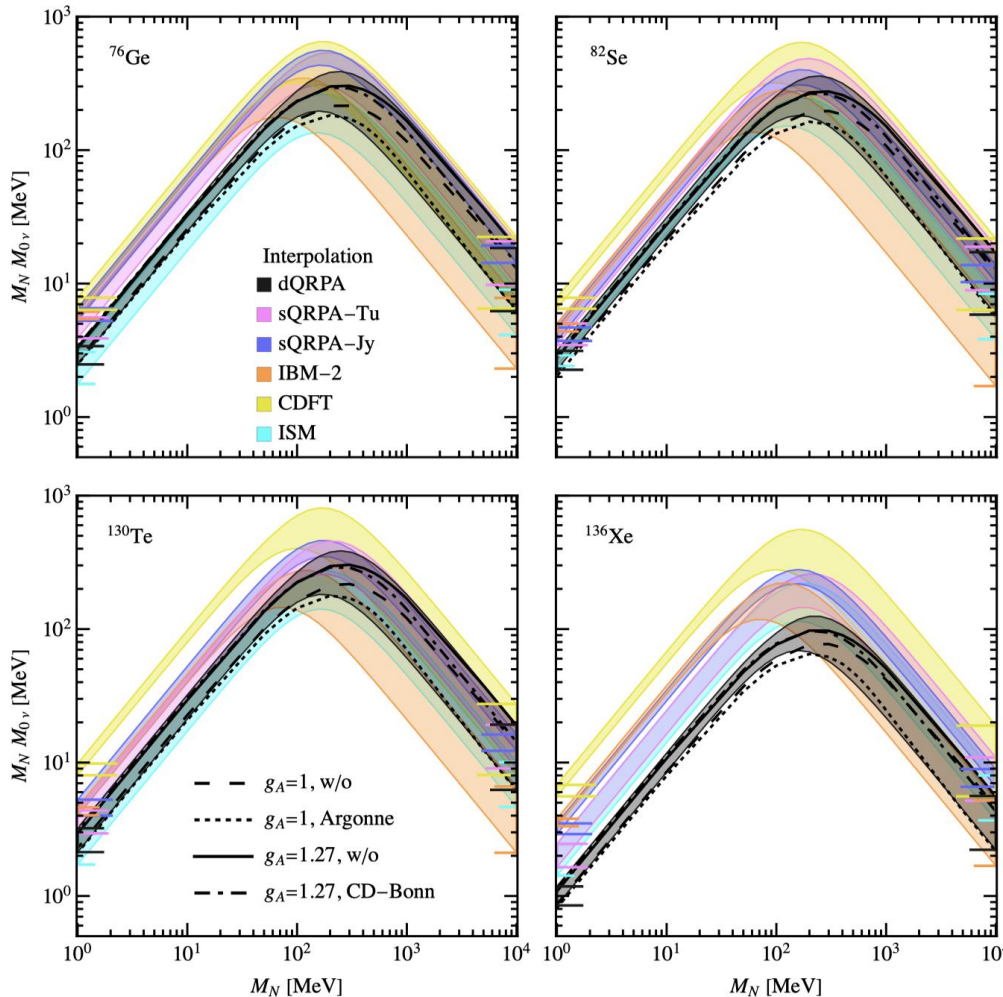
	g_A	src	dQRPA [74]	sQRPA-Tu [75]	sQRPA-Jy [77]	IBM-2 [87]	CDFT [80]	ISM [81]
^{76}Ge	1.27	w/o	3.27	-	-	-	7.61	-
		Argonne	3.12	5.157	-	5.98	7.48	2.89
		CD-Bonn	3.40	5.571	6.54	6.16	7.84	3.07
		Miller-Spencer	-	-	-	5.42	6.36	-
	1.00	w/o	2.64	-	-	-	-	-
		Argonne	2.48	3.886	-	-	-	1.77
^{82}Se		CD-Bonn	2.72	4.221	5.26	-	-	1.88
	1.27	w/o	3.01	-	-	-	7.60	-
		Argonne	2.86	4.642	-	4.84	7.48	2.73
		CD-Bonn	3.13	5.018	4.69	4.99	7.83	2.90
		Miller-Spencer	-	-	-	4.37	6.48	-
	1.00	w/o	2.41	-	-	-	-	-
^{130}Te		Argonne	2.26	3.460	-	-	-	2.41
		CD-Bonn	2.49	3.746	3.73	-	-	2.56
	1.27	w/o	3.10	-	-	-	9.55	-
		Argonne	2.90	3.888	-	4.47	9.38	2.76
		CD-Bonn	3.22	4.373	5.27	4.61	9.82	2.96
		Miller-Spencer	-	-	-	4.03	8.03	-
^{136}Xe	1.00	w/o	2.29	-	-	-	-	-
		Argonne	2.13	2.945	-	-	-	1.72
		CD-Bonn	2.37	3.297	4.00	-	-	1.84
	1.27	w/o	1.12	-	-	-	6.62	-
		Argonne	1.11	2.177	-	3.67	6.51	2.28
		CD-Bonn	1.18	2.460	3.50	3.79	6.80	2.45
^{136}Xe		Miller-Spencer	-	-	-	3.33	5.58	-
	1.00	w/o	0.85	-	-	-	-	-
		Argonne	0.86	1.643	-	-	-	1.42
		CD-Bonn	0.89	1.847	2.91	-	-	1.53

- CDFT biggest
- ISM/dQRPA smallest
- different NME ratios between different isotopes

NME of heavy neutrinos

	g_A	src	dQRPA [74]	sQRPA-Tu [75]	sQRPA-Jy [77]	IBM-2 [87]	CDFT [80]	ISM [81]
^{76}Ge	1.27	w/o	385.4				466.8	
		Argonne	187.3	316		107	267	130
		CD-Bonn	293.7	433	401.3	163	378.1	188
		Miller-Spencer				48.1	135.7	
	1.00	w/o	275.9					
		Argonne	129.7	204				86
		CD-Bonn	207.2	287	298.3			122
^{82}Se	1.27	w/o	358.7				454	
		Argonne	175.9	287		84.4	261.4	121
		CD-Bonn	273.6	394	287.1	132	369	175
		Miller-Spencer				35.6	132.7	
	1.00	w/o	257.4					
		Argonne	122.1	186	-	-	-	80
		CD-Bonn	193.4	262	214.3	-	-	113
^{130}Te	1.27	w/o	401.1				573	
		Argonne	191.4	292		92	339.2	146
		CD-Bonn	303.5	400	338.3	138	472.8	210
		Miller-Spencer				44	168.5	
	1.00	w/o	281.2					
		Argonne	130.2	189	-	-	-	97
		CD-Bonn	209.5	264	255.7	-	-	136
^{136}Xe	1.27	w/o	117.1				394.5	
		Argonne	66.9	166		72.8	234.3	116
		CD-Bonn	90.5	228	186.3	109	326.2	167
		Miller-Spencer	-	-	-	35.1	116.3	
	1.00	w/o	82.7					
		Argonne	46.3	108	-	-	-	77
		CD-Bonn	62.8	152	137.3	-	-	108

- CDFT/sQRPA-Tu biggest
- IBM-2 smallest



➤ **dQRPA:** Numerical calculation

➤ **Others:** interpolation with two extreme values

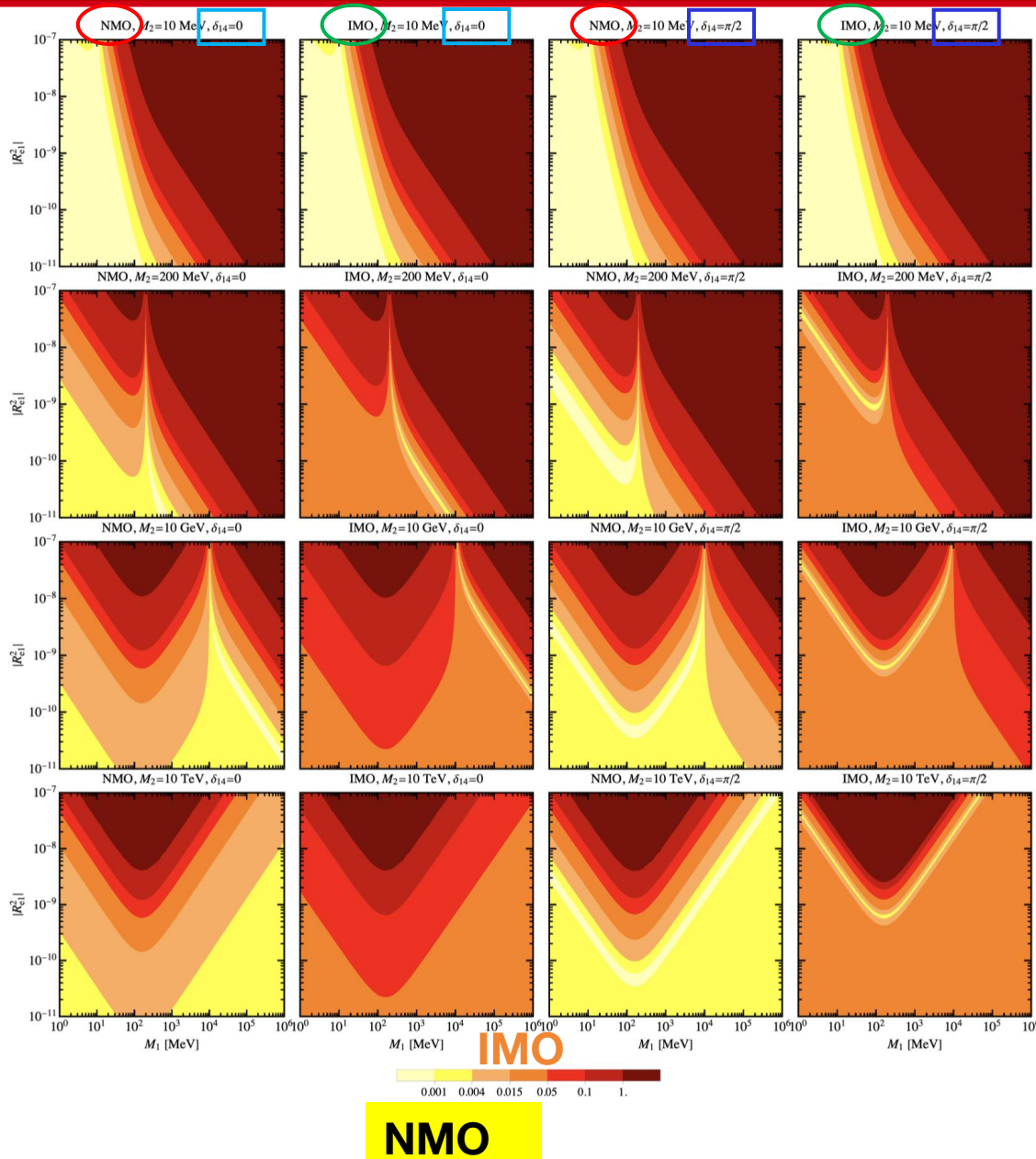
$$M_{0\nu}(m_j) = \frac{m_p m_e}{\langle p^2 \rangle + m_j^2} M_H$$

