

Illuminating M87* Inner Shadow with Dark Matter Annihilation

Ding Ran



Yifan Chen, RD, Yuxin Liu, Yosuke Mizuno, Jing Shu, Haiyue Yu and Yanjie Zeng, [arXiv:2404.16673](https://arxiv.org/abs/2404.16673)

理论物理前沿与交叉科学研讨会

2024.04

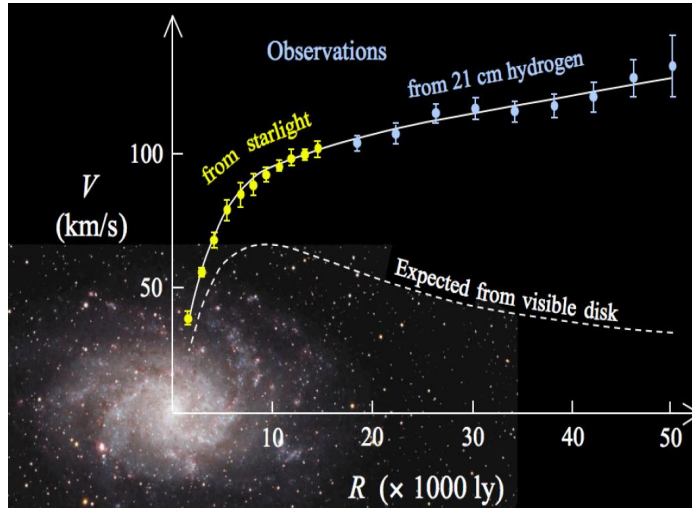
Outline

- Introduction
- Synchrotron emission around SMBH due to DM annihilation
- Constraints from the EHT observations
- Summary

