

# NEW DEVELOPMENTS FOR LAMB-SHIFT POLARIMETER

26<sup>TH</sup> FEBRUARY 2024    NICOLAS FAATZ

# SPIN PHYSICS

- Precision physics
- Nuclear magnetic resonance (NMR)
- Nuclear fusion

# LSP USED FOR DIFFERENT EXPERIMENTS

- Los Alamos → invention of the first spin filter

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A. Solovev et.al., JINST., **15**, (2020)

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- RHIC → optically pumped polarized H<sup>-</sup> source  
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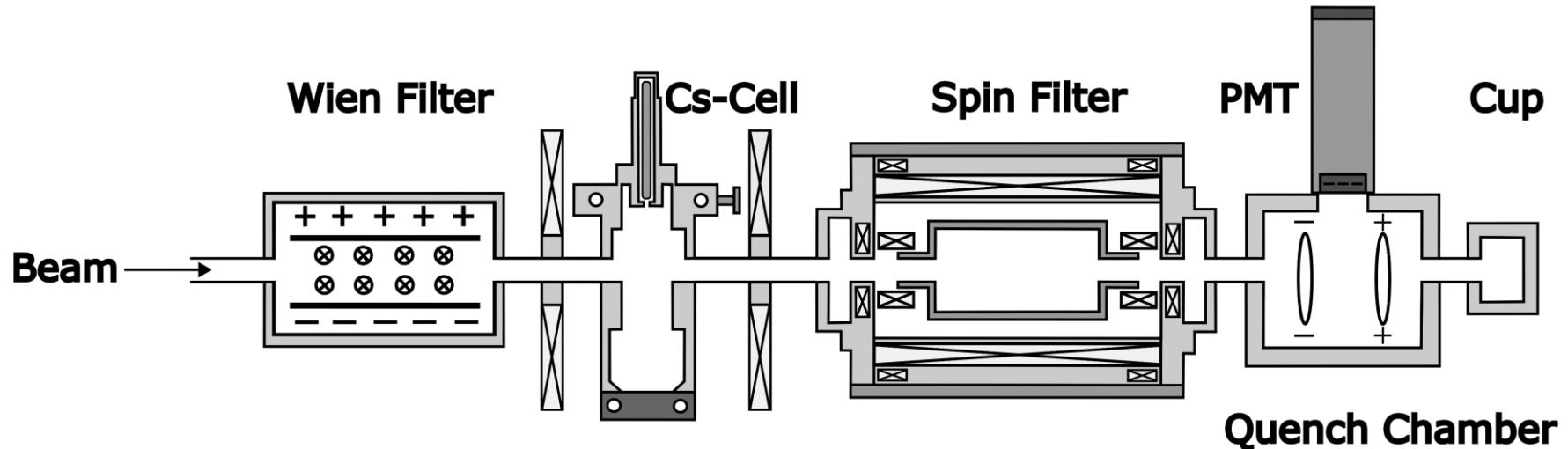
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- PNPI → investigations for double-polarized DD-fusion  
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# START IN JÜLICH

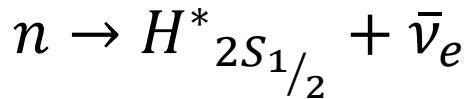


- Measuring the nuclear polarization created by the ABS
- Simple and cheap detection method
- Working for hydrogen atoms their isotopes molecules and ions

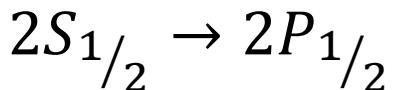
# MOTIVATION

- Nuclear polarized sources

- Bound beta decay (BoB)

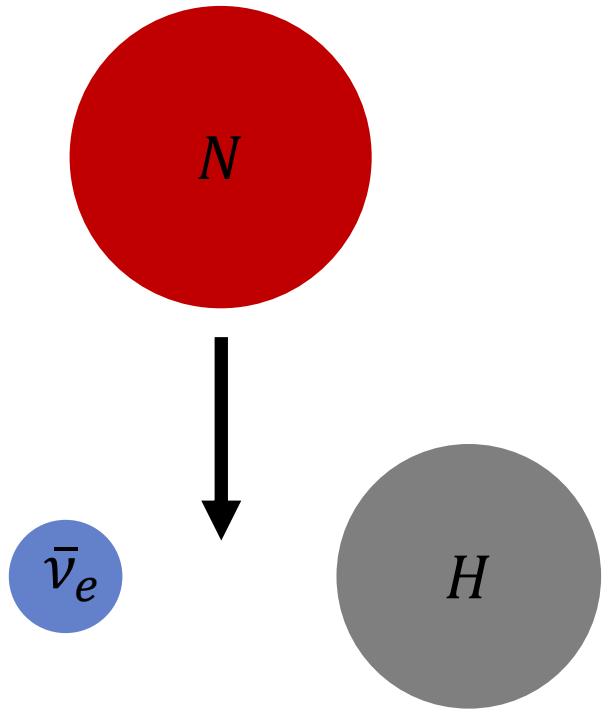


- Parity violation



$$P = (-1)^l: 0 \rightarrow 1$$

- Sona transition unit



# HYDROGEN-LIKE WAVEFUNCTIONS

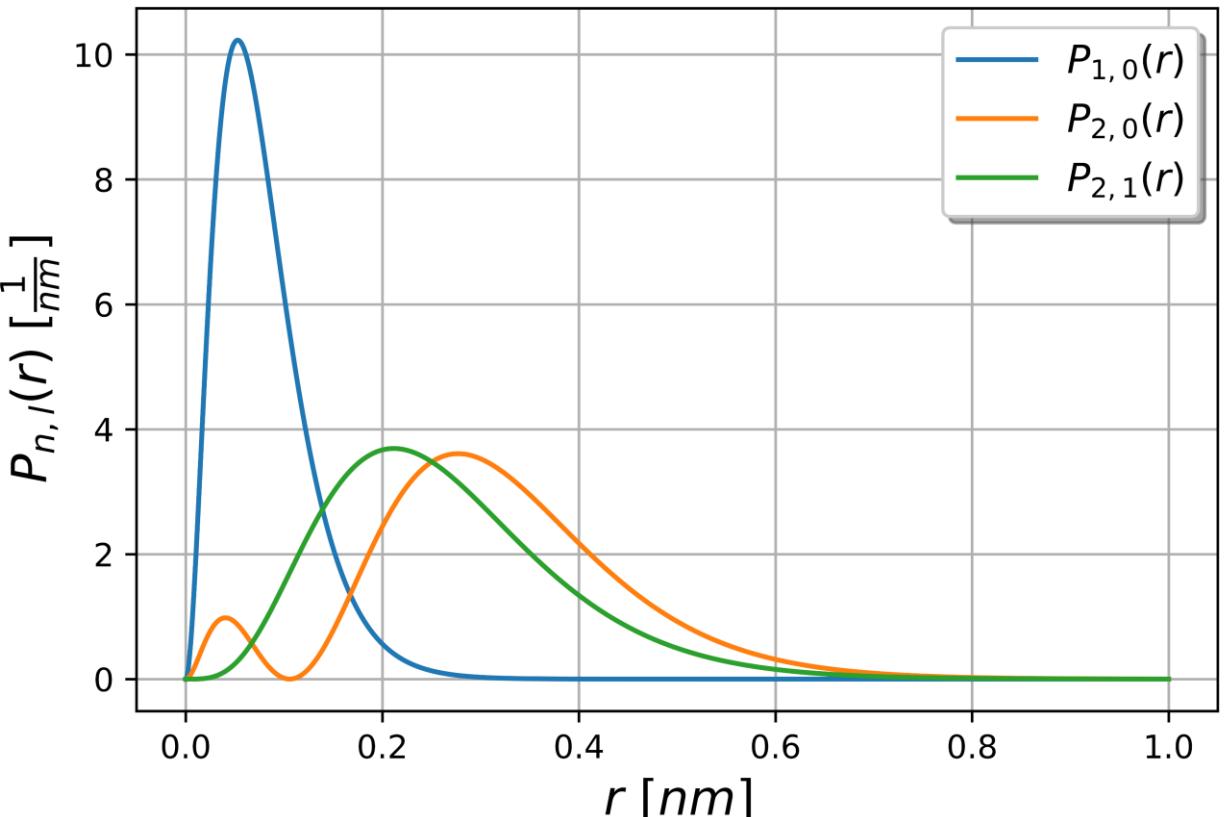
$$\psi_{100} = \sqrt{\frac{4Z^3}{a_0^3}} e^{-\frac{Zr}{a_0}} \frac{1}{\sqrt{4\pi}}$$

$$\psi_{200} = \sqrt{\frac{Z^3}{32\pi a_0^3}} \left( -\frac{Zr}{a_0} + 2 \right) e^{-\frac{Zr}{2a_0}}$$

$$\psi_{210} = \sqrt{\frac{Z^3}{32\pi a_0^3}} \left( -\frac{Zr}{a_0} \right) e^{-\frac{Zr}{2a_0}} \cos(\theta)$$

$$\psi_{21\pm 1} = \mp \sqrt{\frac{Z^3}{64\pi a_0^3}} \left( -\frac{Zr}{a_0} \right) e^{-\frac{Zr}{2a_0}} \sin(\theta) e^{\pm i\phi}$$

$$P_{n,l}(r) = r^2 |R_{n,l}(r)|^2$$



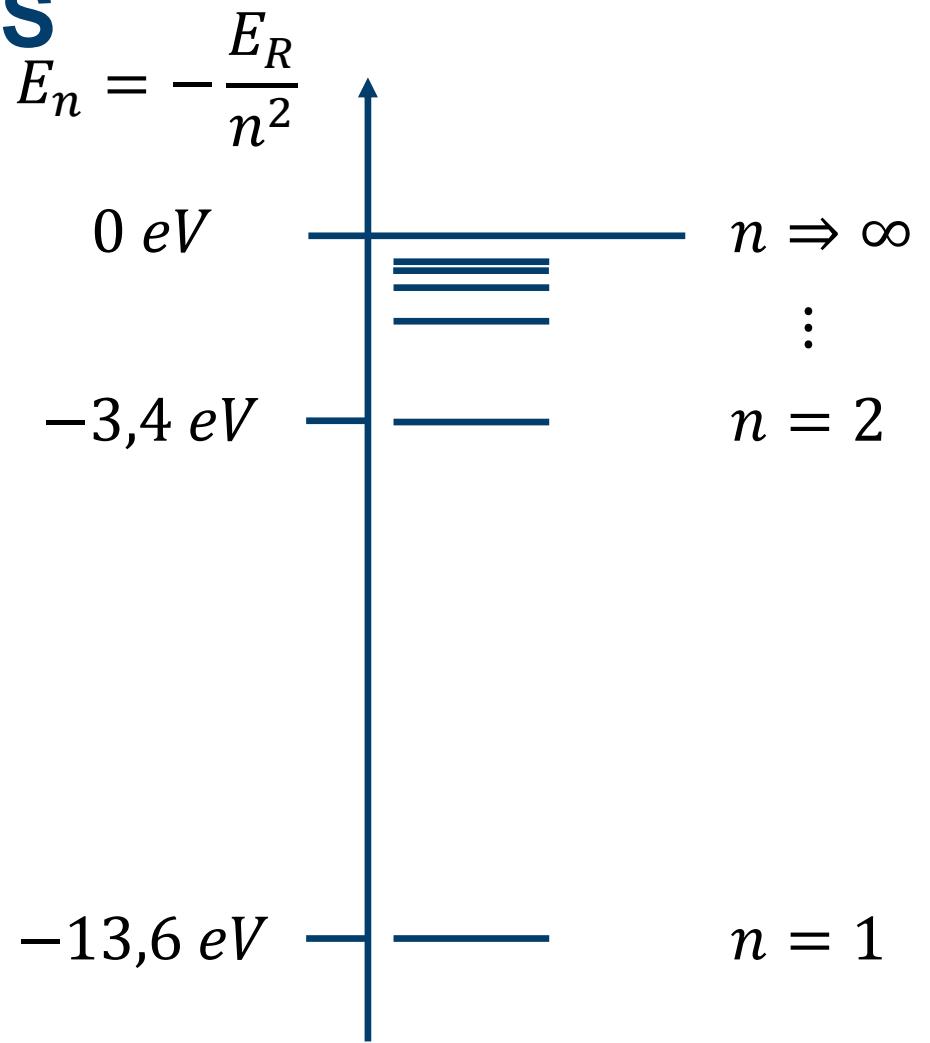
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# STARK EFFECT

