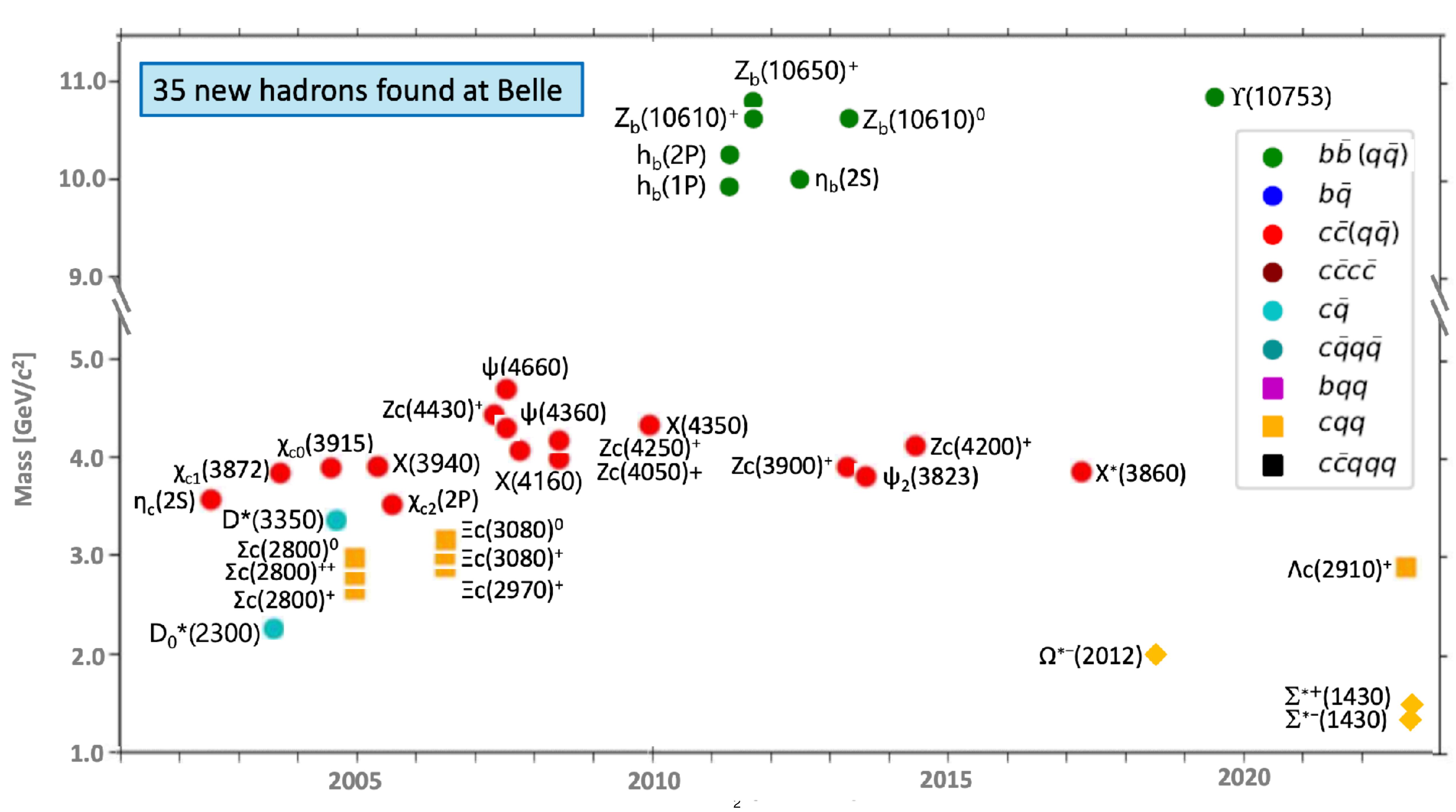


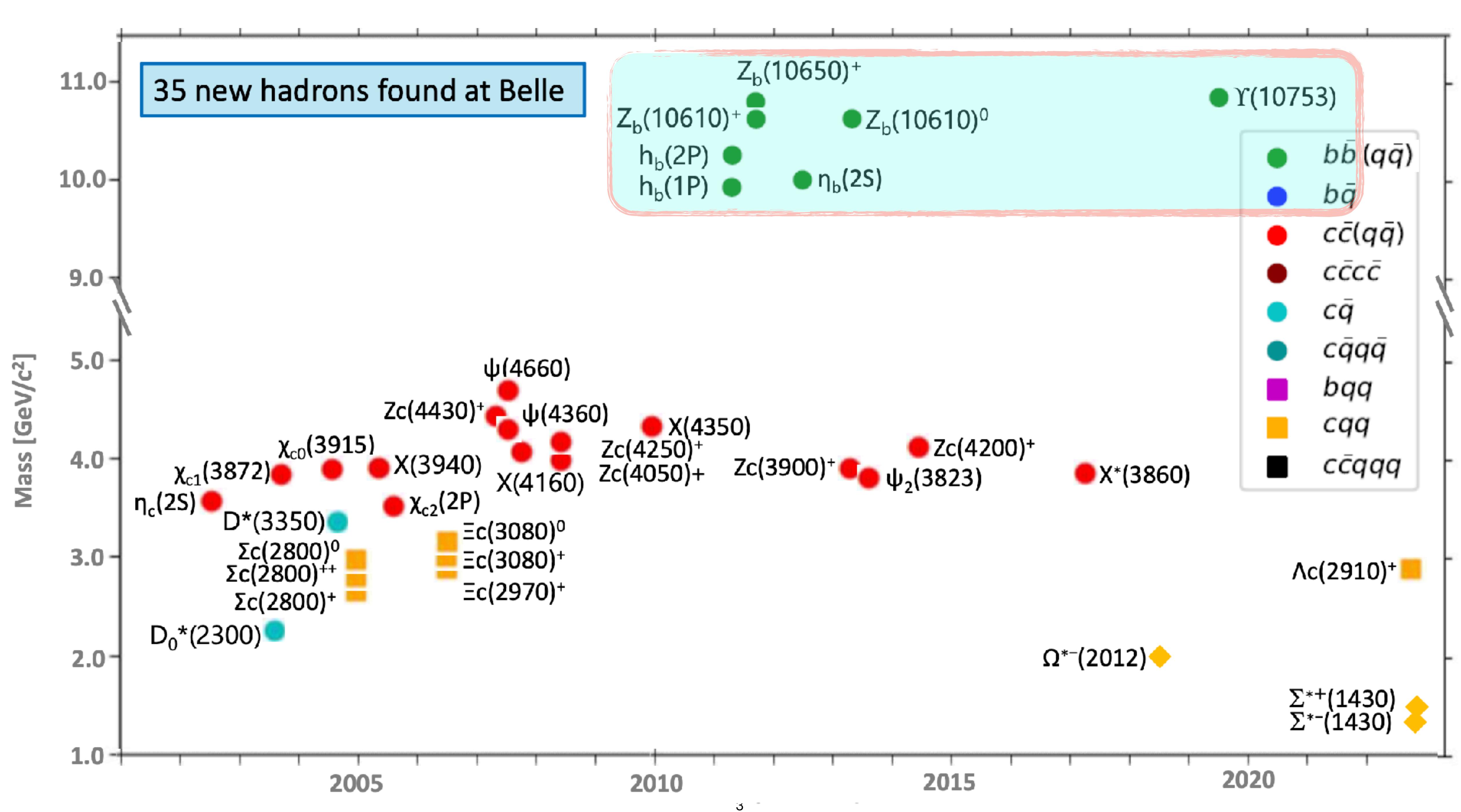


Study of properties of $\Upsilon(10753)$ on Belle II experiment

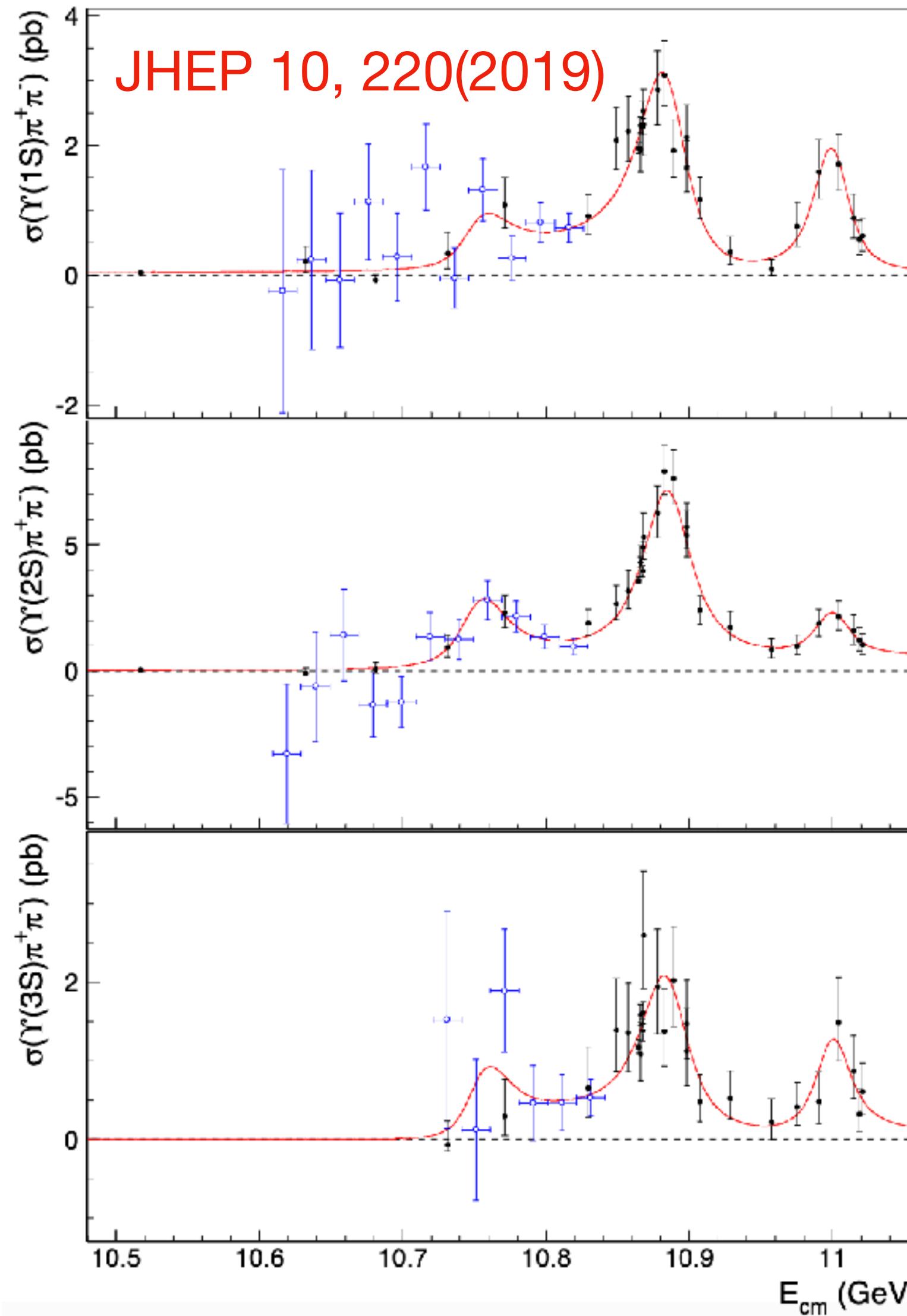
第七届强子谱与强子结构会议

殷俊昊
南开大学

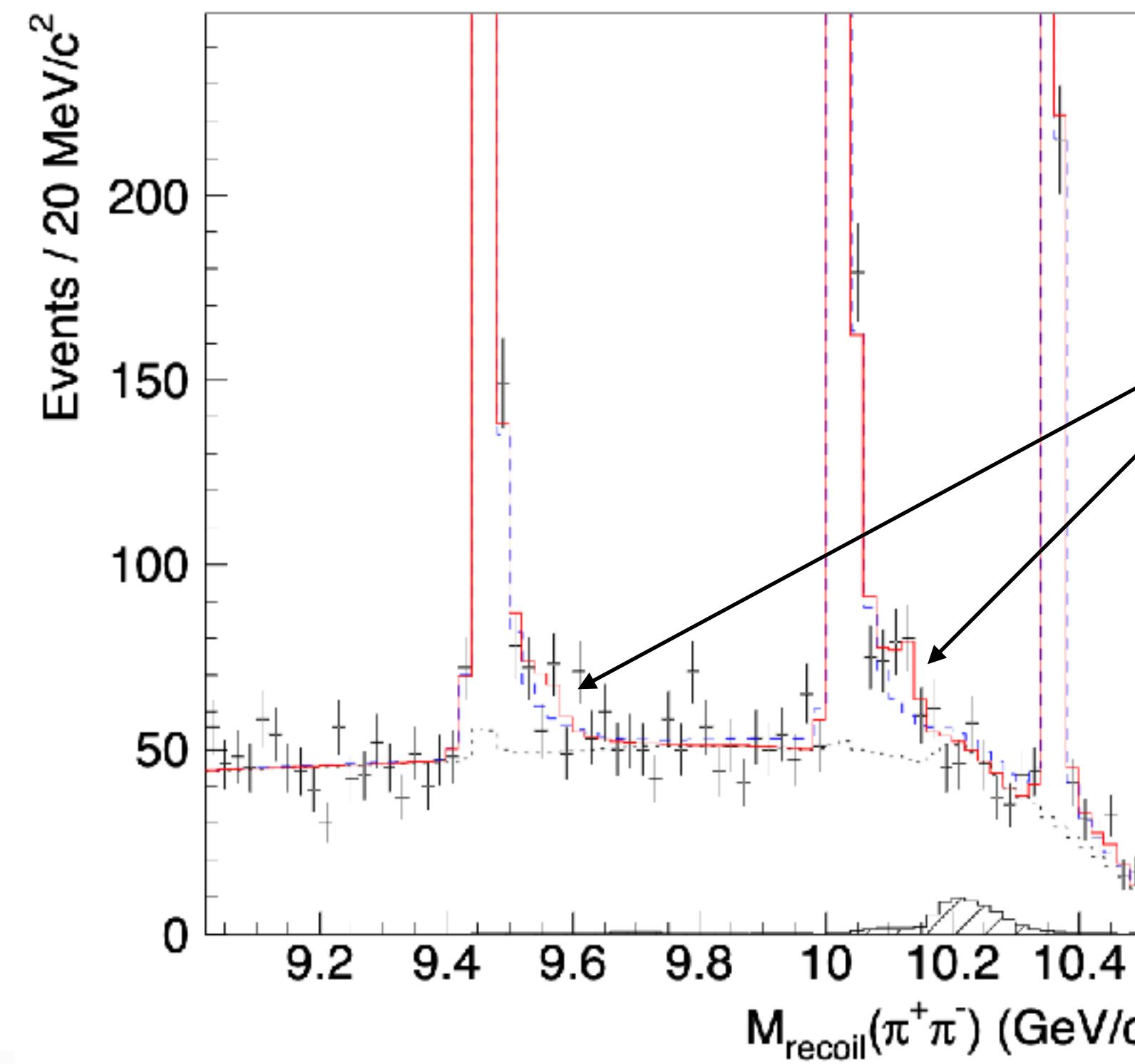




$\Upsilon(10753)$ – discovery and studies

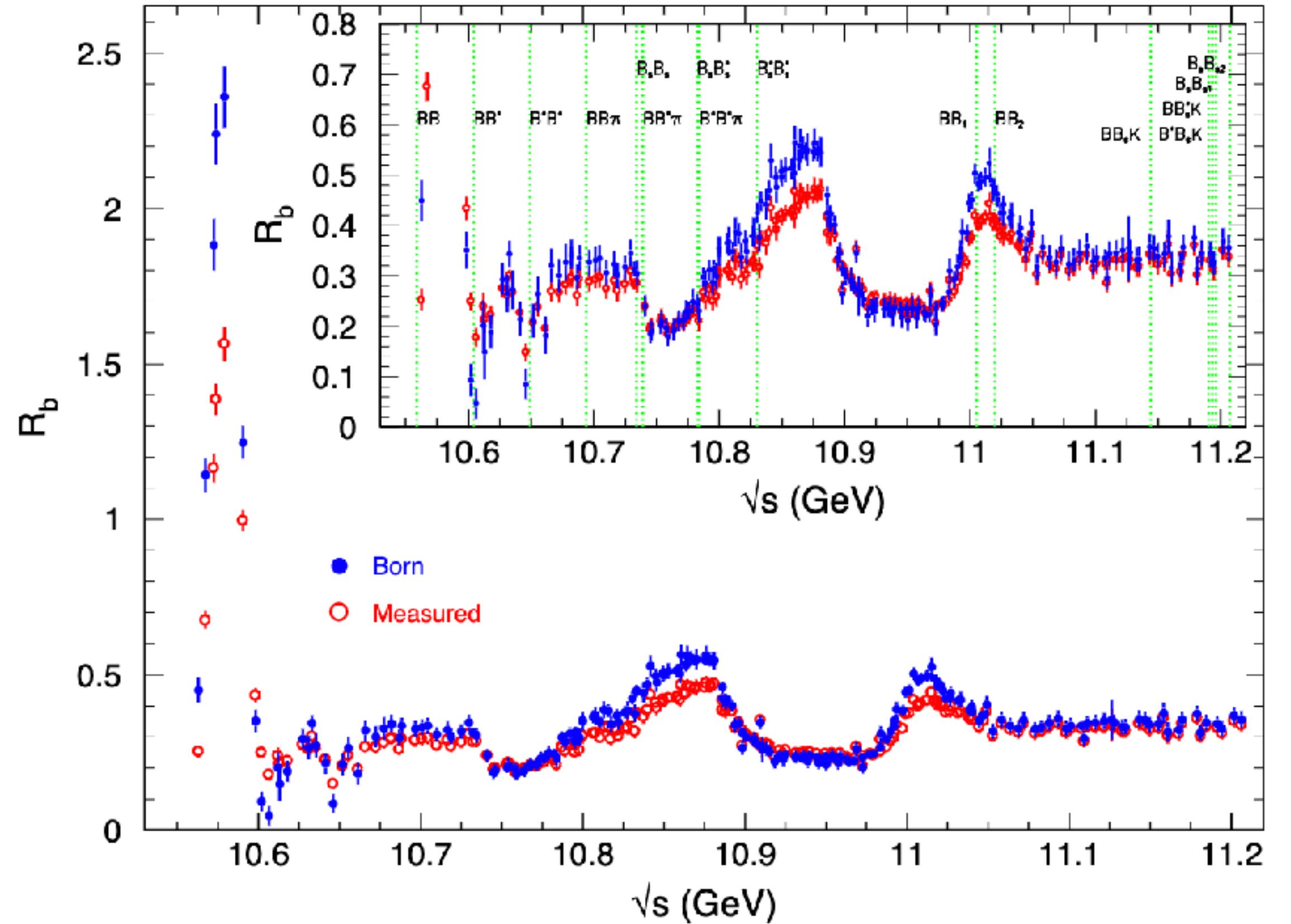


- The $\Upsilon(10753)$ was firstly observed in the process of $e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^- (n = 1,2,3)$ by Belle.
- Simultaneous fit to cross sections and $M_{\text{recoil}}(\pi\pi)$



$$M = (10752.7 \pm 5.9^{+0.7}_{-1.1}) \text{ MeV}/c^2$$

$$\Gamma = (35.5^{+17.6}_{-11.3} {}^{+3.9}_{-3.3}) \text{ MeV}$$



- A dip in the R_b distribution near 10.75 GeV
- Fit to dressed cross section of $b\bar{b}$ with three BWs.

"The results from these fits may change dramatically by including more information on each exclusive mode."

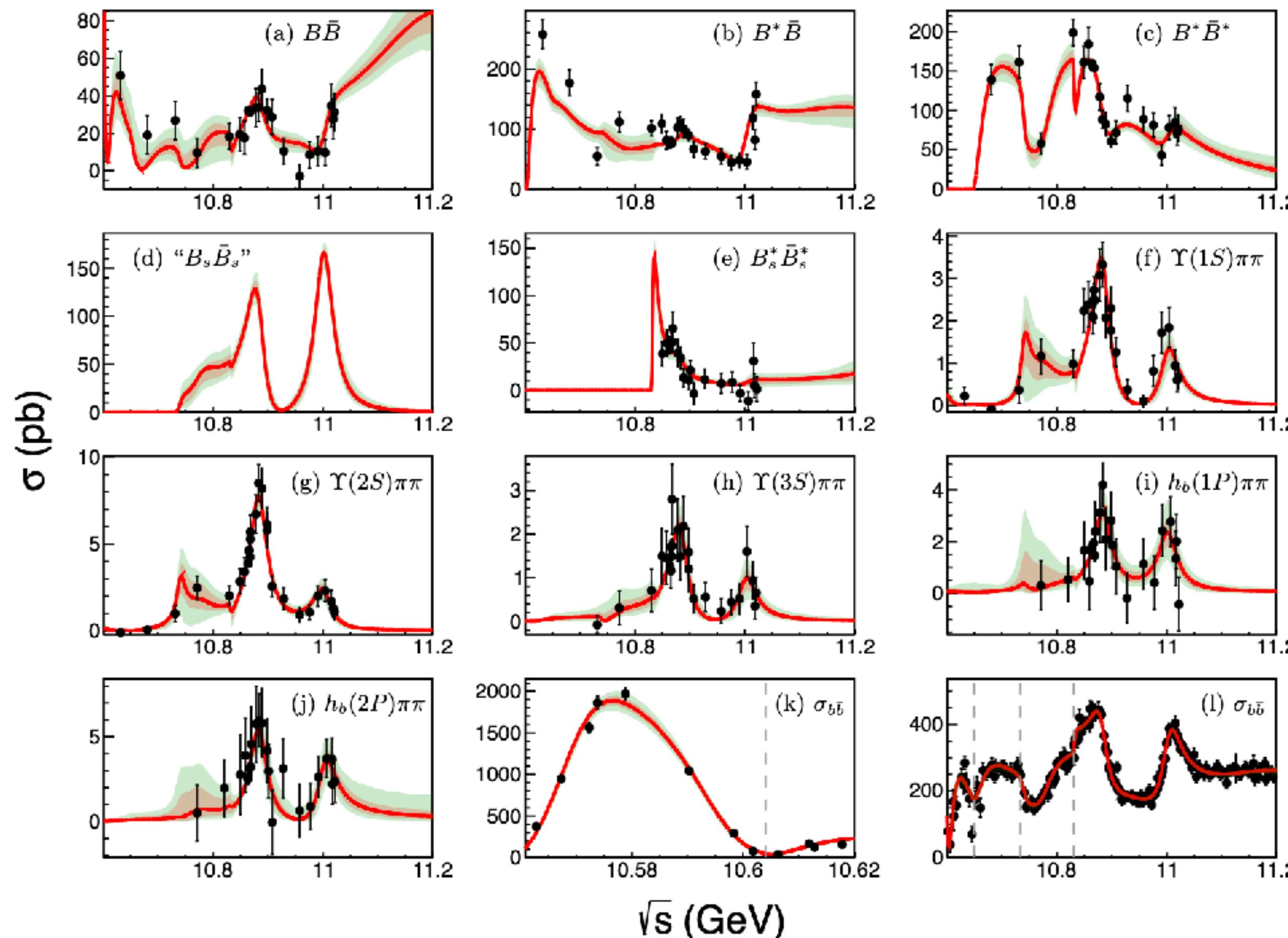
$$M = (10761 \pm 2) \text{ MeV}/c^2$$

$$\Gamma = (48.5 \pm 3.0) \text{ MeV}$$

K-matrix Analysis of e^+e^- Annihilation in the Bottomonium Region

N. Hüsken,^{1,2} R.E. Mitchell,¹ and E.S. Swanson³

Phys.Rev.D 106 (2022) 9, 094013



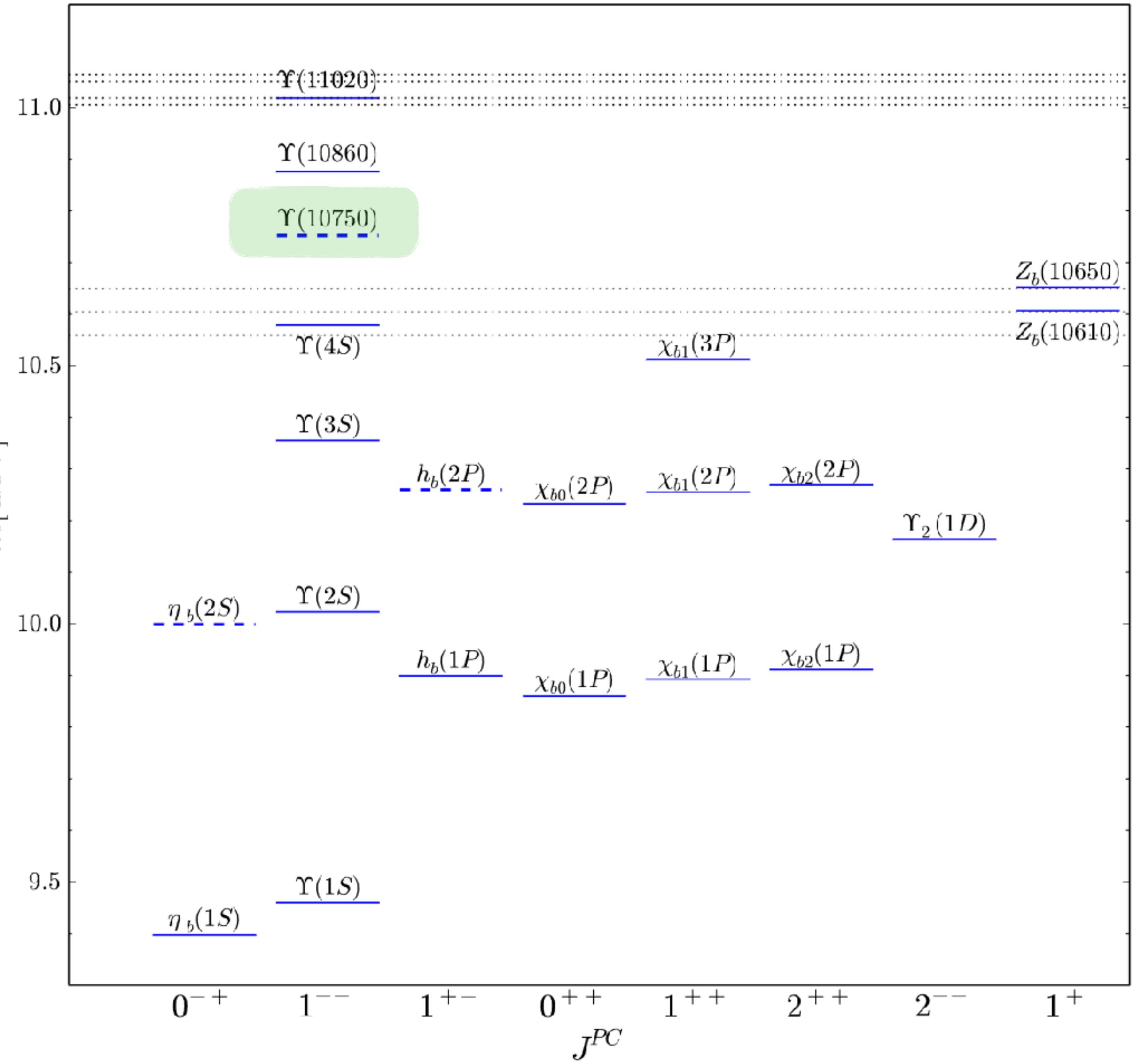
Coupled channel analysis of high energy scan data using the K-matrix formalism shows four poles: $\Upsilon(4S)$, $\Upsilon(10753)$, $\Upsilon(5S)$, $\Upsilon(6S)$.