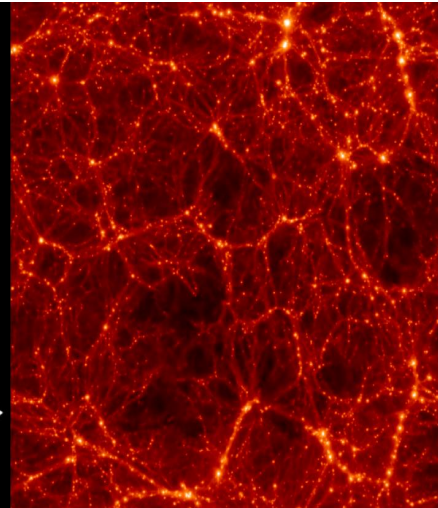
Introduction

● Evidences for DM

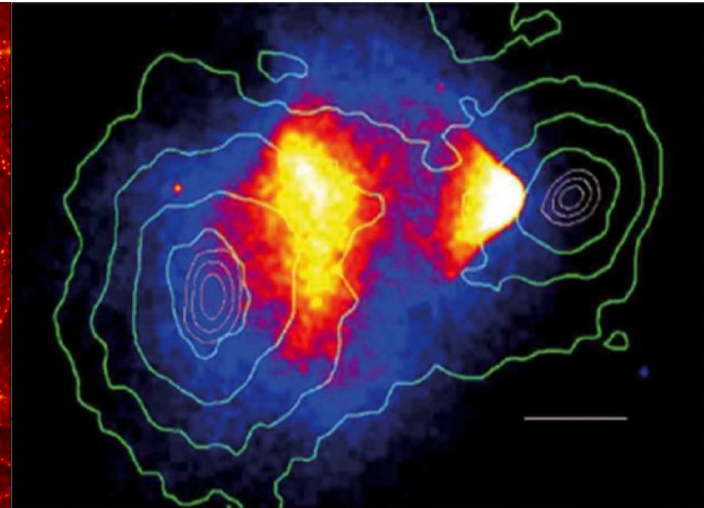
■ Rotation curves



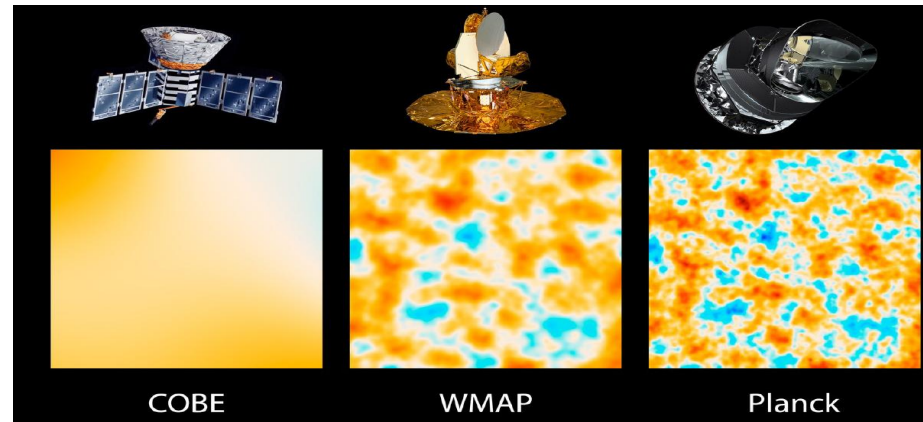
■ LSS



■ Bullet cluster



■ CMB



• DM candidates



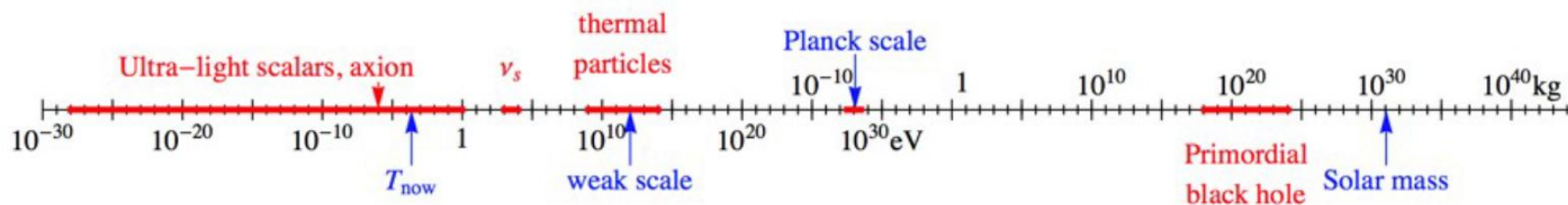
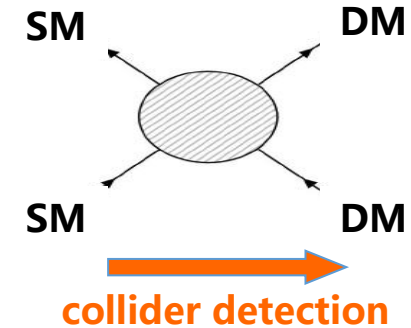
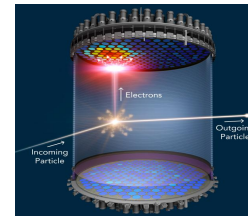
©G. Bertone and T. P. Tait

• DM detections

Cosmic-Ray (CR) physics

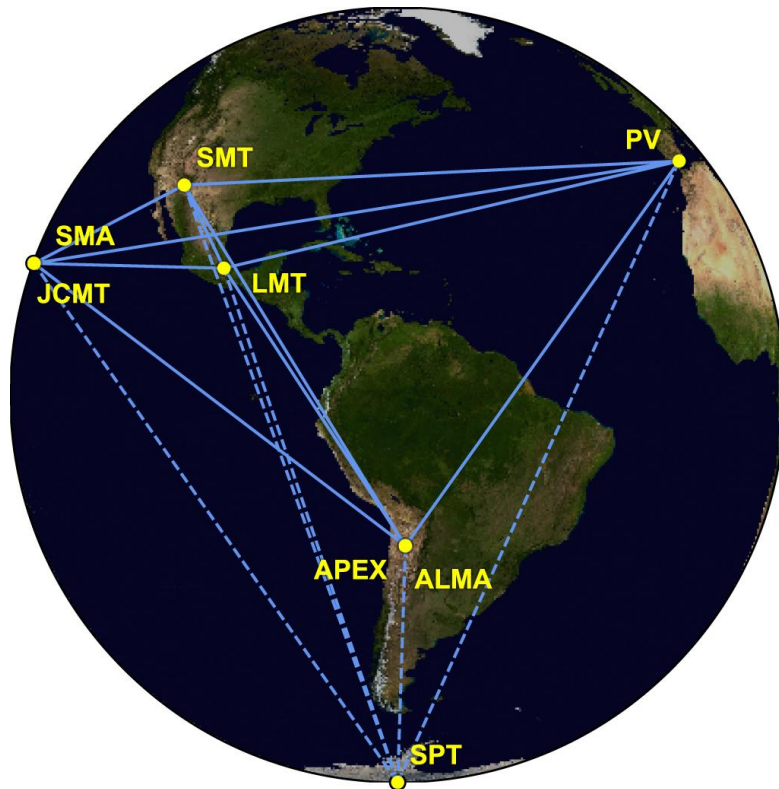


direct detection



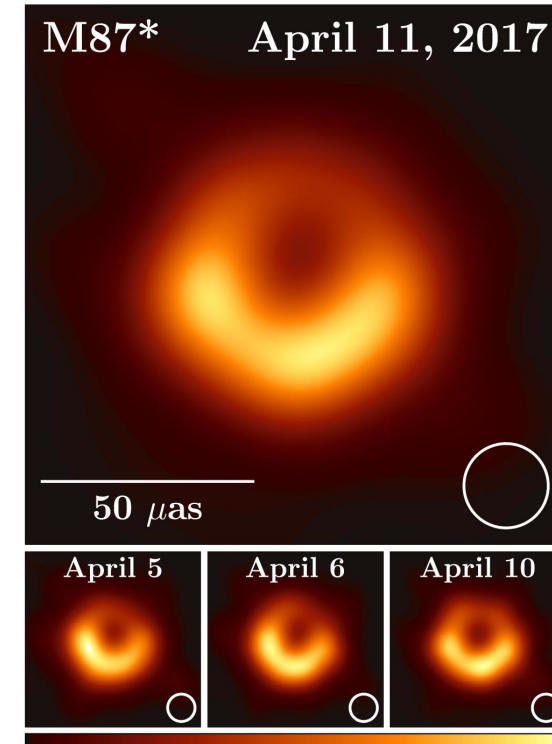
- The Event Horizon Telescope (EHT) project

- VLBI: Very Long Baseline Interferometry, an Earth-sized interferometer.
- EHT collaboration: focus on improving the capability of VLBI at short wavelengths.



- First image of a SMBH

EHT collaboration, *Astrophys. J. Lett.* 875 (2019) L1, [1906.11238]



Symbol	Value	Property
M	$6.2 \times 10^9 M_{\odot}$	Compact object mass
D	16.9 Mpc	Compact object distance
$\nu_{\text{obs},0}$	230 GHz	Observing frequency

- Synchrotron emission due to DM annihilations can be stringently constrained!

● DM spike model

- Adiabatic growth of SMBH will significantly enhance the DM density and form a spike structure.