$$V_{Stark}(t) = e\vec{E}(t) \cdot \vec{r}$$

$$E_2 = -\frac{E_R}{4}$$

$$\delta = \frac{3a_0e\varepsilon}{Z}$$

$$|\psi_+\rangle = \frac{1}{\sqrt{2}}(|2,0,0\rangle - |2,1,0\rangle)$$

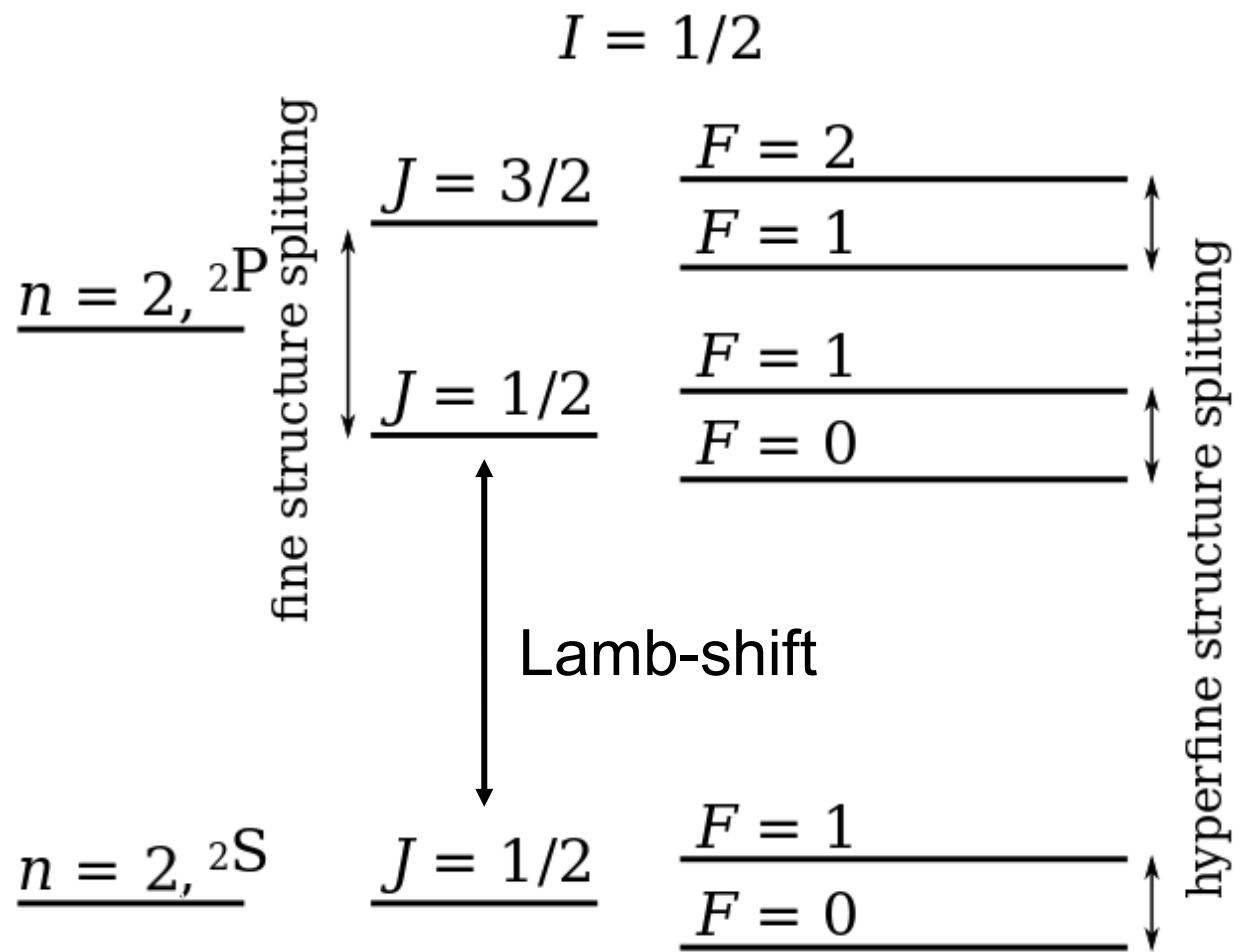
$\delta$

$\delta$

$$|\psi_{1,2}\rangle = |2,1,\pm 1\rangle$$

$$|\psi_-\rangle = \frac{1}{\sqrt{2}}(|2,0,0\rangle + |2,1,0\rangle)$$

# ENERGY SPLITTINGS



[https://en.wikipedia.org/wiki/Hyperfine\\_structure](https://en.wikipedia.org/wiki/Hyperfine_structure)

# BREIT-RABI FORMULAS

$$H = \Delta E_{Lamb} \frac{\vec{L} \cdot \vec{S}}{\hbar^2} + A \frac{\vec{J} \cdot \vec{I}}{\hbar^2} + \left( g_j \mu_B \frac{\vec{J}}{\hbar} - g_I \mu_k \frac{\vec{I}}{\hbar} \right) \cdot \vec{B}$$

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Example for  $2S_{1/2}$

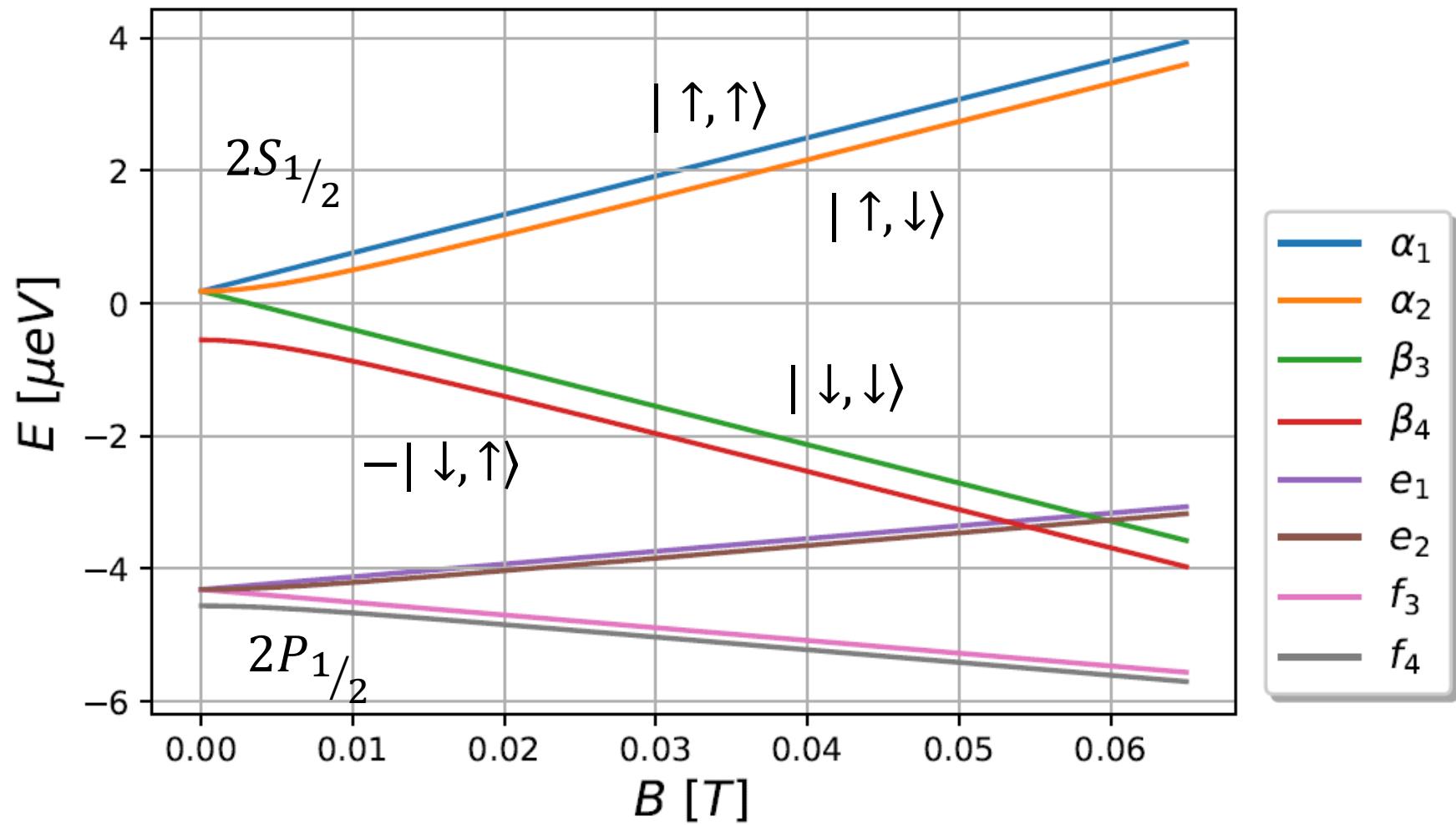
$$E_{\alpha_1} = \frac{A}{4} + \frac{1}{2} (g_j \mu_B - g_I \mu_k) B$$

$$E_{\alpha_2} = -\frac{A}{4} + \frac{1}{2} \sqrt{A^2 + (g_j \mu_B + g_I \mu_k)^2 B^2}$$

$$E_{\beta_3} = \frac{A}{4} - \frac{1}{2} (g_j \mu_B - g_I \mu_k) B$$

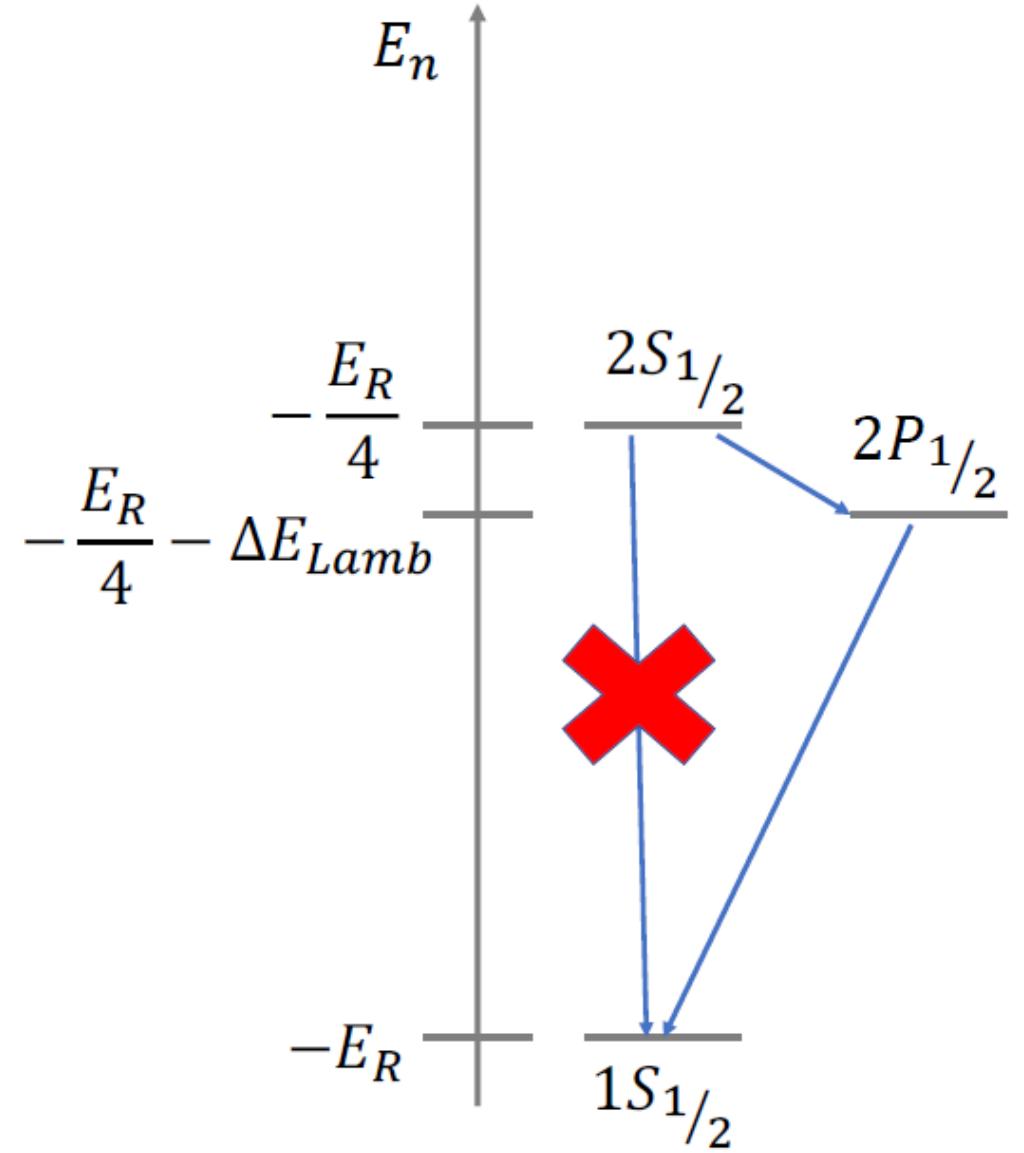
$$E_{\beta_4} = -\frac{A}{4} - \frac{1}{2} \sqrt{A^2 + (g_j \mu_B + g_I \mu_k)^2 B^2}$$

# BREIT-RABI DIAGRAM



# METASTABLE ATOMS

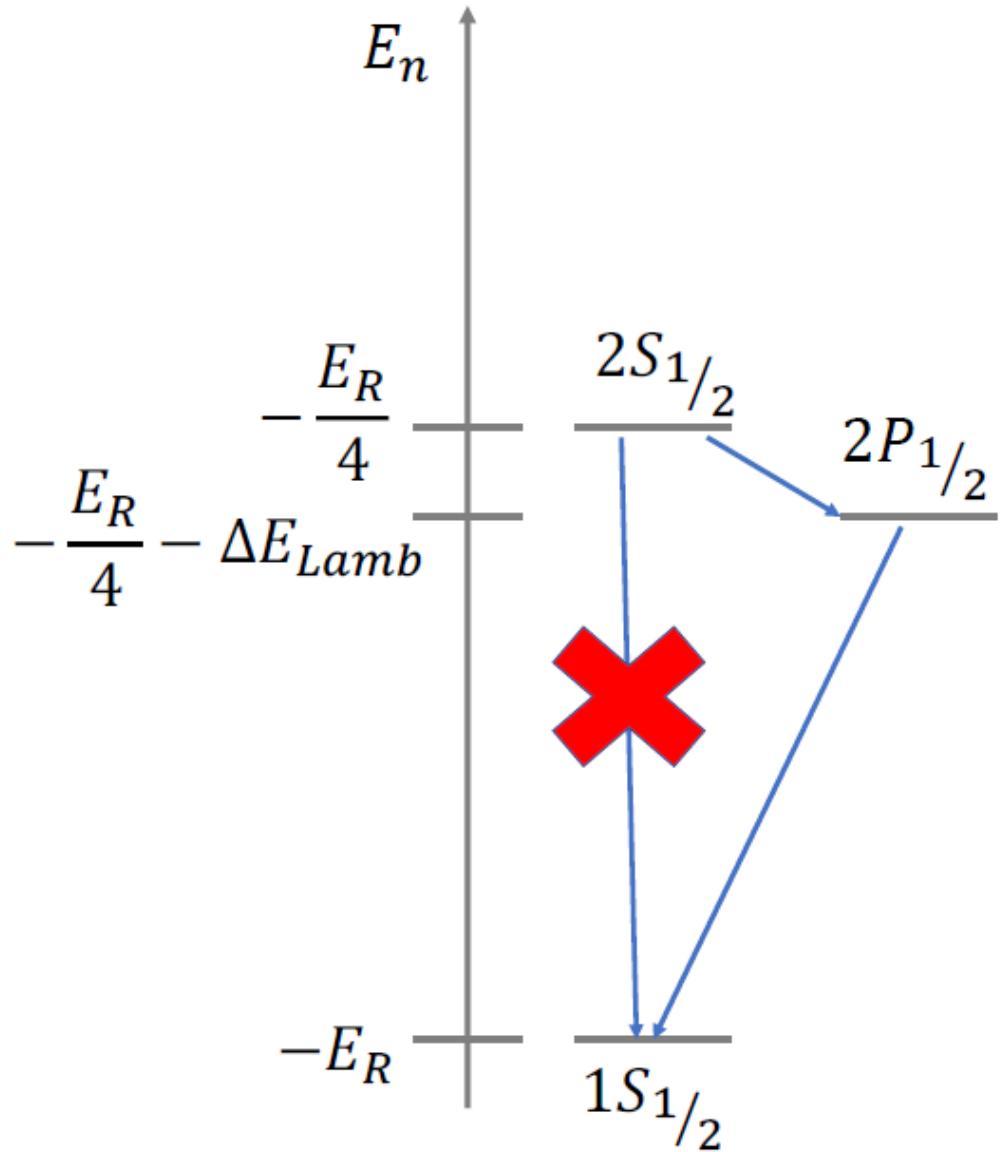
$$V_{Life} = -i \frac{\hbar}{2\tau}$$



# METASTABLE ATOMS

$$V_{Life} = -i \frac{\hbar}{2\tau}$$

$$i\hbar \frac{\partial}{\partial t} |\psi_n(t)\rangle = (H + V_{Life})|\psi_n(t)\rangle$$