Strong evidence for $\Upsilon(10753)$ with significance $>10\sigma$

Pole locations varies with models.

state	RPP	our estimate	GM	ARM	NR	bbg	SOEF	LGT
1^3S_1	9460		9465	9444	9454	9445	9502	9419.1(4)
2^3S_1	10023		10003	10029	10010	10002	10015	9981(4)
3^3S_1	10355		10354	10374	10344	10339	10349	10384(12)
4^3S_1	10579 (10590 - 10610)		10635	10641	10614	10610	10607	
5^3S_1	10885 (10878 - 10884)		10878	10865	10849	10848	10818	
6^3S_1	11000 (11000 - 11008)		11102	11065	11064	11064	10995	
1^3D_1			10138	10156	10146	10148	10117	10191(9)
2^3D_1			10441	10453	10432	10435	10414	10718(33)
3^3D_1			10698	10697	10679	10684	10653	
$\Upsilon(10750)$	10753 (10630 - 10780)							
hybrid							11093	10952(33)

TABLE IV. Experimental and Theoretical Vector Bottomonium Masses (MeV).



Bottomonium?

Phys. Rev. D 101, 014020 (2020)

Phys. Lett. B 803, 135340 (2020)

Eur. Phys. J. C 80, 59 (2020)

Phys. Rev. D 102, 014036 (2020)

Prog. Part. Nucl. Phys. 117, 103845 (2021)

Phys. Rev. D 104, 034036 (2021)

Phys. Rev. D 105, 074007 (2022)

etc...

Hybrid?

Phys. Rept. 873, 1 (2020)

Phys. Rev. D 104, 034019 (2021)

etc...

Tetraquark?

Phys. Lett. B 802, 135217 (2020)

Chin. Phys. C 43, 123102 (2019)

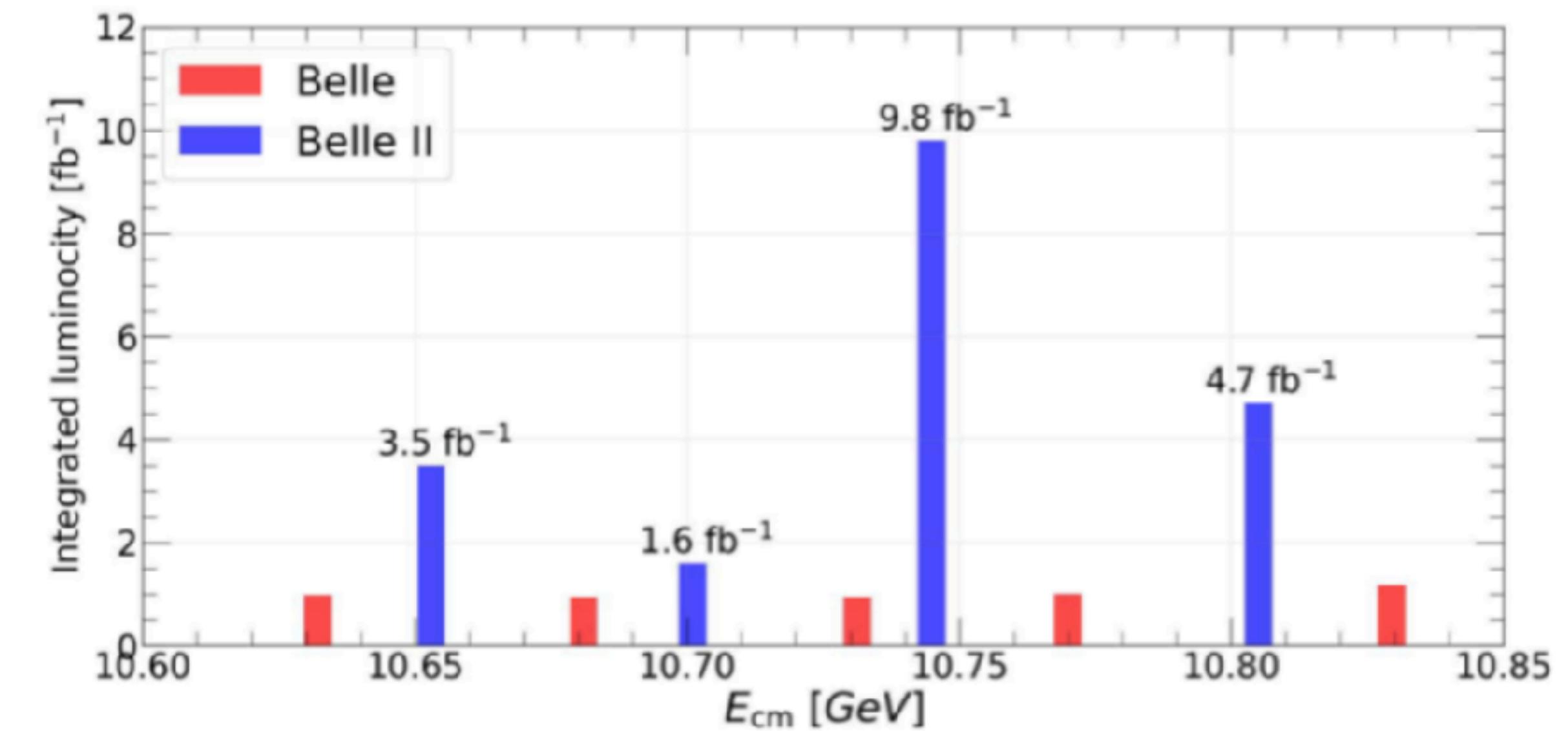
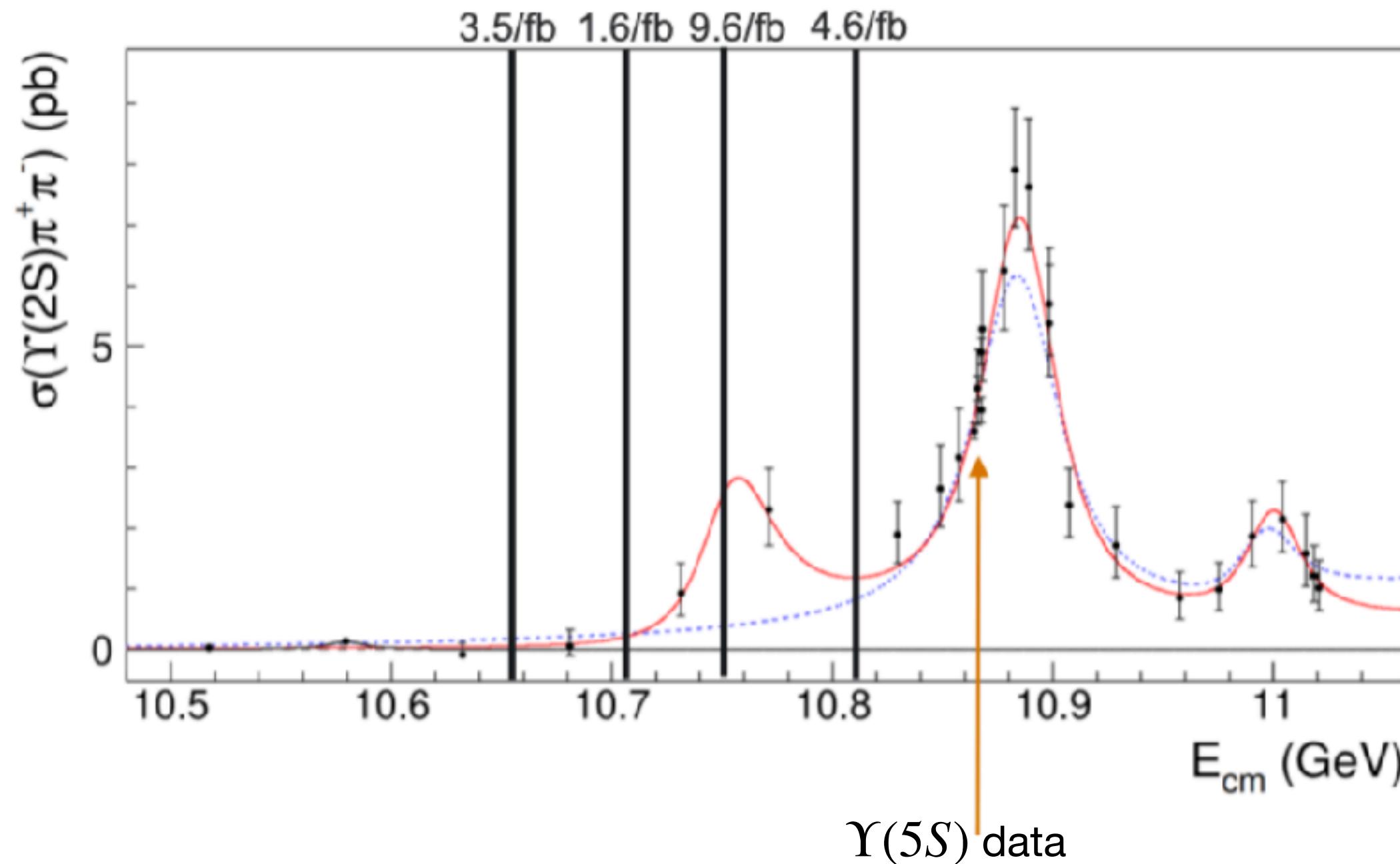
Phys. Rev. D 103, 074507 (2021)

Phys. Rev. D 107, 094515 (2023)

etc...

Unique data

- Largest bottomonium data sample
- In Nov. 2021, Belle II collected $\sim 20/\text{fb}$ of unique scan data at energies near 10.75 GeV
 - Fill the gaps in Belle Scan data
 - Physics goal is to understand the nature of $\Upsilon(10753)$

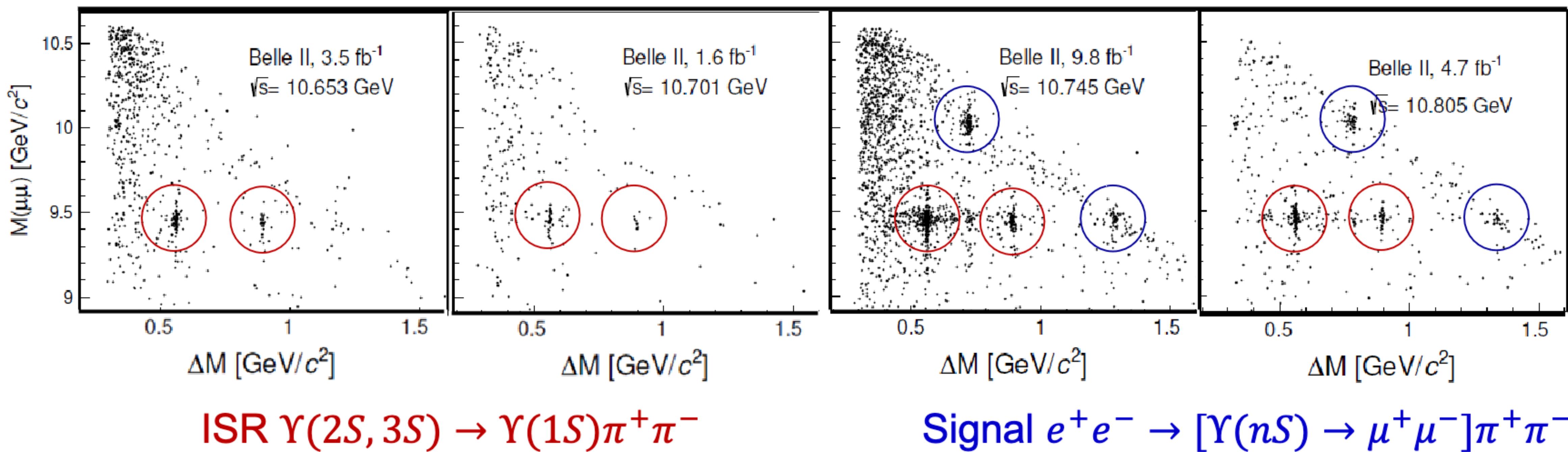


Confirmation of $\Upsilon(10753)$ on Belle II

- Full reconstruction of $\pi^+\pi^-\Upsilon(nS)$, $n = 1,2,3$, where $\Upsilon(nS) \rightarrow \mu^+\mu^-$.

$$\Delta M = M(\pi\pi\mu\mu) - M(\mu\mu)$$

Belle-II preliminary, arxiv:2401.12021



Fit with three coherent BW, convoluting a Gaussian modeling energy spread:

$$\sigma \propto \left| \sum_i^3 \frac{\sqrt{12\pi\Gamma_i \mathcal{B}_i}}{s - M_i + iM_i\Gamma_i} \cdot \sqrt{\frac{f(\sqrt{s})}{f(M_i)}} e^{i\phi_i} \right|^2 \otimes G(0, \delta E)$$

All parameters are free, except $\delta E = 0.0056$ GeV

Parameters of $\Upsilon(10753)$:

$$M = 10756.6 \pm 2.7_{\text{(stat.)}} \pm 0.8_{\text{(syst.)}} \text{ MeV}/c^2$$

$$\Gamma = 29.0 \pm 8.8_{\text{(stat.)}} \pm 1.2_{\text{(syst.)}} \text{ MeV}$$

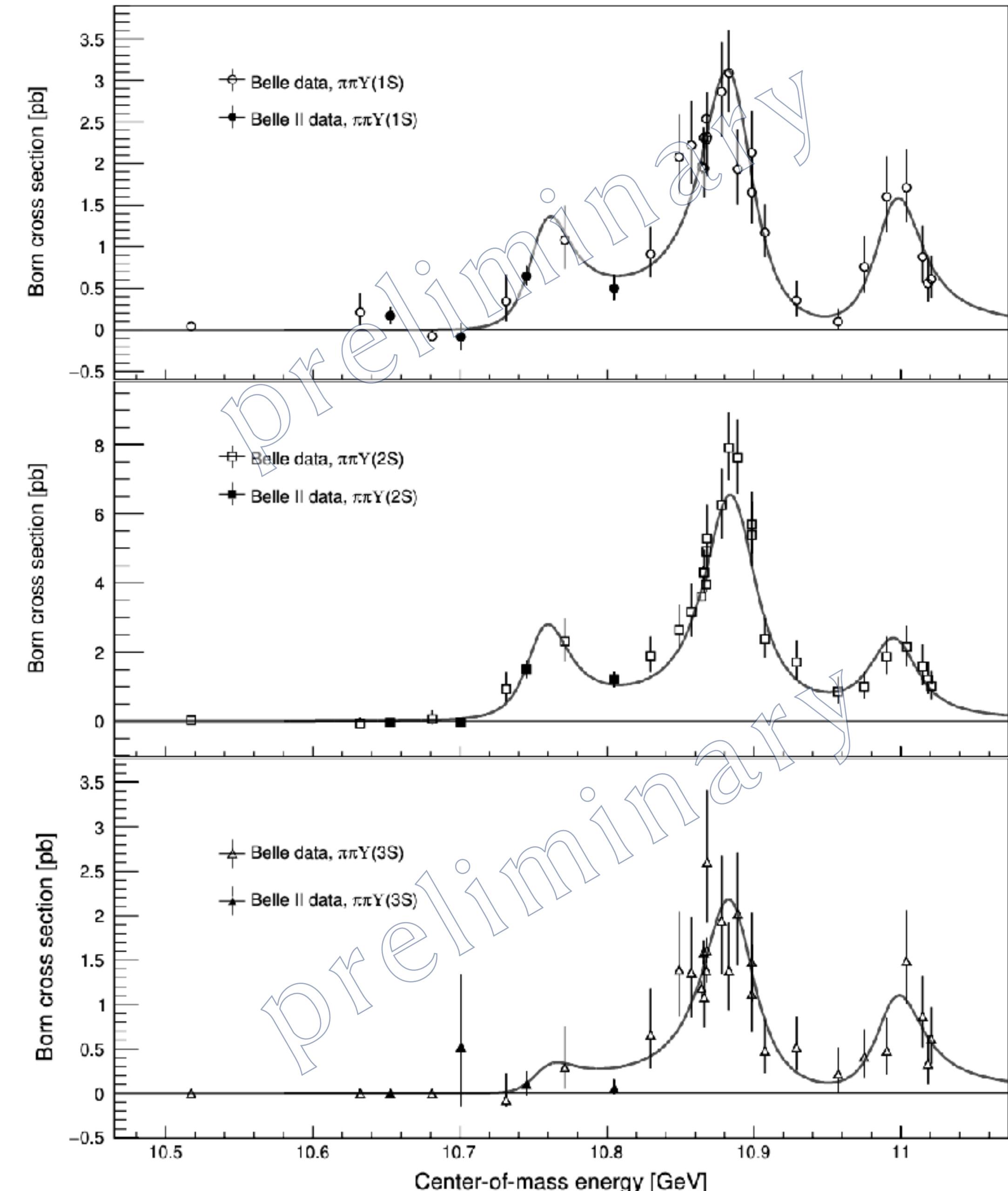
Agree with previous Belle measurement.

Improve uncertainties ~2 times smaller

	resonance mass (MeV/ c^2)	width (MeV)
--	------------------------------	-------------

$\Upsilon(5S)$	10884.7 ± 1.2	38.7 ± 3.7
----------------	-------------------	----------------

$\Upsilon(6S)$	10995.5 ± 4.2	34.6 ± 8.6
----------------	-------------------	----------------



Relative ratios

Relative ratios of the Born cross section at the resonance peak.

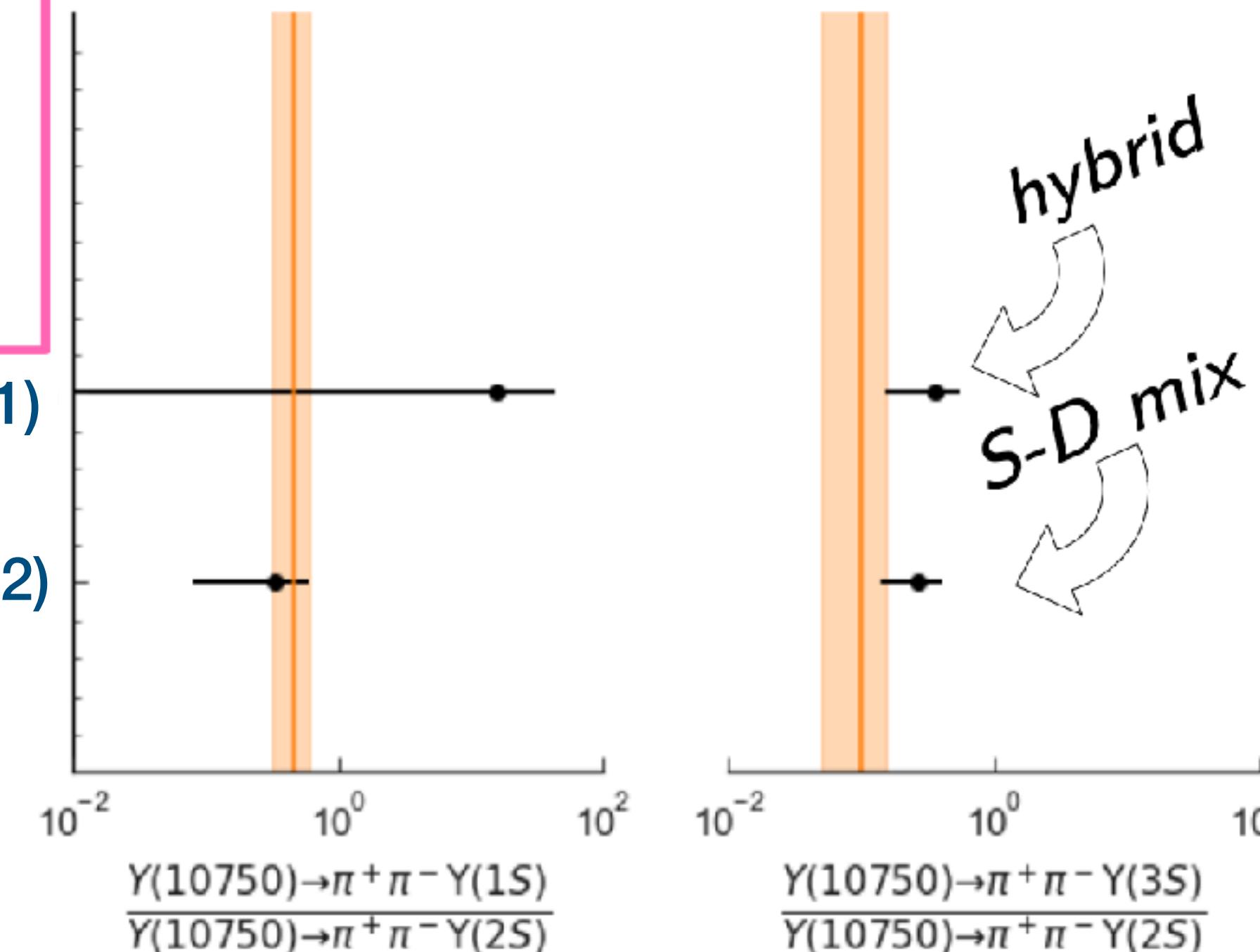
	$\mathcal{R}_{\sigma(1S/2S)}^{\Upsilon(10753)}$	$\mathcal{R}_{\sigma(3S/2S)}^{\Upsilon(10753)}$	$\mathcal{R}_{\sigma(1S/2S)}^{\Upsilon(5S)}$	$\mathcal{R}_{\sigma(3S/2S)}^{\Upsilon(5S)}$	$\mathcal{R}_{\sigma(1S/2S)}^{\Upsilon(6S)}$	$\mathcal{R}_{\sigma(3S/2S)}^{\Upsilon(6S)}$
Ratios	$0.46^{+0.15}_{-0.12}$	$0.10^{+0.05}_{-0.04}$	$0.45^{+0.04}_{-0.04}$	$0.32^{+0.04}_{-0.03}$	$0.64^{+0.23}_{-0.13}$	$0.41^{+0.16}_{-0.12}$

