



# Flavor-spin symmetry of the $P_\Psi^N/H_{\Omega_{ccc}}^N$ and $P_{\Psi_S}^\Lambda/H_{\Omega_{cccs}}^\Lambda$ molecular states

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# Outline

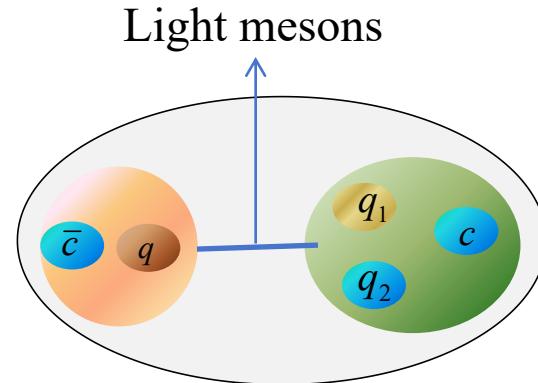
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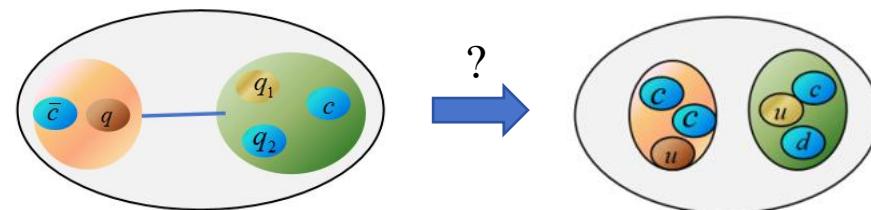
# Motivation

## Hadronic Molecule

$P_\Psi^N(4312)$ ,  $P_\Psi^N(4440)$ ,  $P_\Psi^N(4457)$ ,  $P_\Psi^N(4337)$   
 $P_{\Psi_S}^\Lambda(4338)$ ,  $P_{\Psi_S}^\Lambda(4459)$ ...



Light quarks: provide the attractive force  
Heavy quarks: stabilize the system



$$P_\Psi^N / P_{\Psi_S}^\Lambda$$

$$H_{\Omega_{ccc}}^N / H_{\Omega_{cccS}}^\Lambda$$

# Motivation

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## Triply charmed hexaquark states

One-boson-exchange

R. Chen, F. L. Wang, A. Hosaka and X. Liu, Phys. Rev. D 97, no.11, 114011 (2018).

Lattice QCD

P. Junnarkar and N. Mathur, Phys. Rev. Lett. 123, no.16, 162003 (2019).

QCD sum rule

Z. G. Wang, Phys. Rev. D 102, no.3, 034008 (2020).

Effective field theory

Y. W. Pan, M. Z. Liu, F. Z. Peng, M. Sánchez Sánchez, L. S. Geng and M. Pavon Valderrama, Phys. Rev. D 102, no.1, 011504 (2020).

# Motivation

## Heavy diquark-antiquark symmetry (HDAS)

Quark content	System and threshold					
$(nnc)(n\bar{c})$	$\Lambda_c \bar{D}$	$\Lambda_c \bar{D}^*$	$\Sigma_c \bar{D}$	$\Sigma_c^* \bar{D}$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}^*$
	4153.7	4295.0	4320.8	4385.4	4462.1	4526.7
$(nnc)(ncc)$	$\Lambda_c \Xi_{cc}$	$\Lambda_c \Xi_{cc}^*$	$\Sigma_c \Xi_{cc}$	$\Sigma_c^* \Xi_{cc}$	$\Sigma_c \Xi_{cc}^*$	$\Sigma_c^* \Xi_{cc}^*$
	5907.9	6013.5	6074.9	6139.5	6180.5	6245.1
$(nnc)(s\bar{c})$	$\Lambda_c \bar{D}_s$	$\Lambda_c \bar{D}_s^*$	$\Sigma_c \bar{D}_s$	$\Sigma_c^* \bar{D}_s$	$\Sigma_c \bar{D}_s^*$	$\Sigma_c^* \bar{D}_s^*$
	4255.5	4398.7	4422.5	4487.1	4565.7	4630.3
$(nsc)(n\bar{c})$	$\Xi_c \bar{D}$	$\Xi_c \bar{D}^*$	$\Xi'_c \bar{D}$	$\Xi_c^* D$	$\Xi'_c \bar{D}^*$	$\Xi_c^* \bar{D}^*$
	4336.7	4478.0	4446.0	4513.2	4587.4	4654.5
$(nnc)(scc)$	$\Lambda_c \Omega_{cc}$	$\Lambda_c \Omega_{cc}^*$	$\Sigma_c \Omega_{cc}$	$\Sigma_c^* \Omega_{cc}$	$\Sigma_c \Omega_{cc}^*$	$\Sigma_c^* \Omega_{cc}^*$
	6064.5	6158.5	6231.5	6296.1	6325.5	6390.1
$(nsc)(ncc)$	$\Xi_c \Xi_{cc}$	$\Xi_c \Xi_{cc}^*$	$\Xi'_c \Xi_{cc}$	$\Xi_c^* \Xi_{cc}$	$\Xi'_c \Xi_{cc}^*$	$\Xi_c^* \Xi_{cc}^*$
	6090.5	6196.1	6199.9	6267.4	6305.5	6373.0

The masses of  $\Xi_{cc}^*$  and  $\Omega_{cc}^{(*)}$  baryon: D. Ebert, R. N. Faustov, V. O. Galkin and A. P. Martynenko, Phys. Rev. D 66, 014008 (2002).