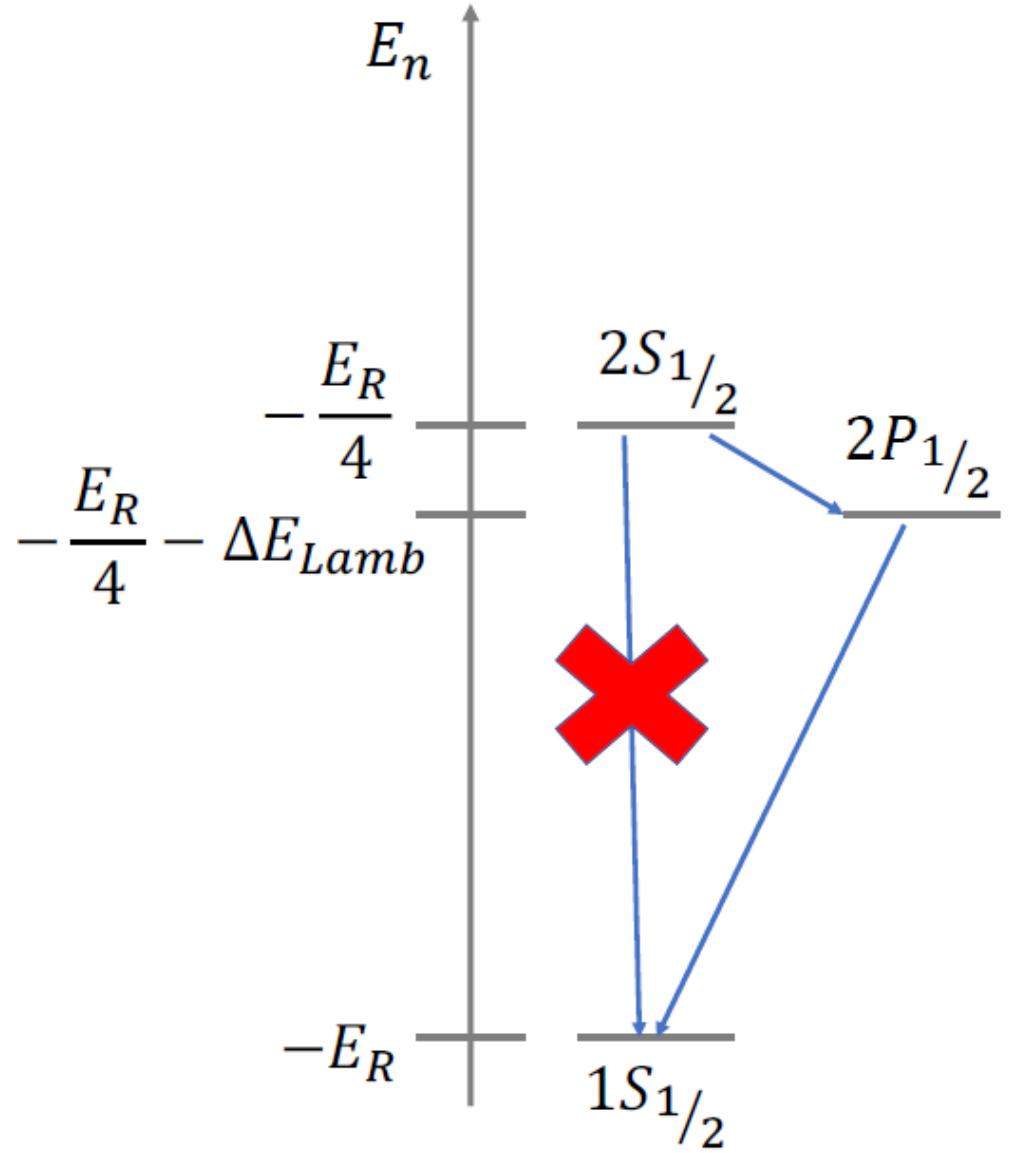


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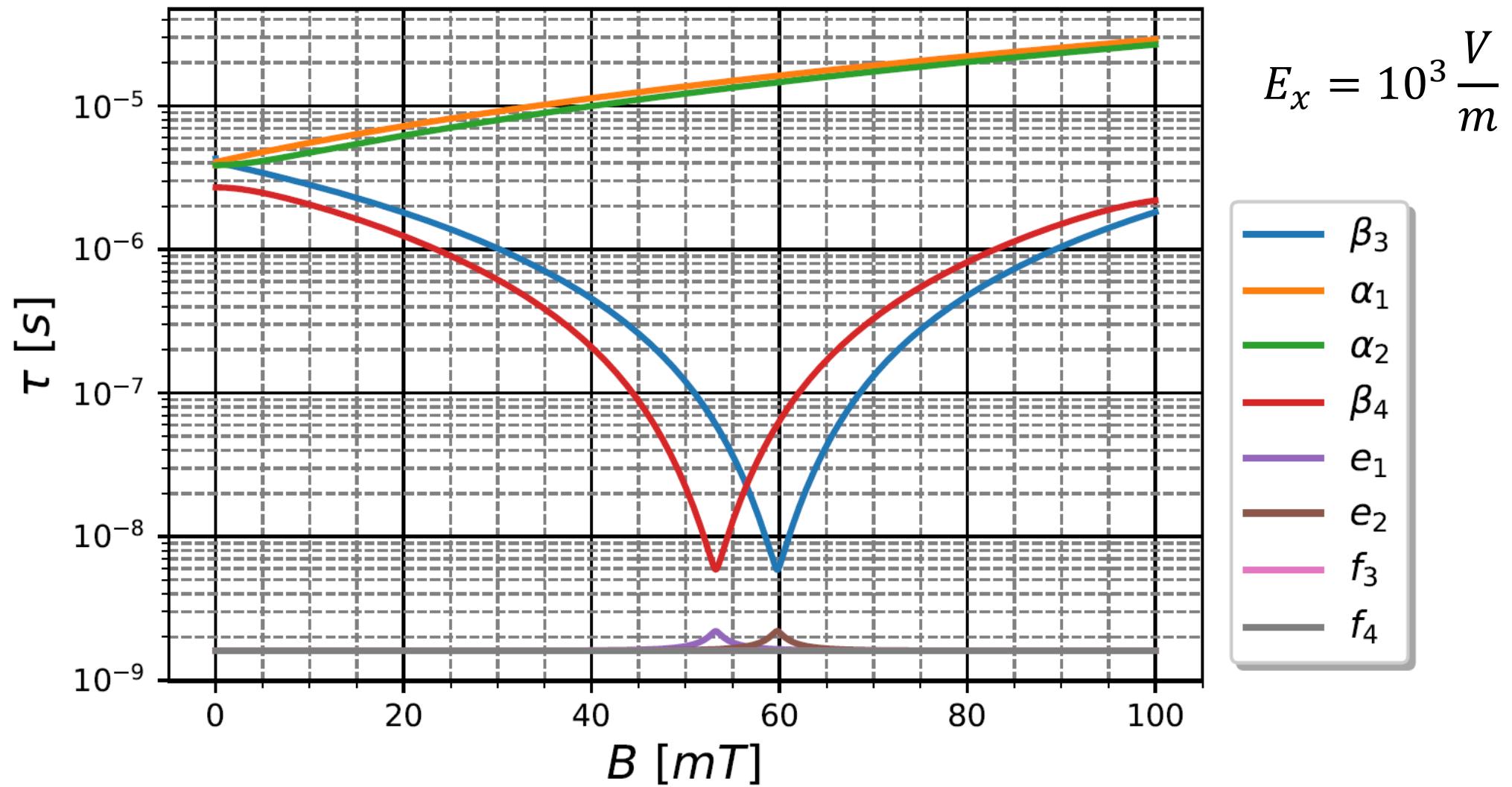
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$$i\hbar \frac{\partial}{\partial t} |\psi_n(t)\rangle = (H + V_{Life})|\psi_n(t)\rangle$$

$$\langle \psi_n(t) | \psi_n(t) \rangle = |C(t) \exp\left(-i \frac{(E_n - i \frac{\hbar}{2\tau})}{\hbar}\right)|^2 = e^{-\frac{t}{\tau}}$$



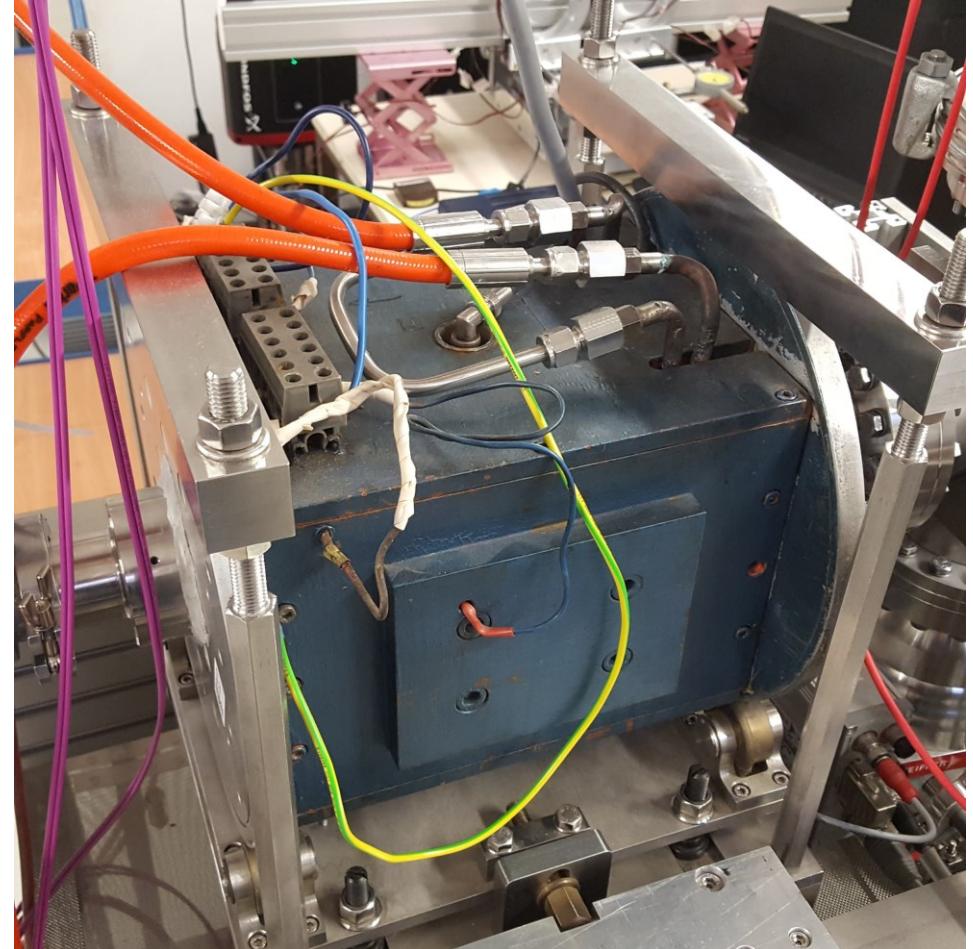
# LIFETIME



# WIEN-FILTER

- Electric and magnetic field perpendicular to beam direction

$$\vec{v} \perp \vec{\epsilon} \perp \vec{B}$$



# WIEN-FILTER

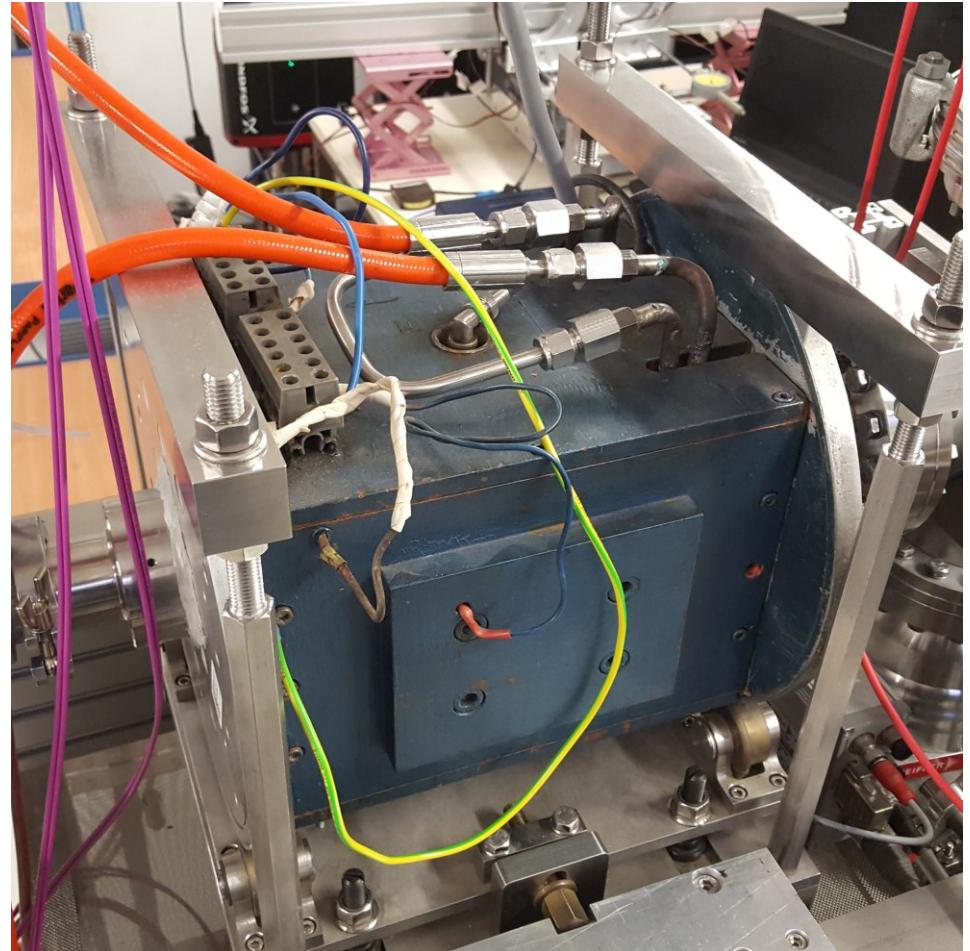
- Electric and magnetic field perpendicular to beam direction