P. Dehnen, MNRAS 265,250-256 (1993)

G.D. Quinlan, Hernquist, S.sigurdsson , APJ 440;554-564250-256 (1995)

P. Gondolo & J. Silk,PRL 83(1999) 1719{1722, [astro-ph/9906391]

O. Y. Gnedin & J. R. Primack, PRL 93 (2004) 061302, [astro-ph/0308385]

P. Ullio, H. Zhao & M. Kamionkowski, PRD 64 (2001) 043504, [astro-ph/0101481]

R. Aloisio, P. Blasi & A. V. Olinto, JCAP 05 (2004) 007, [astro-ph/0402588]

T. Lacroix, M. Karami, A. E. Broderick, J. Silk & C. Boehm, PRD 96 (2017) 063008,[1611.01961]

- Scaling relation arguments

G.D. Quinlan, Hernquist, S.sigurdsson , APJ 440;554-564250-256 (1995)

Assume a power-law initial density profile $\rho_i \sim r^{-\gamma}$

Conservation of mass

$$\rho_i r_i^2 dr_i = \rho_f r_f^2 dr_f \Rightarrow r_i^{3-\gamma} \sim r_f^{3-\gamma_{\text{sp}}}$$

Conservation of angular momentum

$$r_i M_i(r) \simeq r_f M_{\text{BH}} \Rightarrow r_i^{4-\gamma} \sim r_f$$

$$\left. \begin{array}{l} \rho_i r_i^2 dr_i = \rho_f r_f^2 dr_f \Rightarrow r_i^{3-\gamma} \sim r_f^{3-\gamma_{\text{sp}}} \\ r_i M_i(r) \simeq r_f M_{\text{BH}} \Rightarrow r_i^{4-\gamma} \sim r_f \end{array} \right\} \rightarrow \gamma_{\text{sp}} = \frac{9-2\gamma}{4-\gamma}$$

- General phase space arguments

Differential energy distribution $N(E) = g(E)f(E)$

G.D. Quinlan, Hernquist, S.sigurdsson , APJ 440;554-564250-256 (1995)

Density of state

$$g_i(E_i) \sim \int_0^{\Phi_i^{-1}(E_i)} dr r^2 \sqrt{\Phi_i(r) - E_i} \sim E_i^{(8-\gamma)/2(2-\gamma)}$$

Distribution function

$$f_i(E_i) \sim [\Phi(0)_i - E_i]^{-n}$$

Invariance of radial action

$$E_i \sim E_f^{-(2-\gamma)/(4-\gamma)} \sim r^{(2-\gamma)/(4-\gamma)}$$

$$\left. \begin{array}{l} g_i(E_i) \sim E_i^{(8-\gamma)/2(2-\gamma)} \\ f_i(E_i) \sim [\Phi(0)_i - E_i]^{-n} \\ E_i \sim E_f^{-(2-\gamma)/(4-\gamma)} \end{array} \right\} \rightarrow \rho_f(r) \sim r^{-2} N_f(E_f) \left(\frac{dE_f}{dr} \right) \sim r^{-4} N_i(E_i) \left(\frac{dE_i}{dE_f} \right) \sim r^{-\gamma_{sp}}$$

$$\text{with } \gamma_{sp} = \frac{3}{2} + n \left(\frac{2-\gamma}{4-\gamma} \right)$$

- Final density profile is determined by exact form of distribution function

P. Dehnen, MNRAS 265,250-256 (1993)

Conservation of mass

$$f(E) = \frac{1}{\sqrt{8\pi^2}} \left[\int_E^0 \frac{d^2\rho}{d\Phi^2} \frac{d\Phi}{\sqrt{\Phi - E}} - \frac{(d\rho/d\Phi)_{\Phi=0}}{\sqrt{-E}} \right]$$

$$f(E) = \frac{(3-\gamma)M}{2(2\pi^2GMa)^{3/2}} \int_0^E \frac{(1-y)^2 [\gamma + 2y + (4-\gamma)y^2]}{y^{4-\gamma} \sqrt{E-\Phi}} d\Phi \propto \begin{cases} [\Phi(0) - E]^{-1} & \gamma = 0 \\ [\Phi(0) - E]^{-(6-\gamma)/2(2-\gamma)} & 0 < \gamma < 2 \\ e^{2E} & \gamma = 2 \\ E^{(6-\gamma)/2(\gamma-2)} & 2 < \gamma < 3 \end{cases}$$

$$y = y(\Phi) = \begin{cases} [1 - (2-\gamma)\Phi]^{1/(2-\gamma)} & \gamma \neq 2 \\ e^{-\Phi} & \gamma = 2 \end{cases}$$

- Approximate distribution function for NFW profile

$$f(\varepsilon) = \frac{3M_{\text{BH}}}{2(2\pi)^3 (r_0 G M_{\text{BH}})^{3/2}} \hat{f}(\hat{\varepsilon})$$

$$\hat{\varepsilon} = -\frac{2r_0}{G M_{\text{BH}}} E$$

- DM spike profile with annihilation

$$\rho(\vec{r}) = \begin{cases} 0 & r < r_{\text{crit}}(\theta, a_J), \\ \rho_{\text{sat}} \equiv m_{\text{DM}} / (\langle \sigma v \rangle t_{\text{BH}}) & r_{\text{crit}}(\theta, a_J) \leq r < r_{\text{sat}}, \\ \rho_{\text{sp}}(r) \equiv \rho_0 (r/r_0)^{-\gamma_{\text{sp}}} & r_{\text{sat}} \leq r < r_{\text{sp}}, \\ \rho_{\text{halo}}(r) = \rho_0 (r_{\text{sp}}/r_0)^{-\gamma_{\text{sp}}} (r/r_{\text{sp}})^{-1} & r \geq r_{\text{sp}}. \end{cases}$$