	$I(J^P)$	Channel
$P_\psi^N$	$\frac{1}{2}(\frac{1}{2}^-)$	$\Lambda_c \bar{D}, \Lambda_c \bar{D}^*, \Sigma_c \bar{D}, \Sigma_c \bar{D}^*, \Sigma_c^* \bar{D}^*$
	$\frac{1}{2}(\frac{3}{2}^-)$	$\Lambda_c \bar{D}^*, \Sigma_c^* \bar{D}, \Sigma_c \bar{D}^*, \Sigma_c^* \bar{D}^*$
	$\frac{1}{2}(\frac{5}{2}^-)$	$\Sigma_c^* \bar{D}^*$
$P_{\psi s}^\Lambda$	$0(\frac{1}{2}^-)$	$\Lambda_c \bar{D}_s, \Lambda_c \bar{D}_s^*, \Xi_c \bar{D}, \Xi_c \bar{D}^*, \Xi'_c \bar{D}, \Xi'_c \bar{D}^*, \Xi_c^* \bar{D}^*$
	$0(\frac{3}{2}^-)$	$\Lambda_c \bar{D}_s^*, \Xi_c \bar{D}^*, \Xi_c^* \bar{D}, \Xi'_c \bar{D}^*, \Xi_c^* \bar{D}^*$
	$0(\frac{5}{2}^-)$	$\Xi_c^* \bar{D}^*$
$H_{\Omega_{ccc}}^N$	$\frac{1}{2}(0^+)$	$\Lambda_c \Xi_{cc}, \Sigma_c \Xi_{cc}, \Sigma_c^* \Xi_{cc}^*$
	$\frac{1}{2}(1^+)$	$\Lambda_c \Xi_{cc}, \Lambda_c \Xi_{cc}^*, \Sigma_c \Xi_{cc}, \Sigma_c^* \Xi_{cc}, \Sigma_c \Xi_{cc}^*, \Sigma_c^* \Xi_{cc}^*$
	$\frac{1}{2}(2^+)$	$\Lambda_c \Xi_{cc}^*, \Sigma_c^* \Xi_{cc}, \Sigma_c \Xi_{cc}^*, \Sigma_c^* \Xi_{cc}^*$
$H_{\Omega_{cccs}}^\Lambda$	$\frac{1}{2}(3^+)$	$\Sigma_c^* \Xi_{cc}^*$
	$\frac{1}{2}(0^+)$	$\Lambda_c \Omega_{cc}, \Xi_c \Xi_{cc}, \Xi'_c \Xi_{cc}, \Xi_c^* \Xi_{cc}^*$
	$\frac{1}{2}(1^+)$	$\Lambda_c \Omega_{cc}^*, \Xi_c \Xi_{cc}, \Xi_c \Xi_{cc}^*, \Xi'_c \Xi_{cc}, \Xi_c^* \Xi_{cc}, \Xi'_c \Xi_{cc}^*, \Xi_c^* \Xi_{cc}^*$
	$\frac{1}{2}(2^+)$	$\Xi_c \Xi_{cc}^*, \Xi_c^* \Xi_{cc}, \Xi'_c \Xi_{cc}^*, \Xi_c^* \Xi_{cc}^*$
	$\frac{1}{2}(3^+)$	$\Xi_c^* \Xi_{cc}^*$

# Framework

## Flavor wave function

Meson	$ Im_I\rangle$	$\phi_{Im_I}^M$	Meson	$ Im_I\rangle$	$\phi_{Im_I}^M$
$\bar{D}^{(*)0}$	$ \frac{1}{2}\frac{1}{2}\rangle$	$u\bar{c}$	$\bar{D}^{*-}$	$ \frac{1}{2}-\frac{1}{2}\rangle$	$d\bar{c}$
$\bar{D}_s^{(*)-}$	$ 00\rangle$	$s\bar{c}$			
Baryon	$ Im_I\rangle$	$\phi_{Im_I}^B$	Baryon	$ Im_I\rangle$	$\phi_{Im_I}^B$
$\Lambda_c^+$	$ 00\rangle$	$\frac{1}{\sqrt{2}}(du - ud)c$	$\Sigma_c^{(*)++}$	$ 11\rangle$	$uuc$
$\Sigma_c^{(*)+}$	$ 10\rangle$	$\frac{1}{\sqrt{2}}(ud + du)c$	$\Sigma_c^{(*)0}$	$ 1-1\rangle$	$ddc$
$\Xi_c^+$	$ \frac{1}{2}\frac{1}{2}\rangle$	$\frac{1}{\sqrt{2}}(us - su)c$	$\Xi_c^0$	$ \frac{1}{2}-\frac{1}{2}\rangle$	$\frac{1}{\sqrt{2}}(ds - sd)c$
$\Xi_c'^{(*)+}$	$ \frac{1}{2}\frac{1}{2}\rangle$	$\frac{1}{\sqrt{2}}(us + su)c$	$\Xi_c'^{(*)0}$	$ \frac{1}{2}-\frac{1}{2}\rangle$	$\frac{1}{\sqrt{2}}(ds + sd)c$
$\Xi_{cc}^{(*)++}$	$ \frac{1}{2}\frac{1}{2}\rangle$	$ucc$	$\Xi_{cc}^{(*)+}$	$ \frac{1}{2}-\frac{1}{2}\rangle$	$dcc$
$\Omega_{cc}^{(*)+}$	$ 00\rangle$	$scc$			