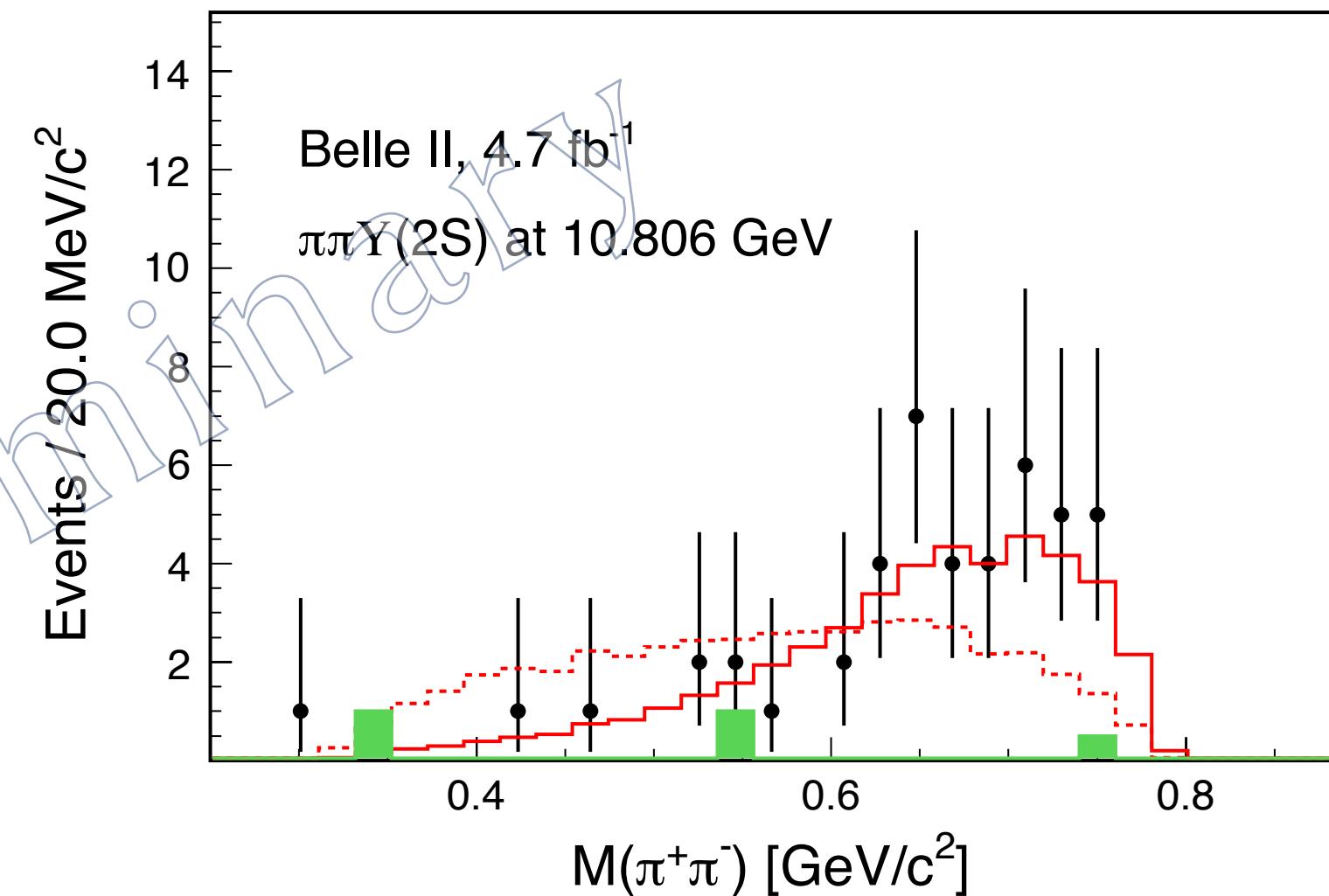
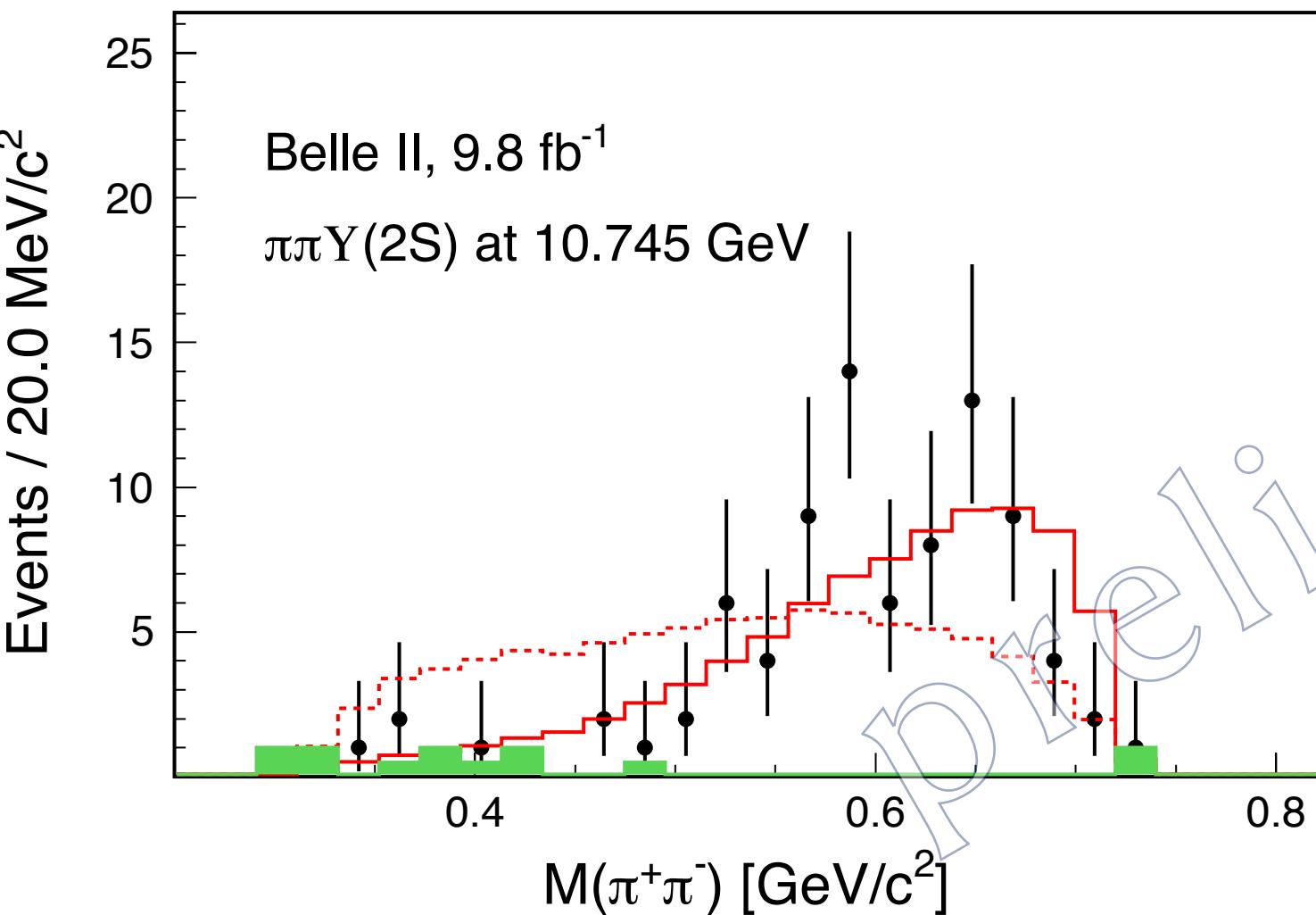
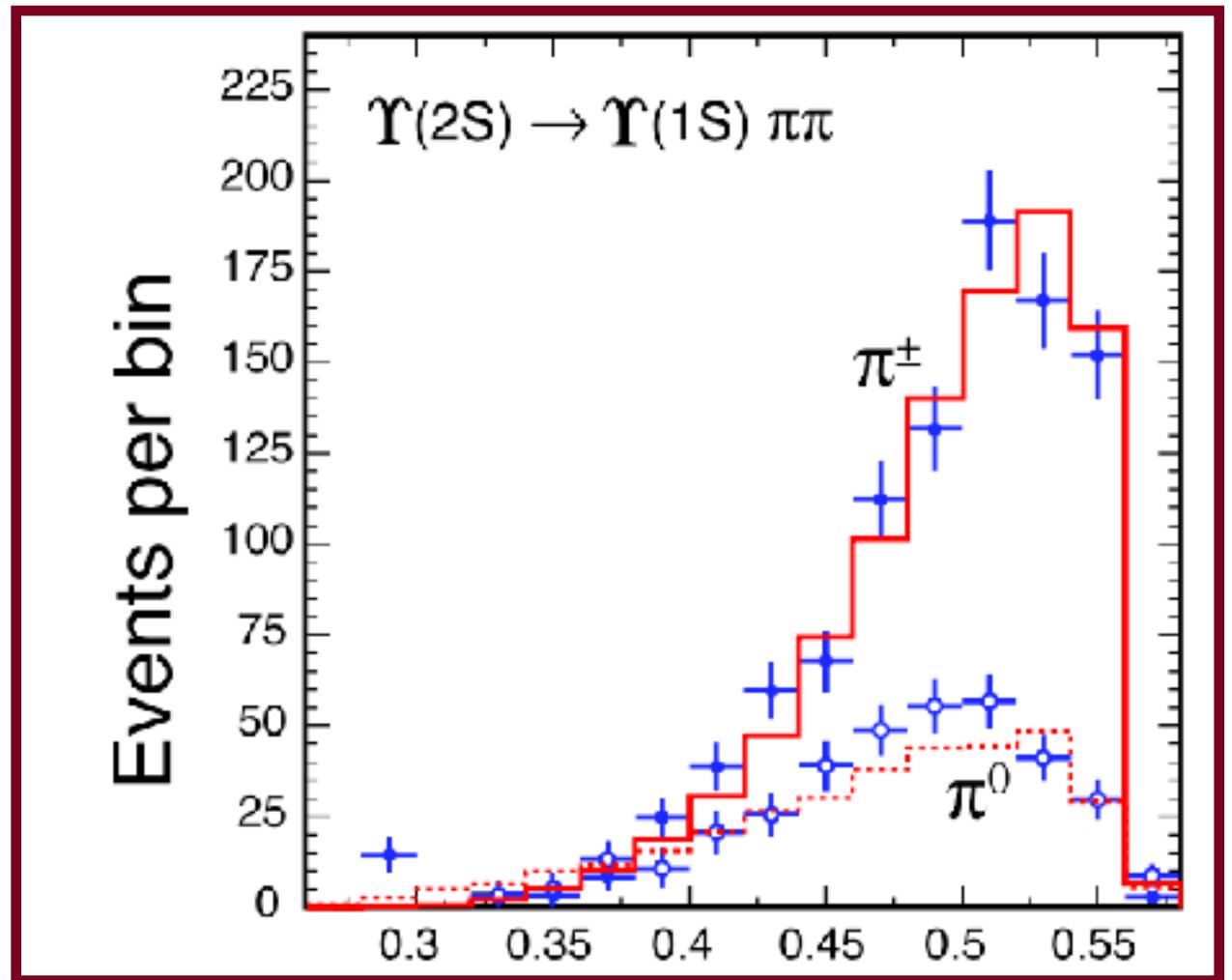
Castella. et. al. Phys. Rev. D 104, 034019 (2021)

Bai. et. al. Phys. Rev. D 105, 074007 (2022)

Mild tension
with all
models?

No significant $\Upsilon(10753) \rightarrow \pi\pi\Upsilon(3S)$





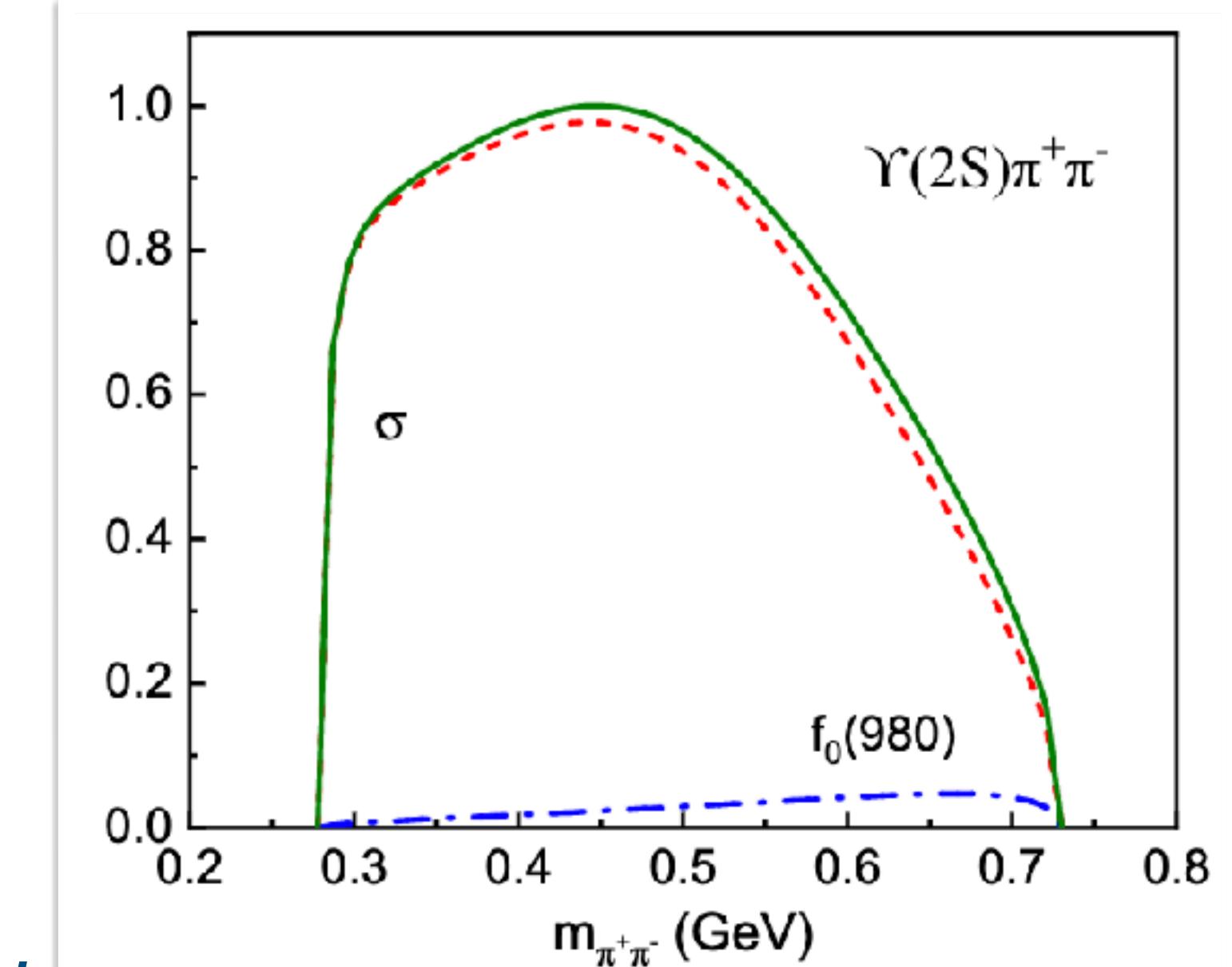
- The $M(\pi^+\pi^-)$ distribution is very similar with that from $\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$

- Use CLEO parameterization:

$$\mathcal{M} \propto \mathcal{A}(q^2 - 2M_\pi^2) + \mathcal{B}E_1E_2 + \mathcal{C}[(\epsilon' \cdot q_1)(\epsilon \cdot q_2) + (\epsilon' \cdot q_2)(\epsilon \cdot q_1)]$$

The \mathcal{C} term could be ignored because of spin flip should be very small.

We fix $\mathcal{A} = 1$, and \mathcal{B} is fitted to be $(1.1 \pm 0.3) + (4.7 \pm 1.5)i$

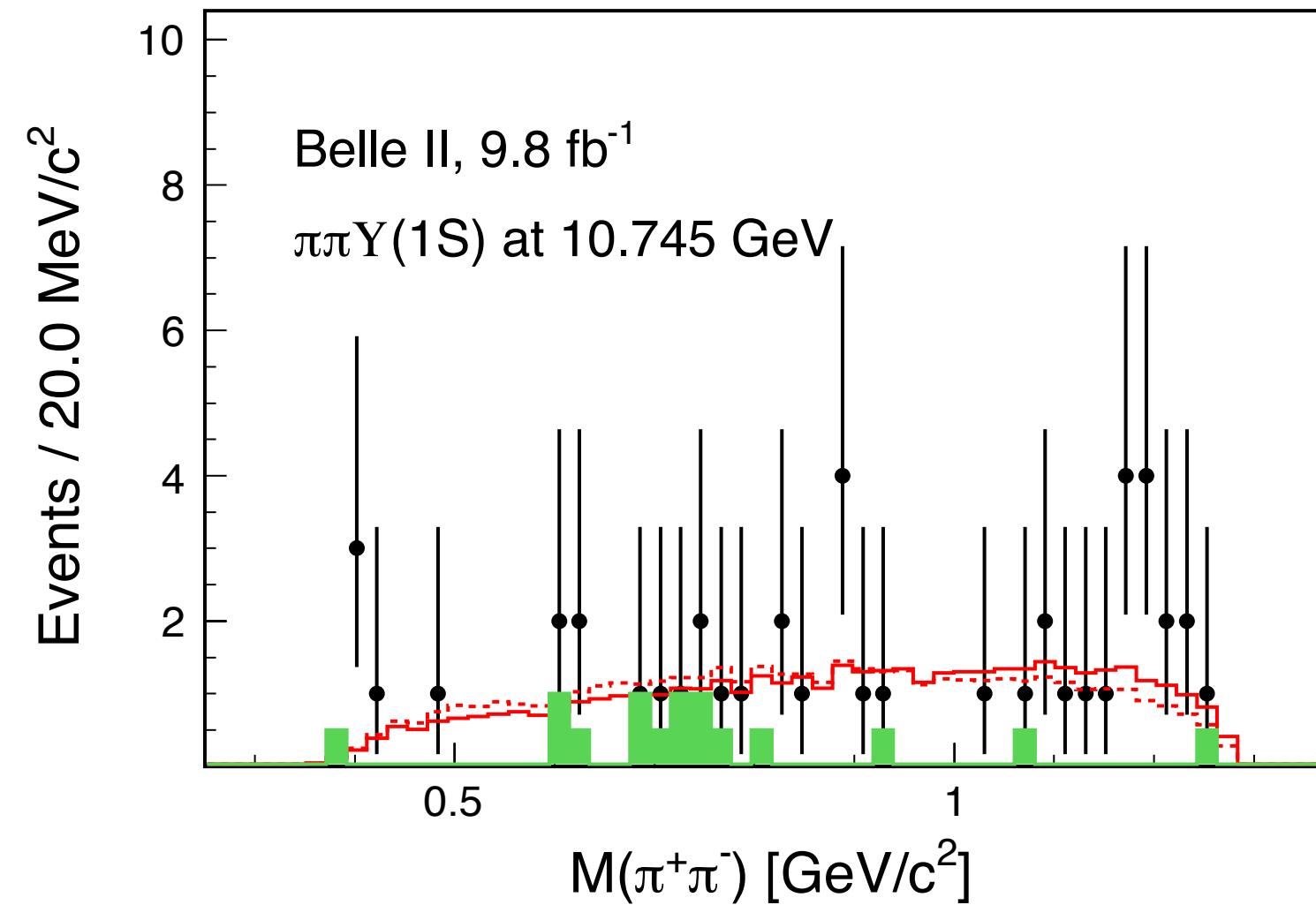


Bai. et. al.

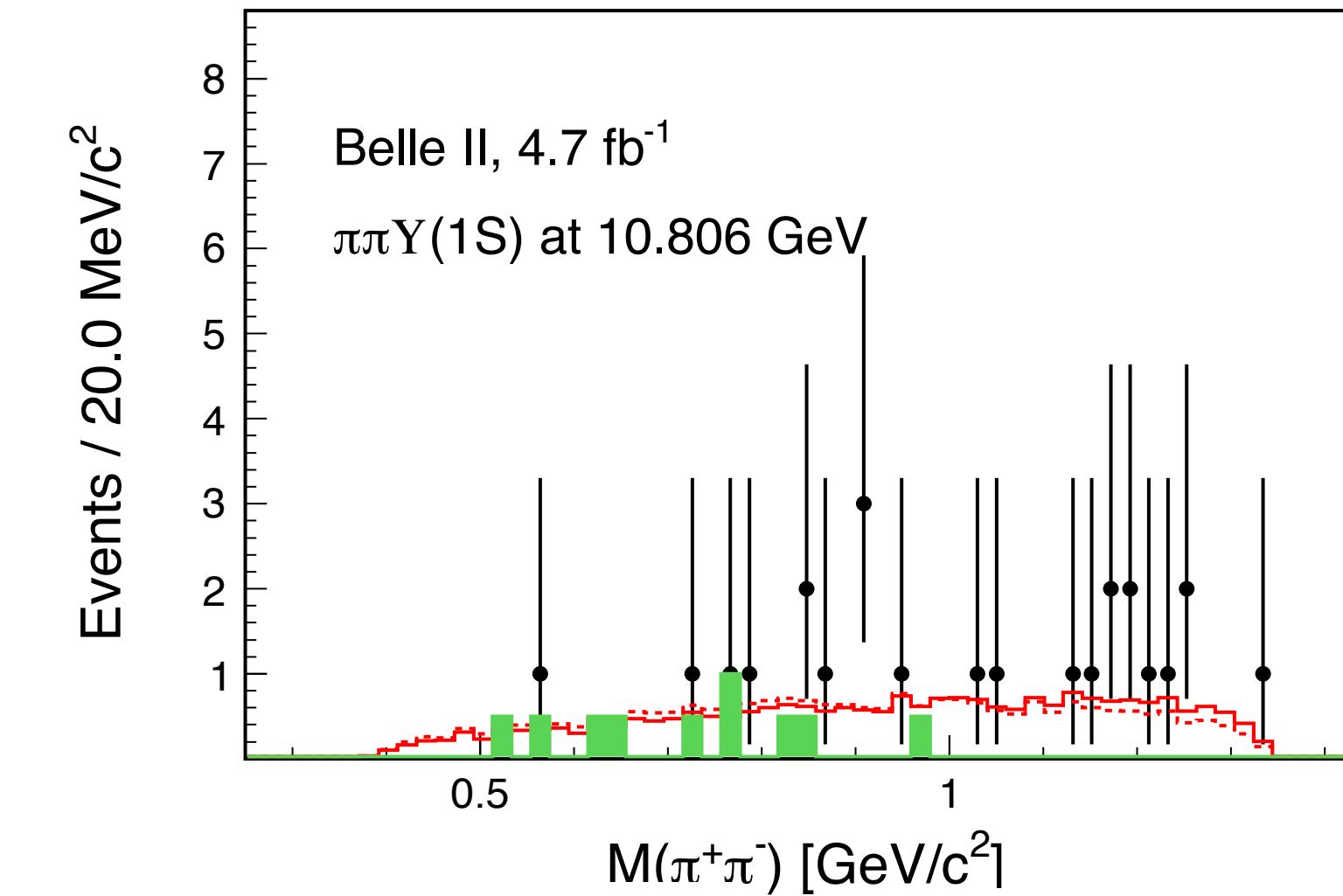
Phys. Rev. D 105, 074007 (2022)