➤ **dQRPA:** agrees with ISM for light neutrinos and tends to be consistent with CDFT for heavy neutrinos

➤ **In light neutrino mass** the NME from **dQRPA** model is smaller than that of the **IBM-2** model, and in heavy neutrino mass the reverse applies.

Parameter space of m_{eff}

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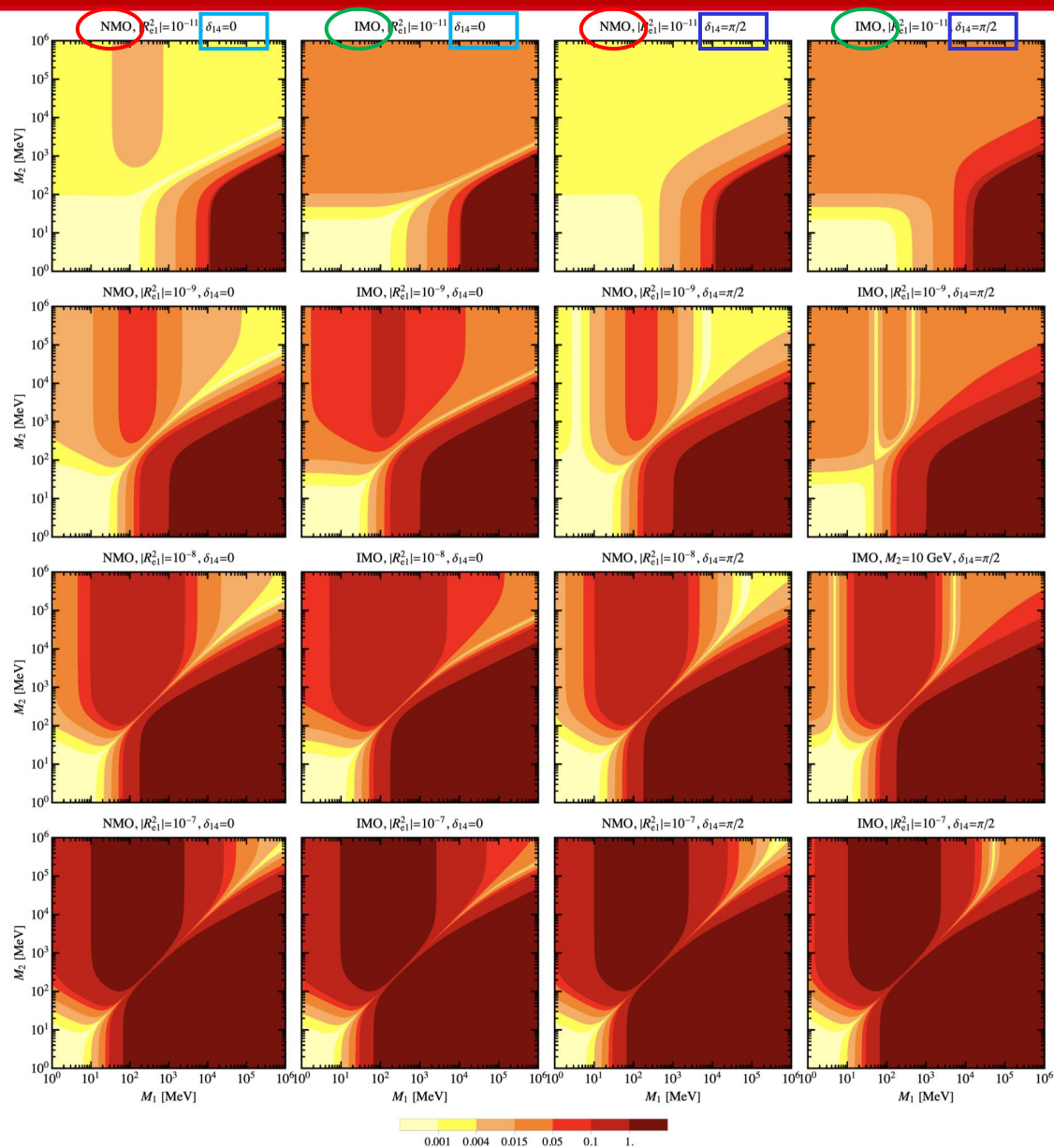


- $g_A=1$, Argonne src
- Some parameter space can be very easily/hardly excluded by current/future $0\nu 2\beta$ experiments
- The NMO/IMO can be very different and δ_{14} matters