## Spin wave function

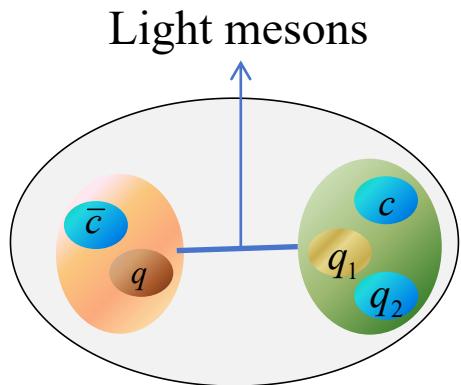
Hadron	$ Sm_S\rangle$	$\phi_{Sm_S}^M$	Hadron	$ Sm_S\rangle$	$\phi_{Sm_S}^M$
$\bar{D}/\bar{D}_s$	$ 00\rangle$	$\frac{1}{\sqrt{2}}(\uparrow\downarrow - \downarrow\uparrow)$	$\bar{D}^*/\bar{D}_s^*$	$ 11\rangle$	$\uparrow\uparrow$
			$ \text{10}\rangle$	$\frac{1}{\sqrt{2}}(\uparrow\downarrow + \downarrow\uparrow)$	
			$ 1-1\rangle$	$\downarrow\downarrow$	
Hadron	$ Sm_S\rangle$	$\phi_{Sm_S}^B$	Hadron	$ Sm_S\rangle$	$\phi_{Sm_S}^B$
$\Lambda_c/\Xi_c$	$ \frac{1}{2}\frac{1}{2}\rangle$	$\frac{1}{\sqrt{2}}(\uparrow\downarrow - \downarrow\uparrow)\uparrow$	$ \frac{3}{2}\frac{3}{2}\rangle$	$\uparrow\uparrow\uparrow$	
	$ \frac{1}{2}-\frac{1}{2}\rangle$	$\frac{1}{\sqrt{2}}(\uparrow\downarrow - \downarrow\uparrow)\downarrow$			
$\Sigma_c/\Xi'_c$	$ \frac{1}{2}\frac{1}{2}\rangle$	$-\frac{1}{\sqrt{6}}(\uparrow\downarrow + \downarrow\uparrow)\uparrow + \sqrt{\frac{2}{3}}\uparrow\uparrow\downarrow$	$\Sigma_c^*/\Xi_c^*$	$ \frac{3}{2}\frac{1}{2}\rangle$	$\sqrt{\frac{1}{3}}(\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow)$
	$ \frac{1}{2}-\frac{1}{2}\rangle$	$\frac{1}{\sqrt{6}}(\uparrow\downarrow + \downarrow\uparrow)\downarrow - \sqrt{\frac{2}{3}}\downarrow\uparrow\uparrow$	$/\Xi_{cc}^*/\Omega_{cc}^*$	$ \frac{3}{2}-\frac{1}{2}\rangle$	$\sqrt{\frac{1}{3}}(\uparrow\downarrow\downarrow + \downarrow\uparrow\downarrow + \downarrow\downarrow\uparrow)$
$\Xi_{cc}/\Omega_{cc}$	$ \frac{1}{2}\frac{1}{2}\rangle$	$-\frac{1}{\sqrt{6}}\uparrow(\uparrow\downarrow + \downarrow\uparrow) + \sqrt{\frac{2}{3}}\downarrow\uparrow\uparrow$		$ \frac{3}{2}-\frac{3}{2}\rangle$	$\downarrow\downarrow\downarrow$
	$ \frac{1}{2}-\frac{1}{2}\rangle$	$\frac{1}{\sqrt{6}}\downarrow(\uparrow\downarrow + \downarrow\uparrow) - \sqrt{\frac{2}{3}}\uparrow\downarrow\downarrow$			

**Total wave function:**  $|[H_1 H_2]_J^I\rangle = \sum_{m_{I_1} m_{I_2}} C_{I_1, m_{I_1}; I_2, m_{I_2}}^{I, I_z} \phi_{I_1, m_{I_1}}^{H_1} \phi_{I_2, m_{I_2}}^{H_2}$

$$\otimes \sum_{m_{S_1}, m_{S_2}} C_{S_1, m_{S_1}, S_2, m_{S_2}}^{J, J_z} \phi_{S_1, m_{S_1}}^{H_1} \phi_{S_2, m_{S_2}}^{H_2}$$

# Framework

Hadronic Molecule



Boson exchange potential: S-wave interaction

Scalar mesons

Axial-vector mesons

$$\mathcal{V} = \tilde{g}_s \boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2 + \tilde{g}_a \boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2 \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2$$

$$\frac{g^2}{m_{\text{ex}}^2 + q^2} \approx \frac{g^2}{m_{\text{ex}}^2} \equiv \tilde{g}_s \text{ or } \tilde{g}_a$$

$$\text{Effective potential: } V_{[H_1 H_2]_J^I} = \left\langle [H_1 H_2]_J^I | V | [H_1 H_2]_J^I \right\rangle$$

Single and coupled-channel Lippmann-Schwinger equation (LSE)

SU(3) breaking effect

$$\boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2 = \sum_{i=1}^8 \lambda_1^i \lambda_2^i$$

$$\boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2 (\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2) = \sum_{i=1}^8 \lambda_1^i \lambda_2^i (\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2)$$

$$\begin{aligned} \tilde{g}_s &\rightarrow \tilde{g}_s g_x \\ \tilde{g}_a &\rightarrow \tilde{g}_a g_x \end{aligned} \quad g_x \in [0,1]$$

for  $i = 4, 5, 6, 7$

Suppression factor  $g_x$  for the exchange of **strange** light meson

# Parameters

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$$\mathcal{V} = \tilde{g}_s \boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2 + \tilde{g}_a \boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2 \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2$$

Scenario 1 :  $P_\psi^N(4440)|\Sigma_c \bar{D}^*; \frac{1}{2}^-\rangle, P_\psi^N(4457)|\Sigma_c \bar{D}^*; \frac{3}{2}^-\rangle$

Scenario 2 :  $P_\psi^N(4457)|\Sigma_c \bar{D}^*; \frac{1}{2}^-\rangle, P_\psi^N(4440)|\Sigma_c \bar{D}^*; \frac{3}{2}^-\rangle$

$$\text{Re} \left| \left| \mathbb{I} - \mathbb{V}_{1/2}^{P_\psi^N} \mathbb{G}_{1/2}^{P_\psi^N} \right| \right| = 0$$

$$\text{Im} \left| \left| \mathbb{I} - \mathbb{V}_{1/2}^{P_\psi^N} \mathbb{G}_{1/2}^{P_\psi^N} \right| \right| = 0$$

$$\text{Re} \left| \left| \mathbb{I} - \mathbb{V}_{3/2}^{P_\psi^N} \mathbb{G}_{3/2}^{P_\psi^N} \right| \right| = 0$$

$$\text{Im} \left| \left| \mathbb{I} - \mathbb{V}_{3/2}^{P_\psi^N} \mathbb{G}_{3/2}^{P_\psi^N} \right| \right| = 0$$

Scenario 1 :  $\tilde{g}_s = 8.28 \text{ GeV}^{-2}, \tilde{g}_a = -1.46 \text{ GeV}^{-2},$   
Scenario 2 :  $\tilde{g}_s = 9.12 \text{ GeV}^{-2}, \tilde{g}_a = 1.25 \text{ GeV}^{-2}.$