- Final DM density profile

$$\rho_{\text{sp}}(r) = \frac{4\pi}{r^2} \int_{\Phi_f}^0 dE \int_{L_{\text{min}}}^{L_{\text{max}}} L dL \frac{f(E^i(E^f, L), L)}{\sqrt{2E - 2\Phi(r) - L^2/r^2}}$$

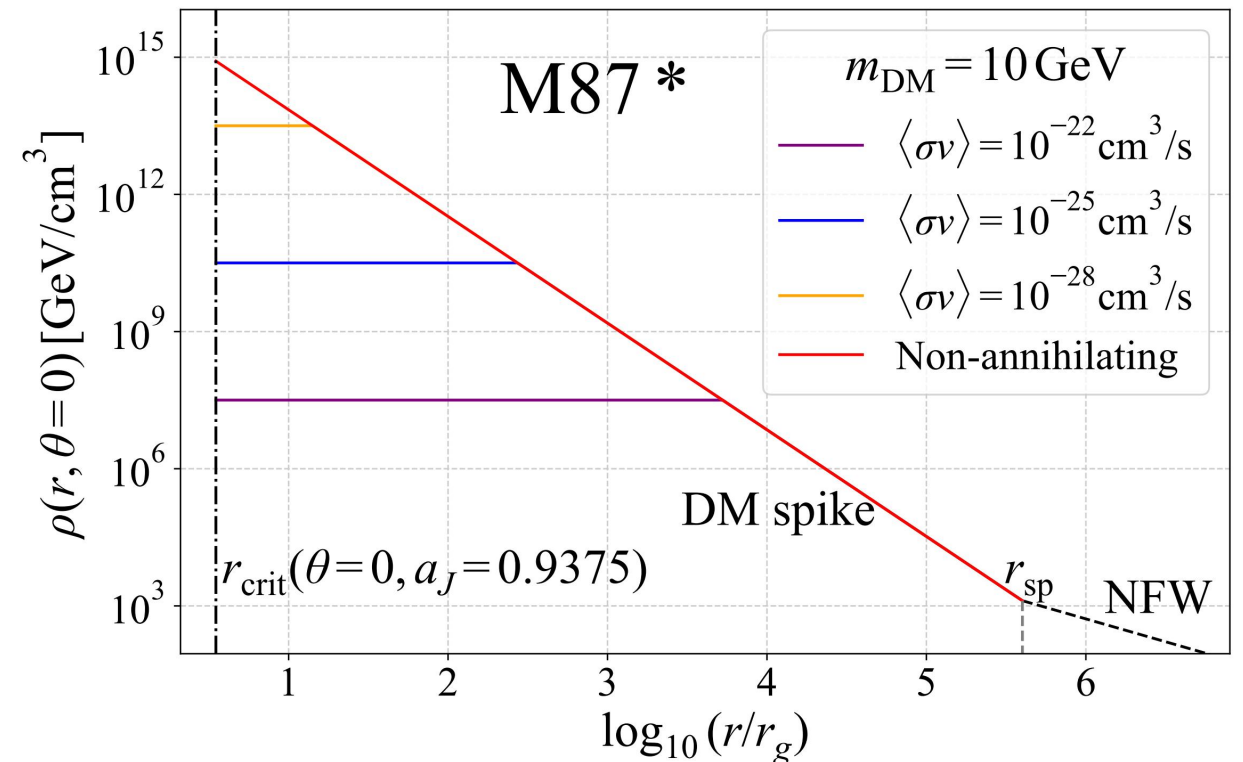
- Approximate power-law model

P. Gondolo & J. Silk, PRL 83(1999)

$$\rho_{\text{sp}}(r) = \rho_r g_\gamma(r) \left(\frac{R_{\text{sp}}}{r} \right)^{\gamma_{\text{sp}}}$$