$$\vec{v} \perp \vec{\epsilon} \perp \vec{B}$$

- Sharpening the beam velocity

$$\vec{F}_{el.} = q\vec{\epsilon} = q(\vec{v} \times \vec{B}) = \vec{F}_{Lorentz}$$

$$|v| = \frac{|\epsilon|}{|B|}$$



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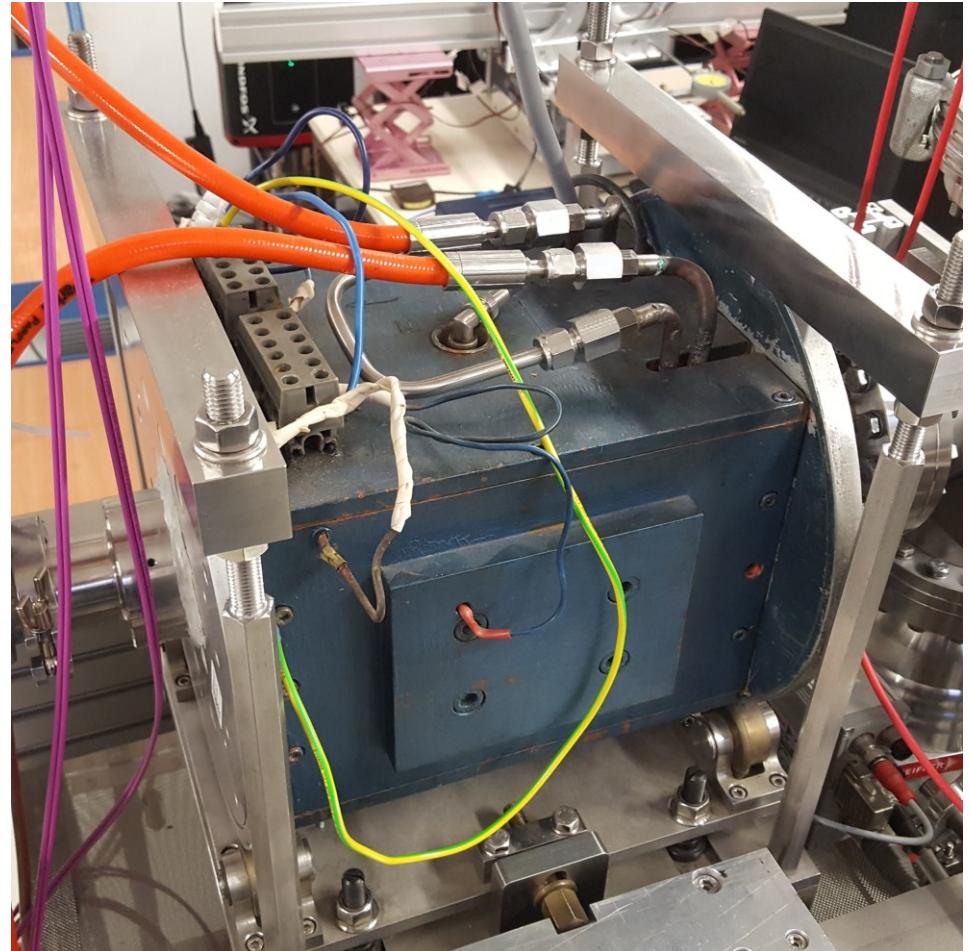
- Sharpening the beam velocity

$$\vec{F}_{el.} = q\vec{\epsilon} = q(\vec{v} \times \vec{B}) = \vec{F}_{Lorentz} \quad |v| = \frac{|\epsilon|}{|B|}$$

- For a fixed beam energy then works as a mass filter

$$E_{kin} = \frac{1}{2}mv^2$$

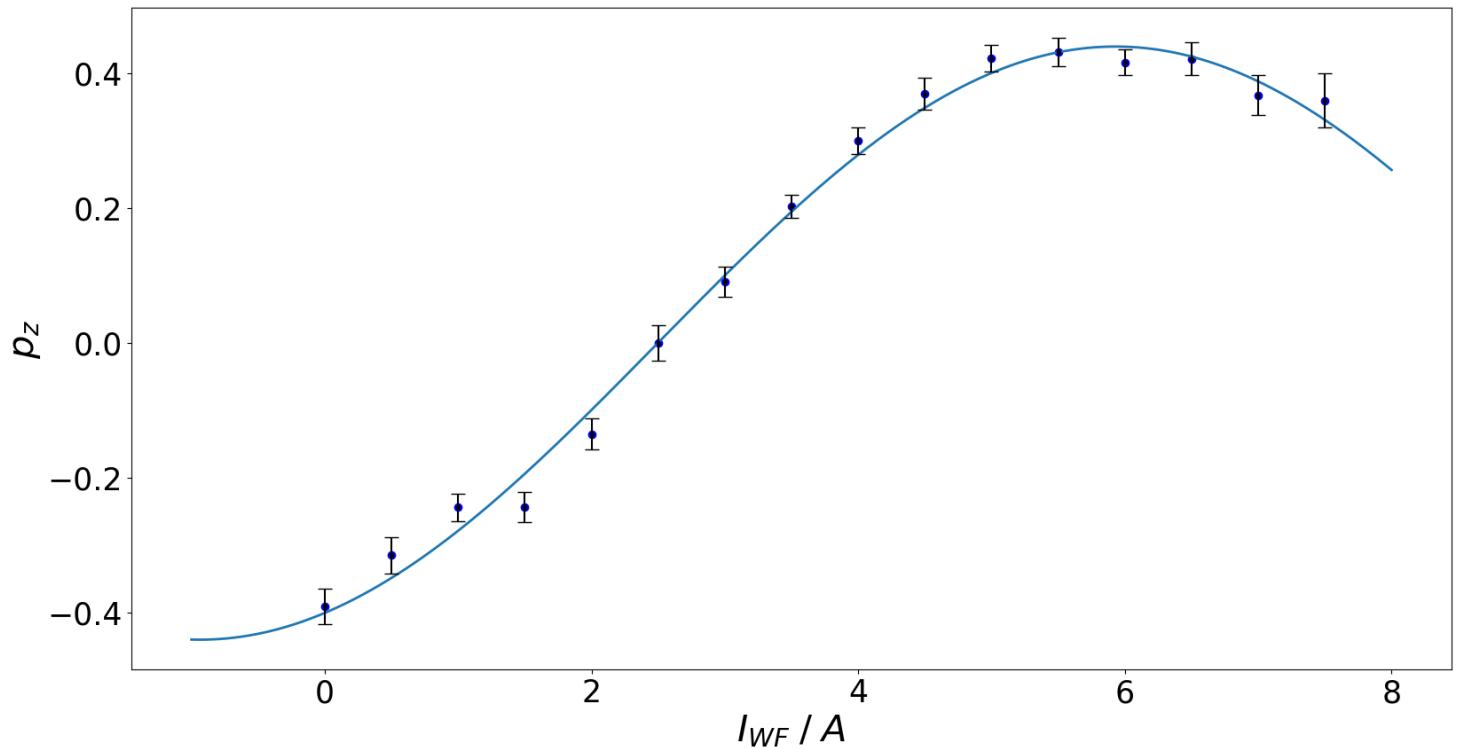
$$m = \frac{2E_{kin}B^2}{\epsilon^2}$$



# WIEN-FILTER

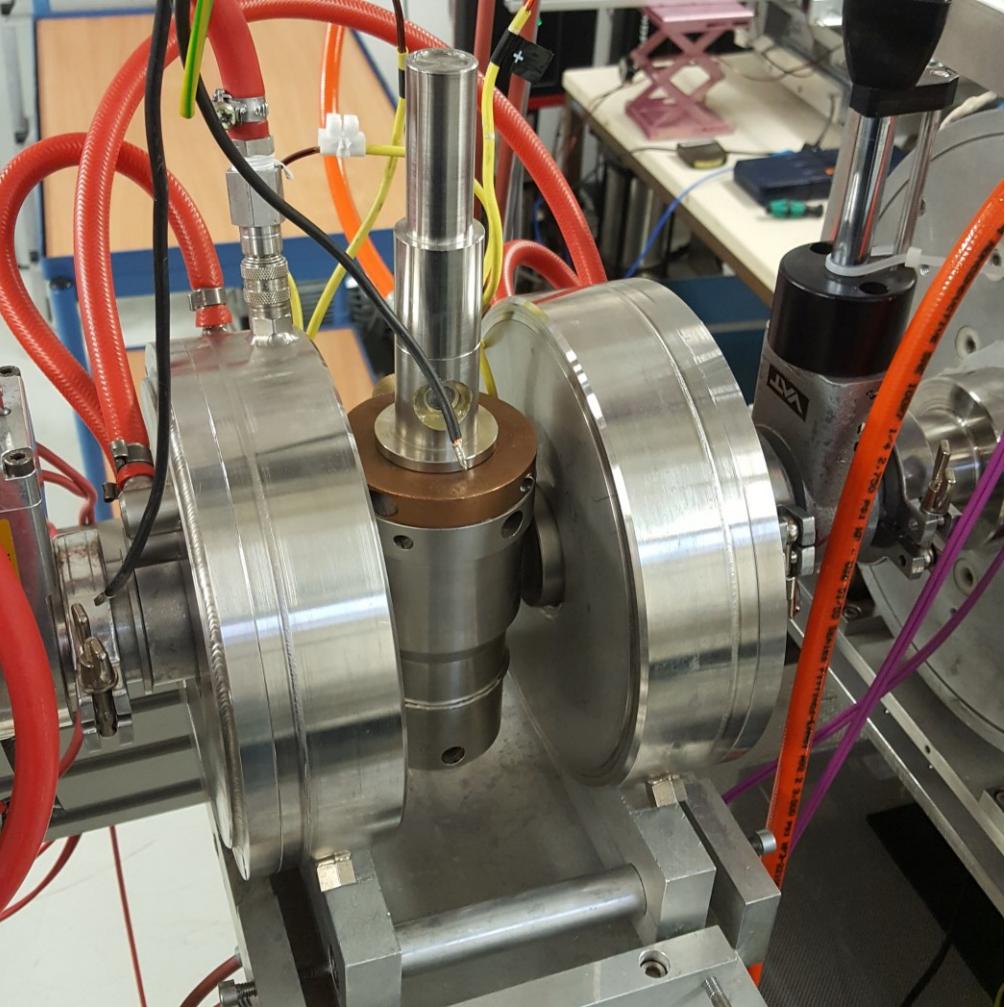
- Spins of the particles interact with the magnetic field

$$\omega_{Larmor} = -\frac{gqB}{2m}$$



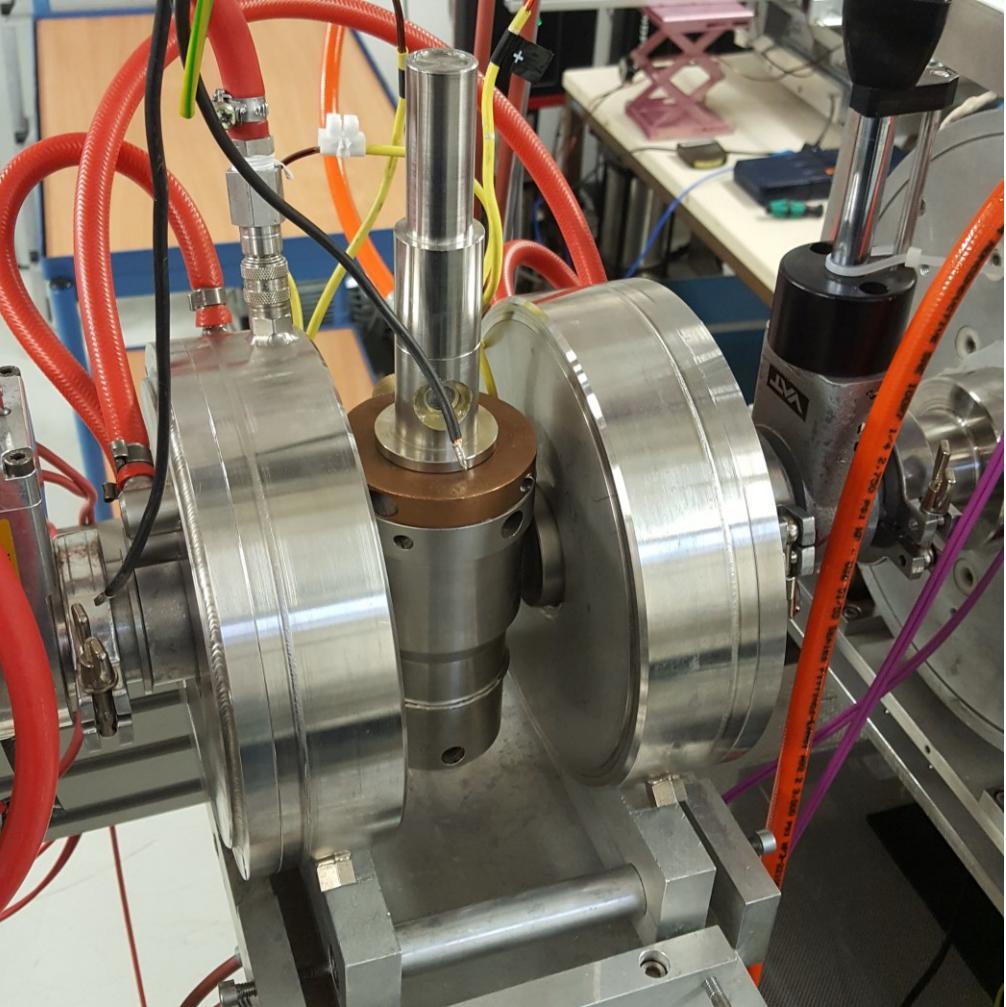
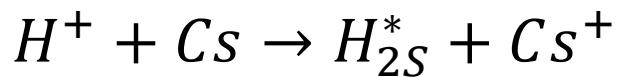
# CAESIUM CELL