# Single-channel case

$$\mathcal{O}^f = \langle \boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2 \rangle$$

$$\mathcal{O}^{fs} = \langle (\boldsymbol{\lambda}_1 \cdot \boldsymbol{\lambda}_2)(\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2) \rangle$$

System	$\mathcal{O}^f$	$\mathcal{O}^{fs}$	System	$\mathcal{O}^f$	$\mathcal{O}^{fs}$
$[\Lambda_c \bar{D}]_{\frac{1}{2}}$	$\frac{2}{3}$	0	$[\Lambda_c \Xi_{cc}]_{0,1}$	$\frac{2}{3}, \frac{2}{3}$	0,0
$[\Lambda_c \bar{D}^*]_{\frac{1}{2}, \frac{3}{2}}$	$\frac{2}{3}, \frac{2}{3}$	0,0	$[\Lambda_c \Xi_{cc}^*]_{1,2}$	$\frac{2}{3}, \frac{2}{3}$	0,0
$[\Sigma_c \bar{D}]_{\frac{1}{2}^A}$	$-\frac{10}{3}$	0	$[\Sigma_c \Xi_{cc}]_{0^B,1}$	$-\frac{10}{3}, -\frac{10}{3}$	$-\frac{20}{9}, \frac{20}{27}$
$[\Sigma_c^* \bar{D}]_{\frac{3}{2}^A}$	$-\frac{10}{3}$	0	$[\Sigma_c^* \Xi_{cc}]_{1,2^C}$	$-\frac{10}{3}, -\frac{10}{3}$	$-\frac{50}{27}, \frac{10}{9}$
$[\Sigma_c \bar{D}^*]_{\frac{1}{2}, \frac{3}{2}^B}$	$-\frac{10}{3}, -\frac{10}{3}$	$\frac{40}{9}, -\frac{20}{9}$	$[\Sigma_c \Xi_{cc}^*]_{1,2^B}$	$-\frac{10}{3}, -\frac{10}{3}$	$\frac{100}{27}, -\frac{20}{9}$
$[\Sigma_c^* \bar{D}^*]_{\frac{1}{2}^D, \frac{3}{2}^E, \frac{5}{2}^E}$	$-\frac{10}{3}, -\frac{10}{3}, -\frac{10}{3}$	$\frac{50}{9}, \frac{20}{9}, -\frac{10}{3}$	$[\Sigma_c^* \Xi_{cc}^*]_{0^D,1,2^C,3^E}$	$-\frac{10}{3}, -\frac{10}{3}, -\frac{10}{3}$	$\frac{50}{9}, \frac{110}{27}, \frac{10}{9}, -\frac{10}{3}$

System	$\mathcal{O}^f$	$\mathcal{O}^{fs}$	System	$\mathcal{O}^f$	$\mathcal{O}^{fs}$
$[\Lambda_c \bar{D}_s]_{\frac{1}{2}^F}$	$-\frac{4}{3}$	0	$[\Lambda_c \Omega_{cc}]_{0^F,1^F}$	$-\frac{4}{3}, -\frac{4}{3}$	0,0
$[\Lambda_c \bar{D}_s^*]_{\frac{1}{2}^F, \frac{3}{2}^F}$	$-\frac{4}{3}, -\frac{4}{3}$	0,0	$[\Lambda_c \Omega_{cc}^*]_{1^F,2^F}$	$-\frac{4}{3}, -\frac{4}{3}$	0,0
$[\Xi_c \bar{D}]_{\frac{1}{2}^A}$	$-\frac{10}{3}$	0	$[\Xi_c \Xi_{cc}]_{0^A,1^A}$	$-\frac{10}{3}, -\frac{10}{3}$	0,0
$[\Xi_c \bar{D}^*]_{\frac{1}{2}^A, \frac{3}{2}^A}$	$-\frac{10}{3}, -\frac{10}{3}$	0,0	$[\Xi_c \Xi_{cc}^*]_{1^A,2^A}$	$-\frac{10}{3}, -\frac{10}{3}$	0,0
$[\Xi'_c \bar{D}]_{\frac{1}{2}^A}$	$-\frac{10}{3}$	0	$[\Xi'_c \Xi_{cc}]_{0^B,1}$	$-\frac{10}{3}, -\frac{10}{3}$	$-\frac{20}{9}, \frac{20}{27}$
$[\Xi_c^* \bar{D}]_{\frac{3}{2}^A}$	$-\frac{10}{3}$	0	$[\Xi_c^* \Xi_{cc}]_{1,2^C}$	$-\frac{10}{3}, -\frac{10}{3}$	$-\frac{50}{27}, \frac{10}{9}$
$[\Xi'_c \bar{D}^*]_{\frac{1}{2}^B, \frac{3}{2}^B}$	$-\frac{10}{3}, -\frac{10}{3}$	$\frac{40}{9}, -\frac{20}{9}$	$[\Xi'_c \Xi_{cc}^*]_{1,2^B}$	$-\frac{10}{3}, -\frac{10}{3}$	$\frac{100}{27}, -\frac{20}{9}$
$[\Xi_c^* \bar{D}^*]_{\frac{1}{2}^D, \frac{3}{2}^E, \frac{5}{2}^E}$	$-\frac{10}{3}, -\frac{10}{3}, -\frac{10}{3}$	$\frac{50}{9}, \frac{20}{9}, -\frac{10}{3}$	$[\Xi_c^* \Xi_{cc}^*]_{0^D,1,2^C,3^E}$	$-\frac{10}{3}, -\frac{10}{3}, -\frac{10}{3}, -\frac{10}{3}$	$\frac{50}{9}, \frac{110}{27}, \frac{10}{9}, -\frac{10}{3}$