See also Fang, Li, Zhang, PLB2022

Parameter space of m_{eff}

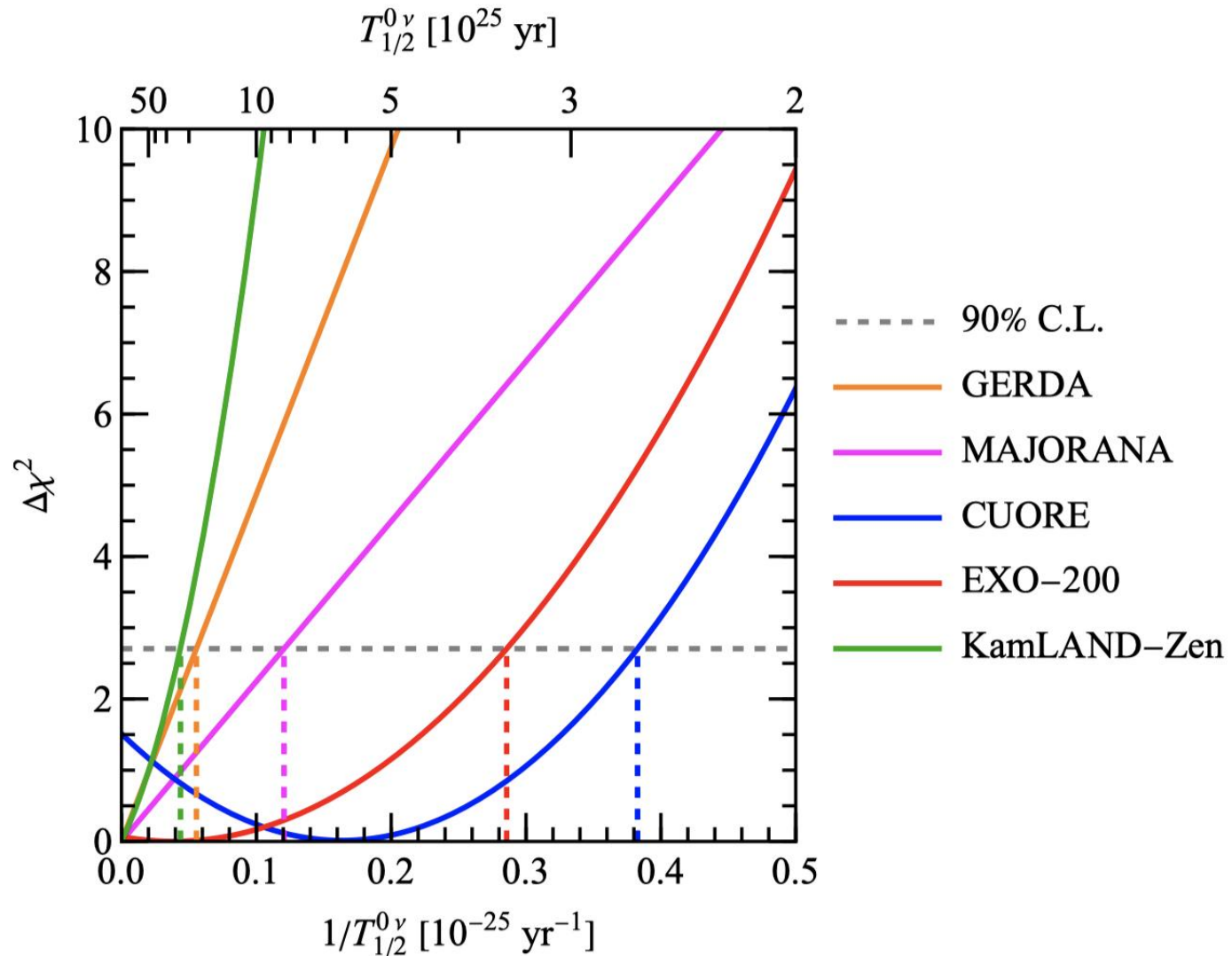
11



$\Delta\chi^2$ functions of inverse half-life

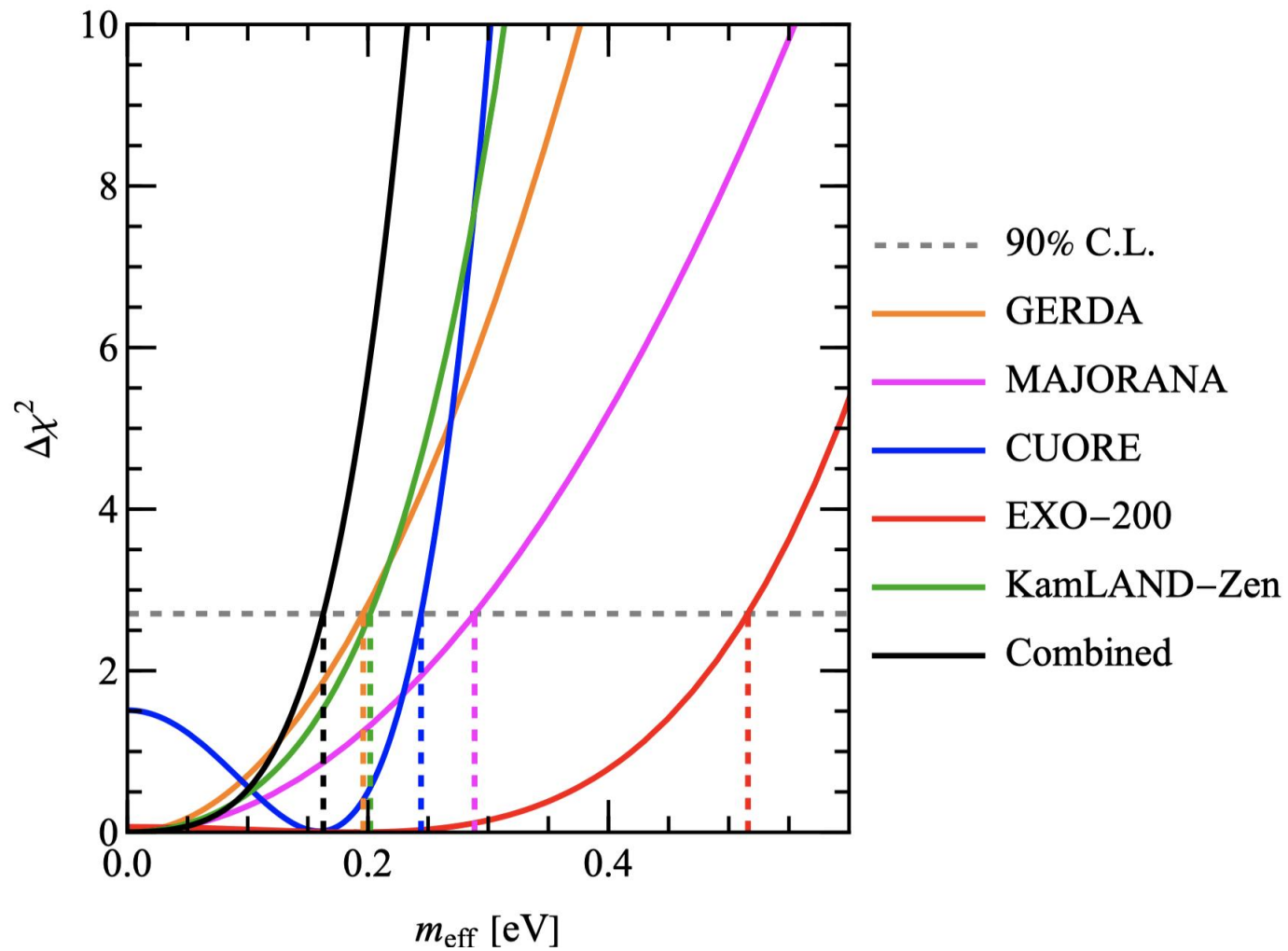
12

$$\Delta\chi_r^2(1/T_{1/2}^{0\nu}) = a_r(1/T_{1/2}^{0\nu})^2 + b_r(1/T_{1/2}^{0\nu}) + c_r$$