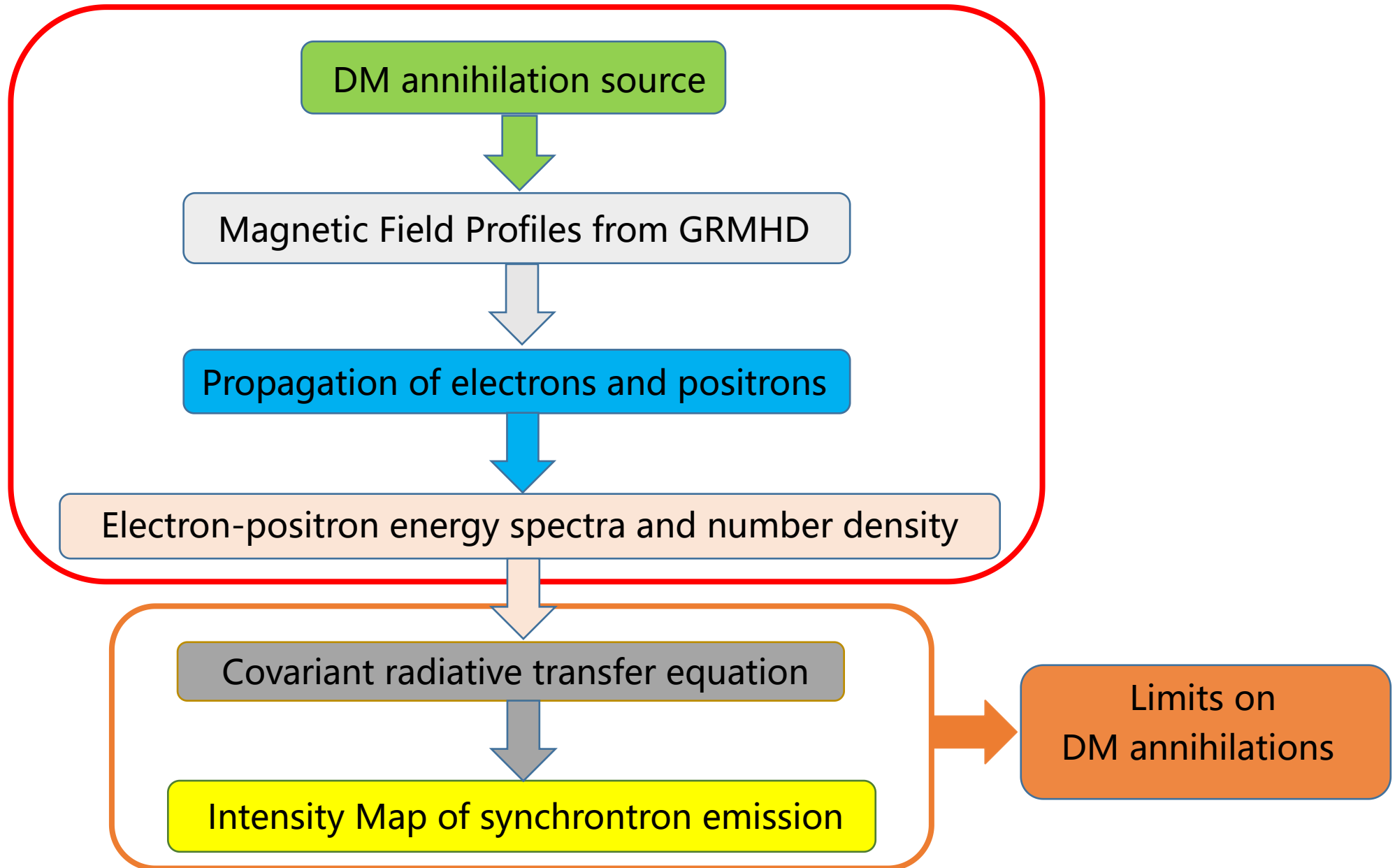
$$\rho_r = \rho_0 \left(\frac{R_{\text{sp}}}{r_0} \right)^{-\gamma}, \quad R_{\text{sp}} = \alpha_\gamma r_0 \left(\frac{M_{\text{BH}}}{\rho_0 r_0^3} \right)^{1/(3-\gamma)}$$