Flavor dominant/Isospin dominant

6 groups: A,B,C,D,E,F

# Single-channel case

	Scenario 1			Scenario 2	
System	Mass (MeV)	BE (MeV)	System	Mass (MeV)	BE (MeV)
$[\Sigma_c \bar{D}]_{\frac{1}{2}^A}$	4312.6	<u>-8.1</u>	$[\Sigma_c \bar{D}]_{\frac{1}{2}^A}$	4307.6	<u>-13.1</u>
$[\Sigma_c^* \bar{D}]_{\frac{3}{2}^A}$	4376.9	<u>-8.5</u>	$[\Sigma_c^* \bar{D}]_{\frac{3}{2}^A}$	4371.7	<u>-13.6</u>
$[\Sigma_c \bar{D}^*]_{\frac{1}{2}, \frac{3}{2}^B}$	4438.8, 4457.5	-23.2, -4.6	$[\Sigma_c \bar{D}^*]_{\frac{1}{2}, \frac{3}{2}^B}$	4456.8, 4440.9	-5.3, -21.1
$[\Sigma_c^* \bar{D}^*]_{\frac{1}{2}^D, \frac{3}{2}, \frac{5}{2}^E}$	4498.8, 4510.3, 4523.8	-27.9, -16.4, -2.9	$[\Sigma_c^* \bar{D}^*]_{\frac{1}{2}^D, \frac{3}{2}, \frac{5}{2}^E}$	4522.9, 4516.6, 4501.6	-3.8, -10.1, -25.1
$[\Xi_c \bar{D}]_{\frac{1}{2}^A}$	4328.1	<u>-8.2</u>	$[\Xi_c \bar{D}]_{\frac{1}{2}^A}$	4323.1	<u>-13.3</u>
$[\Xi_c \bar{D}^*]_{\frac{1}{2}^A, \frac{3}{2}^A}$	4468.0, 4468.0	<u>-9.7, -9.7</u>	$[\Xi_c \bar{D}^*]_{\frac{1}{2}^A, \frac{3}{2}^A}$	4462.5, 4462.5	<u>-15.1, -15.1</u>
$[\Xi'_c \bar{D}]_{\frac{1}{2}^A}$	4436.8	<u>-8.9</u>	$[\Xi'_c \bar{D}]_{\frac{1}{2}^A}$	4431.6	<u>-14.1</u>
$[\Xi_c^* \bar{D}]_{\frac{3}{2}^A}$	4503.9	<u>-9.3</u>	$[\Xi_c^* \bar{D}]_{\frac{3}{2}^A}$	4498.6	<u>-14.6</u>
$[\Xi'_c \bar{D}^*]_{\frac{1}{2}, \frac{3}{2}^B}$	4562.5, 4581.8	-24.5, -5.2	$[\Xi'_c \bar{D}^*]_{\frac{1}{2}, \frac{3}{2}^B}$	4581.1, 4564.7	-5.9, -22.3
$[\Xi_c^* \bar{D}^*]_{\frac{1}{2}^D, \frac{3}{2}, \frac{5}{2}^E}$	4625.3, 4637.0, 4651.2	-29.2, -17.5, -3.4	$[\Xi_c^* \bar{D}^*]_{\frac{1}{2}^D, \frac{3}{2}, \frac{5}{2}^E}$	4650.2, 4643.6, 4628.2	-4.3, -11.0, -26.3

Good flavor-spin symmetry

# Single-channel case

	Scenario 1			Scenario 2	
System	Mass (MeV)	BE (MeV)	System	Mass (MeV)	BE (MeV)
$[\Sigma_c \Xi_{cc}]_{0^B,1}$	6060.8,6050.3	-14.0,-24.6	$[\Sigma_c \Xi_{cc}]_{0^B,1}$	6037.5,6048.1	-37.3,-26.8
$[\Sigma_c^* \Xi_{cc}]_{1,2^C}$	6123.7,6112.7	-15.9,-26.8	$[\Sigma_c^* \Xi_{cc}]_{1,2^C}$	6102.7,6113.2	-36.9,-26.3
$[\Sigma_c \Xi_{cc}^*]_{1,2^B}$	6143.0,6166.0	-37.5,-14.5	$[\Sigma_c \Xi_{cc}^*]_{1,2^B}$	6162.6,6142.4	-17.8,-38.0
$[\Sigma_c^* \Xi_{cc}^*]_{0^D,1}$	6198.3,6205.1	-46.8,-40.1	$[\Sigma_c^* \Xi_{cc}^*]_{0^D,1}$	6232.0,6227.7	-13.2,-17.4
$[\Sigma_c^* \Xi_{cc}^*]_{2^C,3^E}$	6217.7,6233.6	-27.4,-11.6	$[\Sigma_c^* \Xi_{cc}^*]_{2^C,3^E}$	6218.2,6201.9	-26.9,-43.2
$[\Xi_c \Xi_{cc}]_{0^A,1^A}$	6068.5,6068.5	<u>-22.0</u> , <u>-22.0</u>	$[\Xi_c \Xi_{cc}]_{0^A,1^A}$	6061.0,6061.0	<u>-29.5</u> , <u>-29.5</u>
$[\Xi_c \Xi_{cc}^*]_{1^A,2^A}$	6173.6,6173.6	<u>-22.5</u> , <u>-22.5</u>	$[\Xi_c \Xi_{cc}^*]_{1^A,2^A}$	6165.9,6165.9	<u>-30.2</u> , <u>-30.2</u>
$[\Xi'_c \Xi_{cc}]_{0^B,1}$	6184.7,6173.8	-15.2,-26.1	$[\Xi'_c \Xi_{cc}]_{0^B,1}$	6160.8,6171.6	-39.1,-28.3
$[\Xi_c^* \Xi_{cc}]_{1,2^C}$	6250.3,6239.1	-17.1,-28.3	$[\Xi_c^* \Xi_{cc}]_{1,2^C}$	6228.8,6239.6	-38.6,-27.8
$[\Xi'_c \Xi_{cc}^*]_{1,2^B}$	6266.2,6289.8	-39.2,-15.7	$[\Xi'_c \Xi_{cc}^*]_{1,2^B}$	6286.3,6265.7	-19.1,-39.8
$[\Xi_c^* \Xi_{cc}^*]_{0^D,1}$	6324.3,6331.2	-48.7,-41.8	$[\Xi_c^* \Xi_{cc}^*]_{0^D,1}$	6358.7,6354.3	-14.3,-18.6
$[\Xi_c^* \Xi_{cc}^*]_{2^C,3^E}$	6344.0,6360.4	-29.0,-12.6	$[\Xi_c^* \Xi_{cc}^*]_{2^C,3^E}$	6344.6,6327.9	-28.4,-45.1