$\Delta\chi^2$ functions of m_{eff}

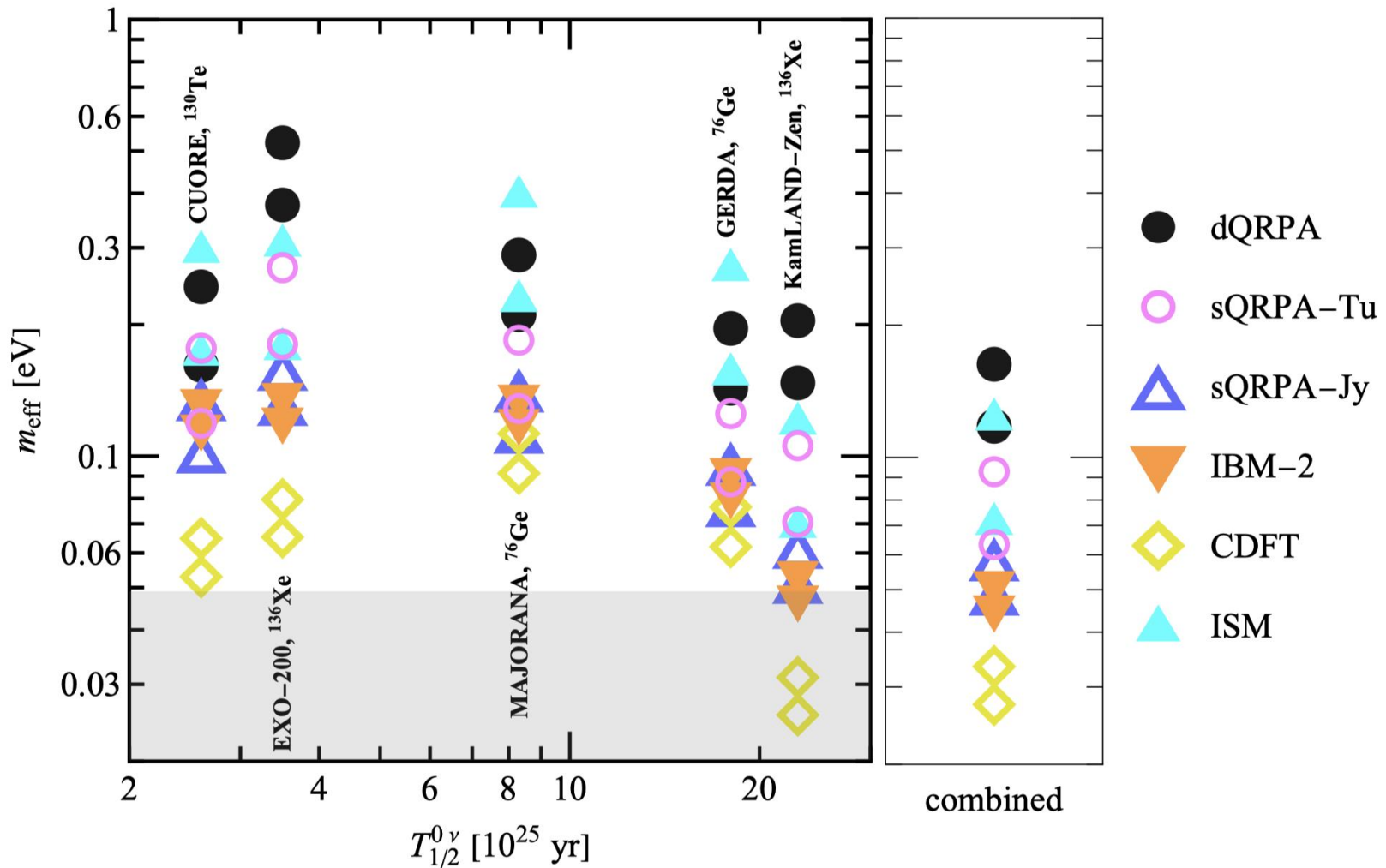
13



$g_A=1$, Argonne src

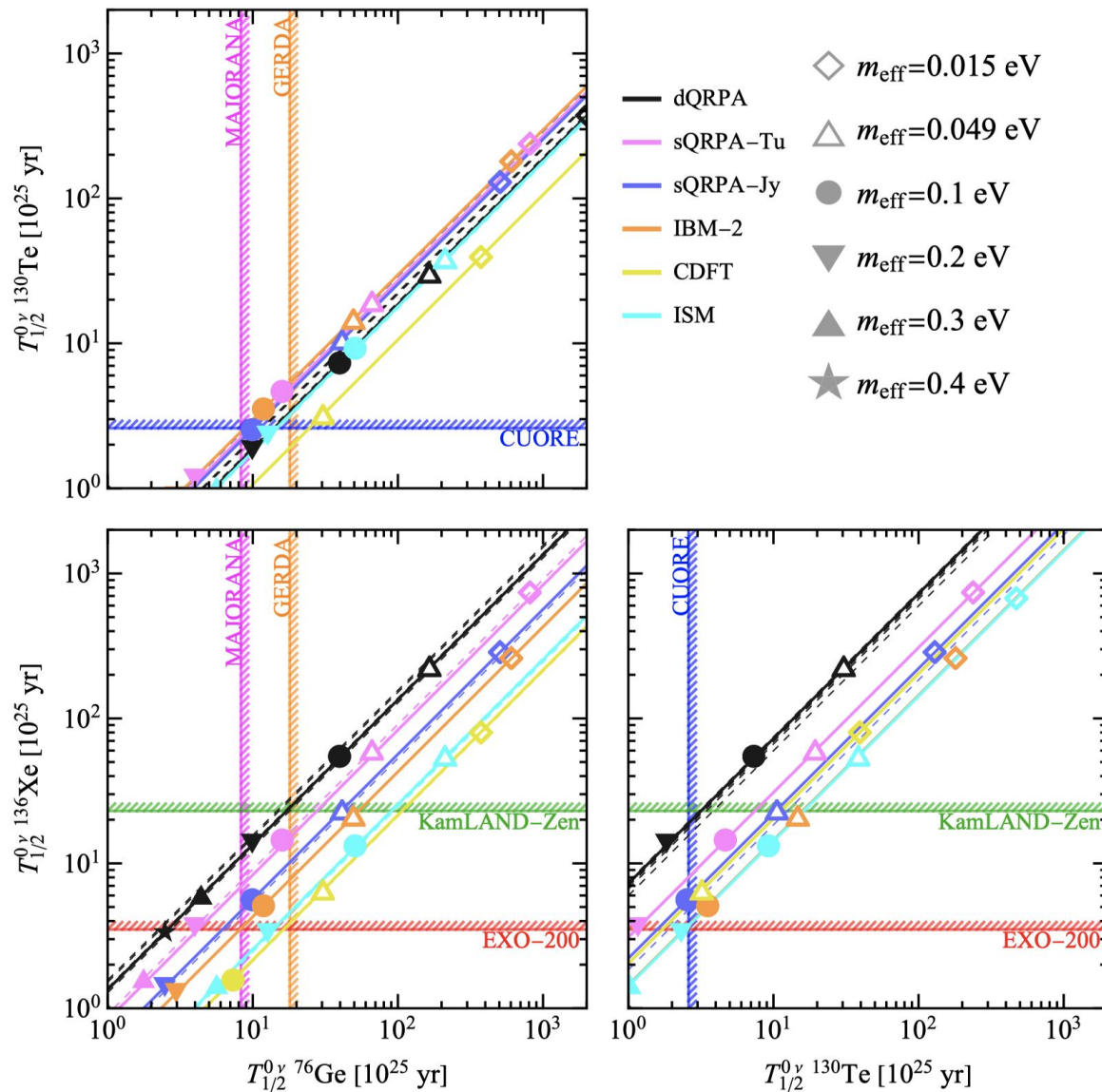
The upper limit of m_{eff}

14



Half-life relations of different isotopes

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$g_A=1.27$, CD-bonn src

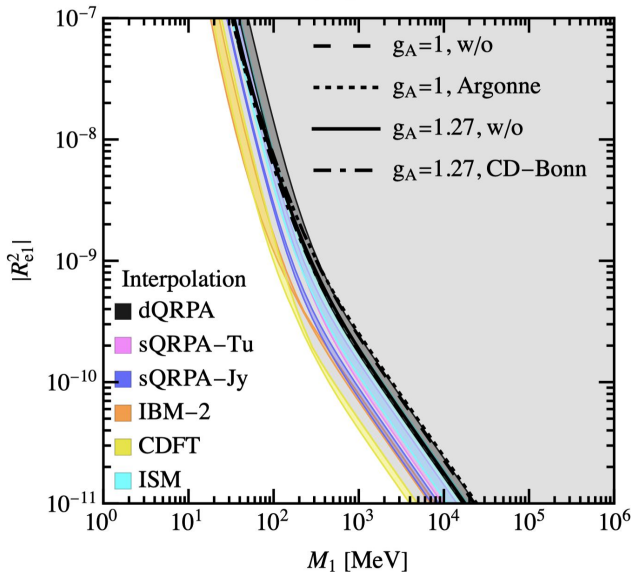
$0\nu 2\beta$ half life

- m_{eff} value
- NME value

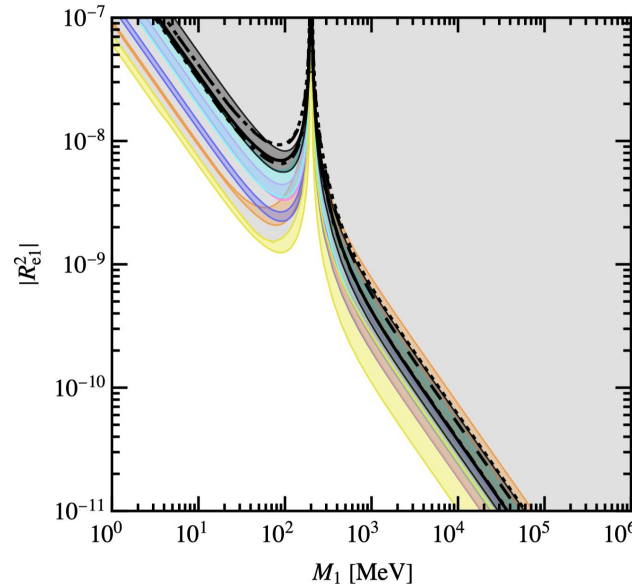
Current limits (M_1 & $|R_{e1}|^2$)

16

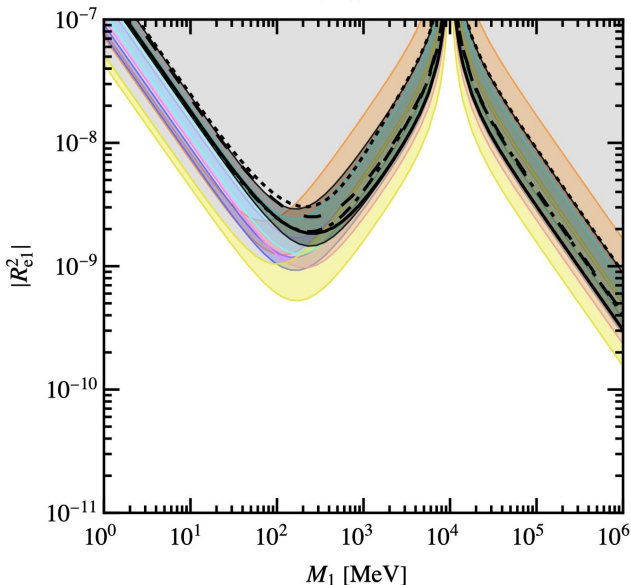
NMO, $M_2 = 10$ MeV



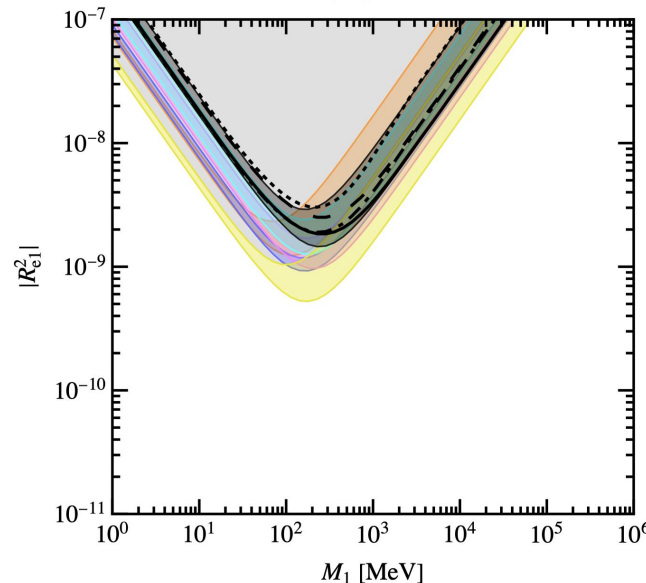
NMO, $M_2 = 200$ MeV



NMO, $M_2 = 10$ GeV



NMO, $M_2 = 10$ TeV

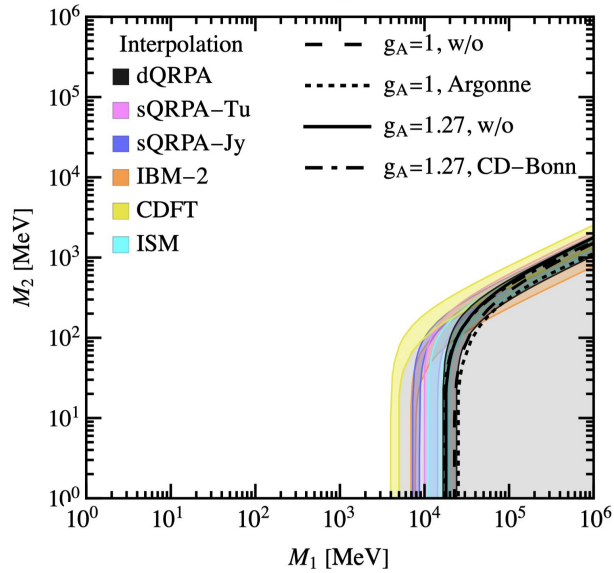


- 3σ C.L
- Gray regions: excluded regions in the case of CDFT model
- Different choices of parameters and models are scanned (not as Gaussian)
- Both the **$0\nu 2\beta$ -decay** and **oscillation data** are used
- The **IMO** case is similar
- The peak shape