S-D mix

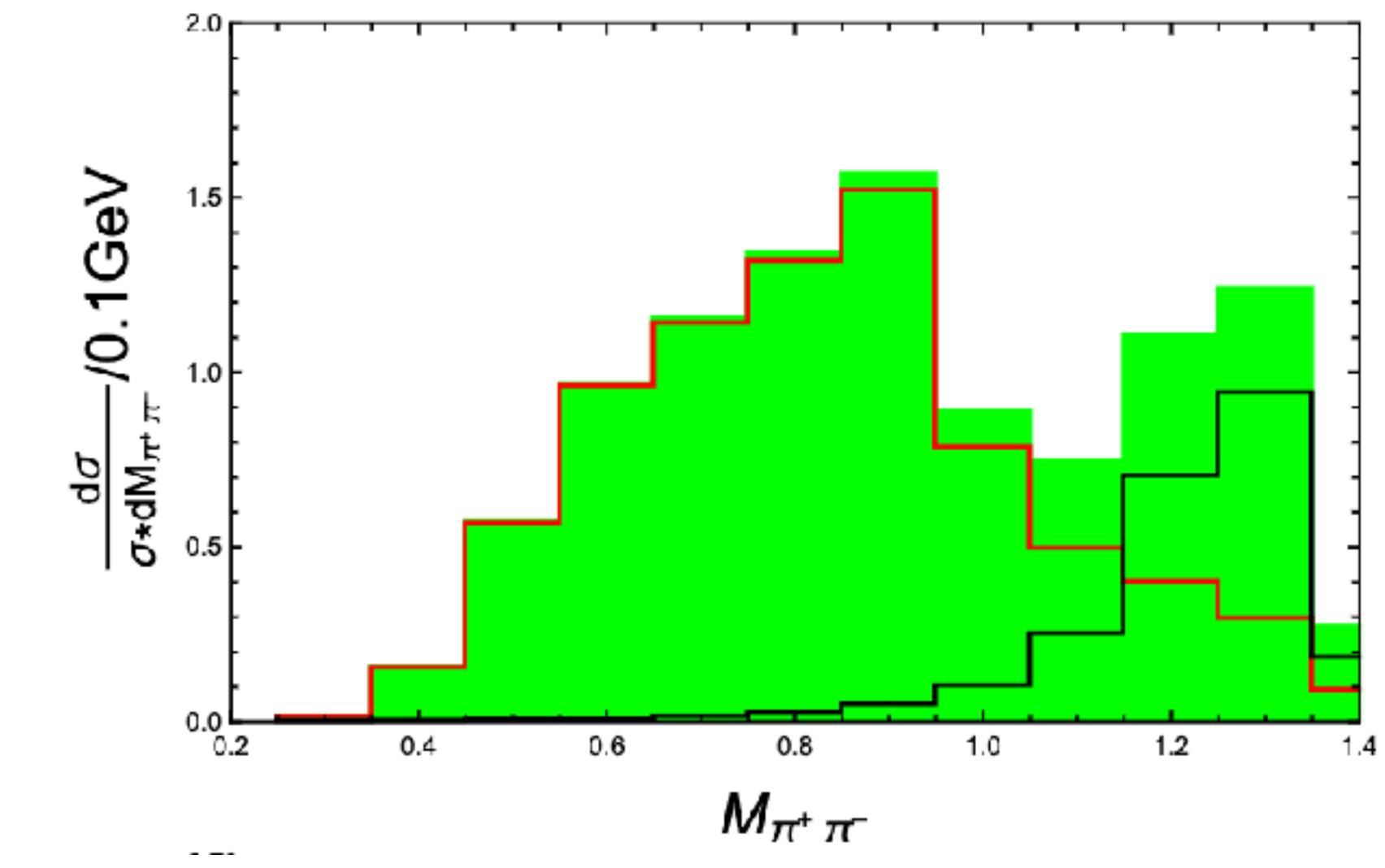
In the case of $\Upsilon(10753) \rightarrow \pi\pi\Upsilon(1S)$



Castella. et. al.
 Phys. Rev. D 104, 034019 (2021)



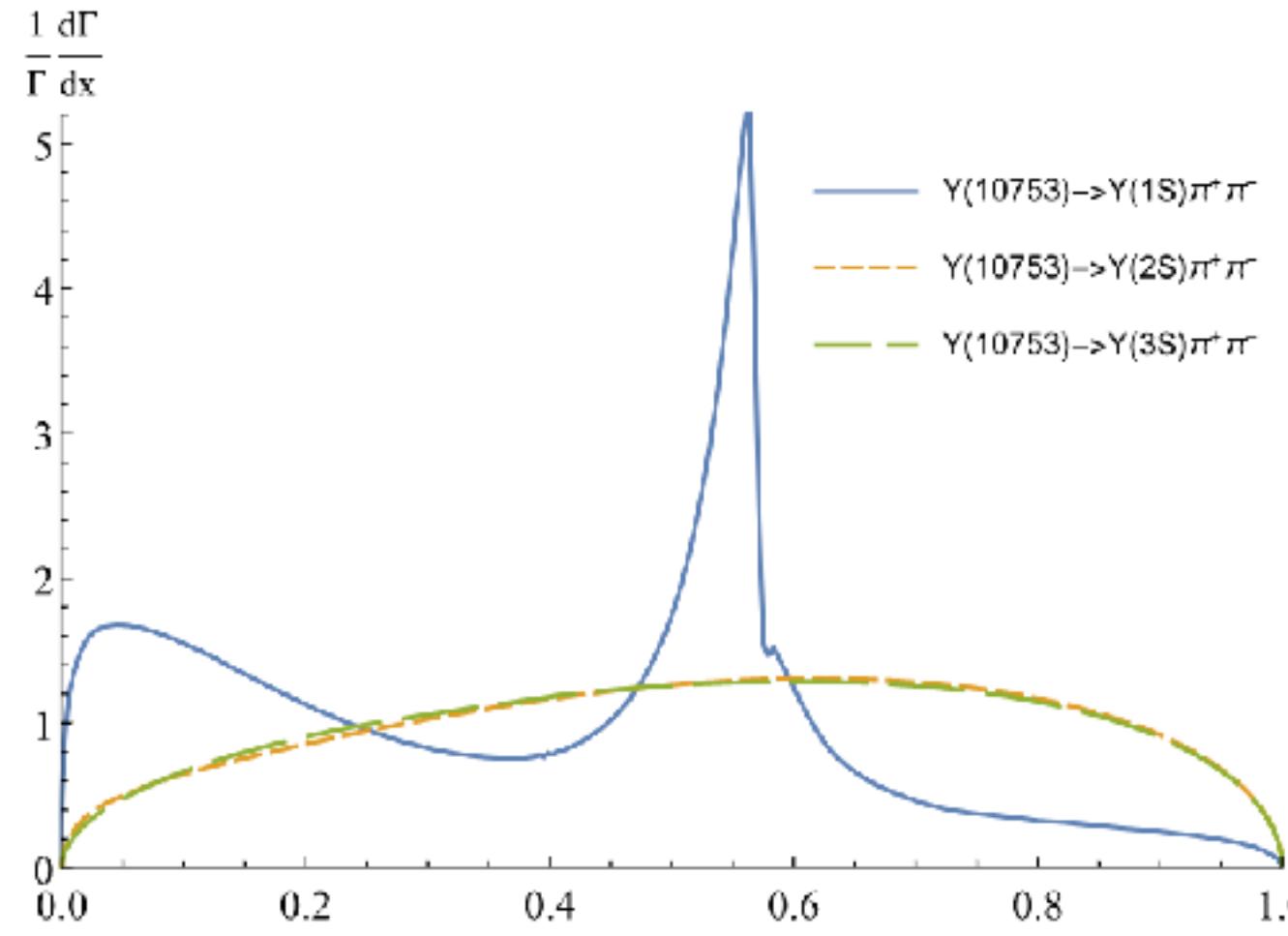
Bai. et. al.
 Phys. Rev. D 105, 074007 (2022)



Tetraquark

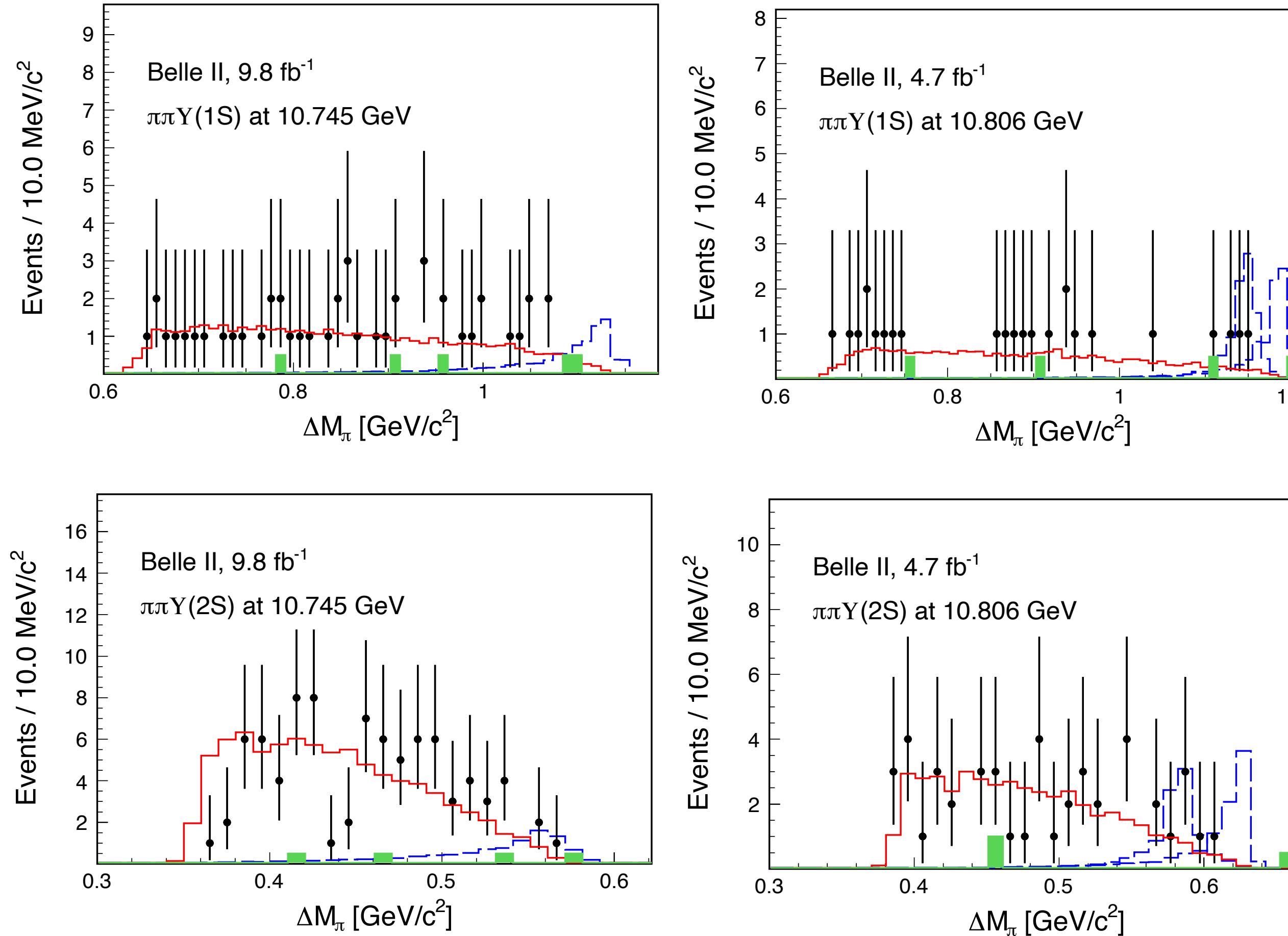
S-D mix

Hybrid



Intermediate state – $\Upsilon(10753) \rightarrow \pi Z_b$

Belle-II preliminary, arxiv:2401.12021

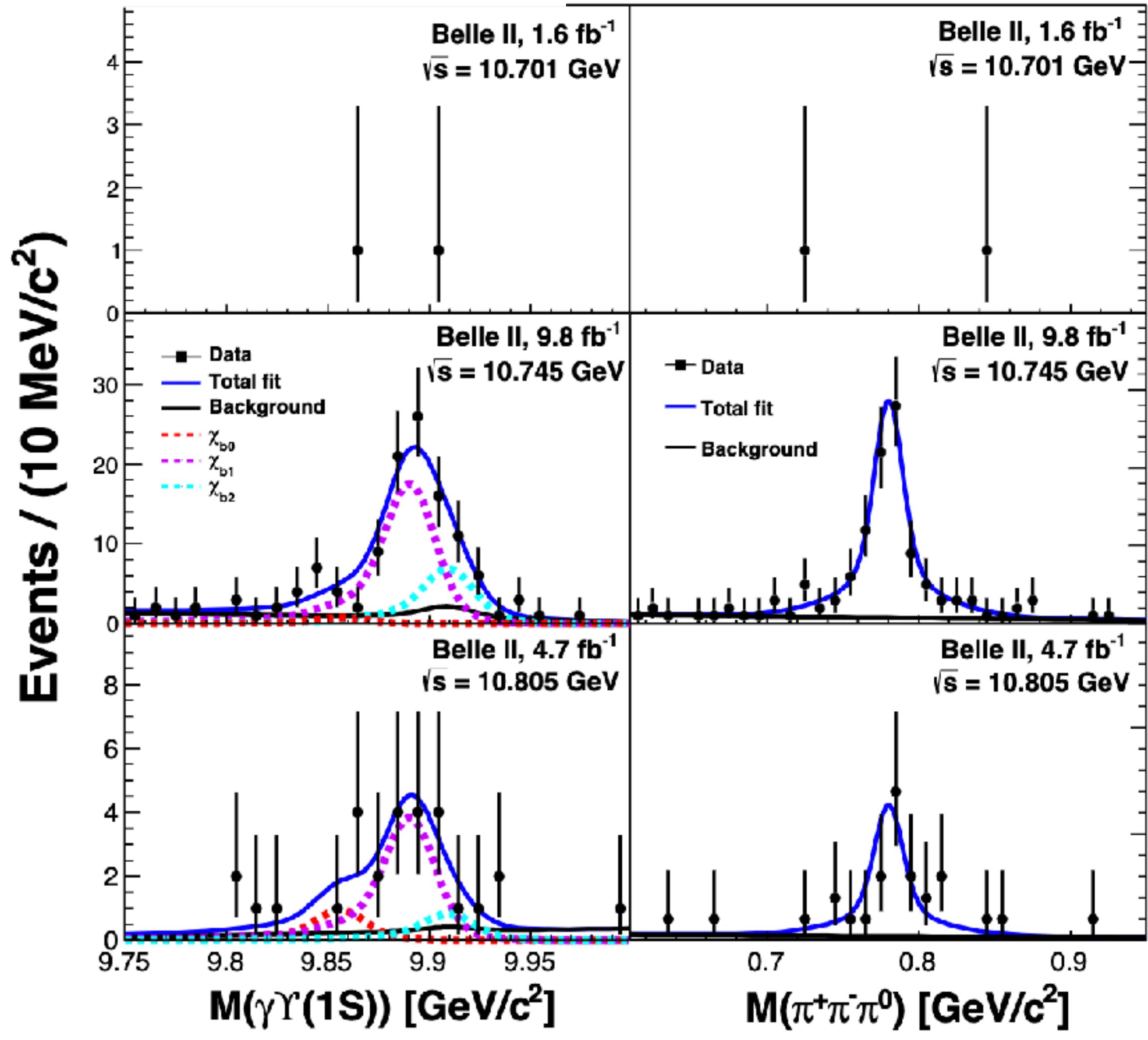


- No Evidence of $Z_b(10610/10650)$.
- Upper limits estimated at 90 % C.L. using Bayesian method.

Mode	$N_{Z_{b1}}$	$N_{Z_{b1}}^{\text{UL}}$	$\sigma_{Z_{b1}}$ (pb)	$\sigma_{Z_{b1}}^{\text{UL}}$ (pb)	$N_{Z_{b2}}^{\text{UL}}$	$N_{Z_{b2}}$	$\sigma_{Z_{b2}}$ (pb)	$\sigma_{Z_{b2}}^{\text{UL}}$ (pb)
10.745 GeV								
$\pi\Upsilon(1S)$	$0.0^{+1.6}_{-0.0}$	< 4.9	$0.00^{+0.04}_{-0.00}$	< 0.13	–	–	–	–
$\pi\Upsilon(2S)$	$5.8^{+5.9}_{-4.6}$	< 13.8	$0.06^{+0.06}_{-0.05}$	< 0.14	–	–	–	–
10.805 GeV								
$\pi\Upsilon(1S)$	$2.5^{+2.4}_{-1.6}$	< 5.2	$0.21^{+0.20}_{-0.13}$	< 0.43	$0.0^{+0.7}_{-0.0}$	< 5.8	$0.00^{+0.03}_{-0.00}$	< 0.28
$\pi\Upsilon(2S)$	$5.2^{+3.8}_{-3.0}$	< 12.3	$0.15^{+0.11}_{-0.09}$	< 0.35	$0.0^{+0.8}_{-0.0}$	< 6.0	$0.00^{+0.04}_{-0.00}$	< 0.30

Observation of $\Upsilon(10753) \rightarrow \omega\chi_{bJ}$

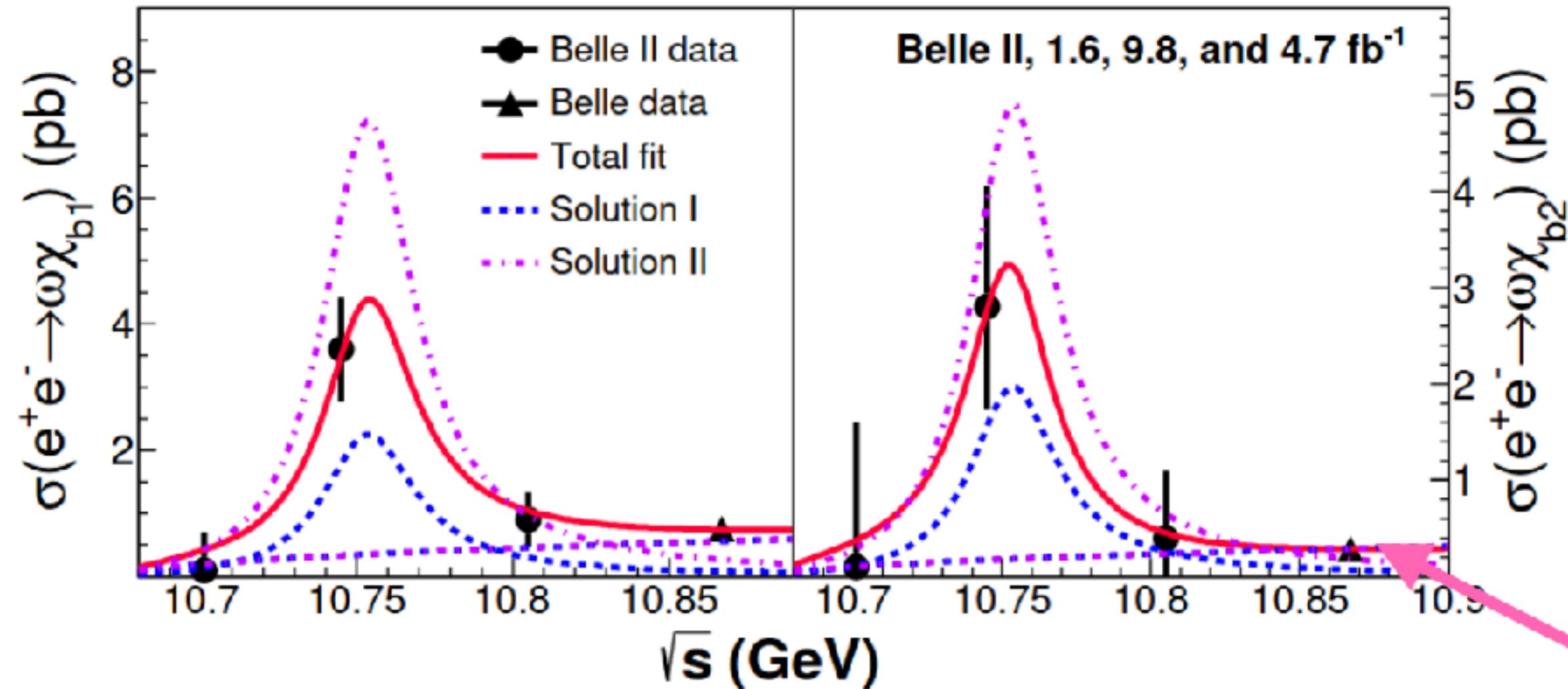
[PRL 130, 091902 (2023)]



- Reconstruct $\omega \rightarrow \pi^+\pi^-\pi^0, \chi_{bJ} \rightarrow \gamma\Upsilon(1S)$
- Clear $\omega\chi_{bJ}$ signals at $\sqrt{s} = 10.745$ and 10.805 GeV
- 2D fit to $M(\pi^+\pi^-\pi^0)$ vs. $M(\gamma\Upsilon(1S))$

Channel	\sqrt{s} (GeV)	N^{sig}	$\sigma_{\text{Born}}^{(\text{UL})}$ (pb)
$\omega\chi_{b1}$	10.745	$68.9^{+13.7}_{-13.5}$	$3.6^{+0.7}_{-0.7} \pm 0.4$
$\omega\chi_{b2}$		$27.6^{+11.6}_{-10.0}$	$2.8^{+1.2}_{-1.0} \pm 0.5$
$\omega\chi_{b1}$	10.805	$15.0^{+6.8}_{-6.2}$	$1.6 @ 90\% \text{ C.L.}$
$\omega\chi_{b2}$		$3.3^{+5.3}_{-3.8}$	$1.5 @ 90\% \text{ C.L.}$

- The total χ_{bJ} signal significances are 11.5σ and 5.2σ at $\sqrt{s} = 10.745$ and 10.805 GeV



$$\sigma[e e \rightarrow \omega\chi_{b0}(1P)] < 11.3 \text{ pb} @ 10.750 \text{ GeV}$$

Two solutions (constr. or destr. interference):

$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega\chi_{b1}(1P)] = \begin{cases} (0.63 \pm 0.39 \pm 0.20) \text{ eV} \\ (2.01 \pm 0.38 \pm 0.76) \text{ eV} \end{cases}$$

$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega\chi_{b2}(1P)] = \begin{cases} (0.53 \pm 0.40 \pm 0.15) \text{ eV} \\ (1.32 \pm 0.44 \pm 0.53) \text{ eV} \end{cases}$$

At $\sqrt{s} = 10.867 \text{ GeV}$:

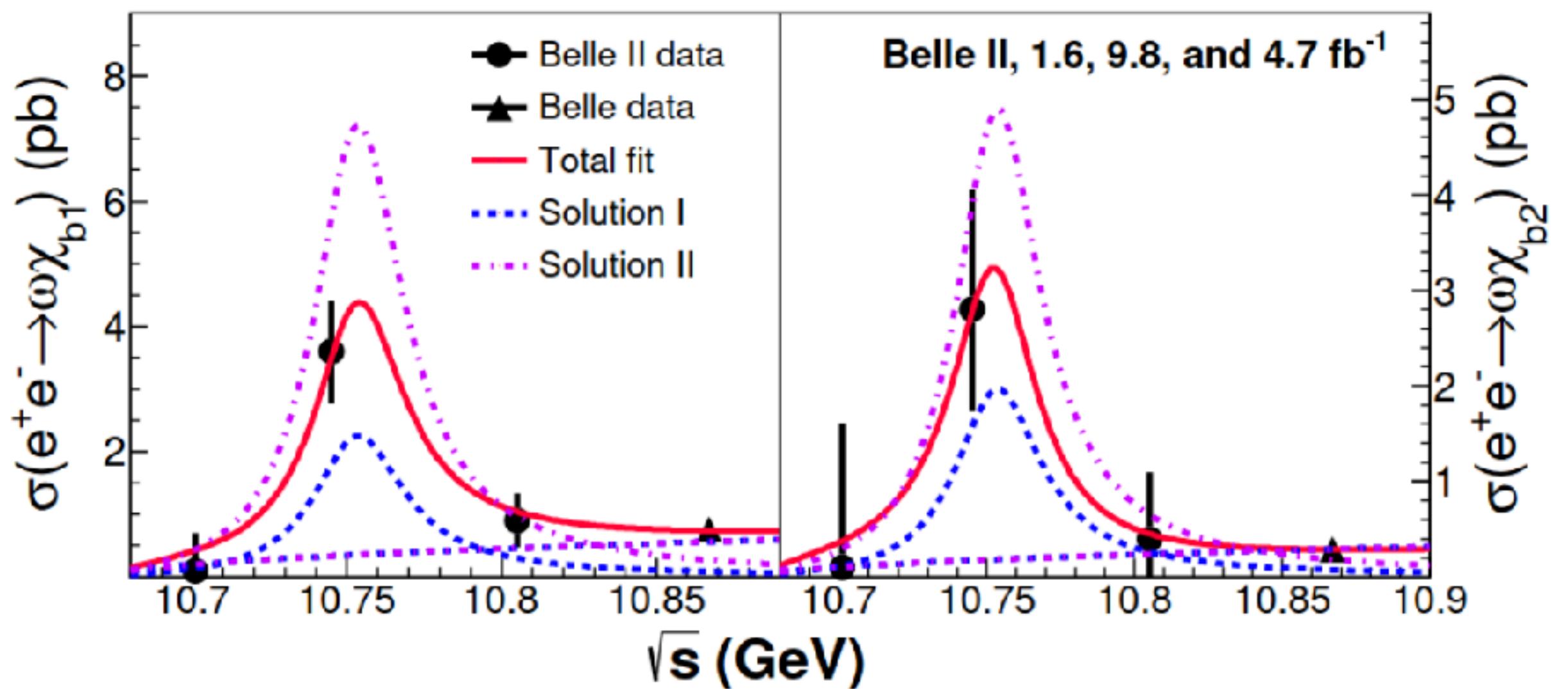
$$\sigma_{\text{Born}}(e^+e^- \rightarrow \omega\chi_{b1}) = (0.76 \pm 0.11 \pm 0.11) \text{ pb}$$

$$\sigma_{\text{Born}}(e^+e^- \rightarrow \omega\chi_{b2}) = (0.29 \pm 0.11 \pm 0.08) \text{ pb}$$

[PRL 113, 142001(2014)]

What we thought was $Y(5S) \rightarrow \omega\chi_{bj}(1P)$ is probably just the tail of the $Y(10750)$!