- Using the properties of alkali metals for charge exchange



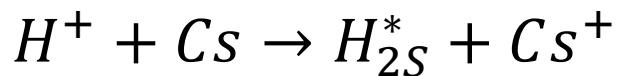
# CAESIUM CELL

- Using the properties of alkali metals for charge exchange
- Creating metastable hydrogen

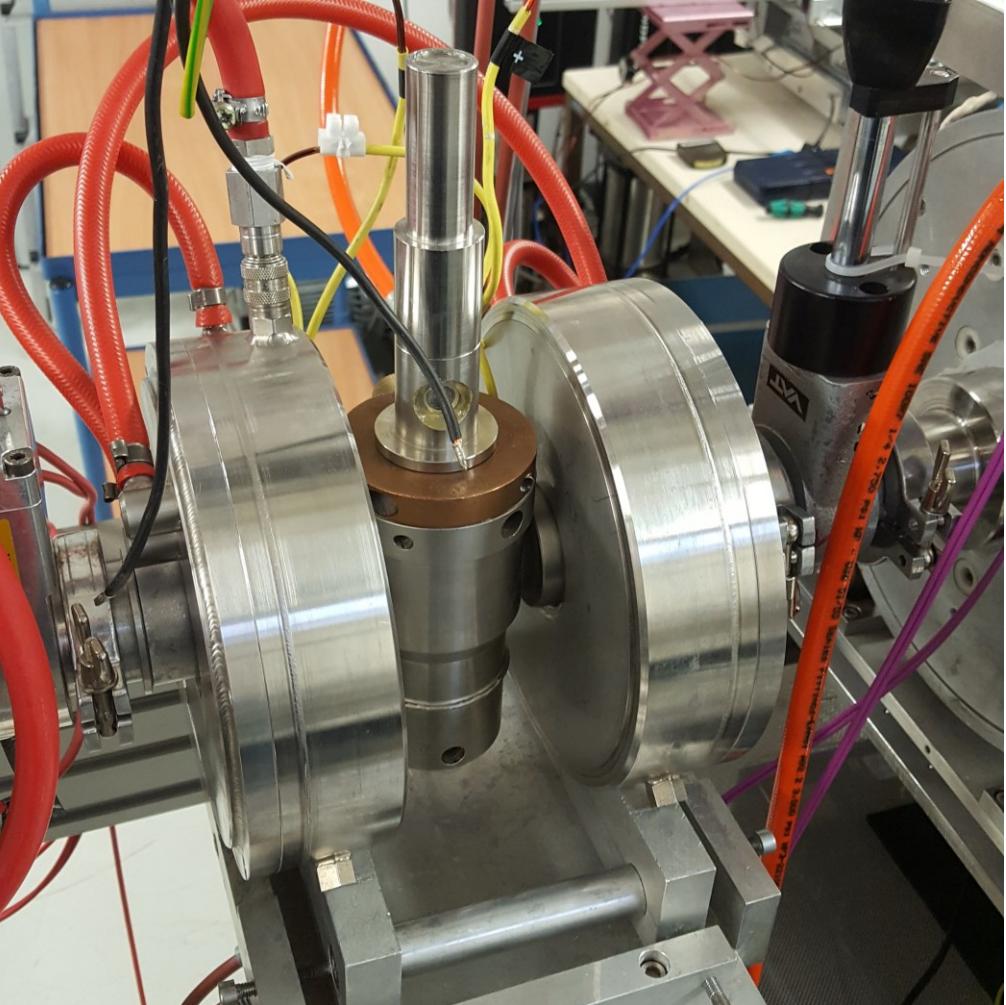


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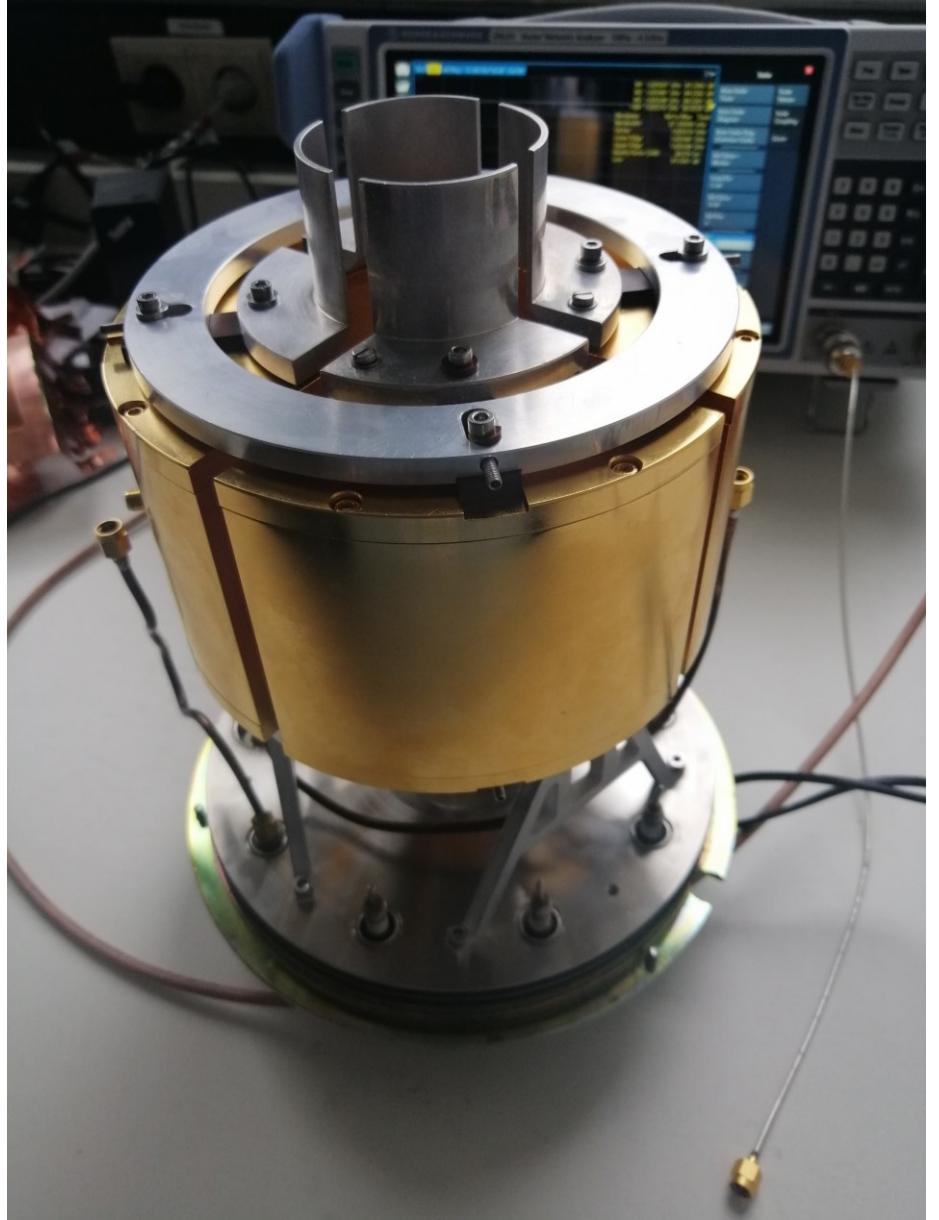


- Lower temperature (Cs: 160 °C / Na: 350 °C)



# SPIN FILTER

- Aim to separate the different Breit-Rabi states
- Contains several coils producing a homogeneous static magnetic field in beam direction
- Embedded sits a cavity in which a radio frequency as well as a static electric field is induced



# THEORY FOR THE SPIN FILTER

$$H_{SF} = H_{BR} + \underbrace{V_{Life} + V_{Stark} + V_{RF}(t)}_{= V(t)}$$

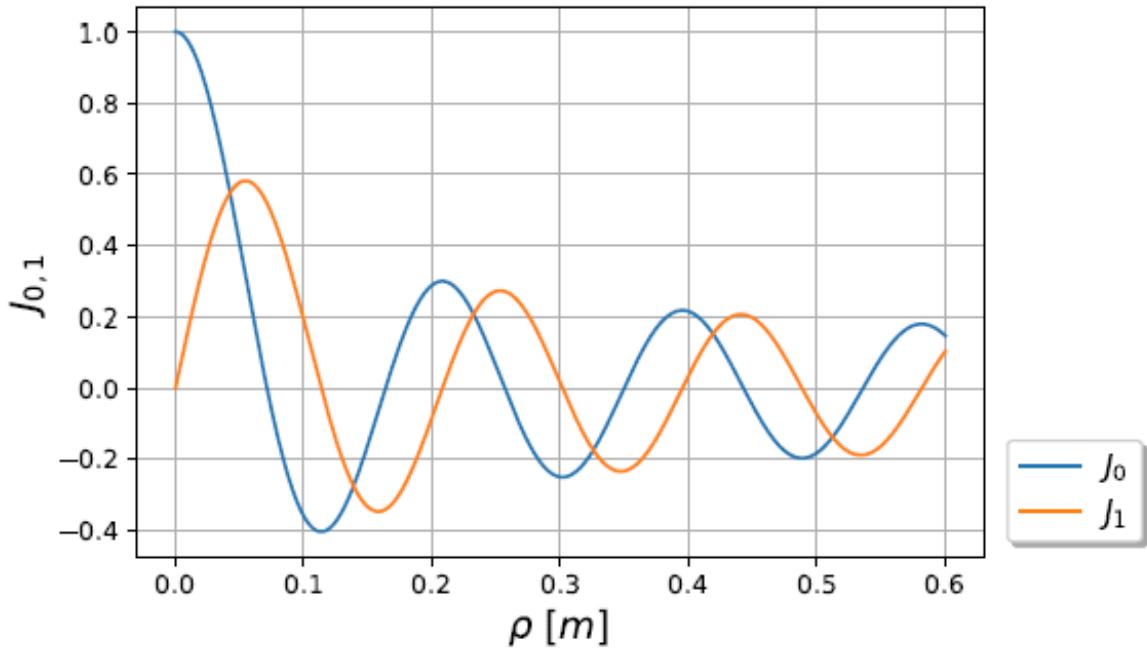
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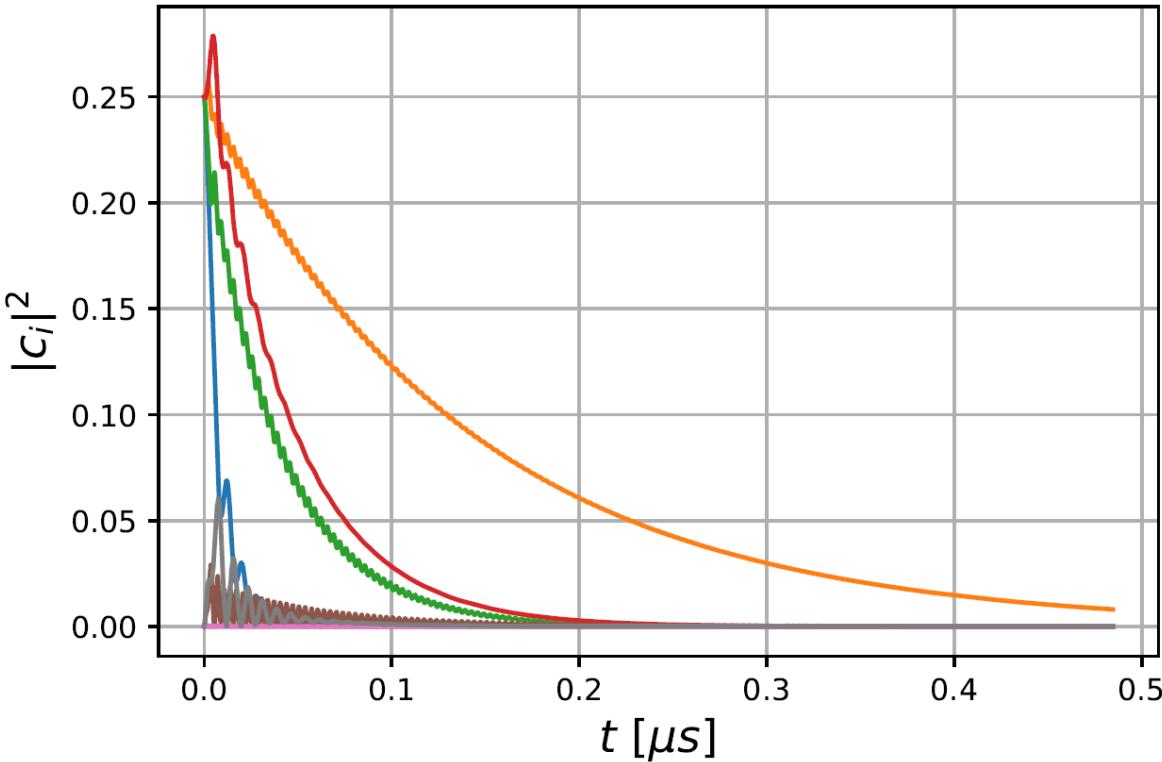
$$\omega_{0,1,0} = \frac{2.405c}{R}$$

$$\vec{E} = Re \left[ E_0 J_0 \left( \frac{2.405\rho}{R} \right) e^{-i\omega_{0,1,0} t} \hat{e}_z \right]$$