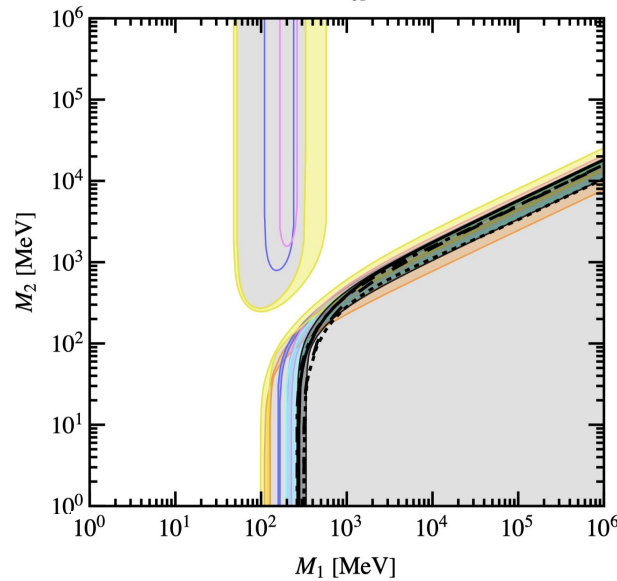
Current limits (M_1 & M_2)

17

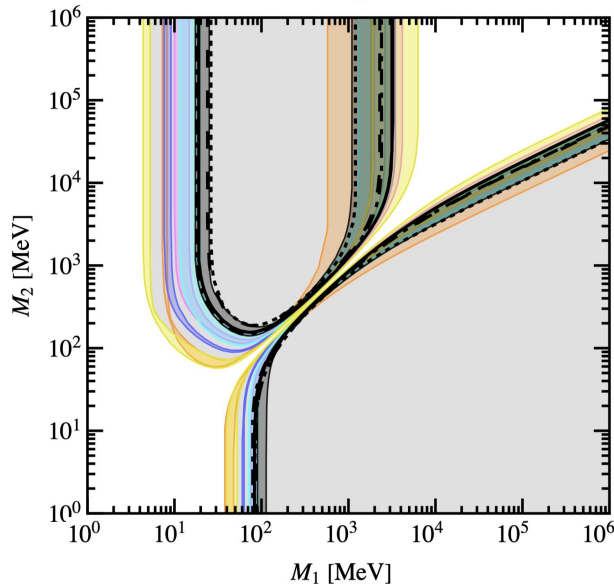
NMO, $|R_{e1}^2|=10^{-11}$



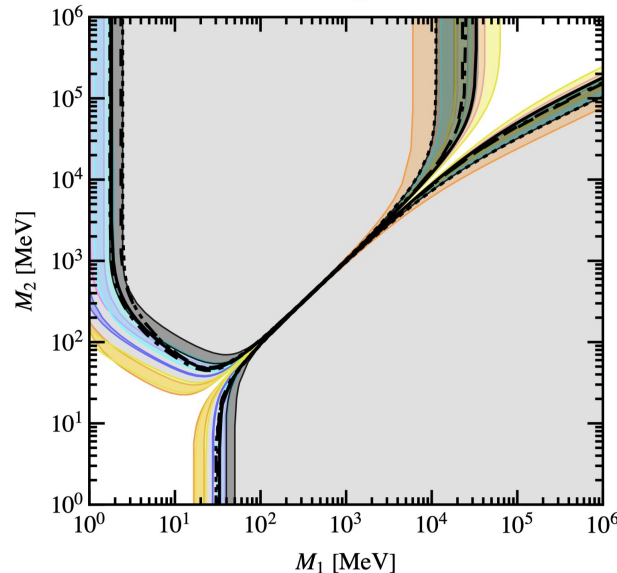
NMO, $|R_{e1}^2|=10^{-9}$



NMO, $|R_{e1}^2|=10^{-8}$



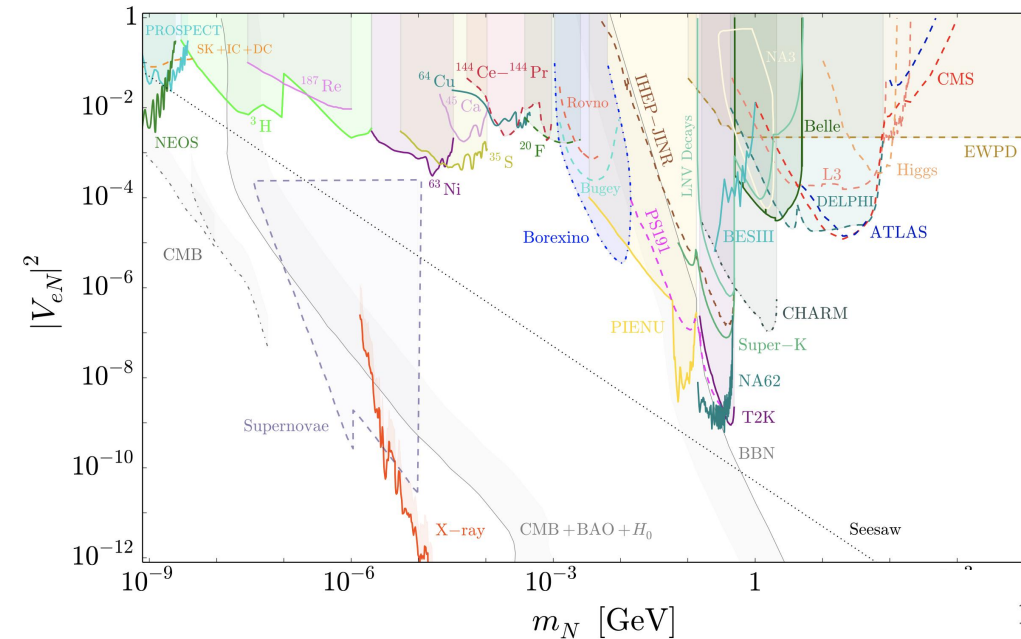
NMO, $|R_{e1}^2|=10^{-7}$



- The IMO case is similar
- The NME hierarchy changes with neutrino mass

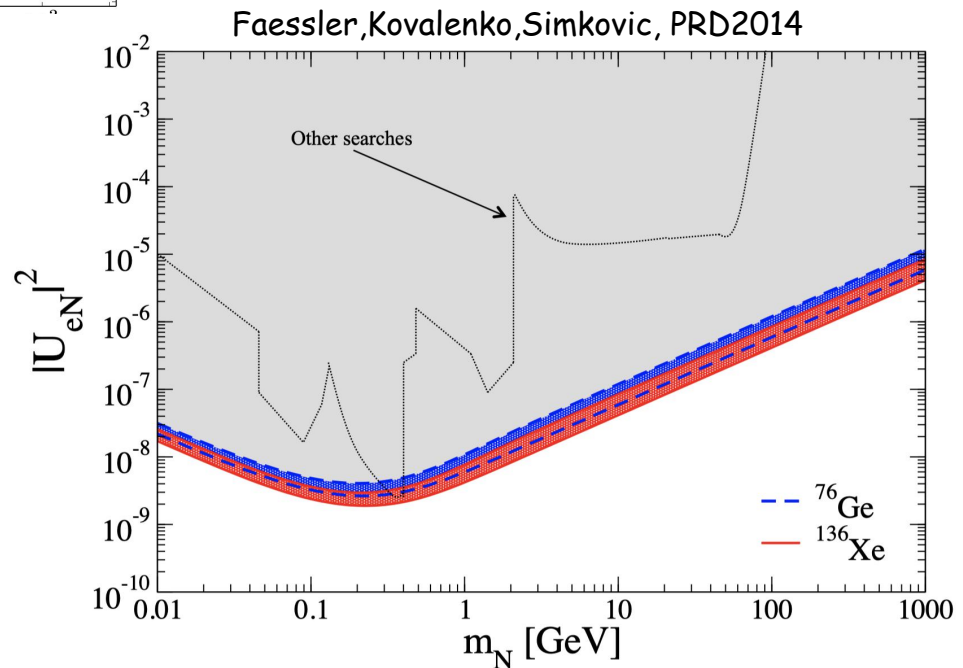
Constraints from other probes

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Bolton, Deppisch, Bhupap Dev, JHEP 2020

- 3+1 case: similar to the case $M_2 \gg M_1$
- $0\nu 2\beta$ data provide strongest limits in the mass range considered here



$$\Delta\chi_{ij}^2(m_{\text{eff}}, (M_{0\nu})_{\alpha j}; m_{\text{eff}}^{\text{True}}, (M_{0\nu})_{\alpha i}^{\text{True}}) = 2 \sum_{\alpha} (N_{\alpha j} - N_{\alpha i}^{\text{True}} + N_{\alpha i}^{\text{True}} \ln \frac{N_{\alpha i}^{\text{True}}}{N_{\alpha j}})$$

Assumed number events

$$N_{\alpha i}^{\text{True}} = B_{\alpha i} + S_{\alpha i}(m_{\text{eff}}^{\text{True}}, (M_{0\nu})_{\alpha i}^{\text{True}})$$

$$N_{\alpha j} = B_{\alpha j} + S_{\alpha j}(m_{\text{eff}}, M_{\alpha j})$$

Assuming no positive $0\nu 2\beta$ signal is observed,
Leading to sensitivities independent of true NME model

$$S_{\alpha i}(m_{\text{eff}}, M_{\alpha i}) = \ln 2 \cdot N_A \cdot \varepsilon_{\alpha} \cdot (T_{1/2}^{0\nu})_{\alpha i}^{-1} \cdot T / (1 \text{ yr})$$