$$g_\gamma(r) = \left(1 - \frac{2R_s}{r} \right)^3, \quad \gamma_{\text{sp}} = \frac{9 - 2\gamma}{4 - \gamma}$$

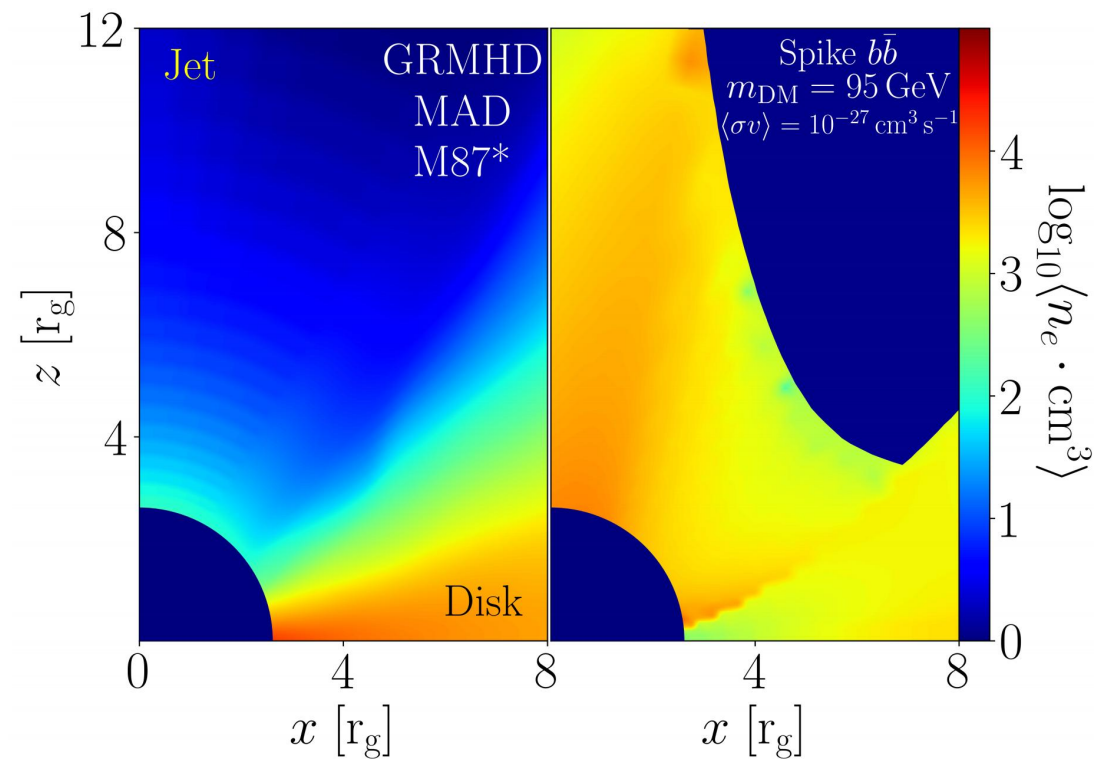
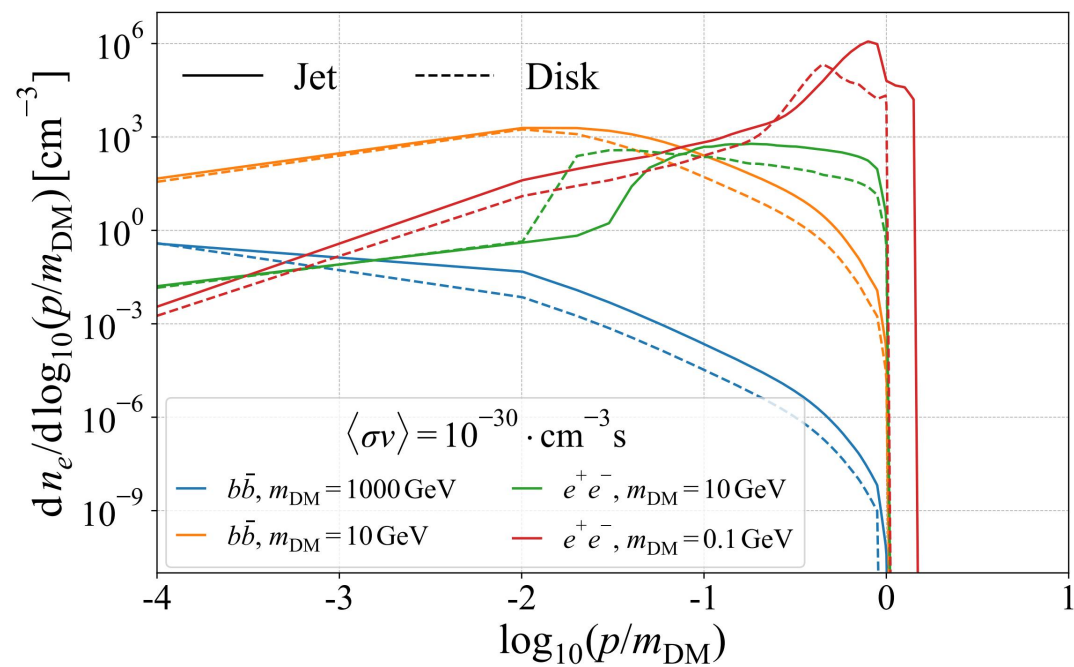