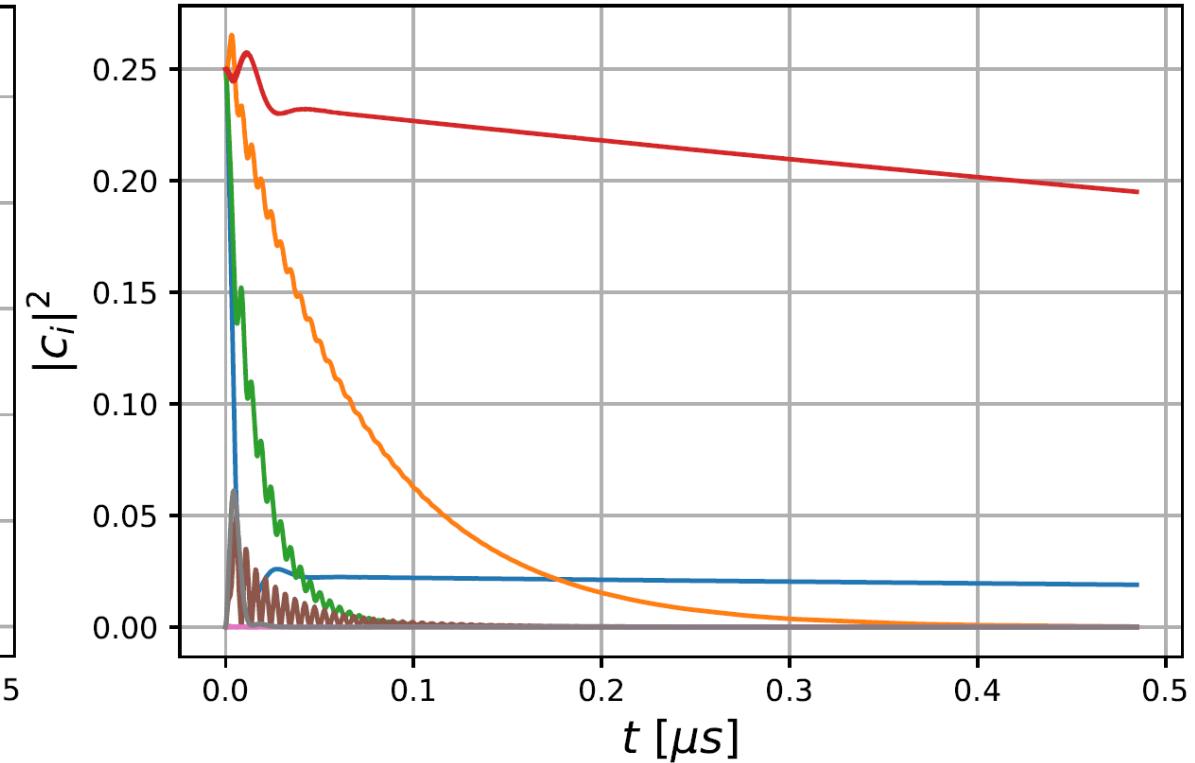
$$\vec{B} = Im \left[ -\frac{E_0}{c} J_1 \left( \frac{2.405\rho}{R} \right) e^{-i\omega_{0,1,0} t} \hat{e}_\phi \right]$$