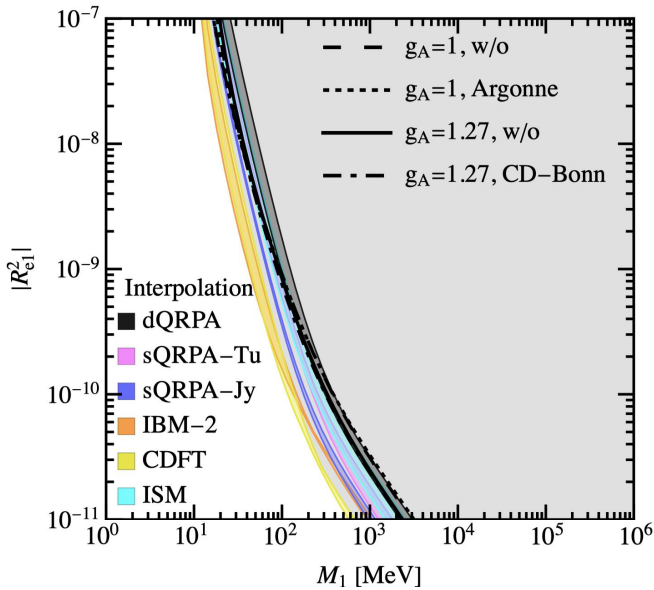
$$B_{\alpha} = b_{\alpha} \cdot \varepsilon_{\alpha} \cdot T / (1 \text{ yr}) \quad \mathbf{T=10 \text{ yr}}$$

Experiment	Isotope	ε [mol· yr]	b [events/(mol· yr)]
LEGEND-1000	^{76}Ge	8736	$4.9 \cdot 10^{-6}$
SuperNEMO	^{82}Se	185	$5.4 \cdot 10^{-3}$
SNO+II	^{130}Te	8521	$5.7 \cdot 10^{-3}$
nEXO	^{136}Xe	13700	$4.0 \cdot 10^{-5}$

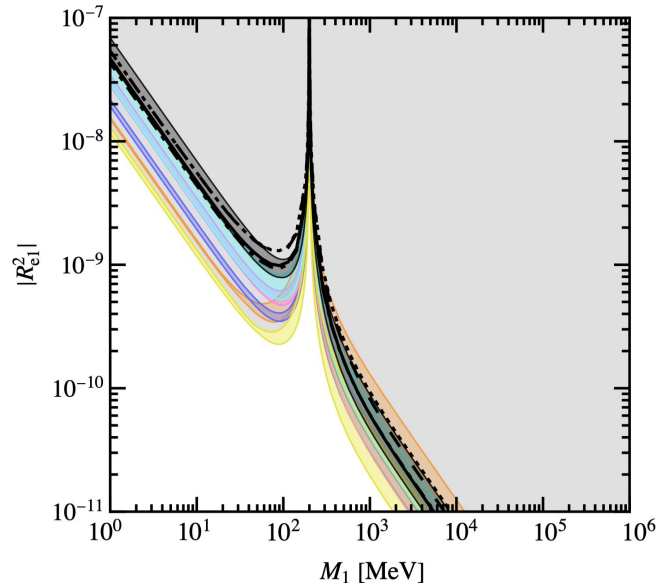
Future sensitivities (M_1 & $|R_{e1}|^2$)

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NMO, $M_2 = 10$ MeV

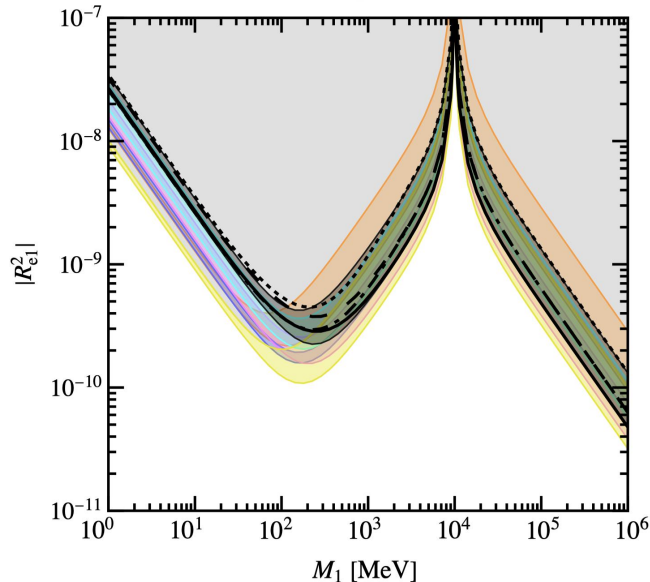


NMO, $M_2 = 200$ MeV

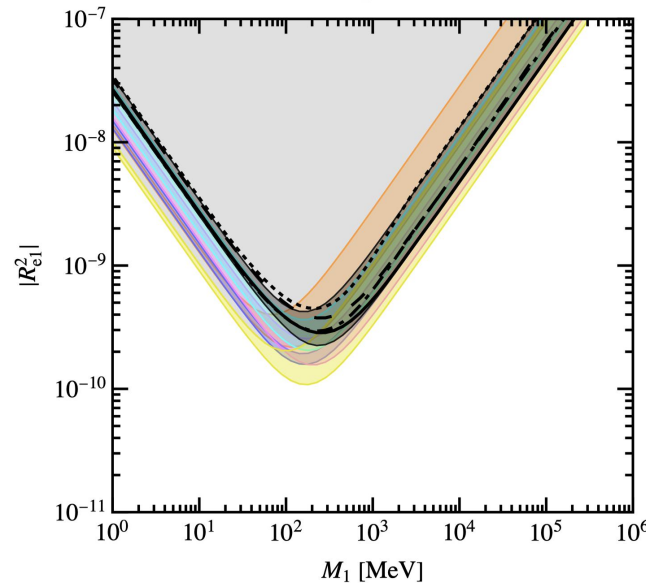


- The NMO case
- More parameter space can be tested when compared the current experiments

NMO, $M_2 = 10$ GeV



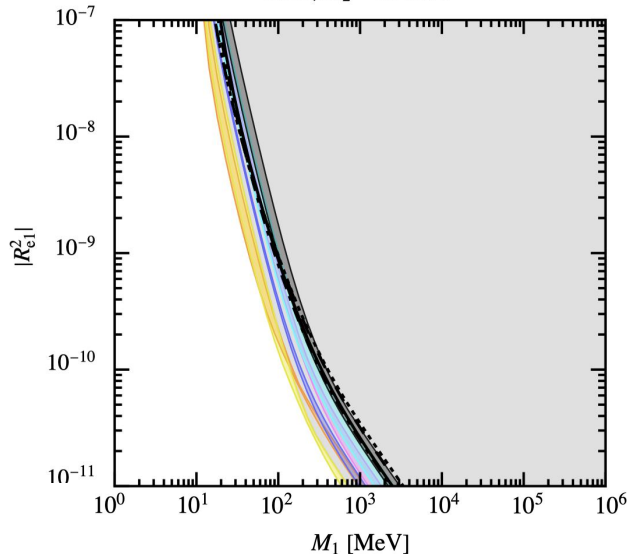
NMO, $M_2 = 10$ TeV



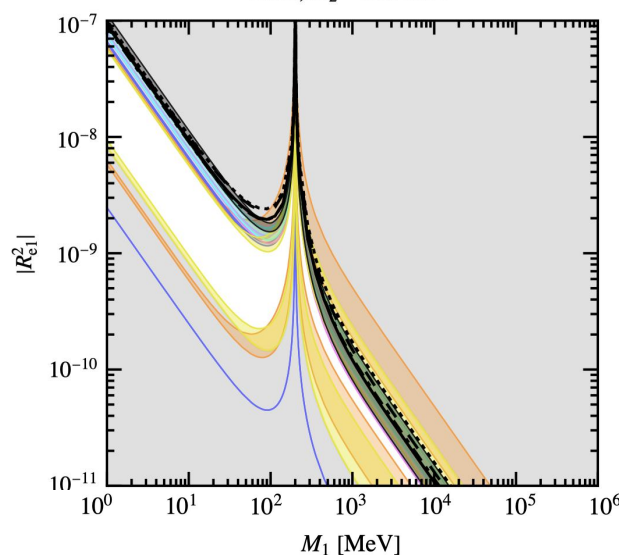
Future sensitivities (M_1 & $|R_{e1}|^2$)

21

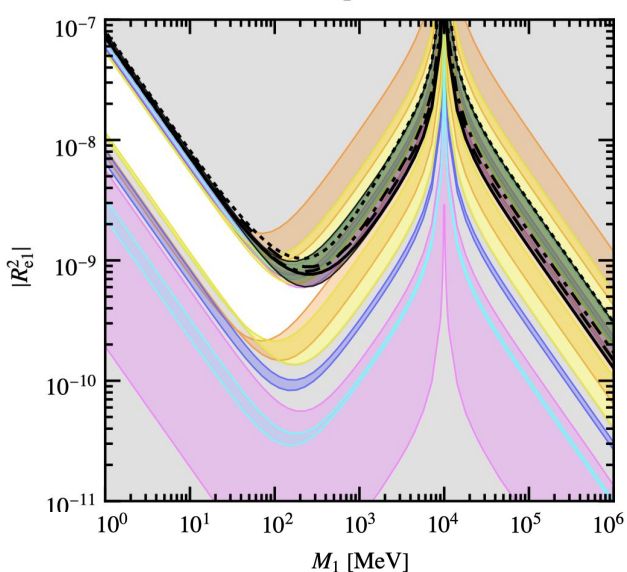
IMO, $M_2 = 10$ MeV



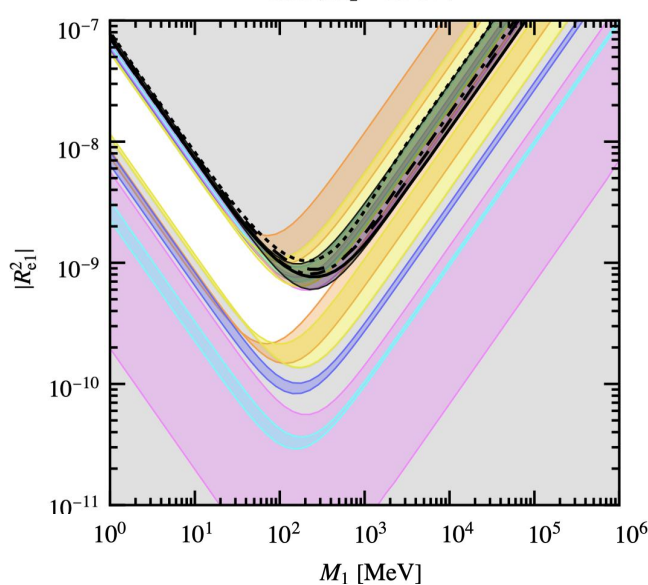
IMO, $M_2 = 200$ MeV



IMO, $M_2 = 10$ GeV



IMO, $M_2 = 10$ TeV



- The IMO case
- Much more parameter space are expected to exclude than NMO case due to zero positive $0\nu 2\beta$ signal assumed