Good flavor-spin symmetry

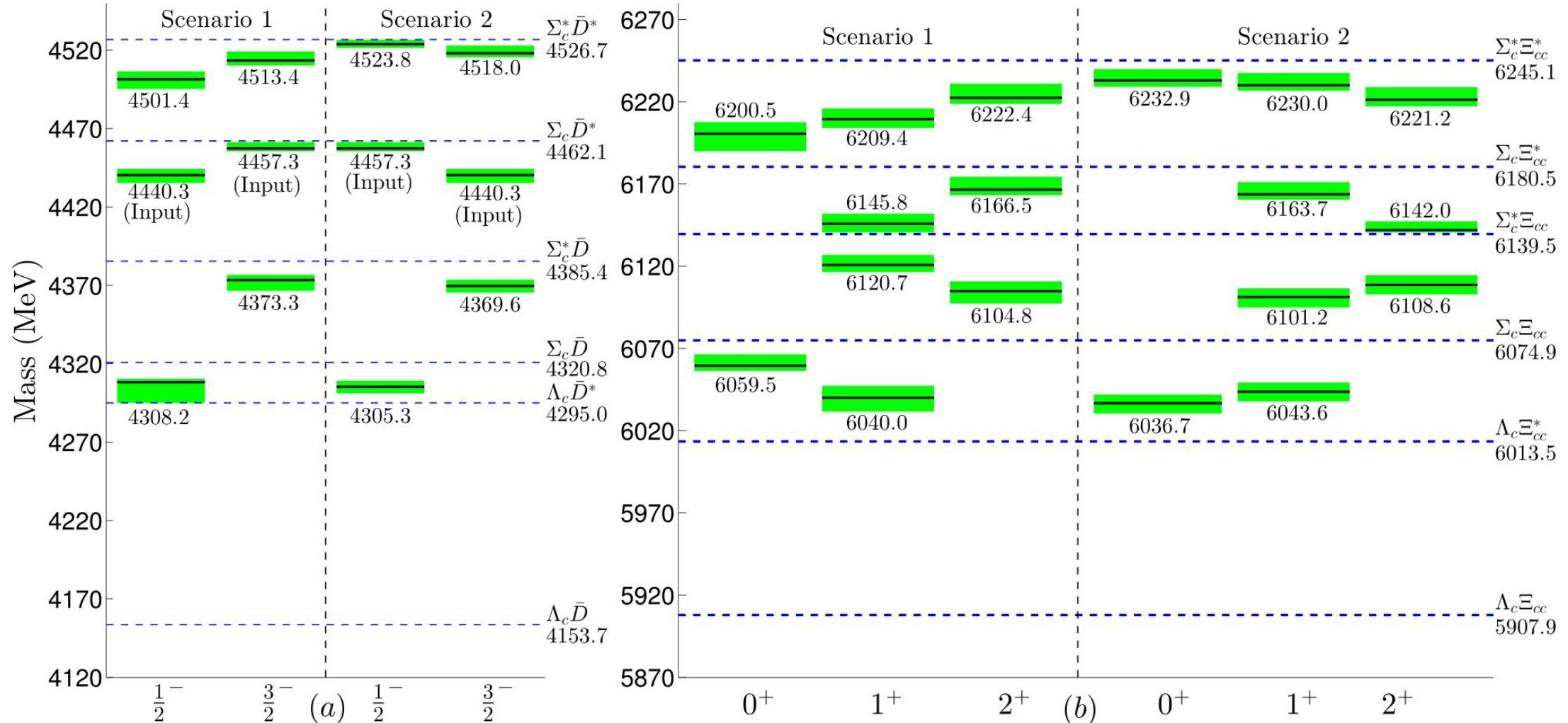
Coupled-channel effect?  
SU(3) breaking effect?