# EVOLUTION IN TIME



$$B = 50 \text{ mT}$$

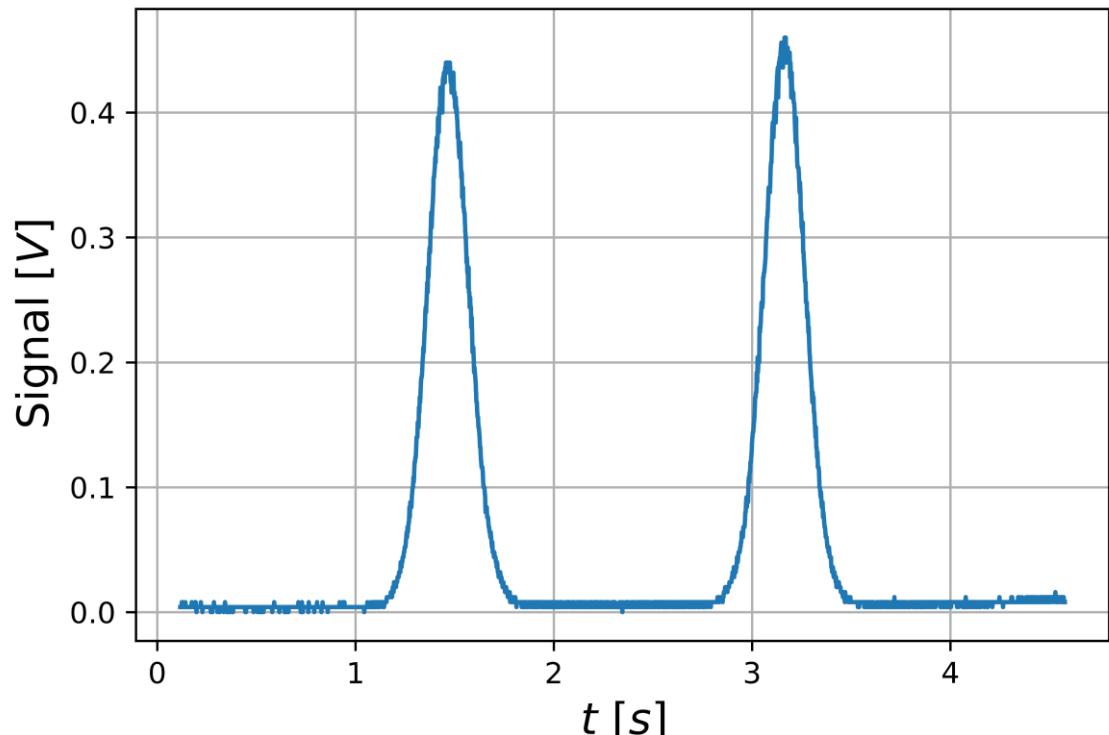


$$|c_{2S_{1/2}}|^2 = 0.25$$

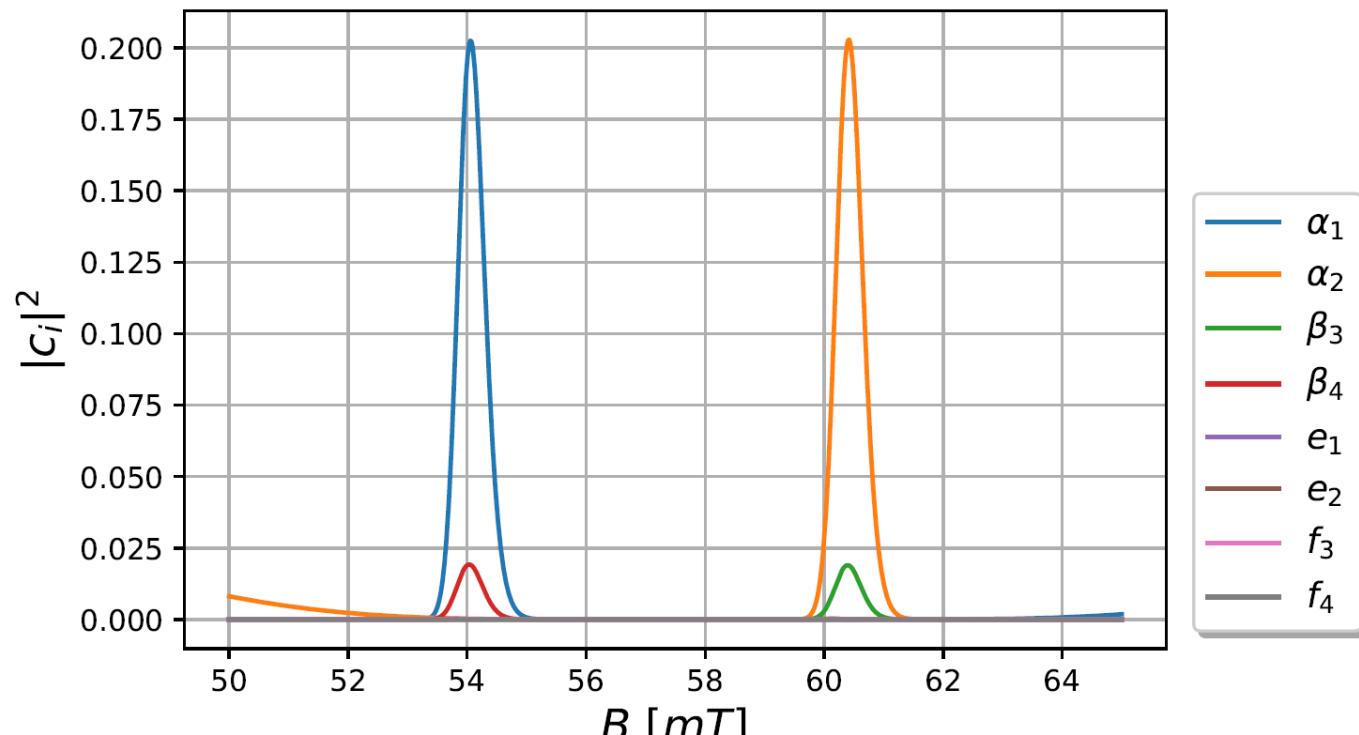
$$B = 54 \text{ mT}$$

# RAMPED MAGNETIC FIELD

Measurement

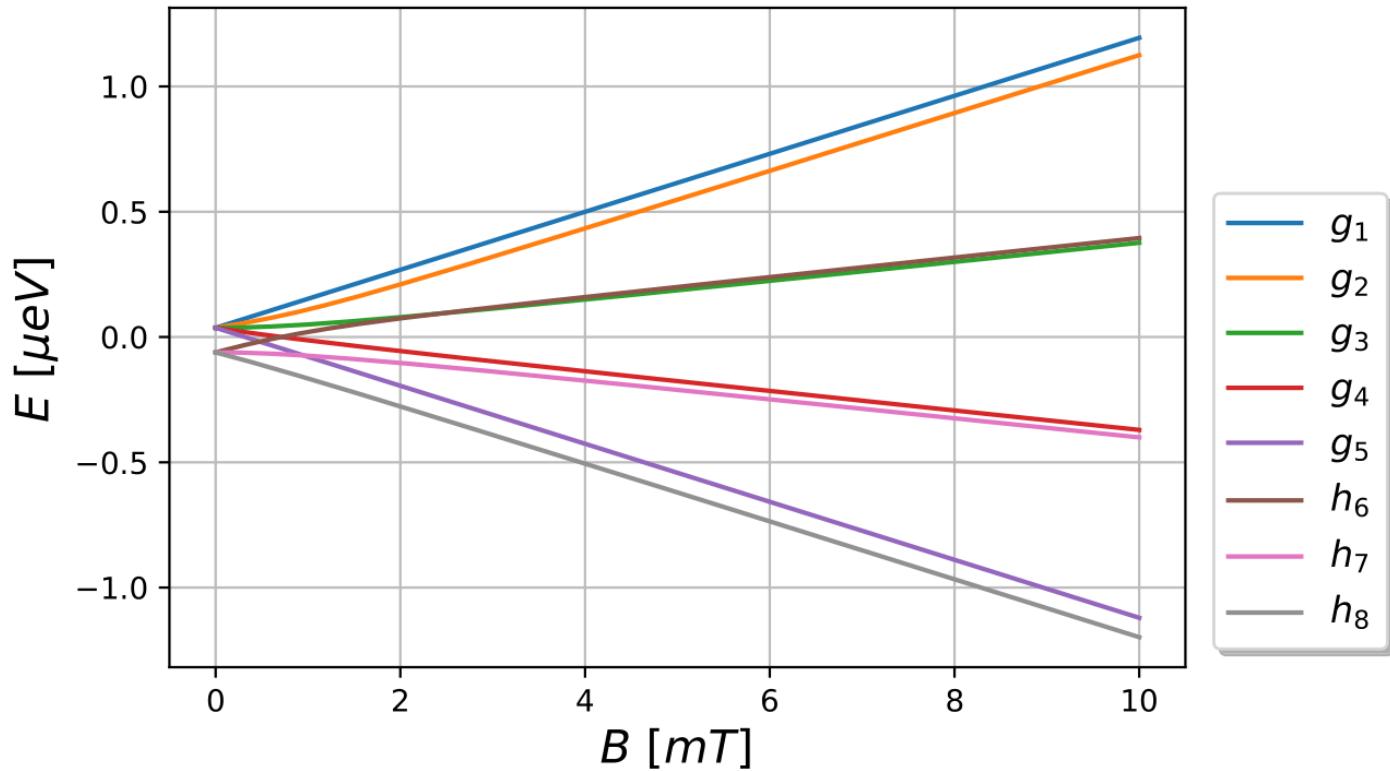


Simulation

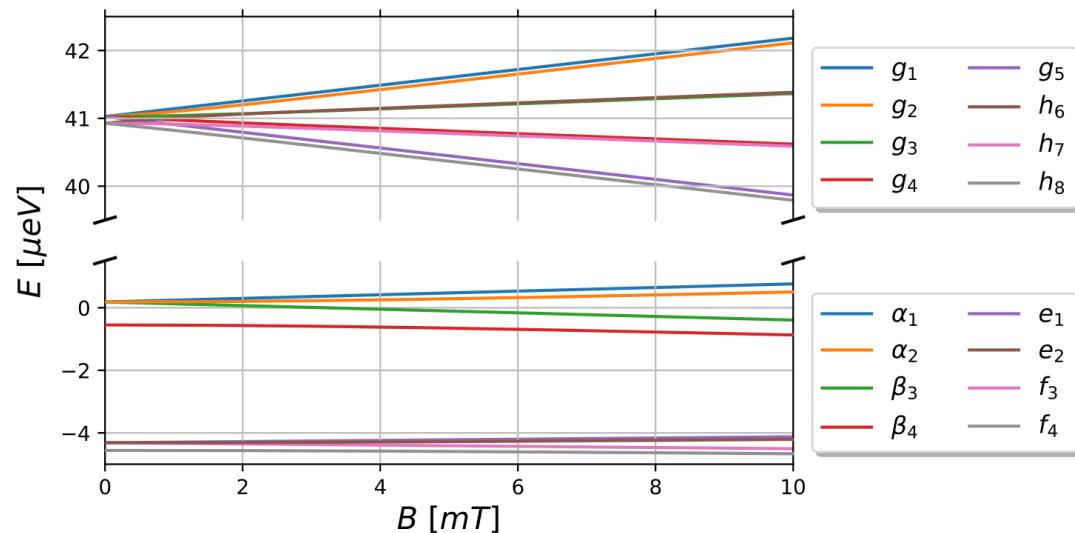


# SECOND GENERATION SPIN FILTER

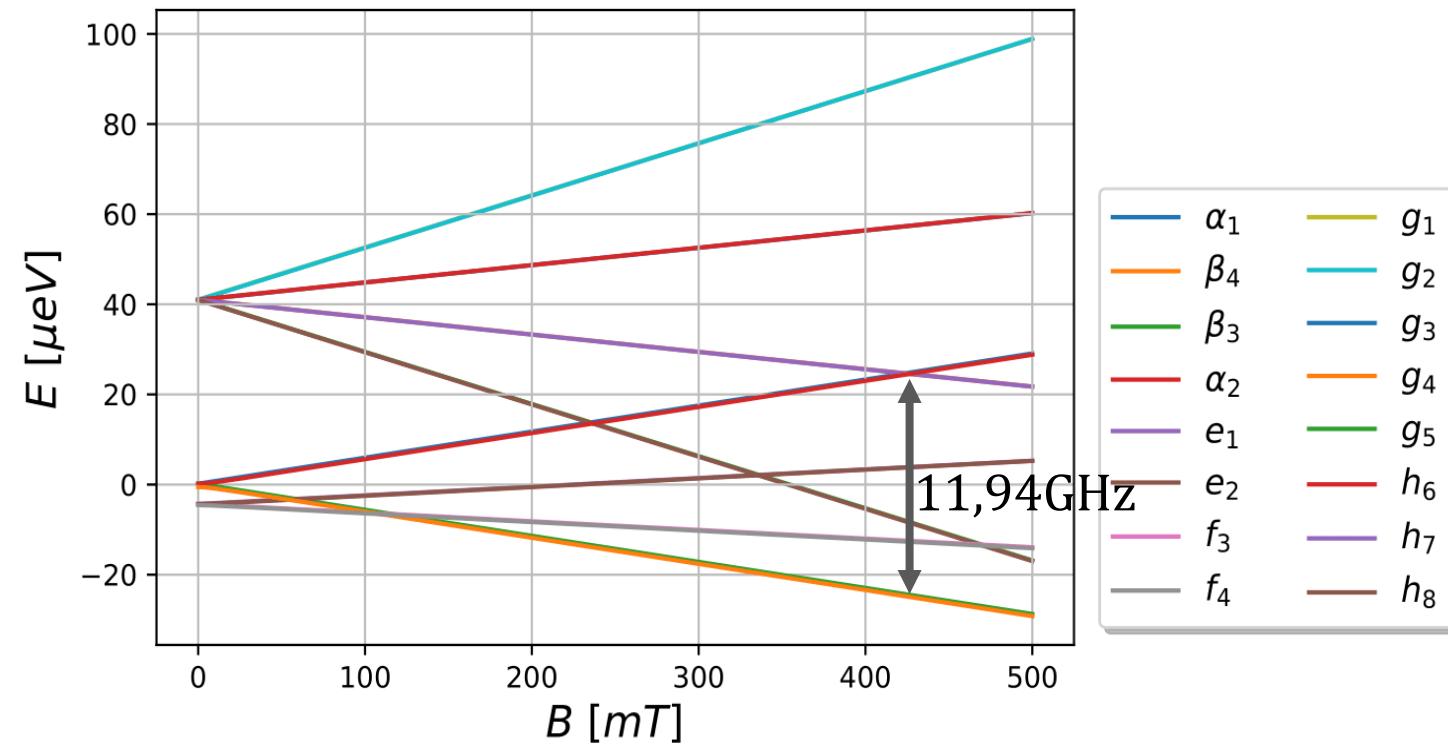
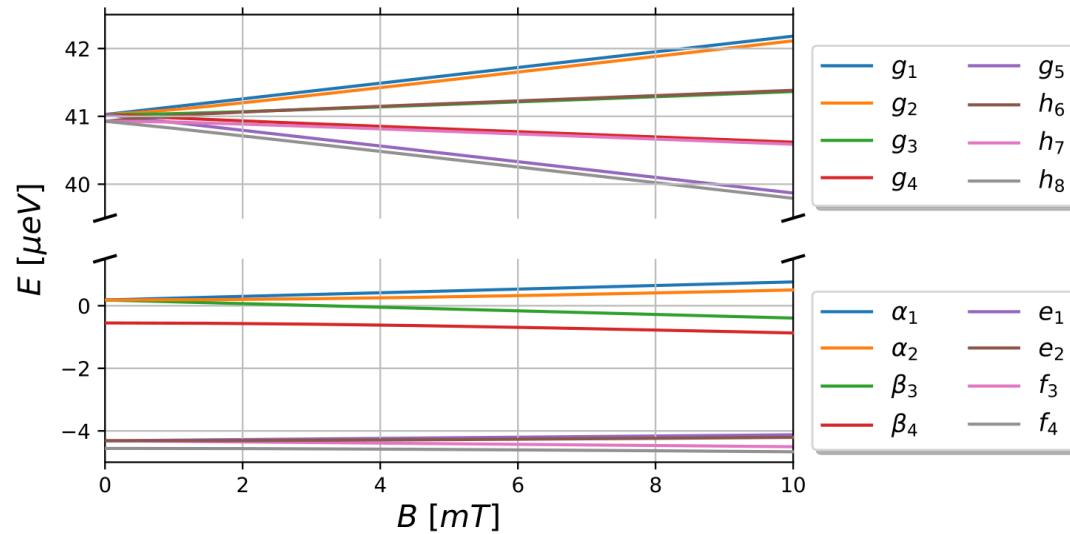
- Extend the spin filter such that also  $\beta$  states can be selected
- Use the interaction with the  $2P_{3/2}$  set



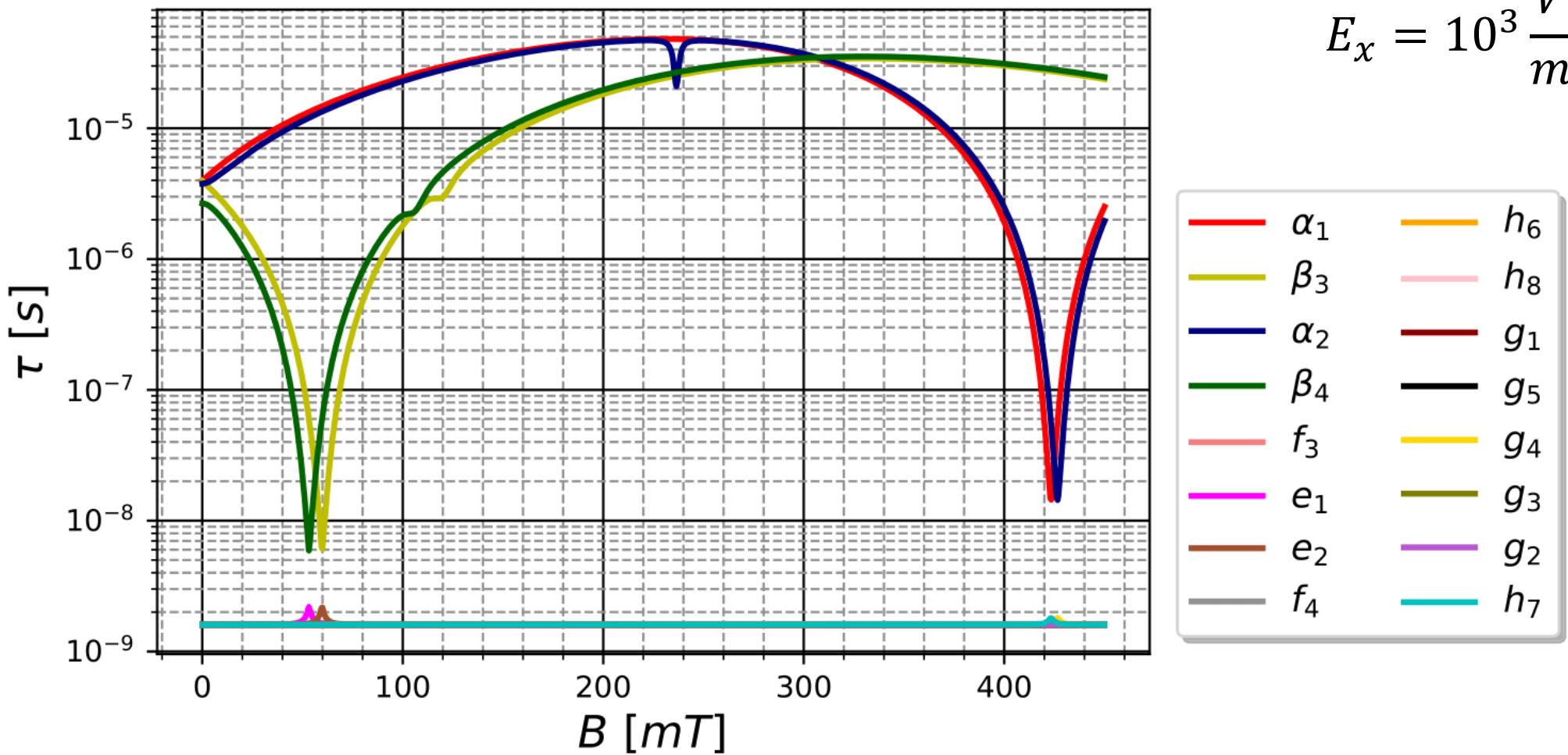
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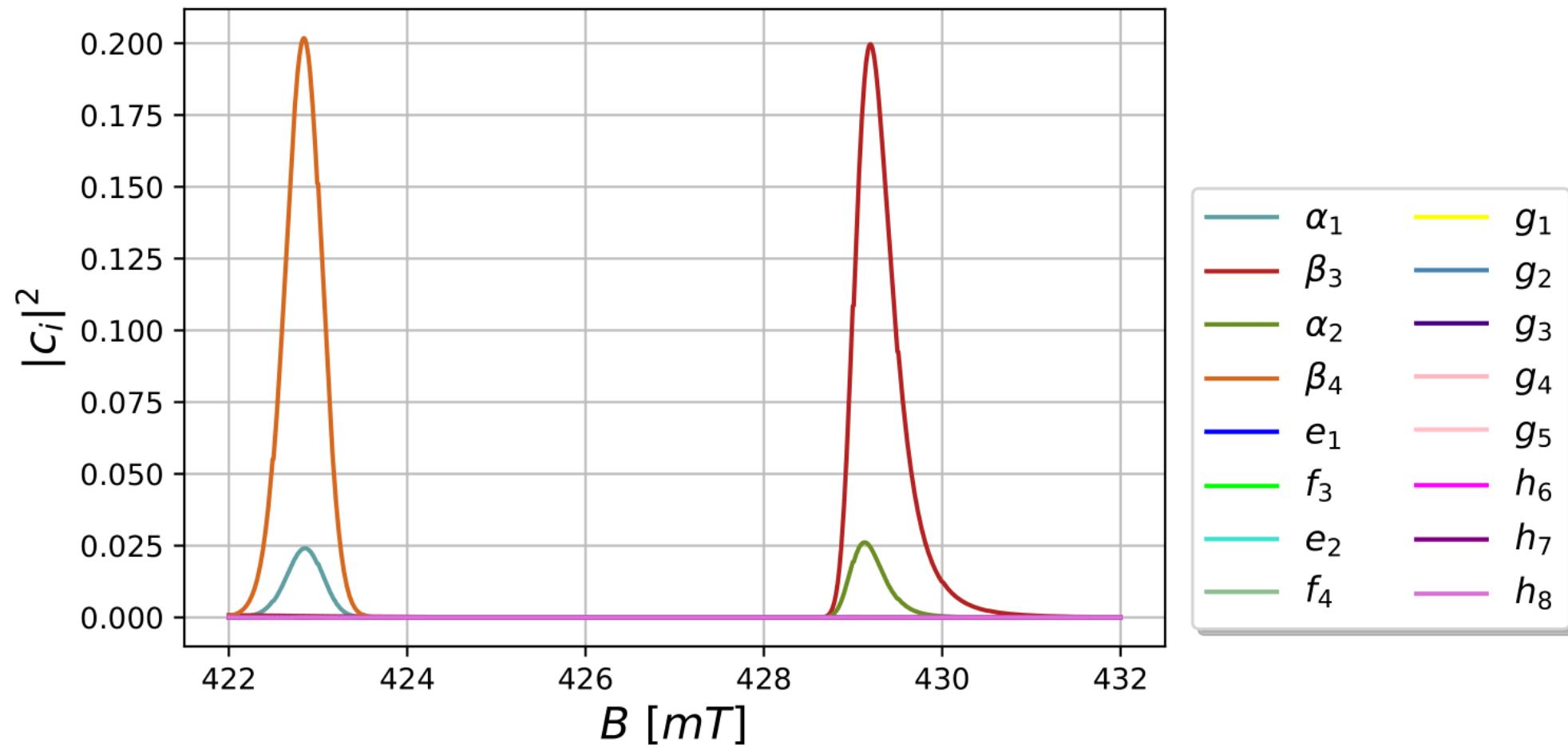
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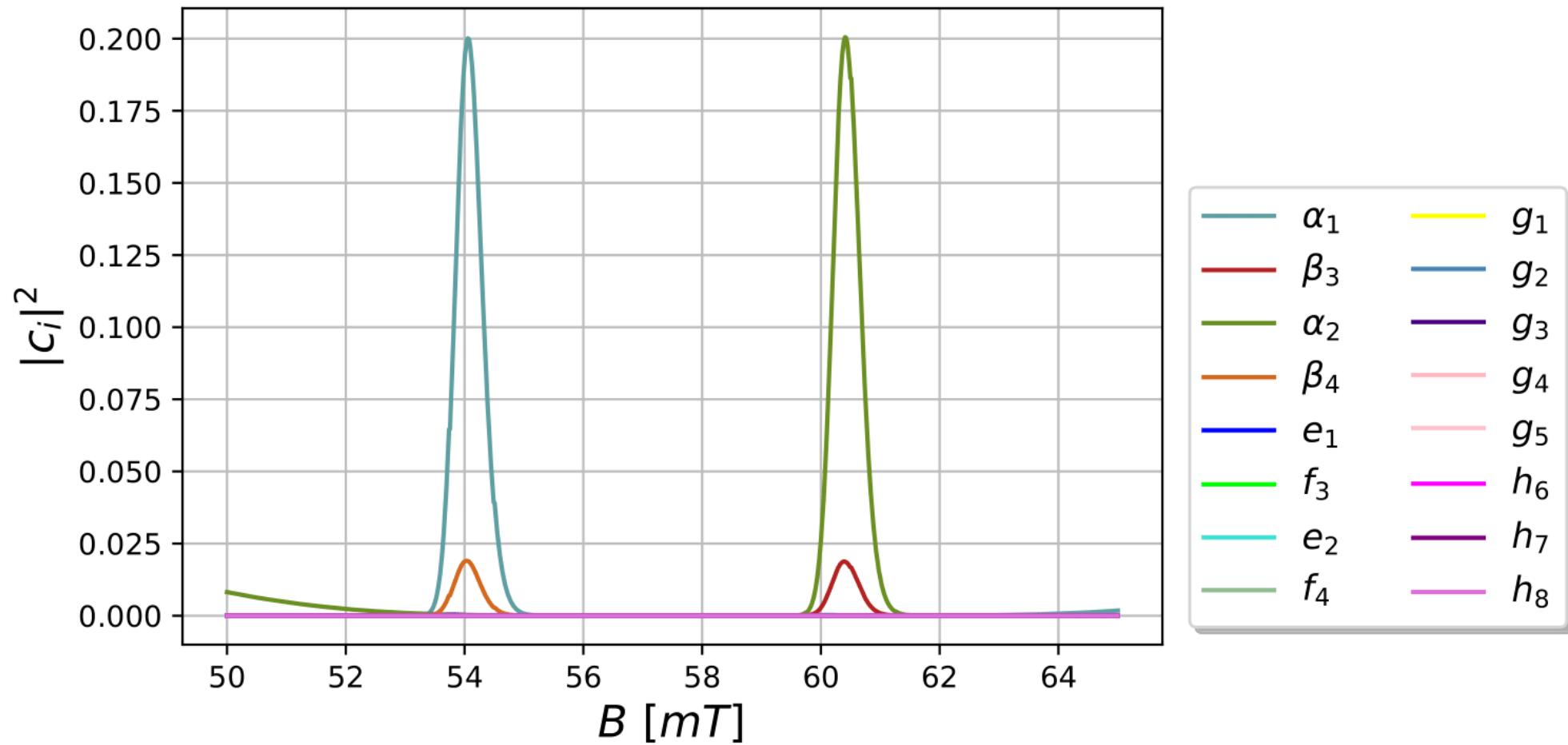
# LIFETIMES INCLUDING $2P_{3/2}$