Combined analysis with Belle data coming soon



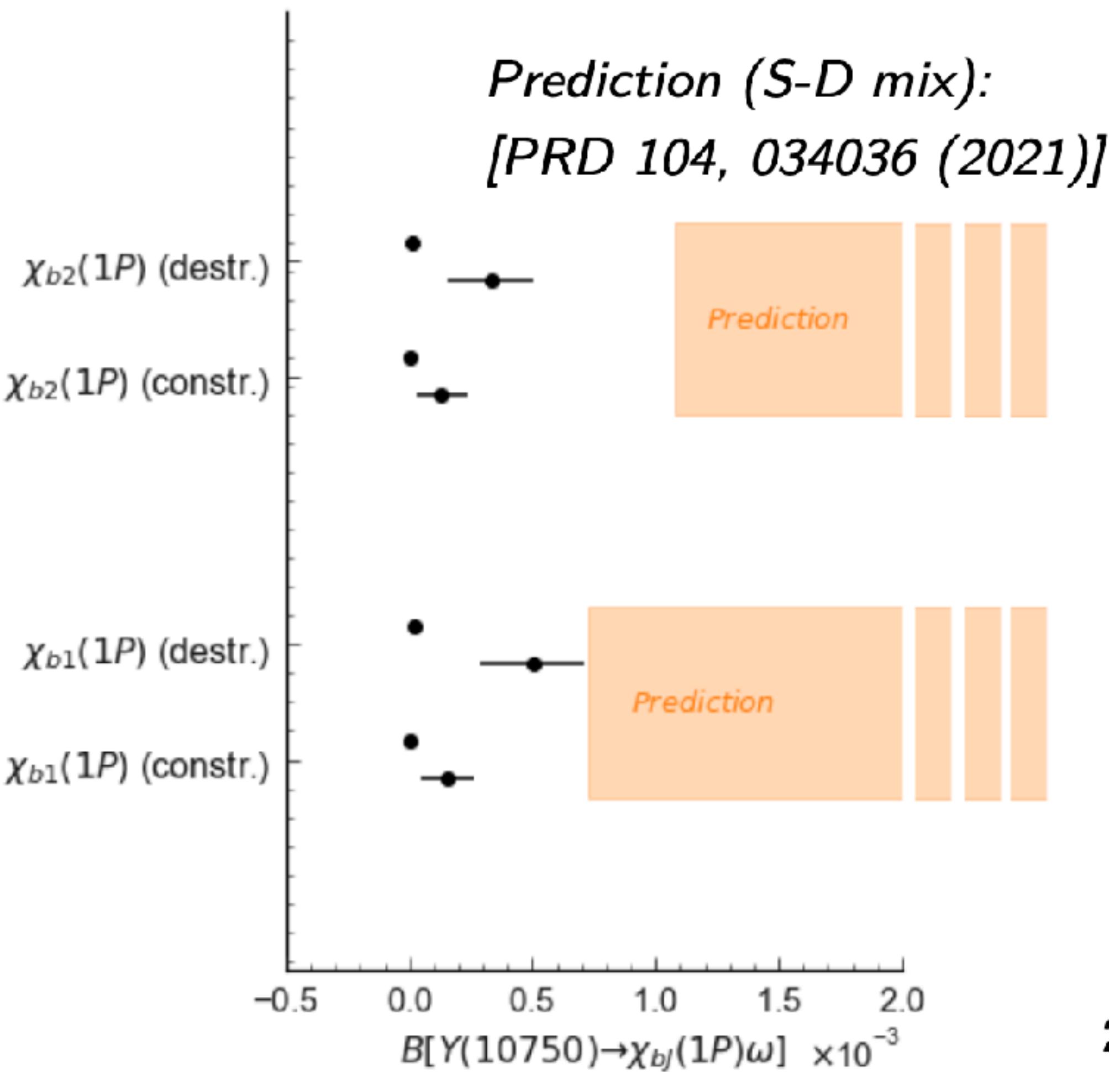
$$\sigma[ee \rightarrow \omega\chi_{b_0}(1P)] < 11.3 \text{ pb} @ 10.750 \text{ GeV}$$

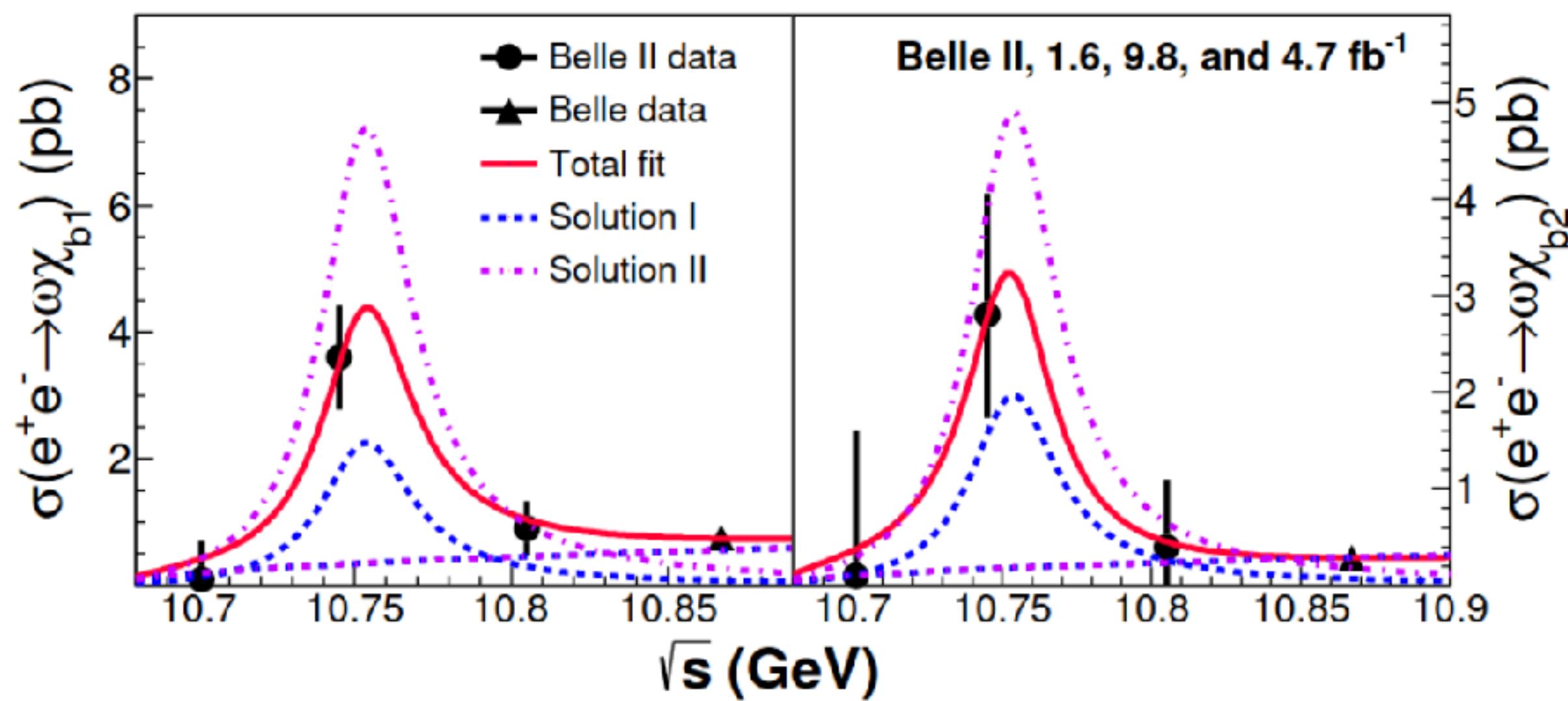
Two solutions (constr. or destr. interference):

$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega\chi_{b_1}(1P)] = \begin{cases} (0.63 \pm 0.39 \pm 0.20) \text{ eV} \\ (2.01 \pm 0.38 \pm 0.76) \text{ eV} \end{cases}$$

$$\Gamma_{ee} \times B[Y(10750) \rightarrow \omega\chi_{b_2}(1P)] = \begin{cases} (0.53 \pm 0.40 \pm 0.15) \text{ eV} \\ (1.32 \pm 0.44 \pm 0.53) \text{ eV} \end{cases}$$

Disagreement with S-D model?

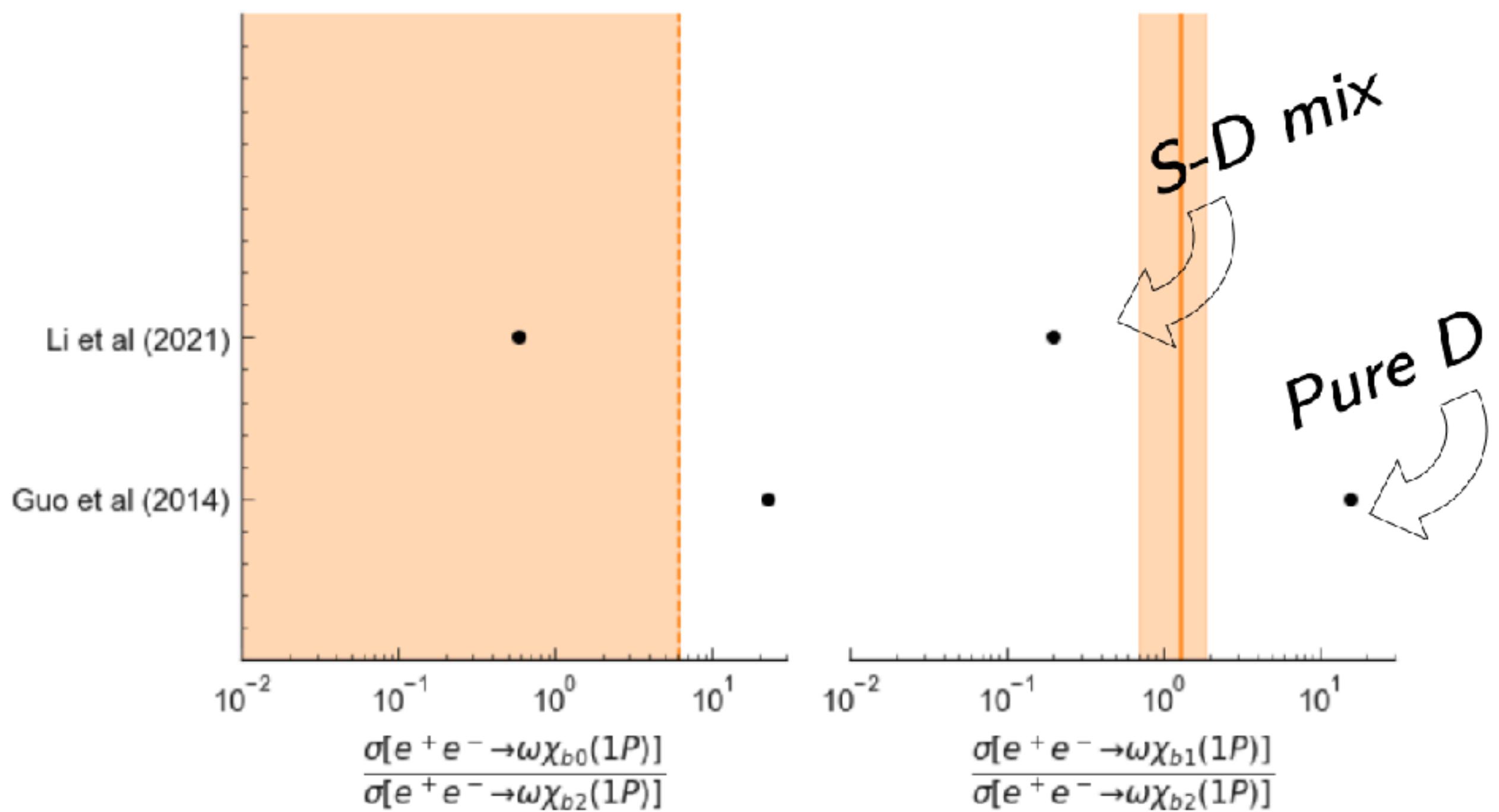




Measured ratios:

$$\frac{B[Y(10750) \rightarrow \omega\chi_{b1}(1P)]}{B[Y(10750) \rightarrow \omega\chi_{b2}(1P)]} = 1.3 \pm 0.6$$

$$\frac{B[Y(10750) \rightarrow \omega\chi_{b0}(1P)]}{B[Y(10750) \rightarrow \omega\chi_{b2}(1P)]} < 7 \quad (\text{private extrapolation})$$



Search for $\Upsilon(10753) \rightarrow \omega\eta_b, \omega\chi_{b0}$

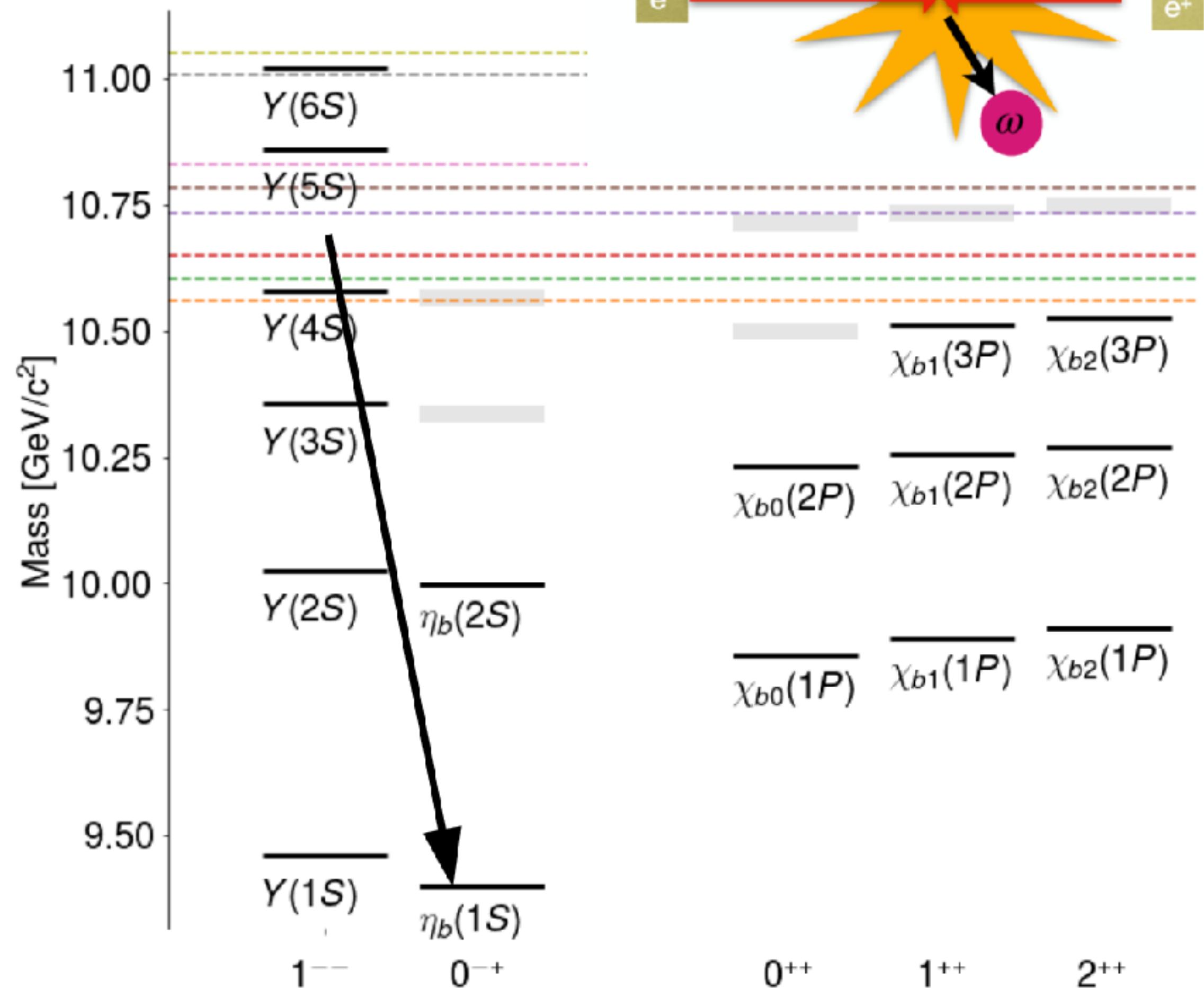
[Wang, Chin. Phys. C 43, 123102 (2019)]

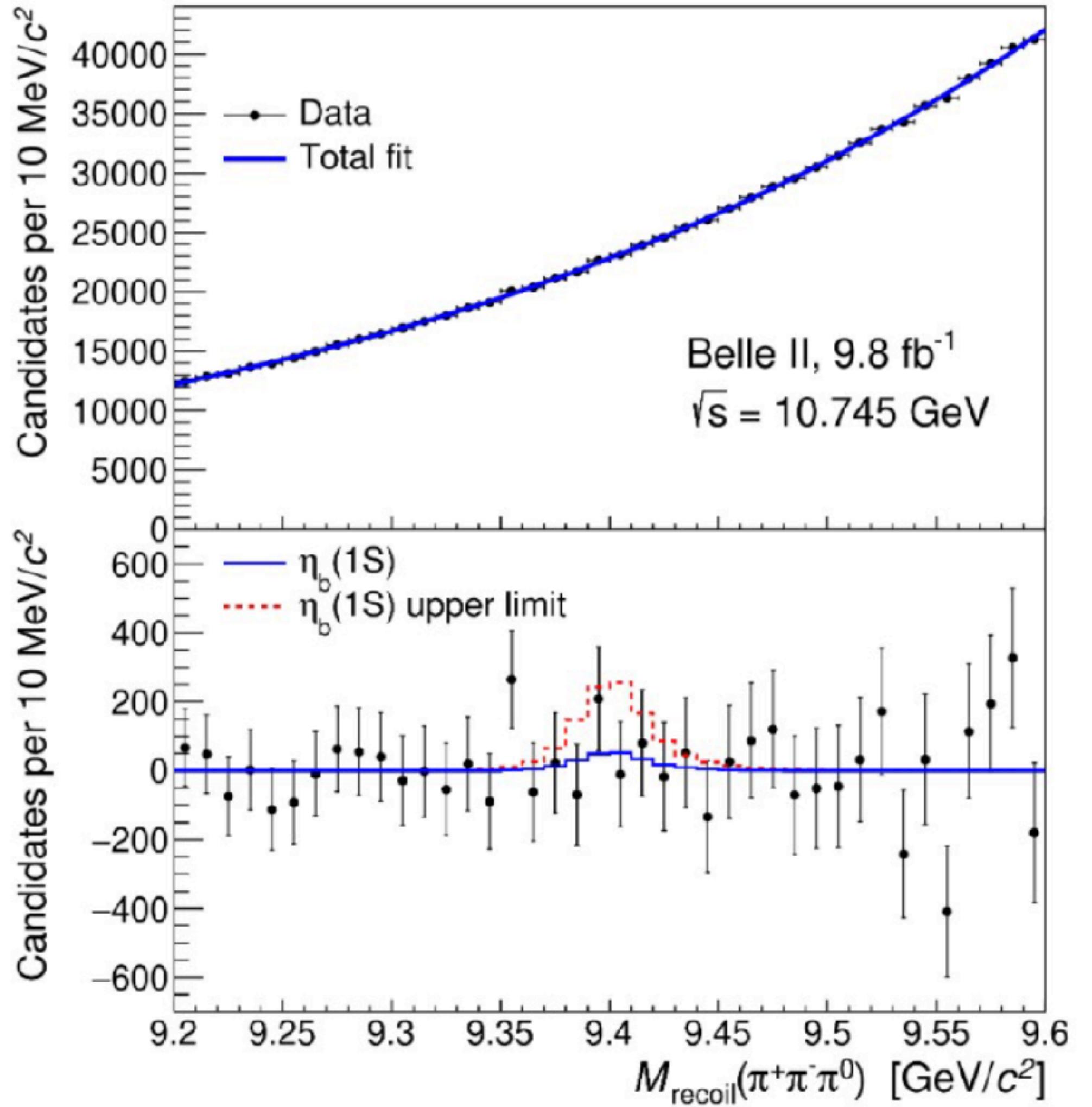
Mode	$\mathcal{B}(4q)$ (%)	$\mathcal{B}(bb)$ (%)
$B\bar{B}$	$39.3^{+38.7}_{-22.9}$	21.3
$B\bar{B}^*$	~ 0.2	14.3
$B^*\bar{B}^*$	$52.3^{+54.9}_{-31.7}$	64.1
$B_s\bar{B}_s$	-	0.3
$\omega\eta_b$	$7.9^{+14.0}_{-5.0}$	-
$f_0(1370)\Upsilon$	$0.2^{+0.6}_{-0.2}$	-
$\omega\Upsilon$	~ 0	-

Strategy:

- Reconstruct ω
- Measure its recoil mass

No convenient reconstruction decay channels for $\eta_b(1S)$

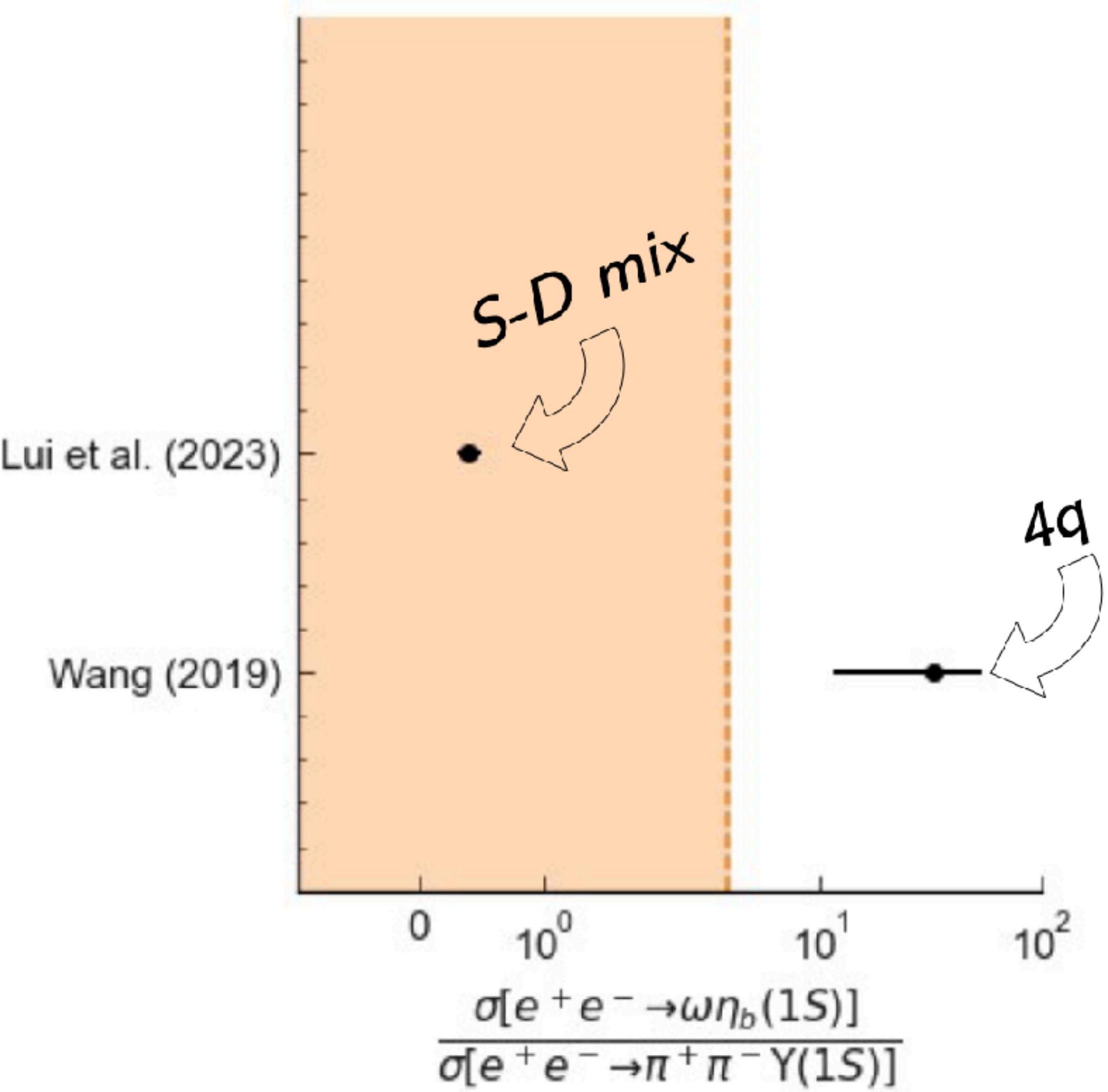




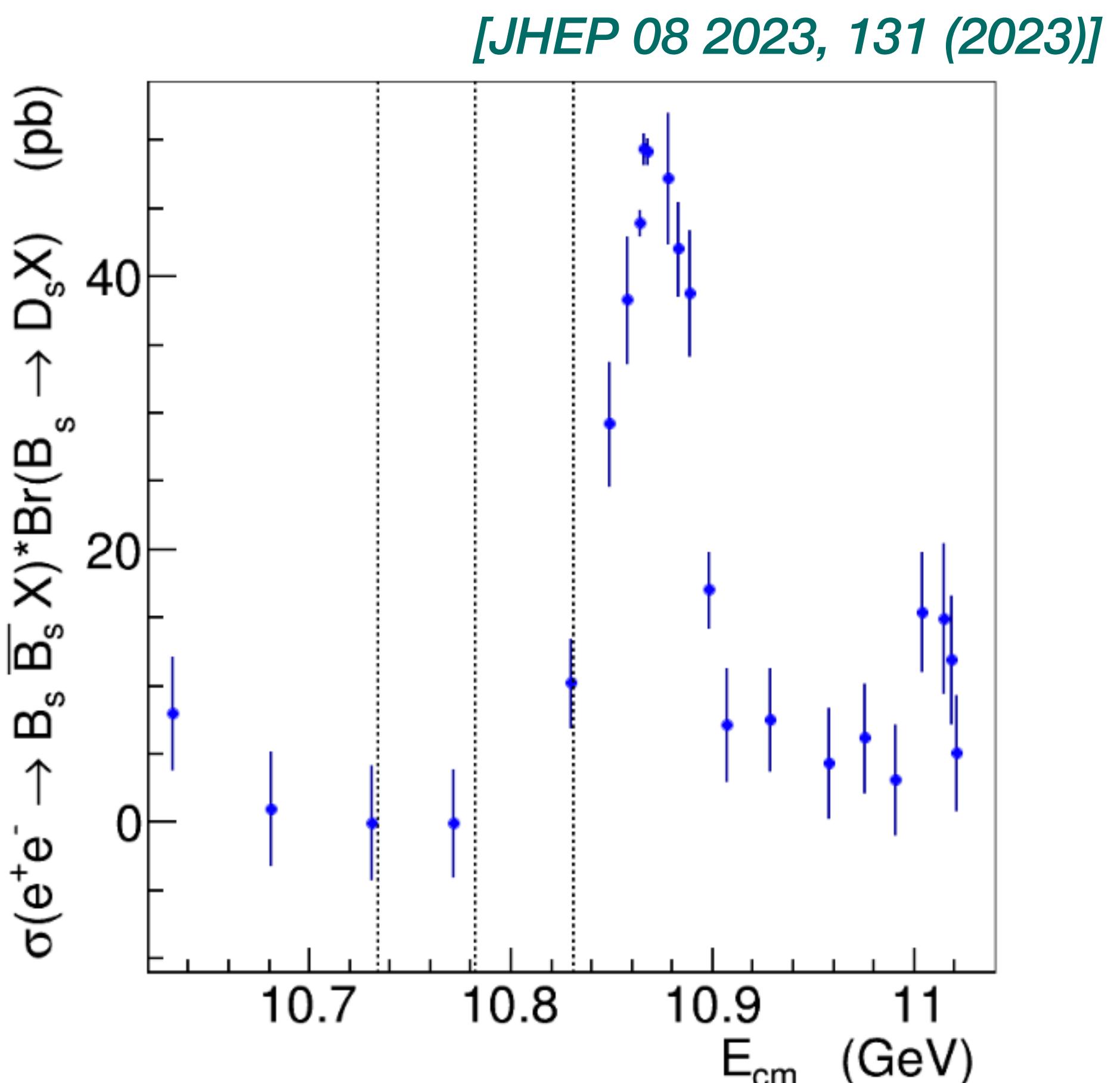
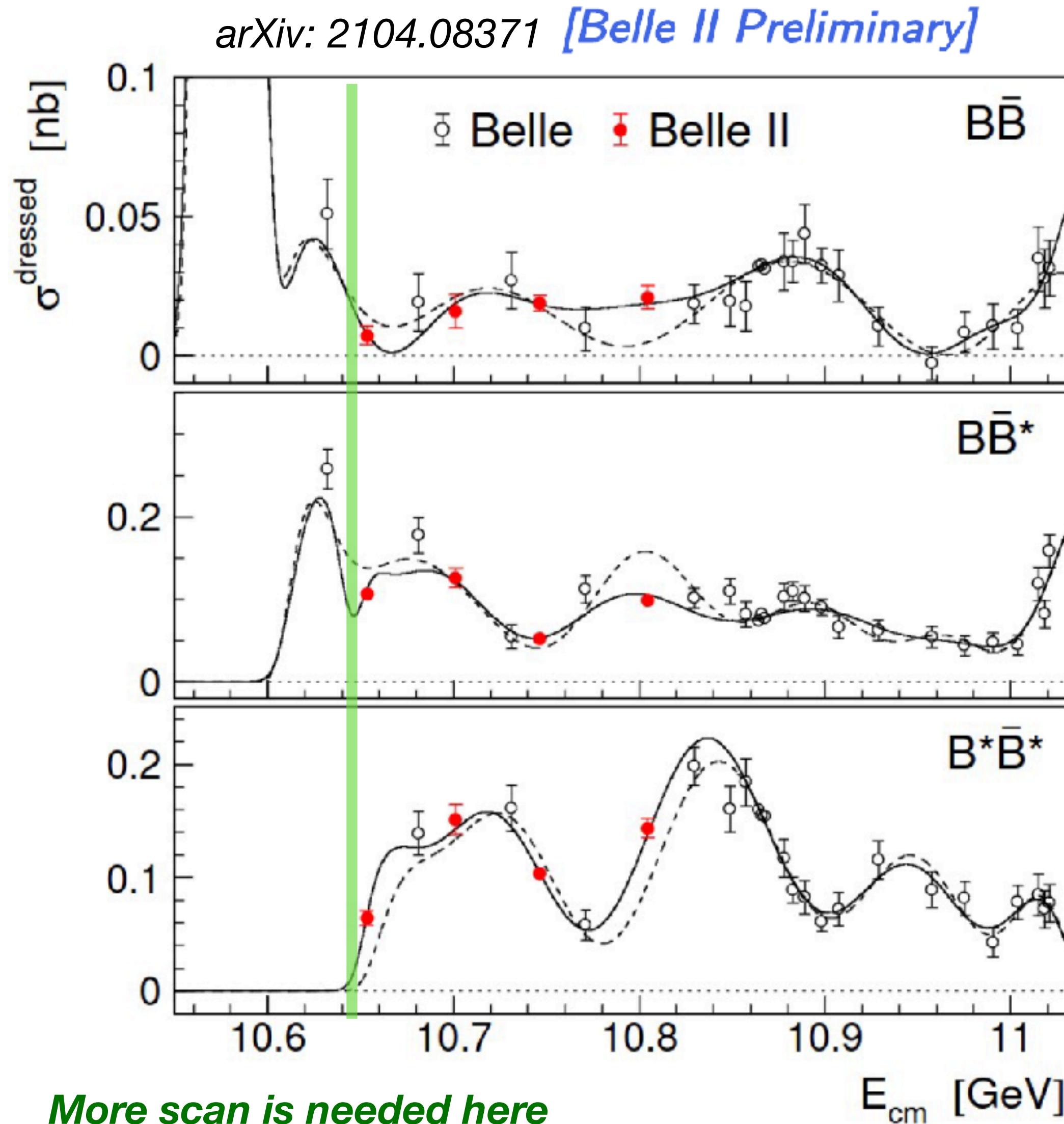
No evidence of ω transition to $\eta_b(1S)$!

$$\sigma_B(e^+e^- \rightarrow \eta_b(1S)\omega) < 2.5 \text{ pb}$$

Compatible with S-D mixed



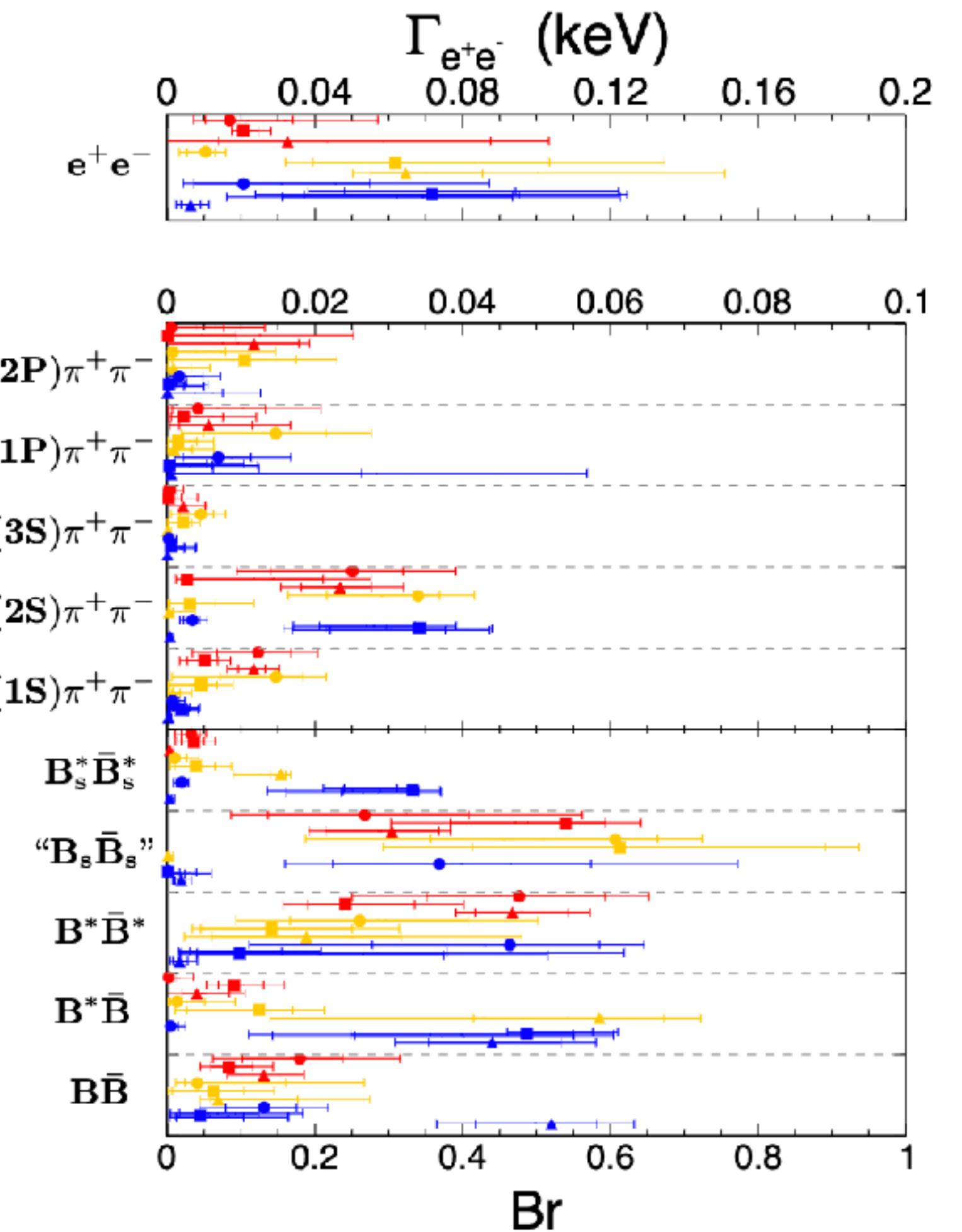
Measurement of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}, B_s^{(*)}\bar{B}_s^{(*)}$



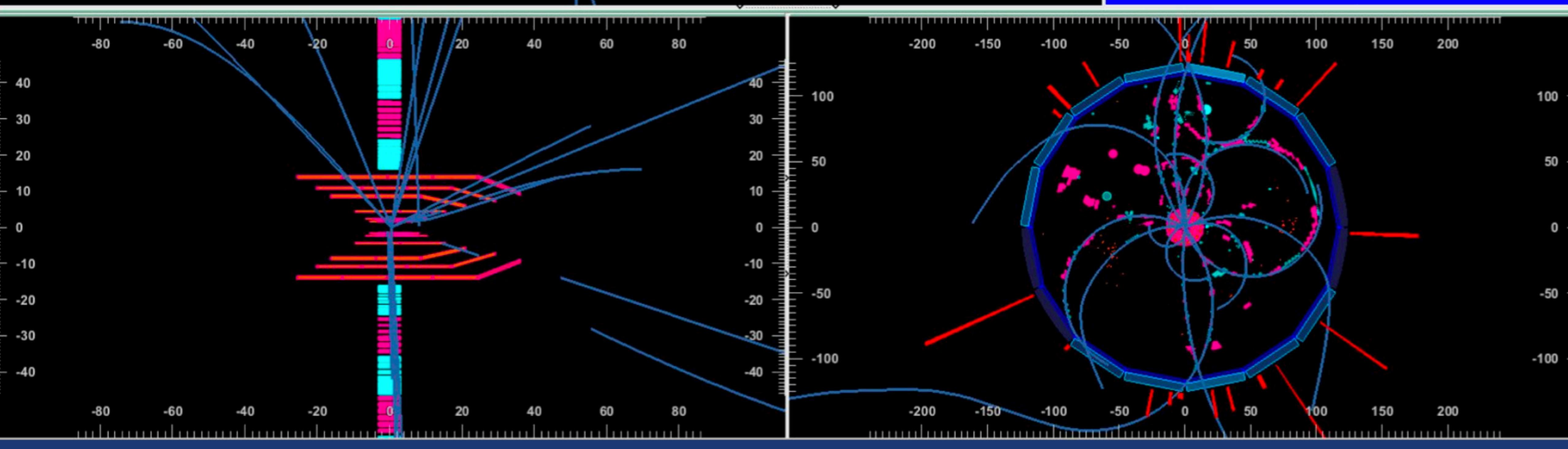
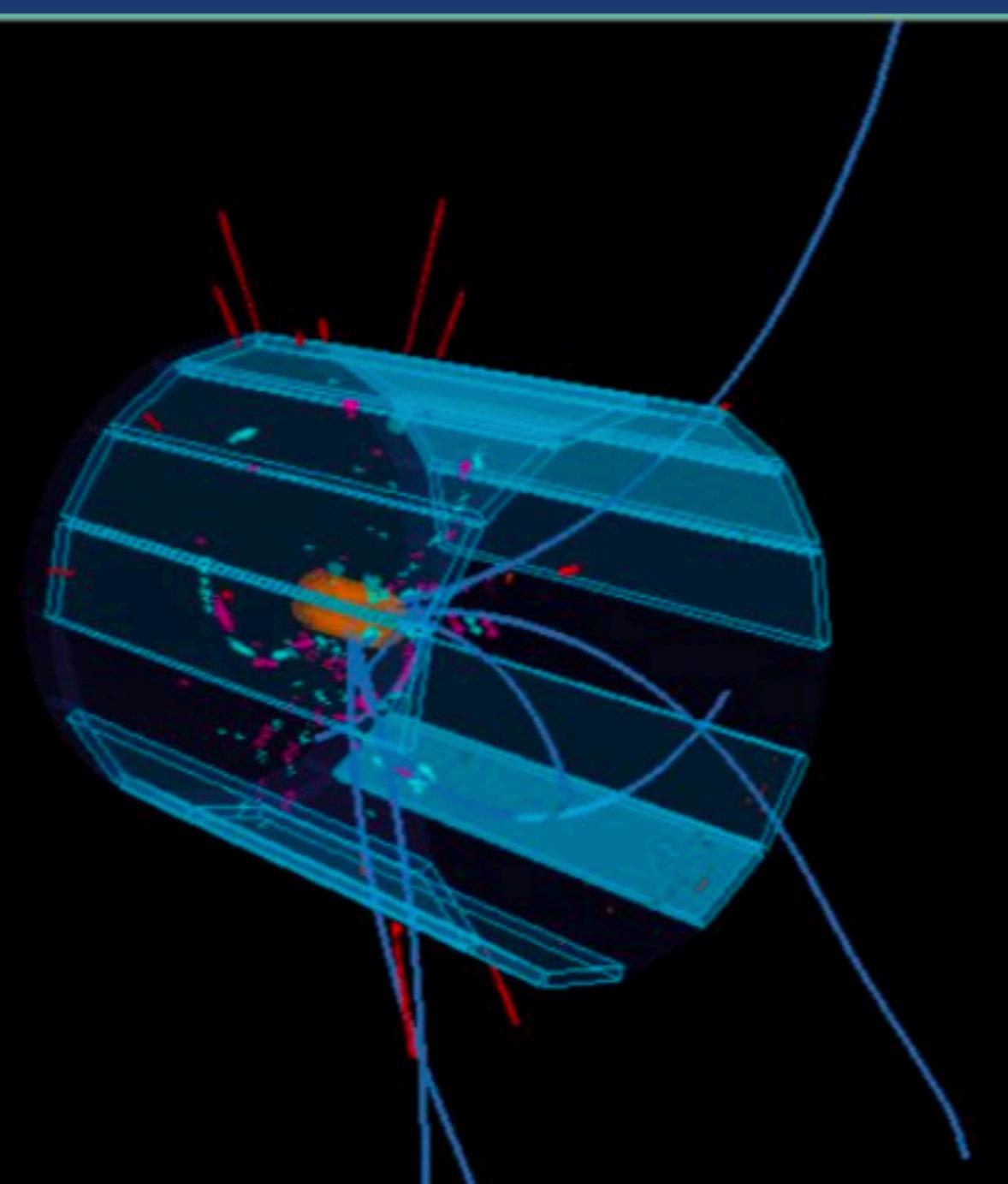
$\Upsilon(10753) \rightarrow B_s \bar{B}_s$ is small

Summary

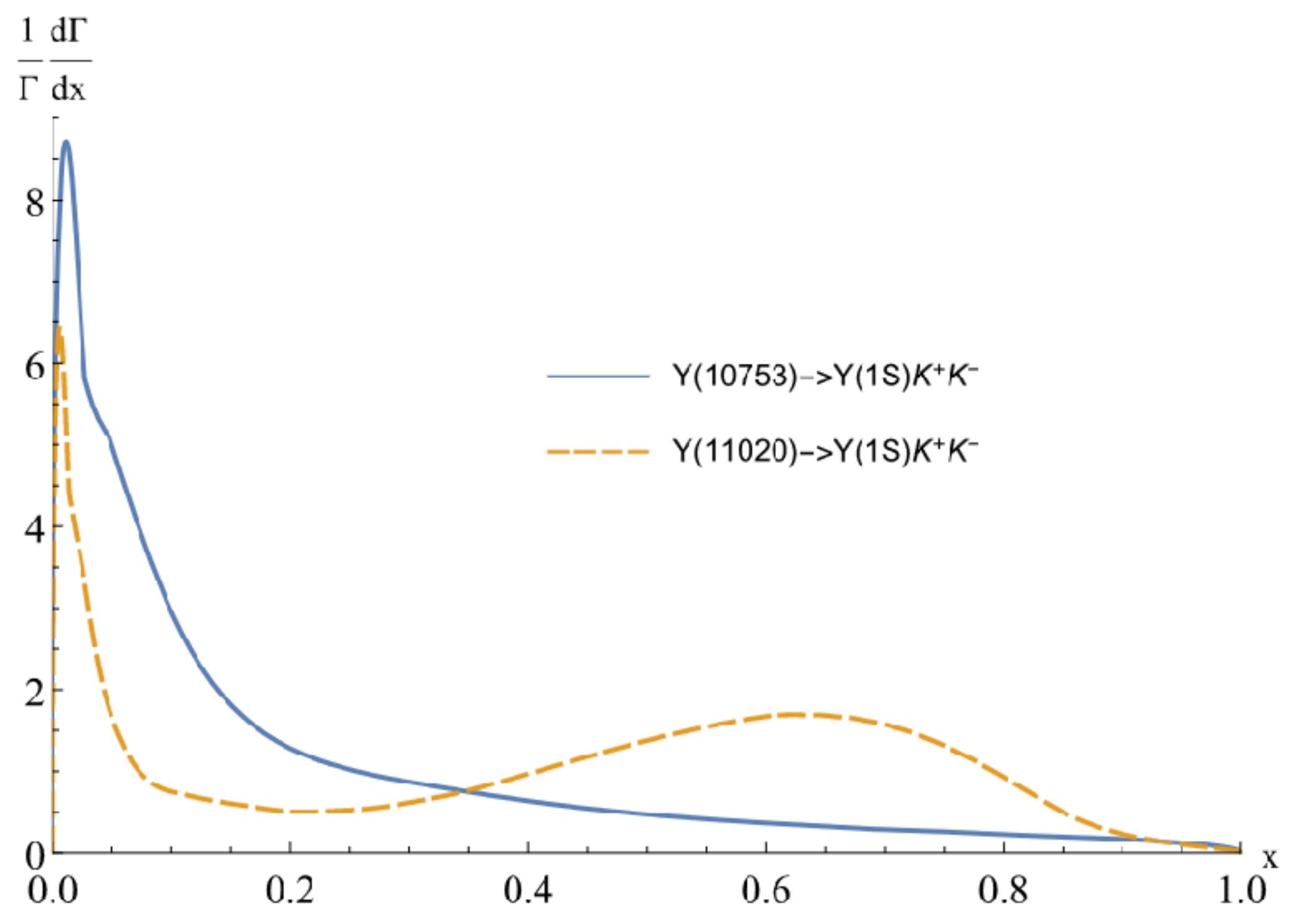
- Suggestive of a conventional bottomonium state
- More analyses are ongoing:
 - $\Upsilon(10753) \rightarrow K^+K^-\Upsilon(nS)$
 - $\Upsilon(10753) \rightarrow \eta(\eta')\Upsilon(nS)$
 - $\Upsilon(10753) \rightarrow \gamma\chi_{bJ}$
 - ...
- Up to 79% branching fraction is missing^[1]. Where are they?
- Belle II has collected 424/fb data, including ~380/fb $\Upsilon(4S)$.
 - More results other than $\Upsilon(10753)$ will come out.
- Long shutdown has finished, is accumulating more data.
 - More data, more new results