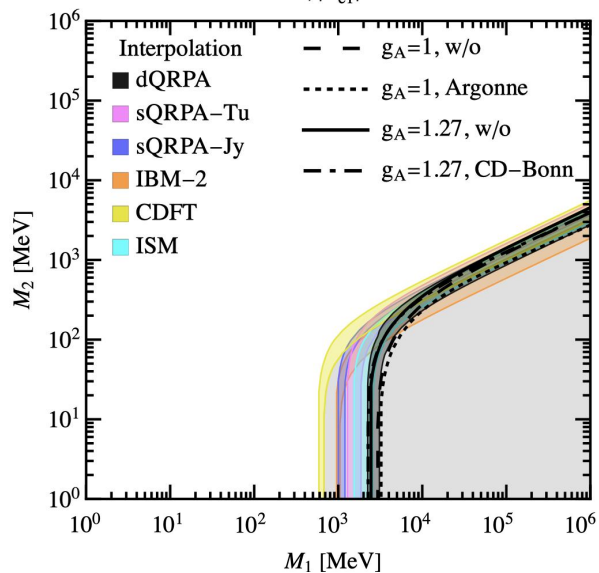
- By assuming **enough positive $0\nu 2\beta$ signal**, possible to **discriminate NME calculations** and more parameter space can be **excluded in the NMO case**

Future sensitivities (M_1 & M_2)

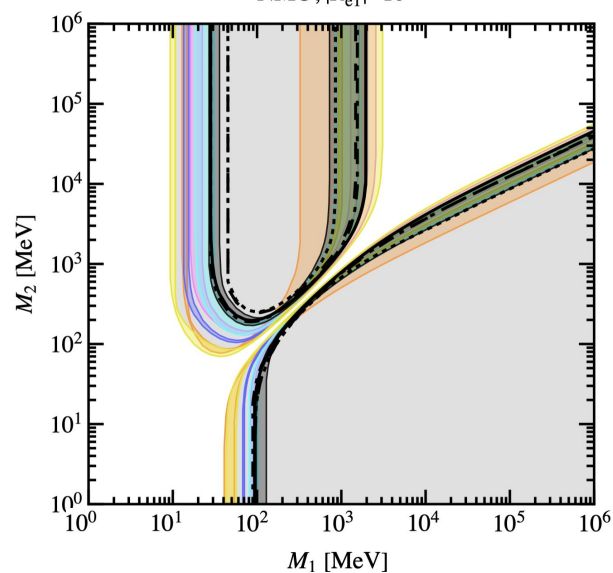
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The NMO case

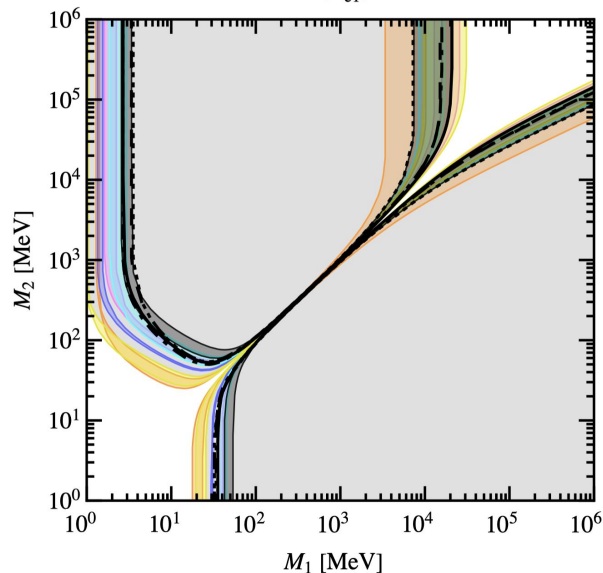
NMO, $|R_{e1}^2|=10^{-11}$



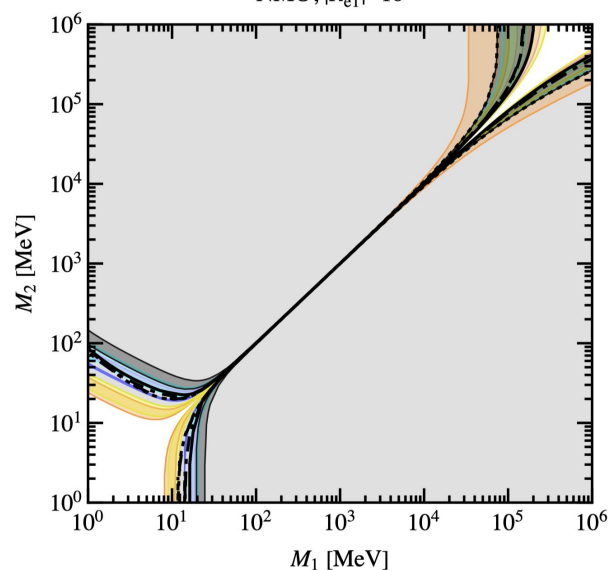
NMO, $|R_{e1}^2|=10^{-9}$



NMO, $|R_{e1}^2|=10^{-8}$

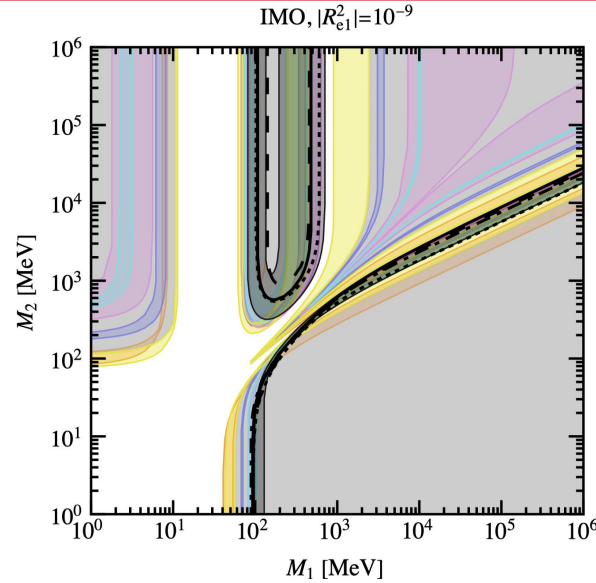
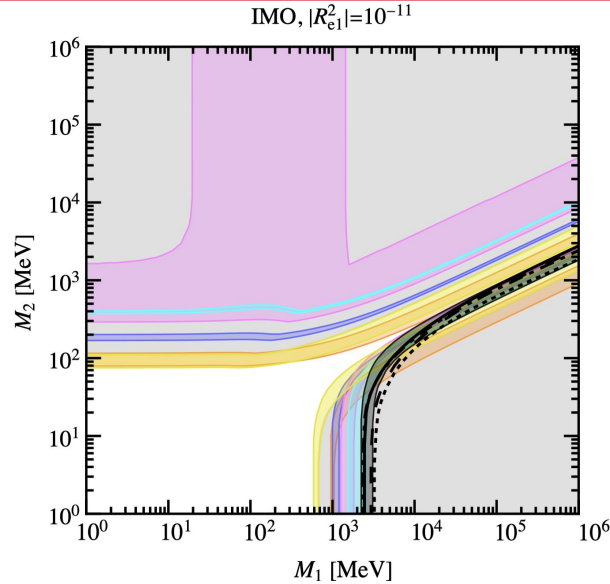


NMO, $|R_{e1}^2|=10^{-7}$

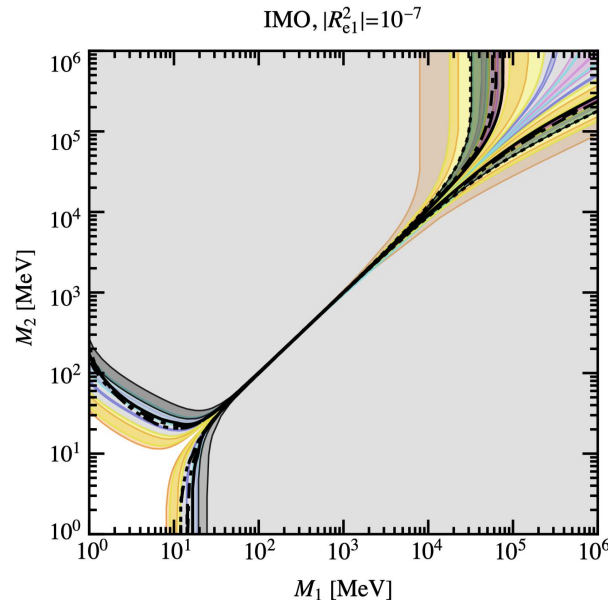
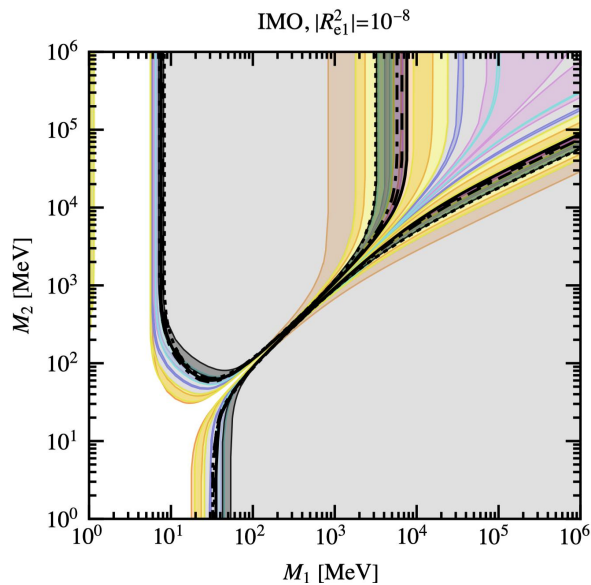