# METASTABLE HYDROGEN

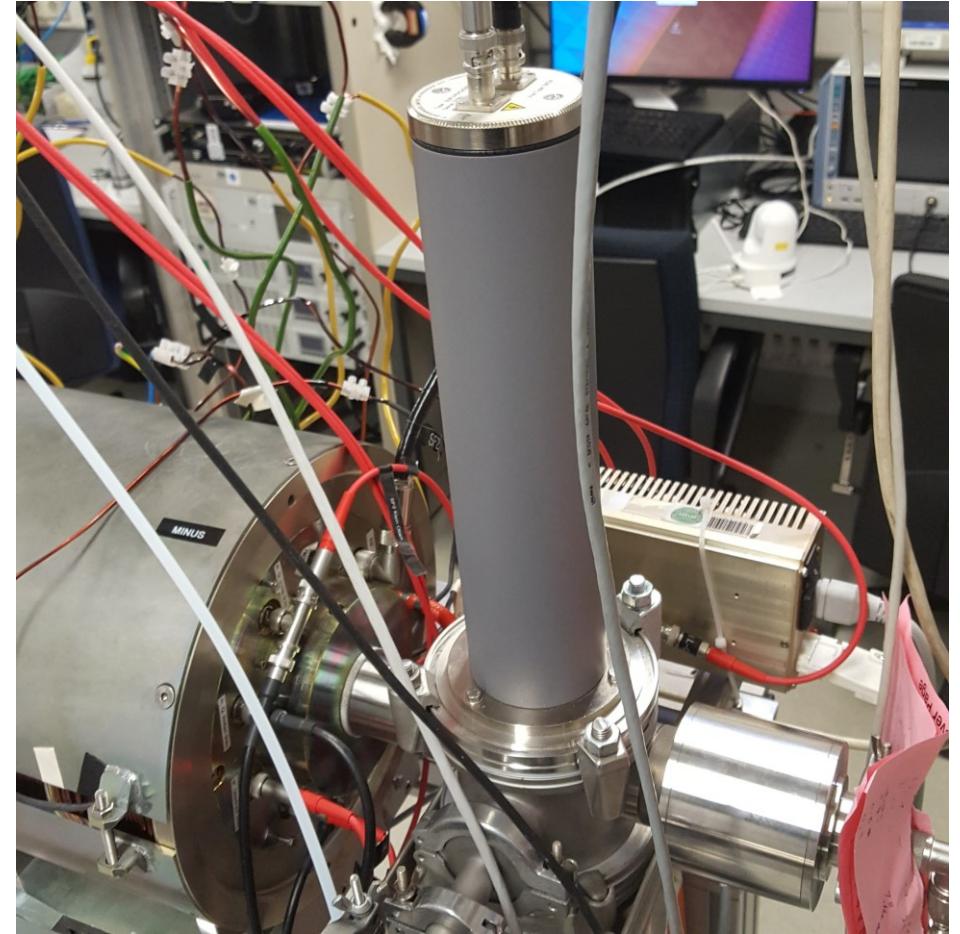


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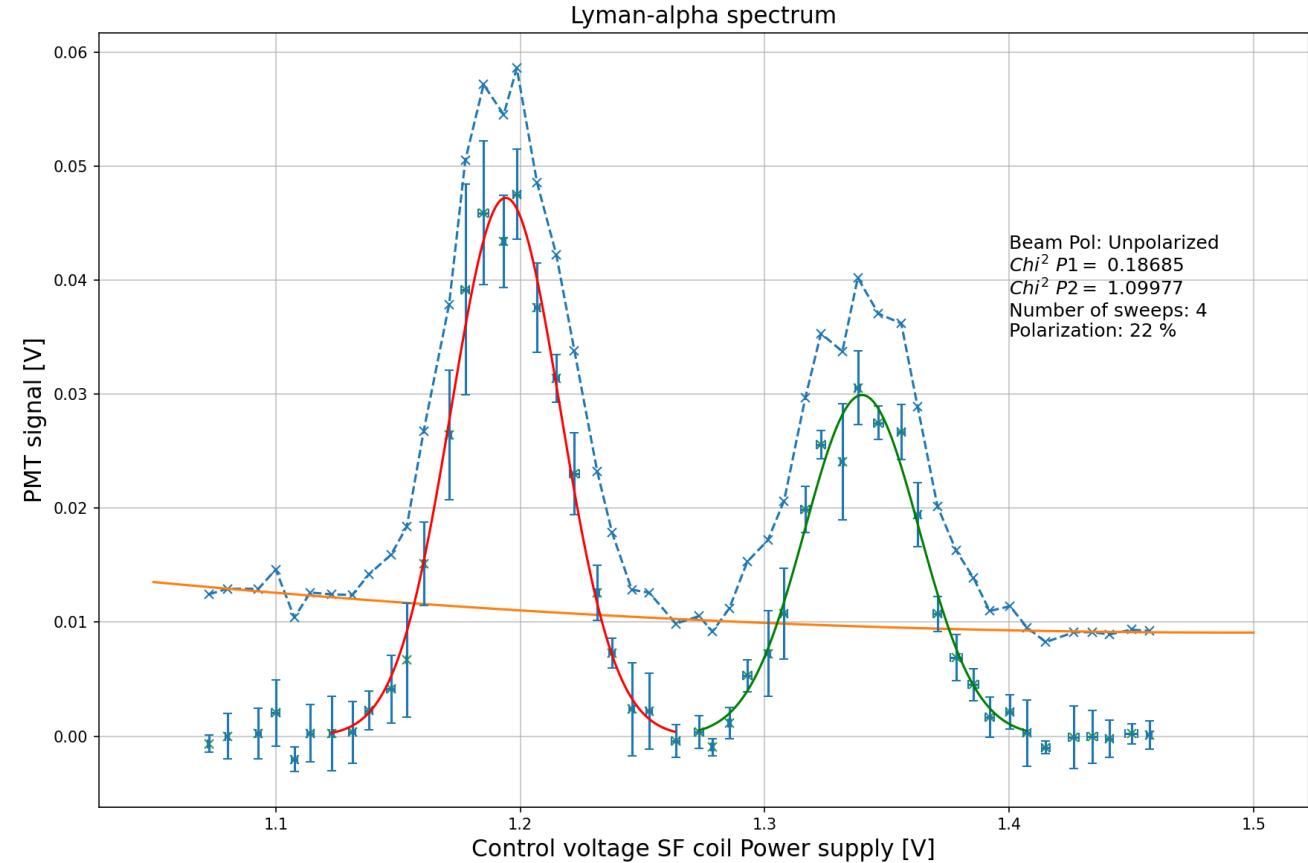
# QUENCHING CHAMBER

- Using Stark effect to quench all metastable into the ground state
- Created Ly- $\alpha$  photons are detected by a photomultiplier
- Directly observing the metastable occupation numbers



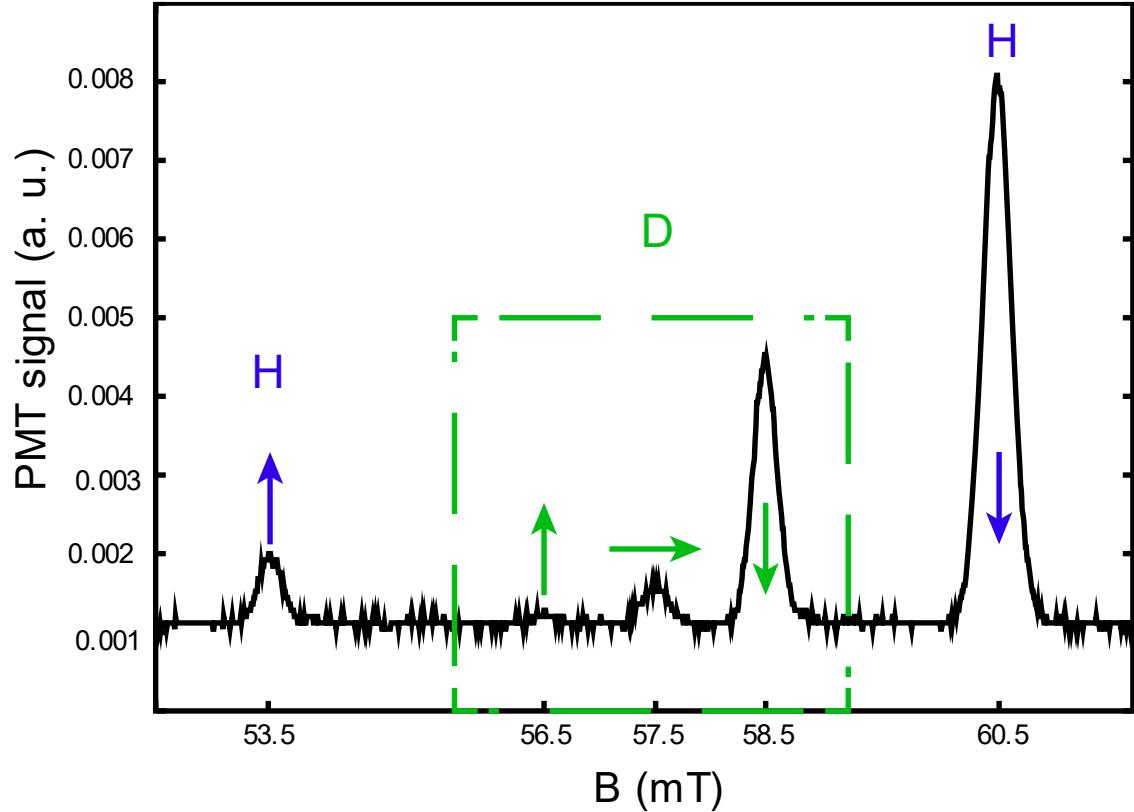
# PULSED H<sup>-</sup> SOURCE

- Direct nuclear polarization measurement
- Pulsed sources detectable
- Uncertainty in the beam transport and polarization preservation and creation



# OUTLOOK AND CONCLUSION

- Lamb-shift is a simple and consistent tool to verify nuclear and electron polarization
- Continuous and pulsed sources detectable
- Usage for hydrogen and its isotopes in atomic, ionic and molecular form



R. Engels et al. , Phys. Rev. Lett. **124**, (2020)