# Single vs multi-channel: finger prints of the flavor-spin symmetry

## System-dependent

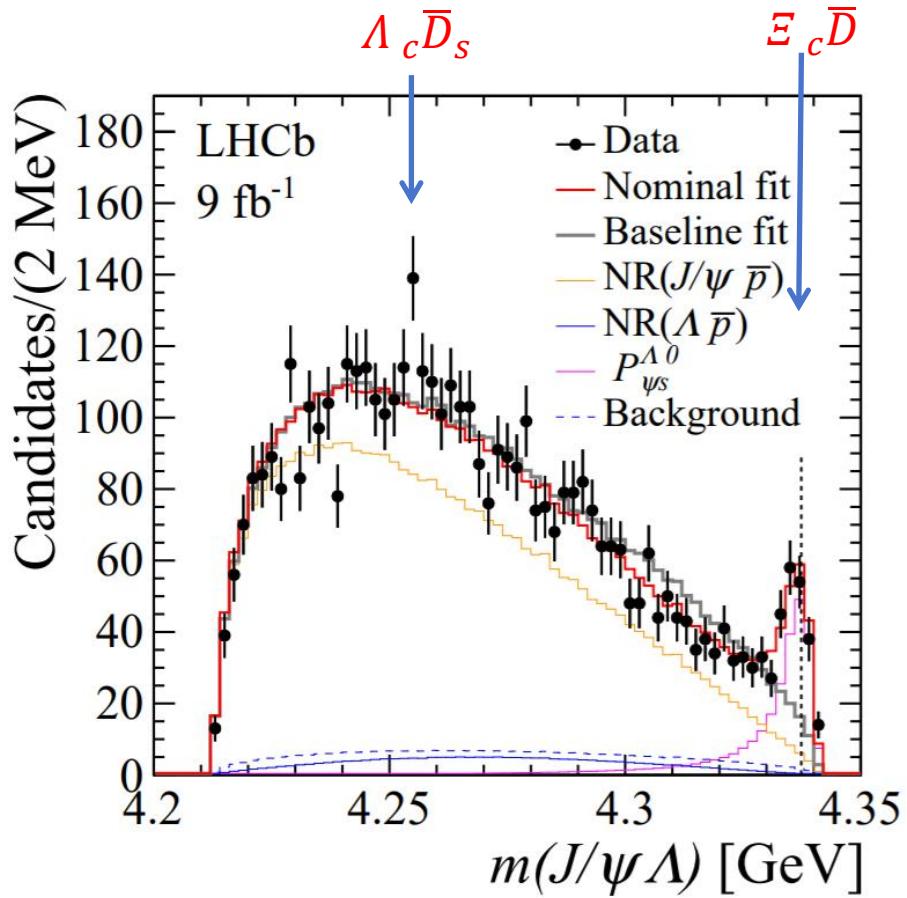
System	Scenario 1		Scenario 2		System	Scenario 1		Scenario 2			
	BE (SC)	BE (MC)	BE (SC)	BE (MC)		BE (SC)	BE (MC)	BE (SC)	BE (MC)		
$[\Sigma_c \bar{D}]_{\frac{1}{2}^A}^\dagger$	-8.1	<u>-12.6</u>	-13.1	<u>-15.5</u>	$[\Sigma_c^* \bar{D}]_{\frac{3}{2}^A}^\dagger$	-8.5	<u>-12.6</u>	-13.6	<u>-15.8</u>		
$[\Sigma_c \bar{D}^*]_{\frac{3}{2}^B}^\dagger$	-4.6	<u>-4.8</u>	-21.1	-21.8	$[\Xi'_c \bar{D}^*]_{\frac{3}{2}^B}^\dagger$	-5.2	<u>-5.2</u>	-22.3	-22.9		
$[\Sigma_c \Xi_{cc}]_{0^B}^\dagger$	-14.0	<u>-15.3</u>	-37.3	-38.2	$[\Sigma_c \Xi_{cc}^*]_{2^B}^\dagger$	-14.5	<u>-14.0</u>	-38.0	-38.5		
$[\Xi'_c \Xi_{cc}]_{0^B}^\dagger$	-15.2	<u>-16.4</u>	-39.1	-39.9	$[\Xi'_c \Xi_{cc}^*]_{2^B}^\dagger$	-15.7	<u>-15.0</u>	-39.8	-39.6		
$[\Sigma_c^* \Xi_{cc}]_{2^C}^\dagger$	<u>-26.8</u>	-34.8	<del>x</del>	-26.3	-30.9	$[\Sigma_c^* \Xi_{cc}^*]_{2^C}^\dagger$	<u>-27.4</u>	-22.7	<del>x</del>	-26.9	-24.0
$[\Xi_c^* \Xi_{cc}]_{2^C}^\dagger$	<u>-28.3</u>	-31.8	<del>x</del>	-27.8	-31.7	$[\Xi_c^* \Xi_{cc}^*]_{2^C}^\dagger$	<u>-29.0</u>	-23.8	<del>x</del>	-28.4	-24.4
$[\Sigma_c^* \bar{D}^*]_{\frac{1}{2}^D}^\dagger$	-27.9	<u>-25.3</u>	-3.8	-2.8	$[\Xi_c^* \bar{D}^*]_{\frac{1}{2}^D}^\dagger$	-29.2	<u>-26.0</u>	-4.3	-3.2		
$[\Sigma_c^* \Xi_{cc}^*]_{0^D}^\dagger$	-46.8	<u>-44.7</u>	-13.2	-12.2	$[\Xi_c^* \Xi_{cc}^*]_{0^D}^\dagger$	-48.7	<u>-46.4</u>	-14.3	-13.2		
$[\Sigma_c^* \bar{D}^*]_{\frac{5}{2}^E}^\dagger$	-2.9	<u>-2.9</u>	-25.1	-25.1	$[\Xi_c^* \bar{D}^*]_{\frac{5}{2}^E}^\dagger$	-3.4	<u>-3.4</u>	26.3	-26.3		
$[\Sigma_c^* \Xi_{cc}^*]_{3^E}^\dagger$	-11.6	<u>-11.6</u>	-43.2	-43.2	$[\Xi_c^* \Xi_{cc}^*]_{3^E}^\dagger$	-12.6	<u>-12.6</u>	-45.1	-45.1		

# Multi-channel $P_\Psi^N/H_{\Omega_{ccc}}^N$ mass spectra



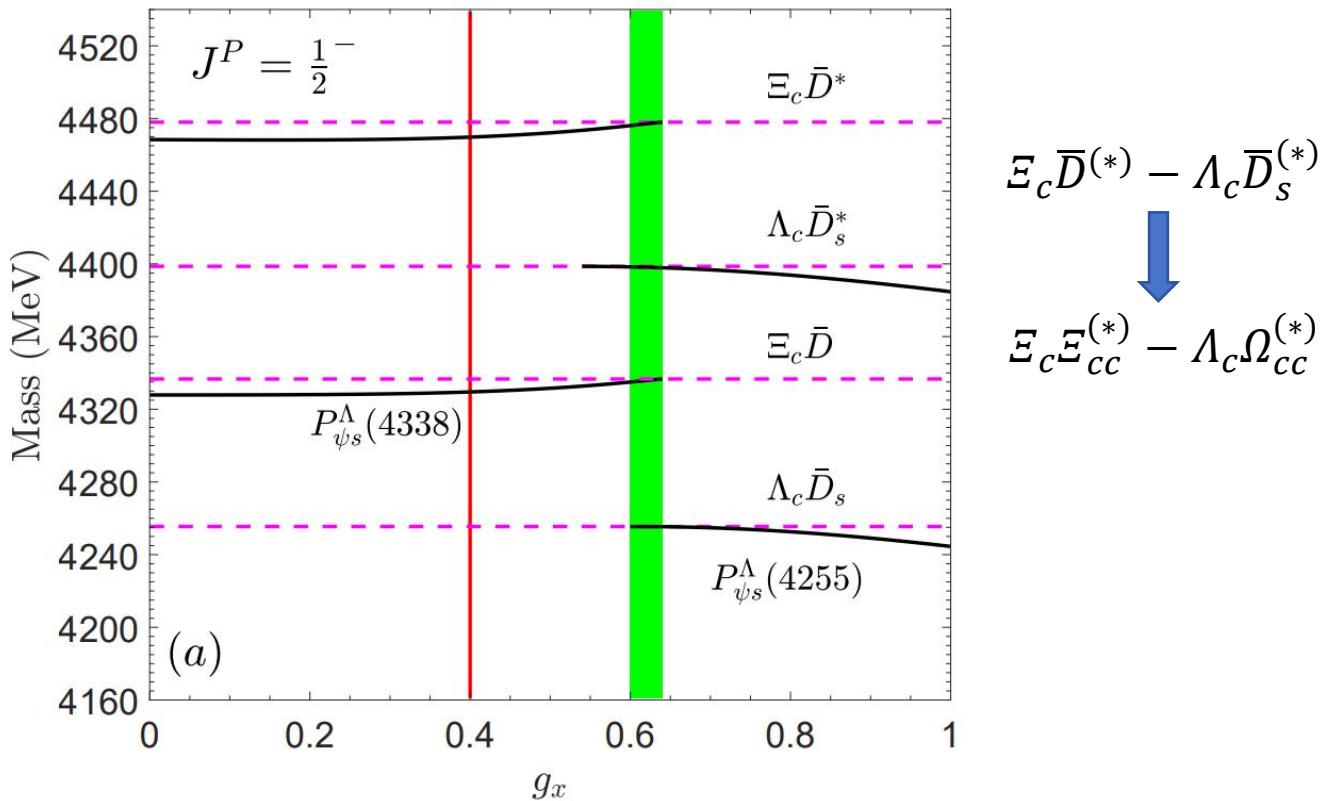
Consistent with: Y. W. Pan, M. Z. Liu, F. Z. Peng, M. Sánchez Sánchez, L. S. Geng and M. Pavon Valderrama, Phys. Rev. D 102, no.1, 011504 (2020).