Future sensitivities (M_1 & M_2)

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- The IMO case
- The wide pink region in the upper left panel: mainly different δ_{14} values



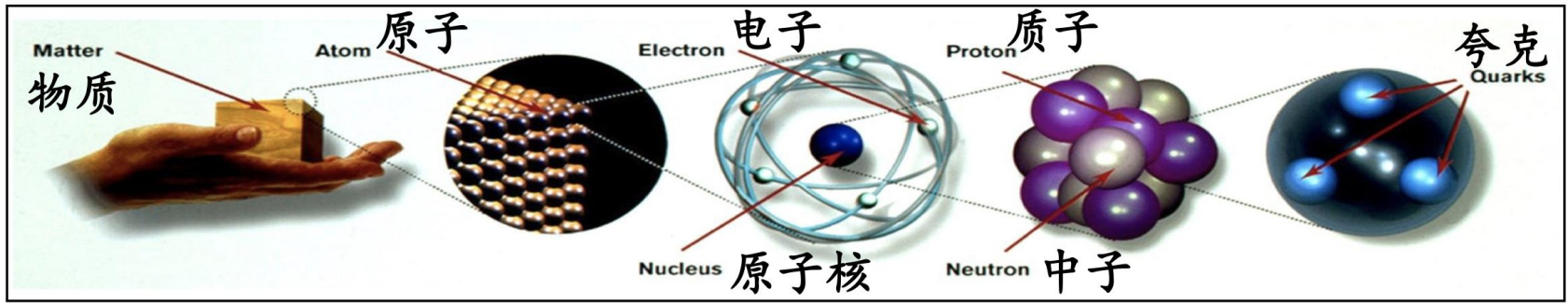
- Comparison of mass dependent NMEs in different nuclear models
- Derivation of limits and sensitivities on the parameter space of minimal type-I seesaw from current and future $0\nu 2\beta$ experiments
- Highlight of the entanglements between new physics exploration and NME calculation
- Possible discrimination of different NME calculations in this framework is on-going.



Thank you for your attention!

Known basics

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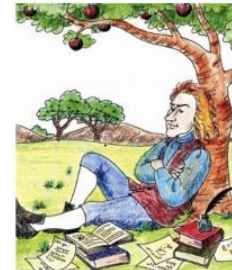


Standard Model of Elementary Particles

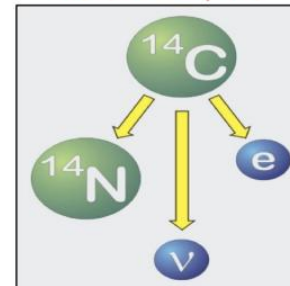
three generations of matter (fermions)			interactions / force carriers (bosons)	
I	II	III		
mass $\approx 2.2 \text{ MeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ u up	mass $\approx 1.28 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ c charm	mass $\approx 173.1 \text{ GeV}/c^2$ charge $\frac{2}{3}$ spin $\frac{1}{2}$ t top	mass 0 charge 0 spin 1 g gluon	mass $\approx 124.97 \text{ GeV}/c^2$ charge 0 spin 0 H higgs
mass $\approx 4.7 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ d down	mass $\approx 96 \text{ MeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ s strange	mass $\approx 4.18 \text{ GeV}/c^2$ charge $-\frac{1}{3}$ spin $\frac{1}{2}$ b bottom	mass 0 charge 0 spin 1 γ photon	
mass $\approx 0.511 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ e electron	mass $\approx 105.66 \text{ MeV}/c^2$ charge -1 spin $\frac{1}{2}$ μ muon	mass $\approx 1.7768 \text{ GeV}/c^2$ charge -1 spin $\frac{1}{2}$ τ tau	mass $\approx 91.19 \text{ GeV}/c^2$ charge 0 spin 1 Z Z boson	
mass $< 1.0 \text{ eV}/c^2$ charge 0 spin $\frac{1}{2}$ ν_e electron neutrino	mass $< 0.17 \text{ MeV}/c^2$ charge 0 spin $\frac{1}{2}$ ν_μ muon neutrino	mass $< 1.8 \text{ GeV}/c^2$ charge 0 spin $\frac{1}{2}$ ν_τ tau neutrino	mass $\approx 80.39 \text{ GeV}/c^2$ charge ± 1 spin 1 W W boson	

QUARKS (left column), **LEPTONS** (left column), **GAUGE BOSONS VECTOR BOSONS** (right column), **SCALAR BOSONS** (right column)

引力相互作用



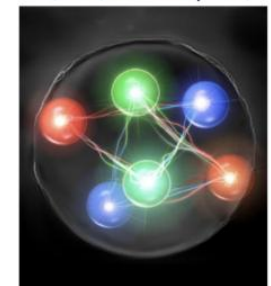
弱相互作用



电磁相互作用

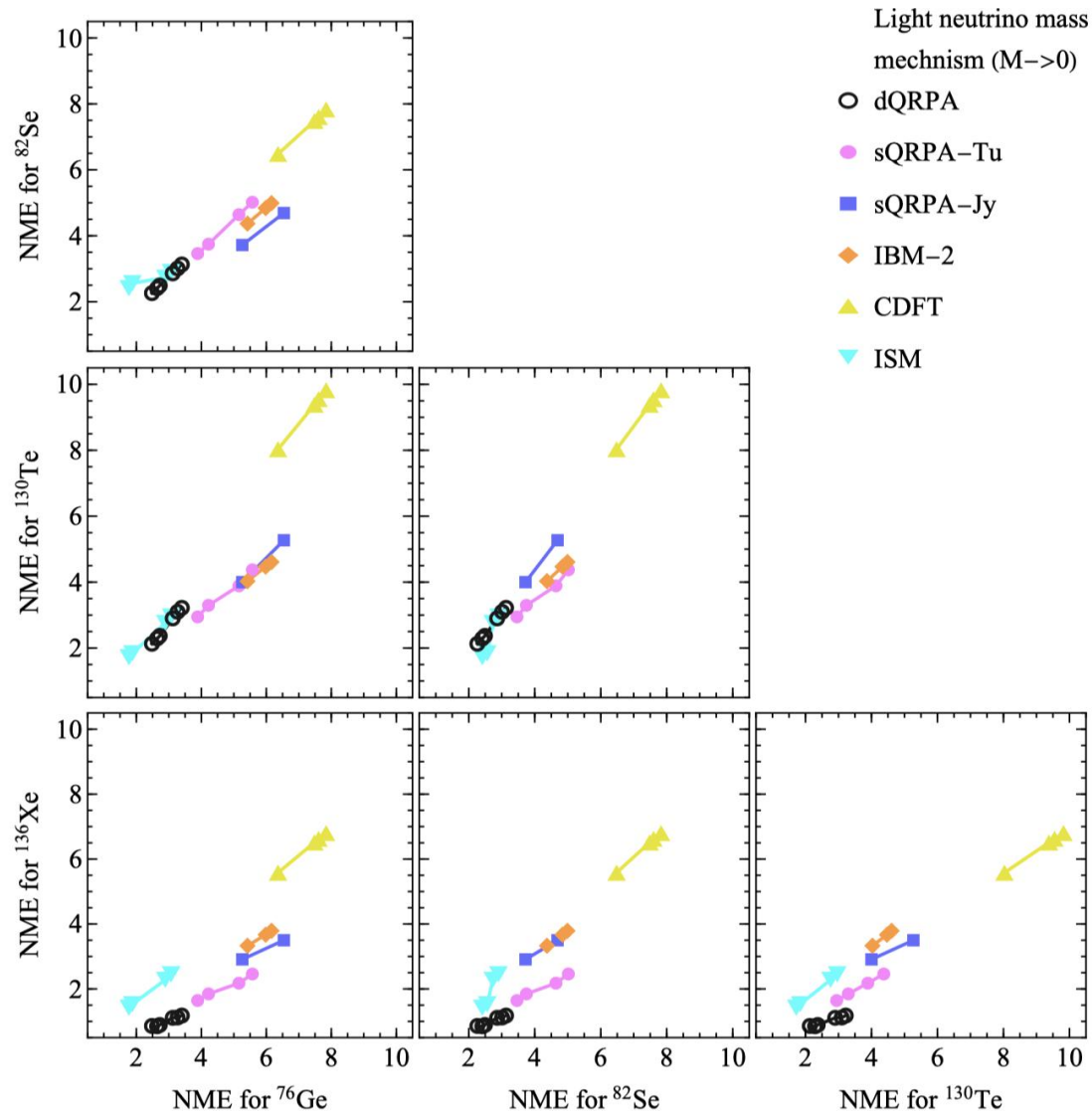


强相互作用



NME of light neutrinos

27



- CDFT biggest
- ISM/dQRPA smallest
- different NME ratios between different isotopes

NME of heavy neutrinos

28