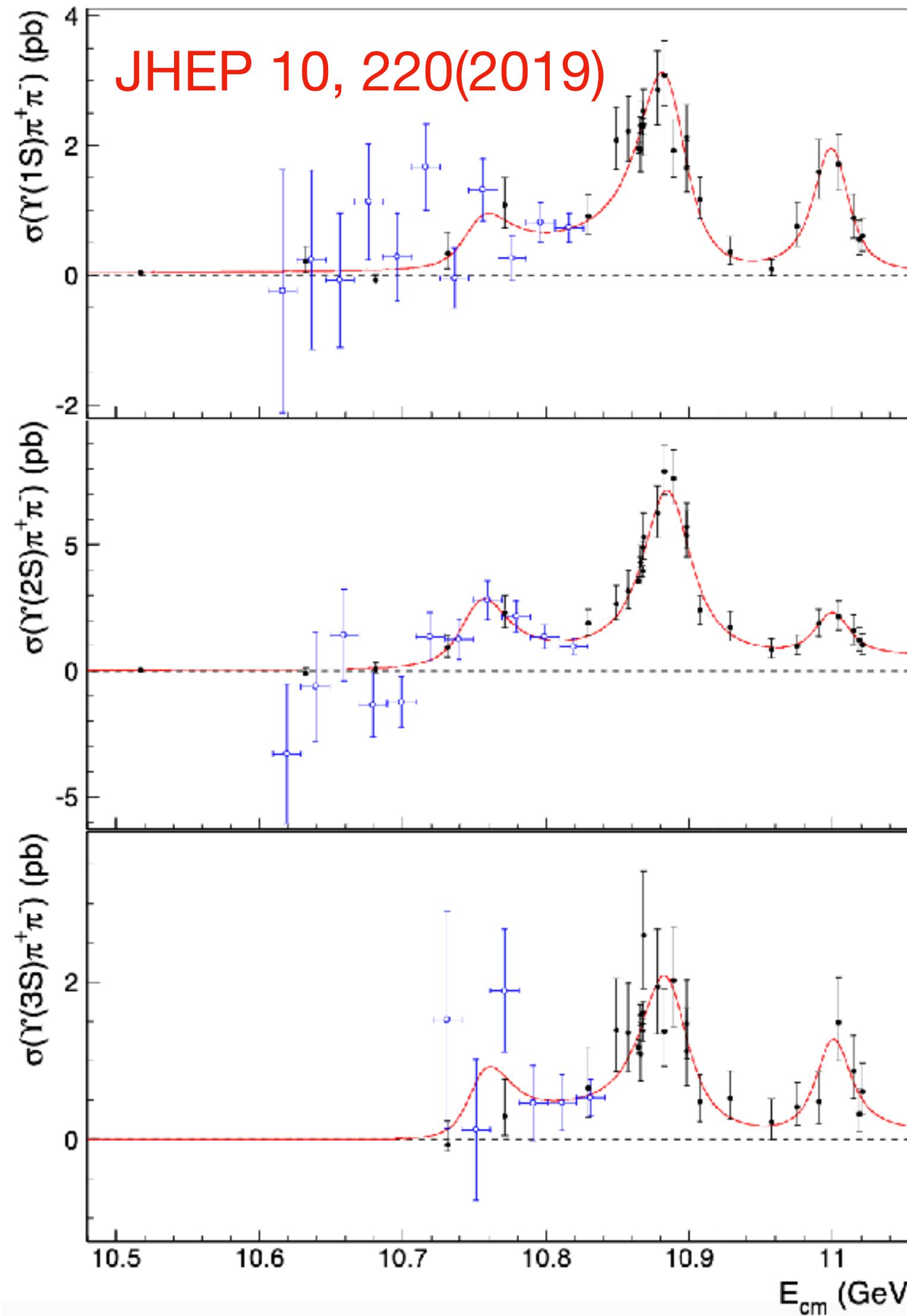
[1]Phys.Rev.D 106 (2022) 9, 094013



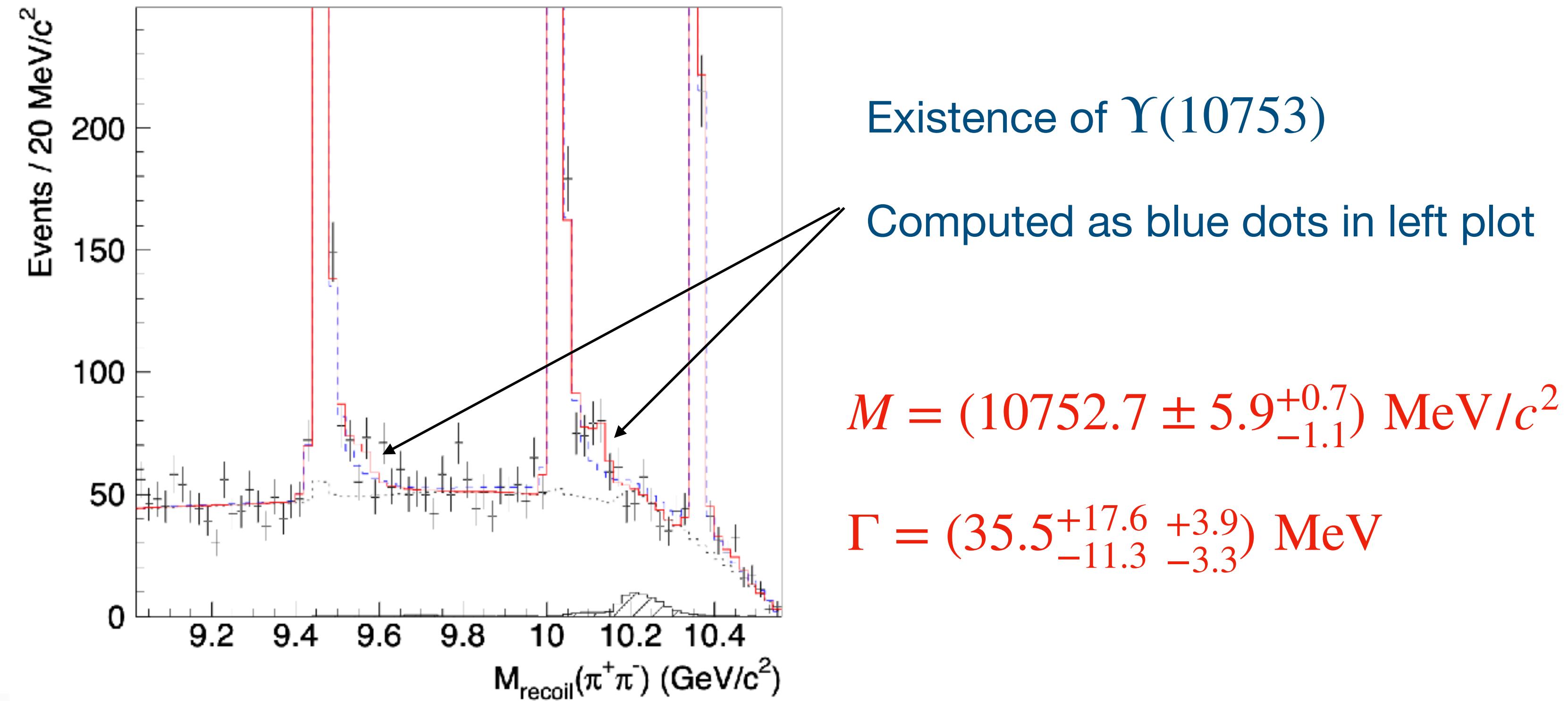
BACK UP

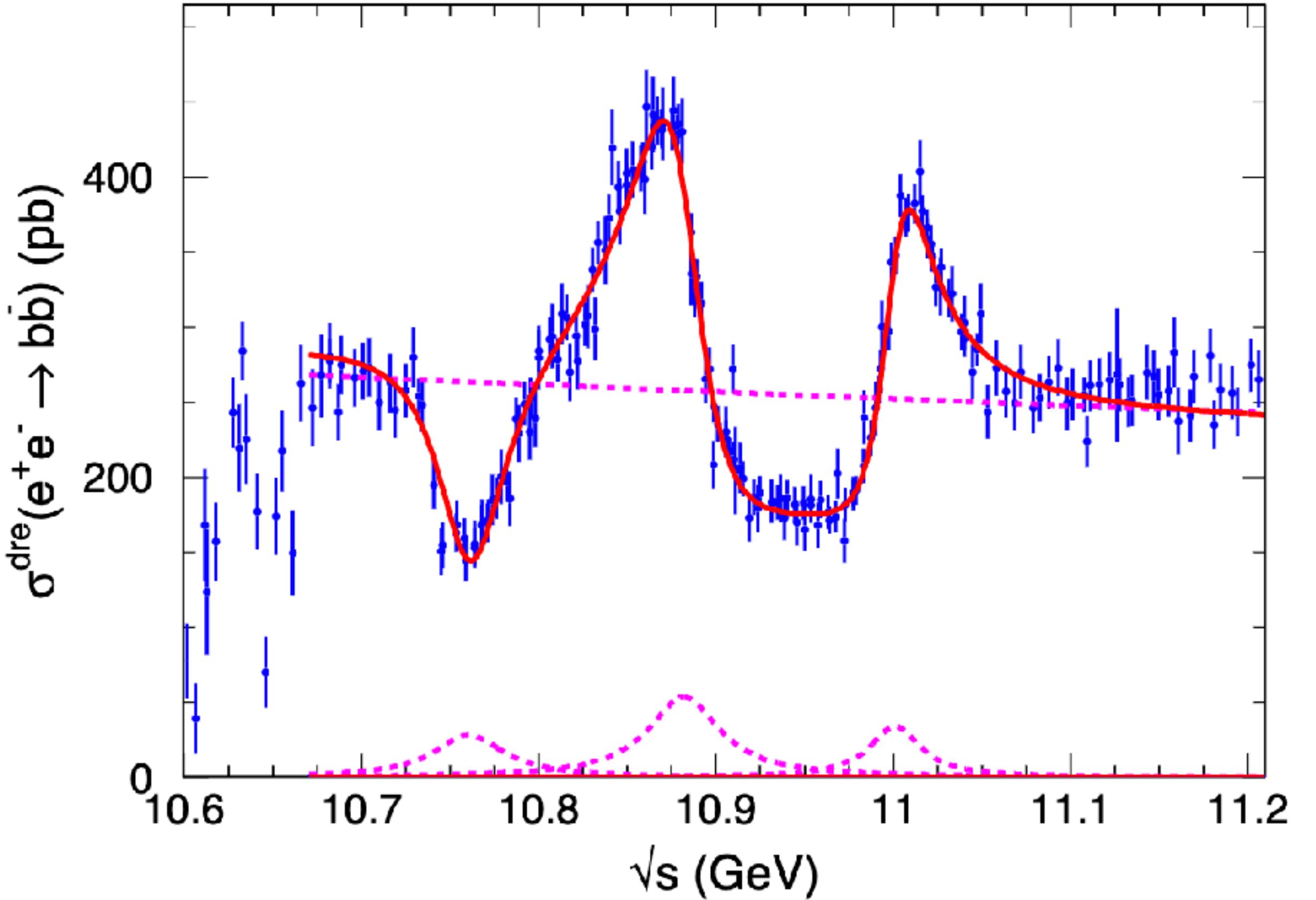
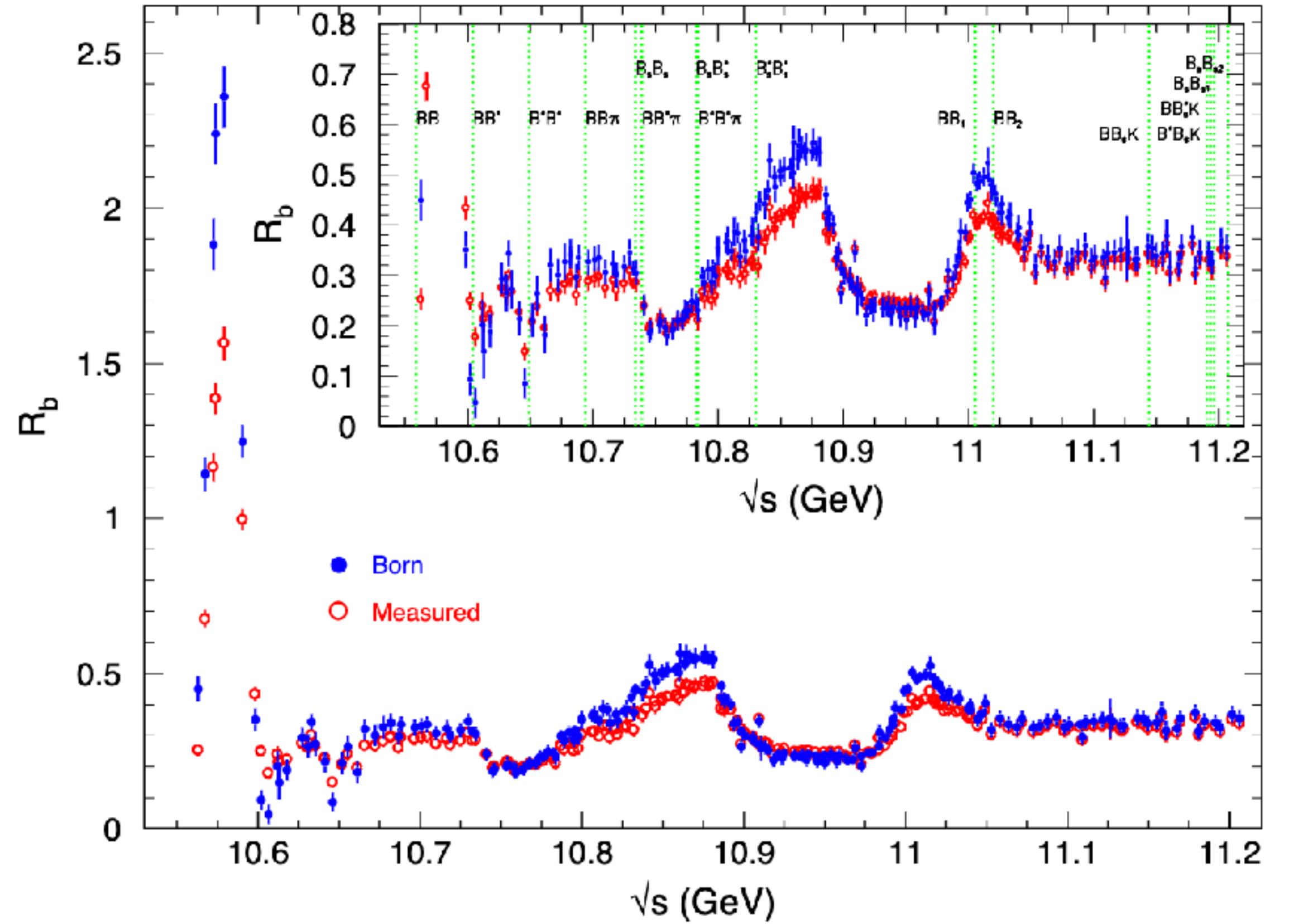


$\Upsilon(10753)$ – discovery and studies



- The $\Upsilon(10753)$ was firstly observed in the process of $e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^- (n = 1,2,3)$ by Belle.
- Simultaneous fit to cross sections and $M_{\text{recoil}}(\pi\pi)$





- A dip in the R_b distribution near 10.75 GeV
- Fit to dressed cross section of $b\bar{b}$ with three BWs.

$$M = (10761 \pm 2) \text{ MeV}/c^2$$

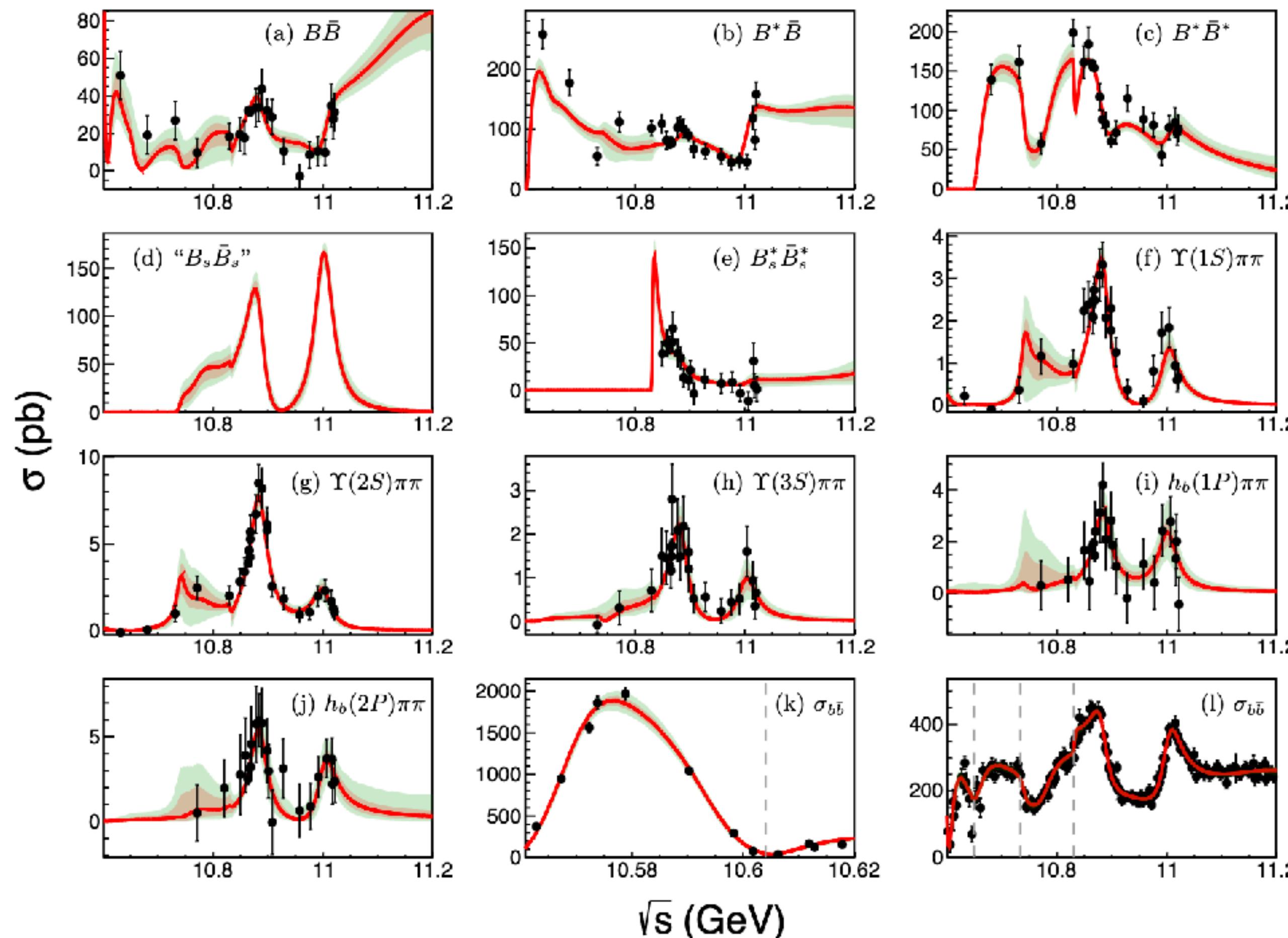
$$\Gamma = (48.5 \pm 3.0) \text{ MeV}$$

“The results from these fits may change dramatically by including more information on each exclusive mode.”

K-matrix Analysis of e^+e^- Annihilation in the Bottomonium Region

N. Hüsken,^{1,2} R.E. Mitchell,¹ and E.S. Swanson³

Phys.Rev.D 106 (2022) 9, 094013

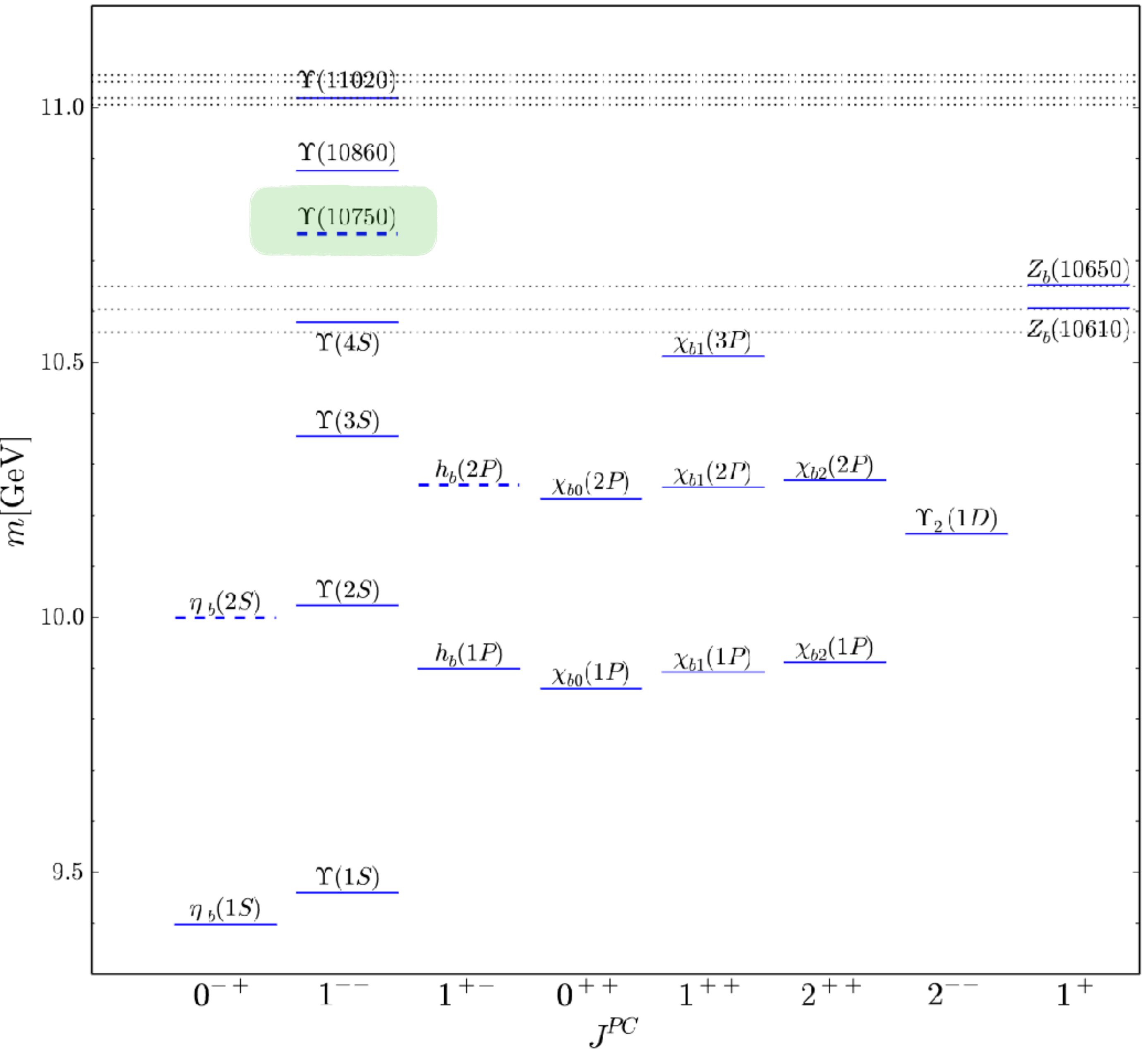


Strong evidence for $\Upsilon(10753)$ with significance $>10\sigma$

Pole locations varies with models.

state	RPP	our estimate	GM	ARM	NR	bbg	SOEF	LGT
1^3S_1	9460		9465	9444	9454	9445	9502	9419.1(4)
2^3S_1	10023		10003	10029	10010	10002	10015	9981(4)
3^3S_1	10355		10354	10374	10344	10339	10349	10384(12)
4^3S_1	10579 (10590 - 10610)		10635	10641	10614	10610	10607	
5^3S_1	10885 (10878 - 10884)		10878	10865	10849	10848	10818	
6^3S_1	11000 (11000 - 11008)		11102	11065	11064	11064	10995	
1^3D_1			10138	10156	10146	10148	10117	10191(9)
2^3D_1			10441	10453	10432	10435	10414	10718(33)
3^3D_1			10698	10697	10679	10684	10653	
$\Upsilon(10750)$	10753 (10630 - 10780)							
hybrid							11093	10952(33)

TABLE IV. Experimental and Theoretical Vector Bottomonium Masses (MeV).



Bottomonium?

Phys. Rev. D 101, 014020 (2020)

Phys. Lett. B 803, 135340 (2020)

Eur. Phys. J. C 80, 59 (2020)

Phys. Rev. D 102, 014036 (2020)

Prog. Part. Nucl. Phys. 117, 103845 (2021)

Phys. Rev. D 104, 034036 (2021)

Phys. Rev. D 105, 074007 (2022)

etc...

Hybrid?

Phys. Rept. 873, 1 (2020)

Phys. Rev. D 104, 034019 (2021)

etc...

Tetraquark?