# SU(3) breaking factor $g_x$



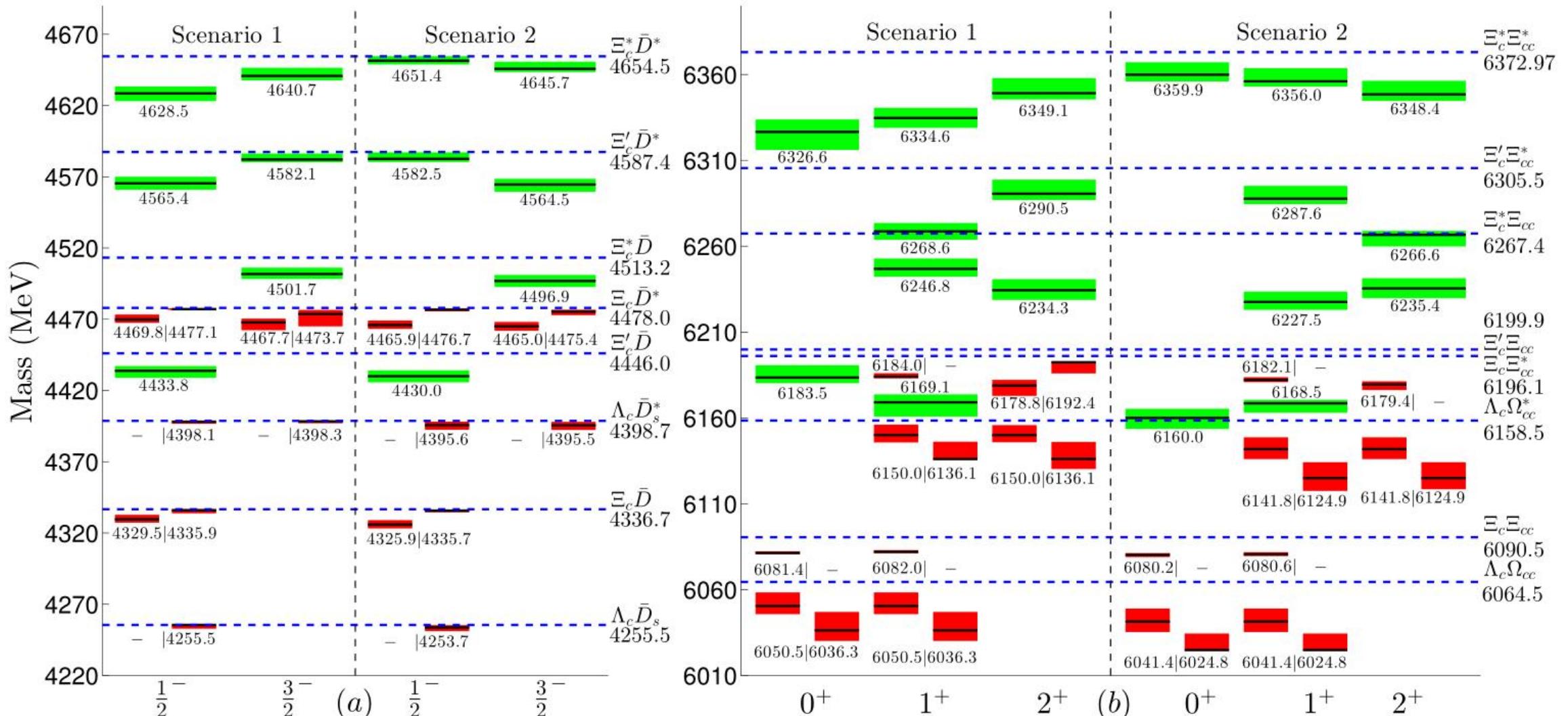
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$$\begin{aligned} & \Xi_c \bar{D}^{(*)} - \Lambda_c \bar{D}_s^{(*)} \\ \downarrow & \\ & \Xi_c \Xi_{cc}^{(*)} - \Lambda_c \Omega_{cc}^{(*)} \end{aligned}$$

# Multi-channel $P\psi_S/\Lambda_{ccc}^{\Lambda}$ mass spectra



# Summary

We suggest **two ways** to check the **existence** of the flavor-spin symmetry among the  $P_\Psi^N/H_{\Omega_{ccc}}^N$  and  $P_{\Psi_S}^\Lambda/H_{\Omega_{cccs}}^\Lambda$  molecular community, i.e.,

1. The **similar** binding energies of the heavy flavor meson-baryon (di-baryon) systems attributed to the same contact potentials.
2. The **mass arrangements** of the  $P_\Psi^N/H_{\Omega_{ccc}}^N/P_{\Psi_S}^\Lambda/H_{\Omega_{cccs}}^\Lambda$  mass spectra.

**Thanks for your attention!**