Synchrotron emission around SMBH due to DM annihilation

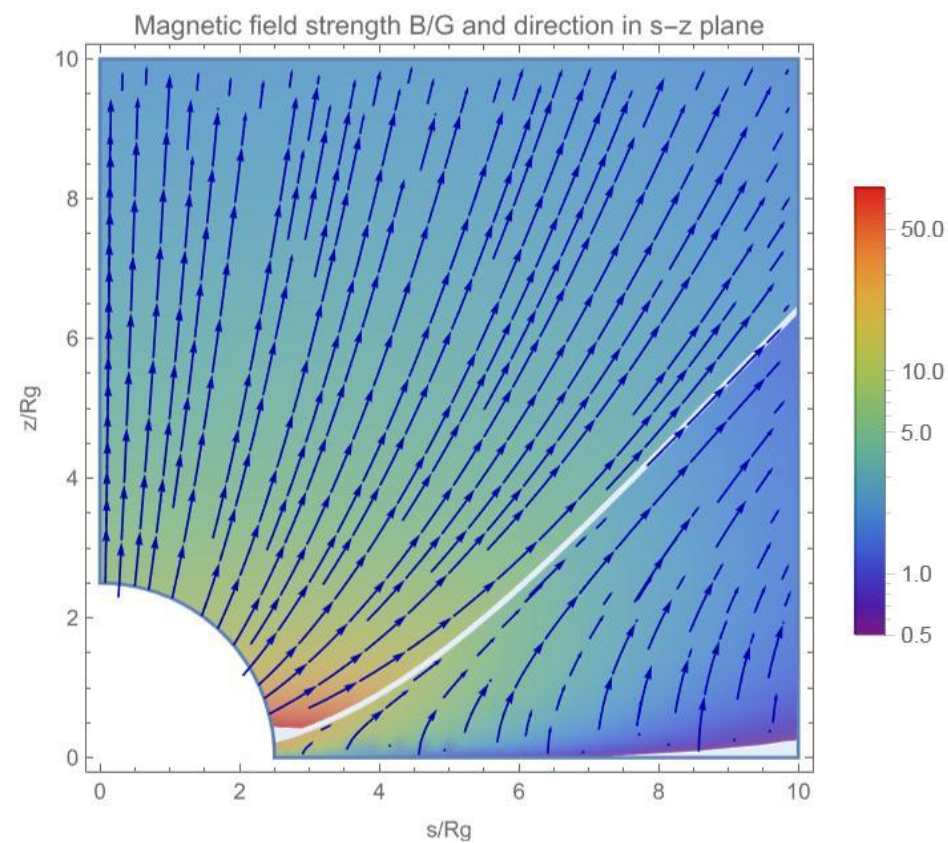
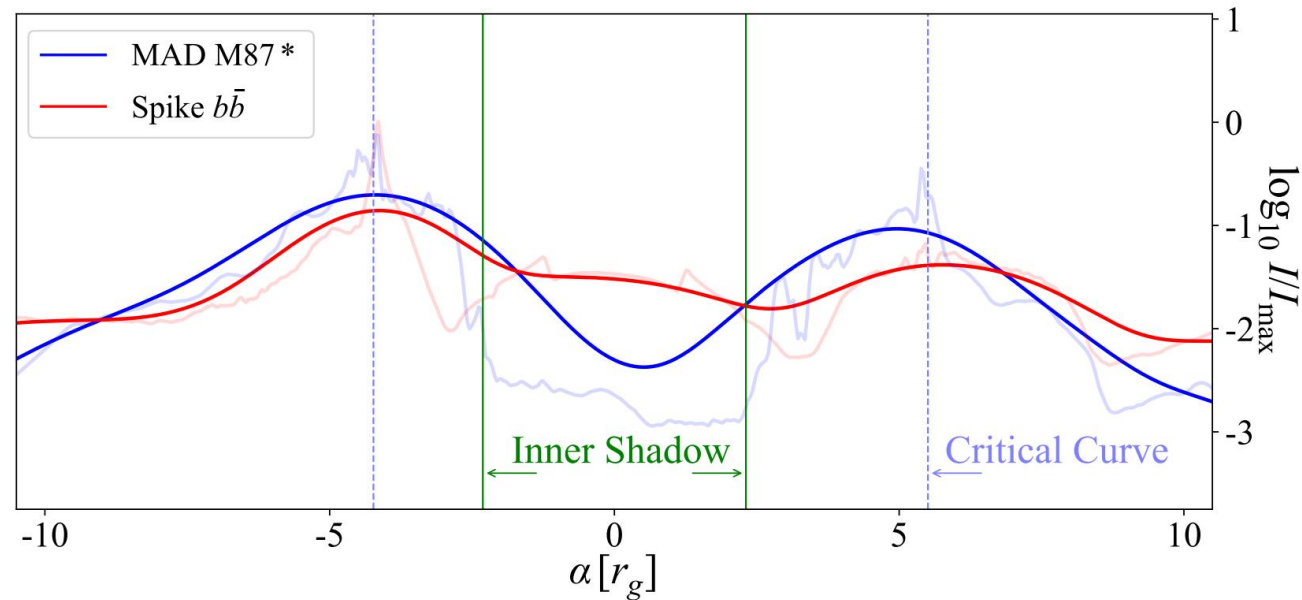
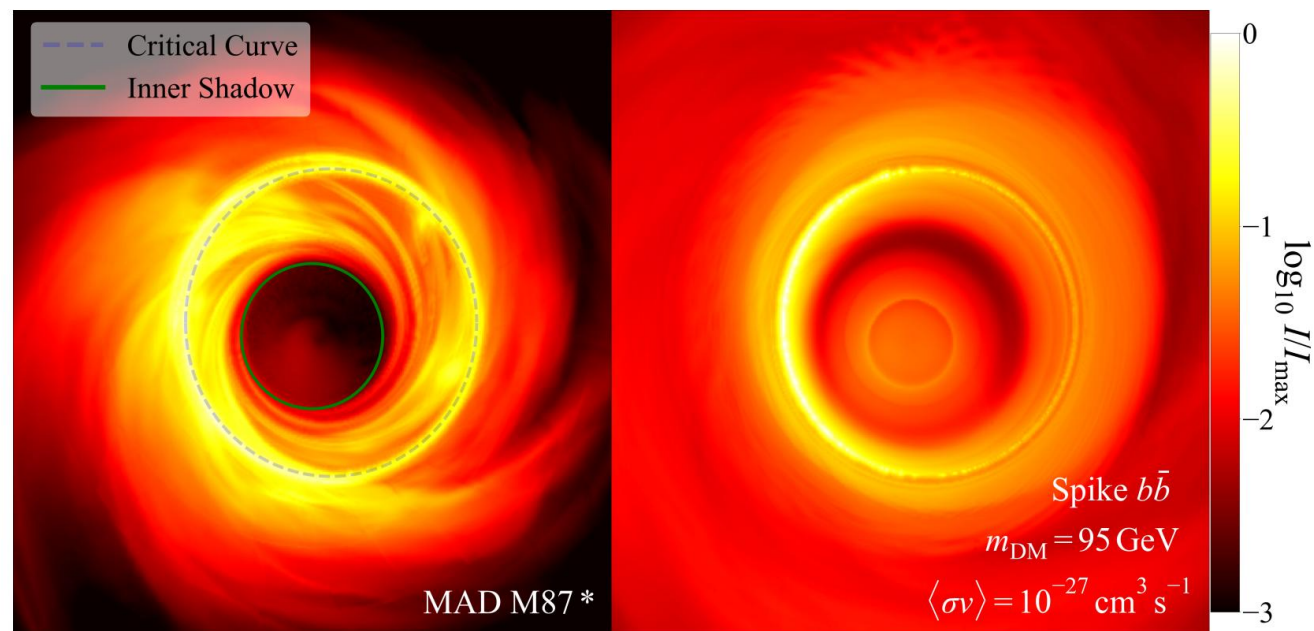
- Calculation framework



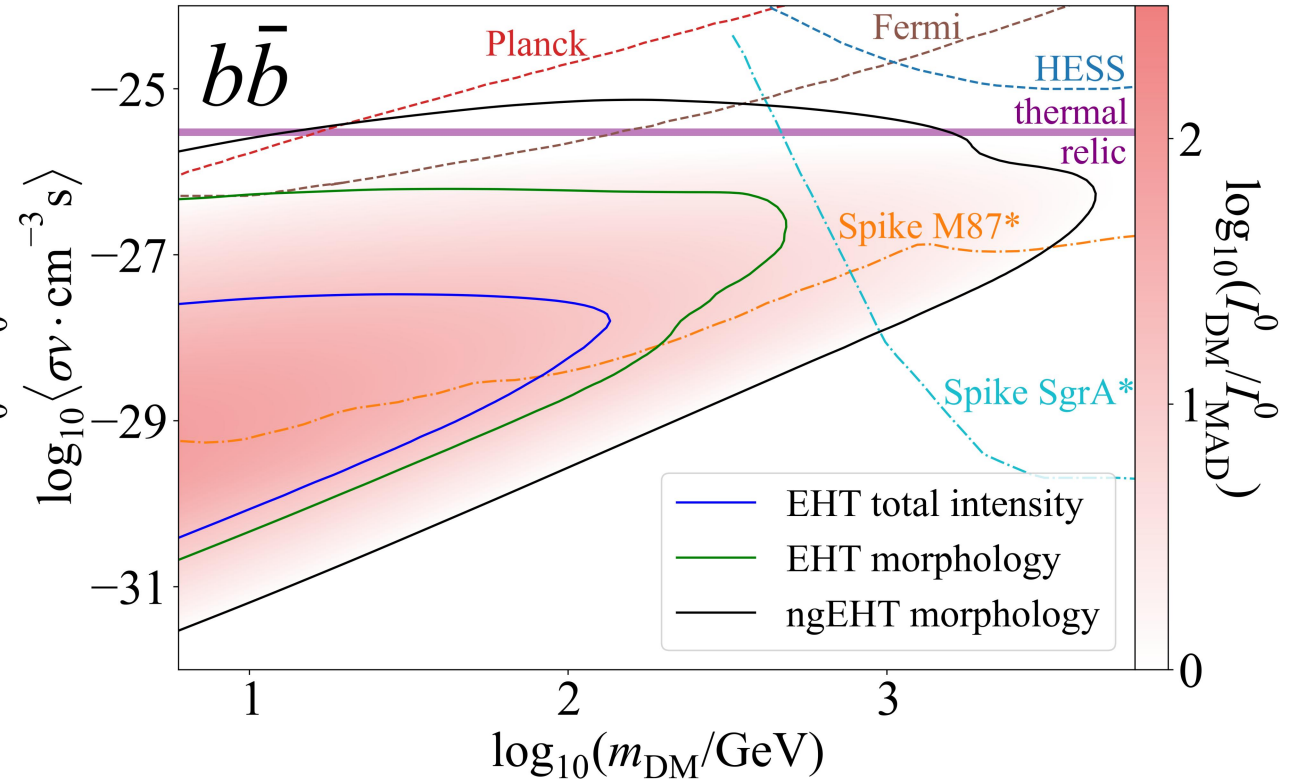
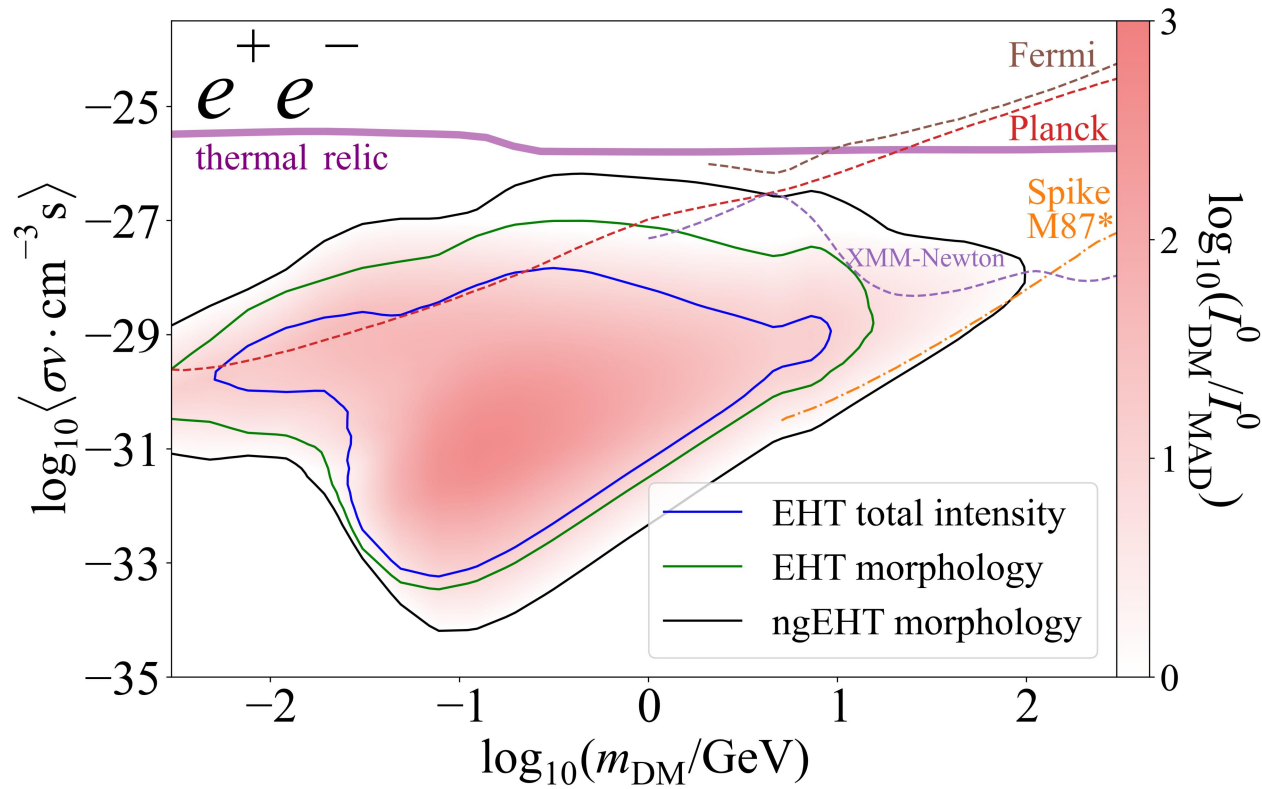
Electron-positron energy spectra and number density



Intensity Map of synchrotron emission



● Limits on DM annihilation cross sections



Summary

- Realistic magnetic field profiles from GRMHD Simulation
- Characteristic electron-positron trajectory configurations captured by the magnetic lines
- Fully GR covariant radiative transfer and Intensity Map
- The effect of the accretion disk

Thanks for your attention