Phys. Lett. B 802, 135217 (2020)

Chin. Phys. C 43, 123102 (2019)

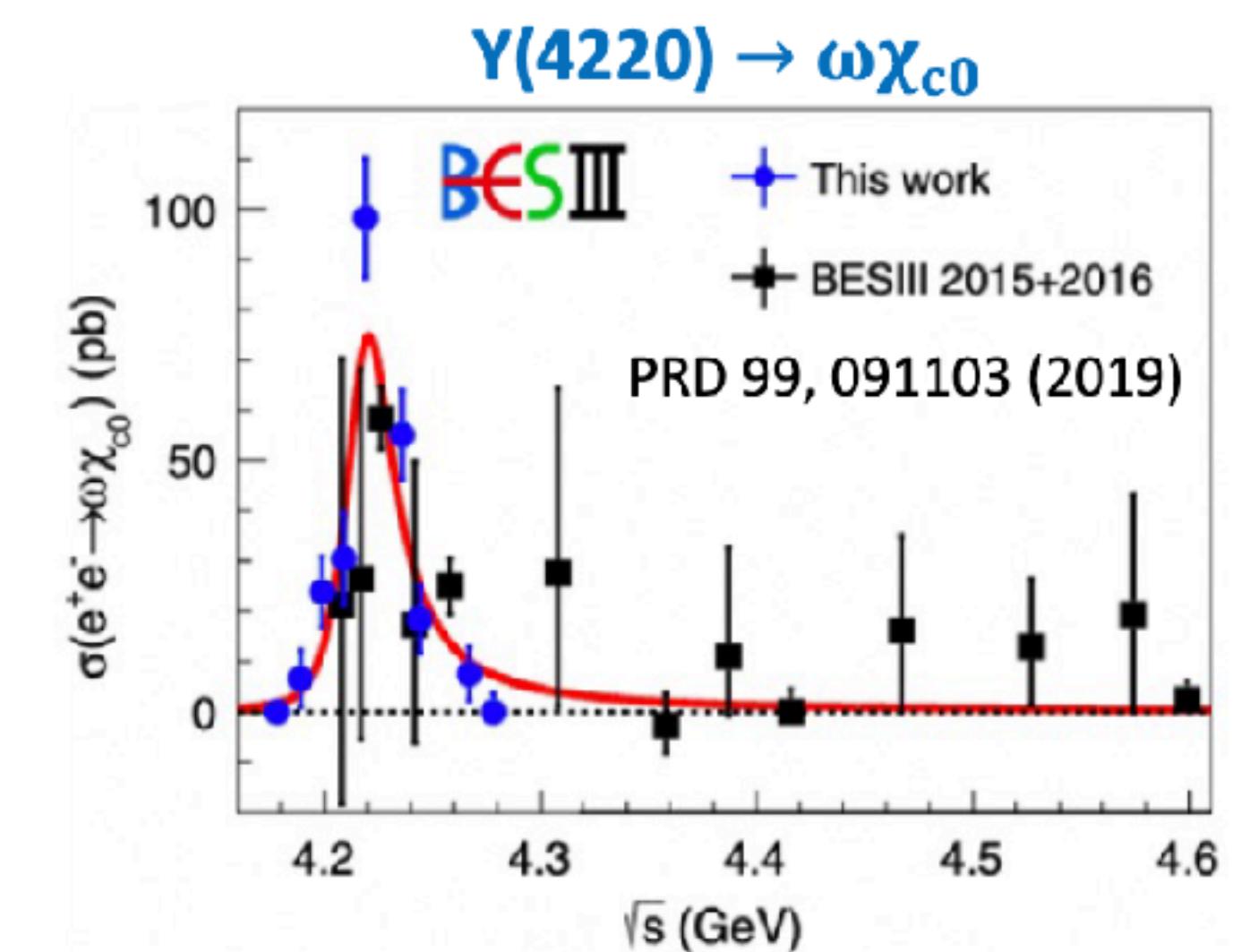
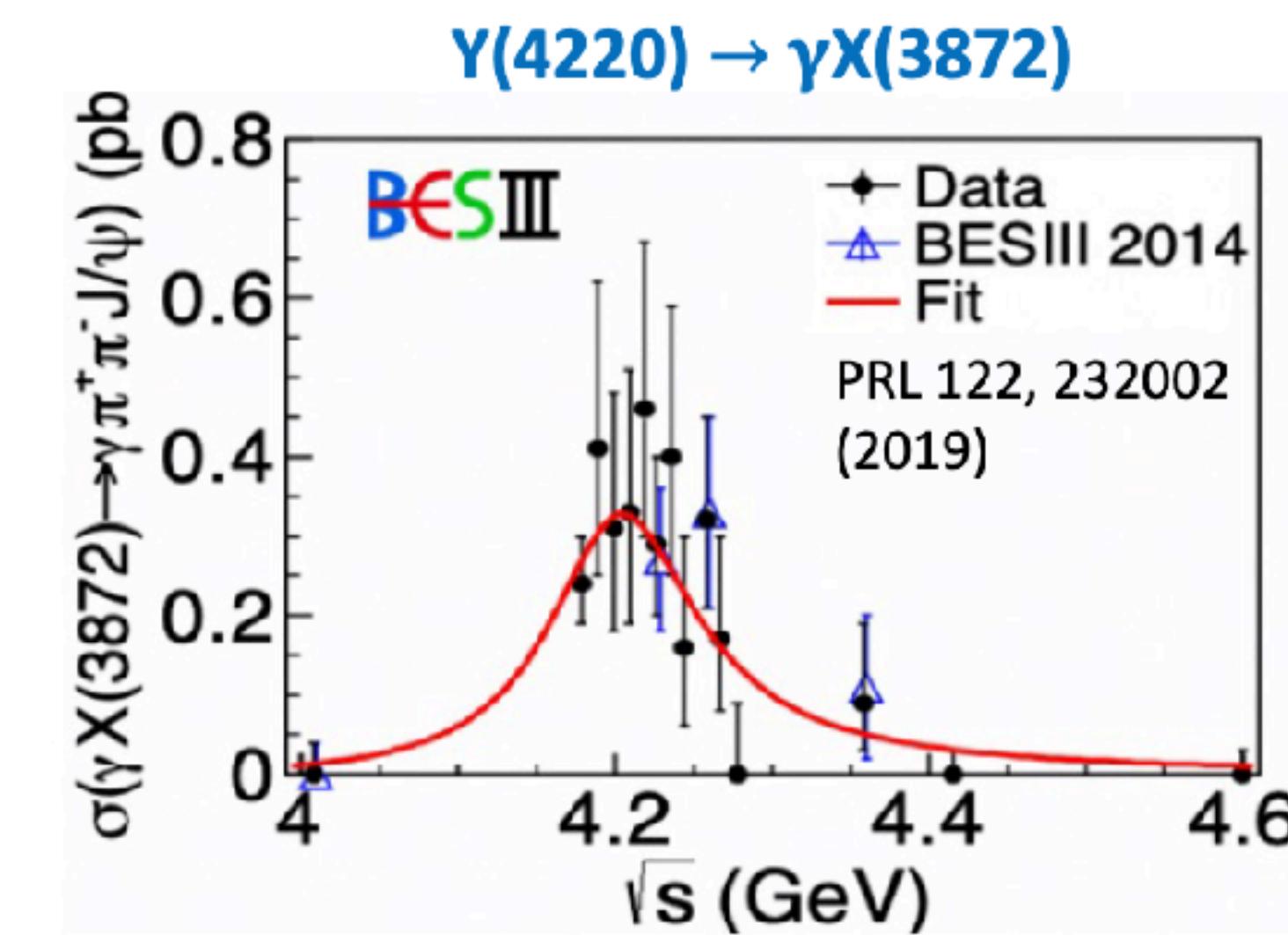
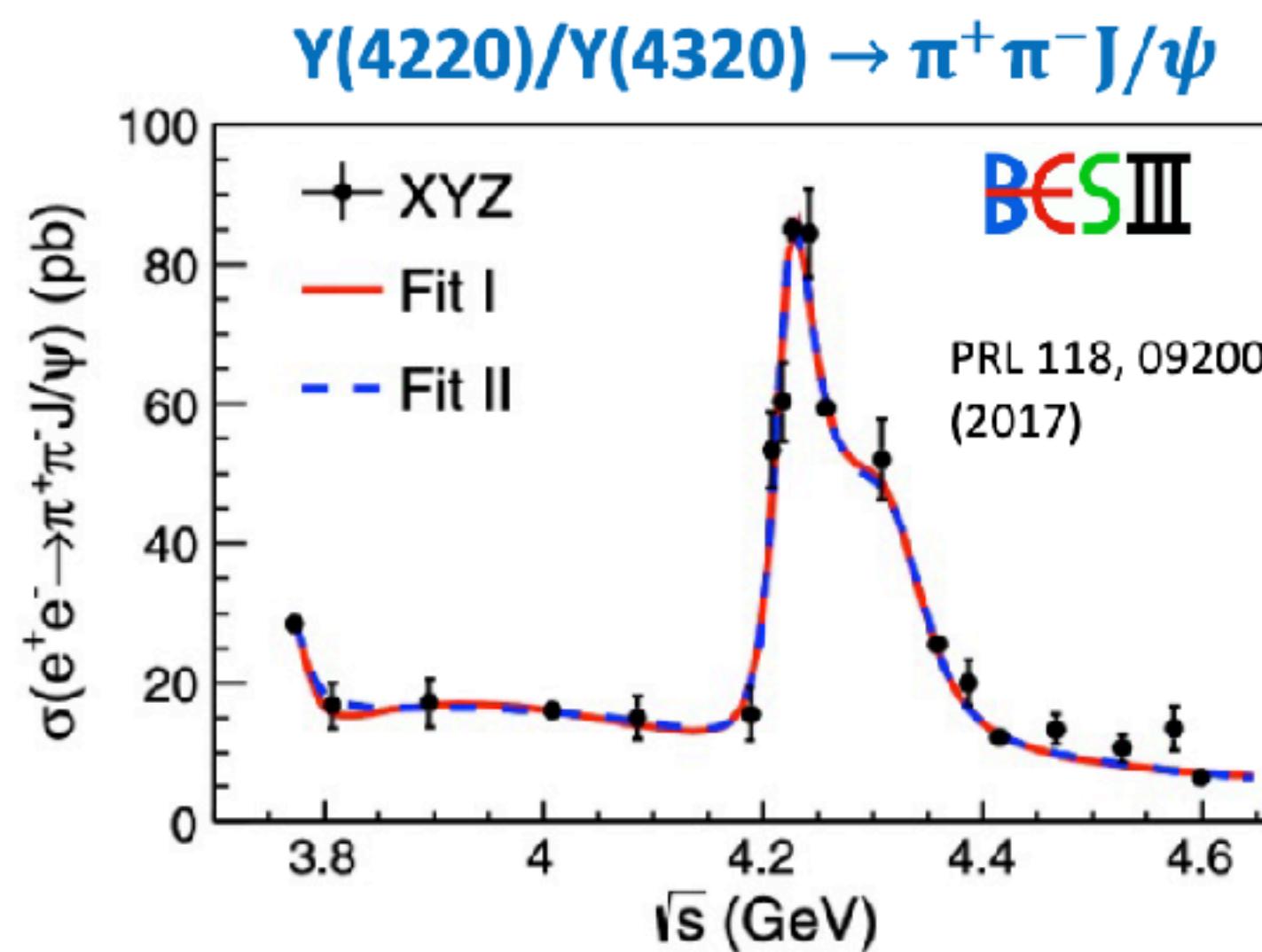
Phys. Rev. D 103, 074507 (2021)

Phys. Rev. D 107, 094515 (2023)

etc...

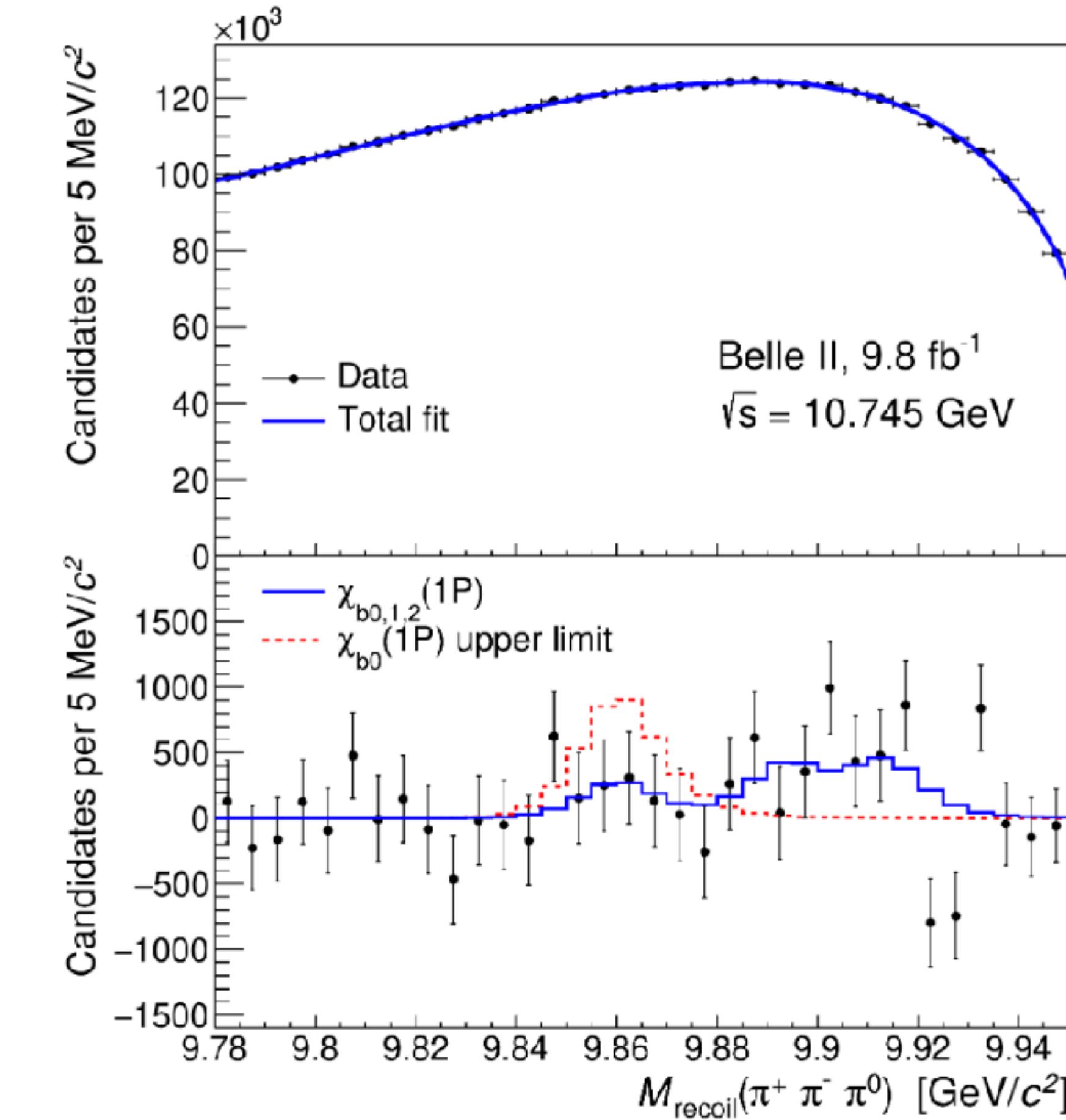
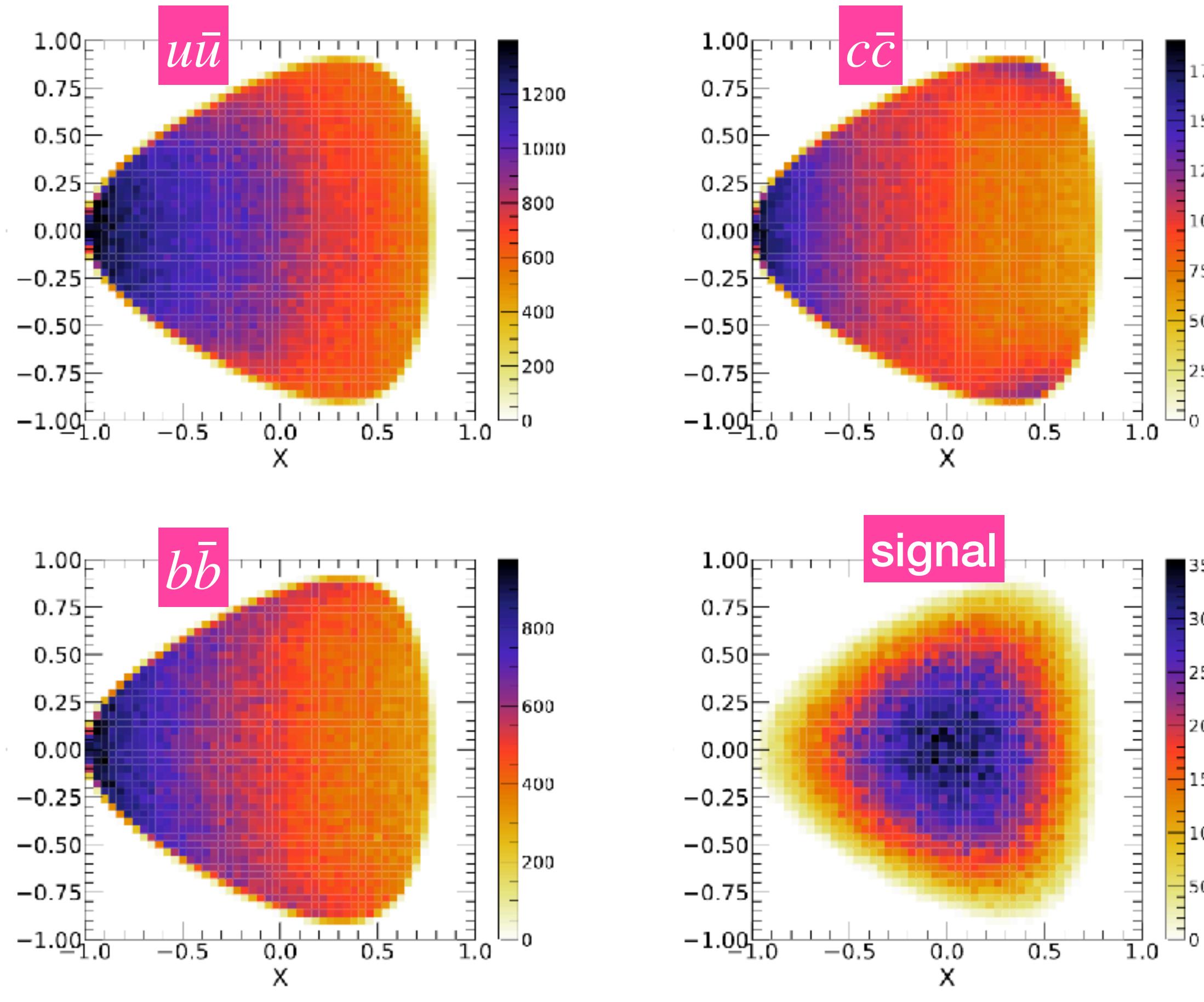


Two close peaks observed in the cross sections for $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ by BESIII and $e^+e^- \rightarrow \pi^+\pi^-\Upsilon(nS)$ by Belle. May suggest similar nature.



- $\Upsilon(4230) \rightarrow \gamma X(3872)$ and $\Upsilon(4230) \rightarrow \omega\chi_{c0}$ were observed by BESIII.
 - Expect the $\Upsilon(10753)$ state to decay into $X_b\gamma$.
 - Should be more easily to be found in $\omega\Upsilon(1S)$ than $\pi\pi\Upsilon(1S)$ [Eur.Phys.J.C 74 (2014) 9, 3063]

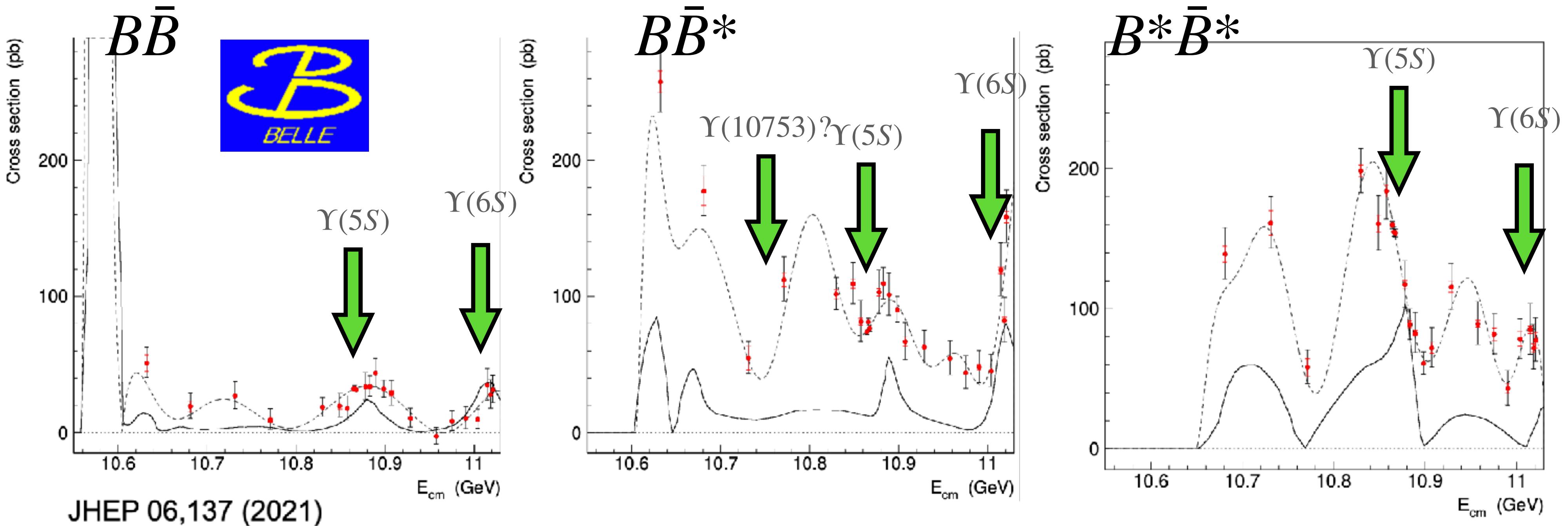
Suppress background with ω -Dalitz plot.



Signal yields: $(1.2 \pm 1.4 \pm 0.9) \times 10^3 \Rightarrow \sigma_{\text{Born}} = (2.6 \pm 3.1 \pm 2.0) \text{ pb}$

$\sigma_{\text{Born}}^{\text{up}} < 8.7 \text{ pb}$, comparable to the UL obtained before (11.3 pb)

Measurement of $e^+e^- \rightarrow B^{(*)}\bar{B}^{(*)}$



- Coupled channel analysis of high energy scan data using the K-matrix formalism shows four poles: $\Upsilon(4S)$, $\Upsilon(10753)$, $\Upsilon(5S)$, $\Upsilon(6S)$.
- Need more data to fill the gaps.

$\Upsilon(10753) \rightarrow \omega \chi_{bJ}$

$\Upsilon(10750) \rightarrow \omega \chi_b$ in the conventional quarkonium model (S-D mixing state)

[Y.S. Li, et al., PRD 104, 034036 (2021)]

$$\mathcal{B}[\Upsilon(10753) \rightarrow \chi_{b0}\omega] = (0.73\text{--}6.94) \times 10^{-3},$$

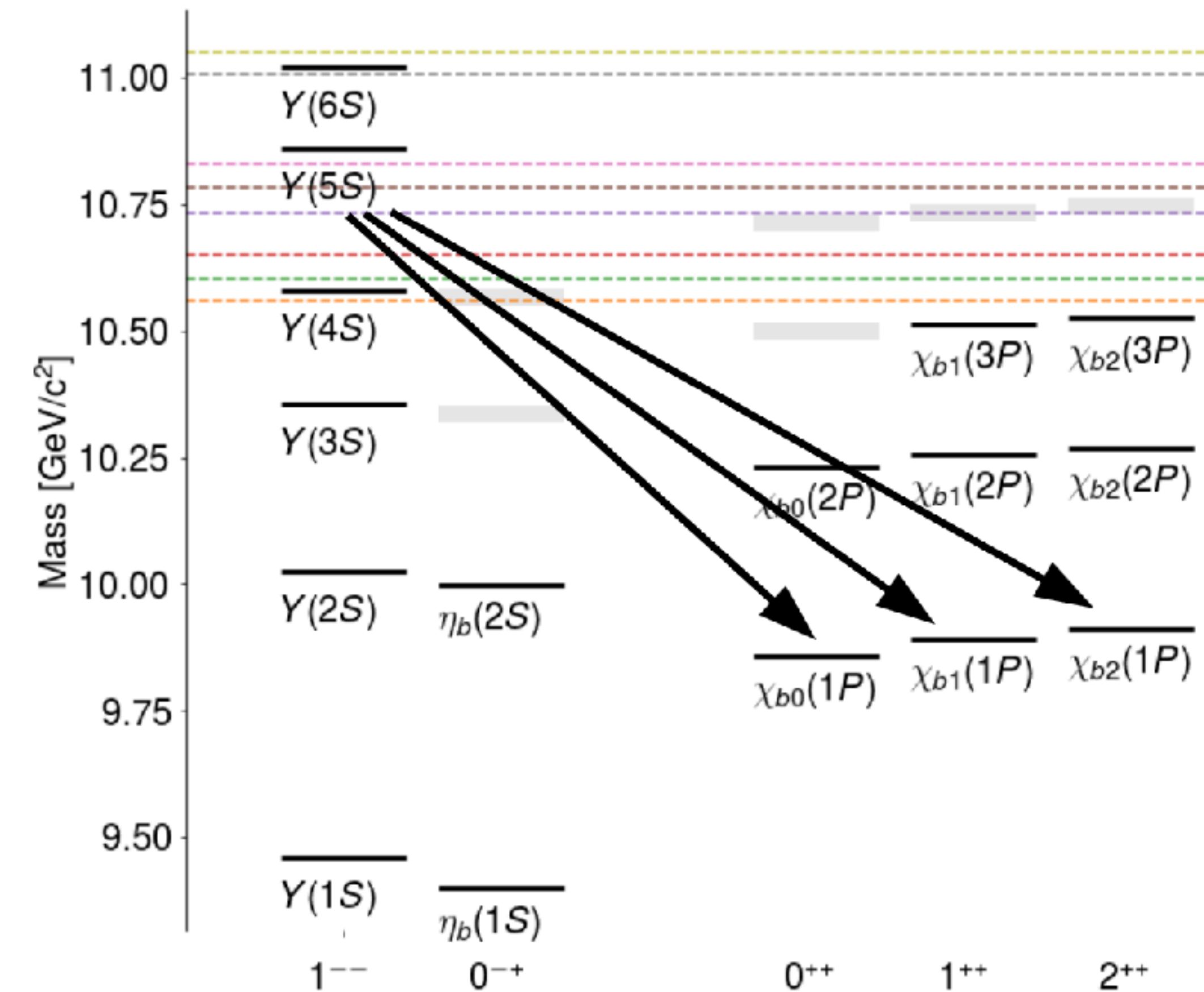
$$\mathcal{B}[\Upsilon(10753) \rightarrow \chi_{b1}\omega] = (0.25\text{--}2.16) \times 10^{-3},$$

$$\mathcal{B}[\Upsilon(10753) \rightarrow \chi_{b2}\omega] = (1.08\text{--}11.5) \times 10^{-3}.$$

$$R_{12} = \frac{\mathcal{B}[\Upsilon(10753) \rightarrow \chi_{b1}\omega]}{\mathcal{B}[\Upsilon(10753) \rightarrow \chi_{b2}\omega]} = (0.18\text{--}0.22)$$

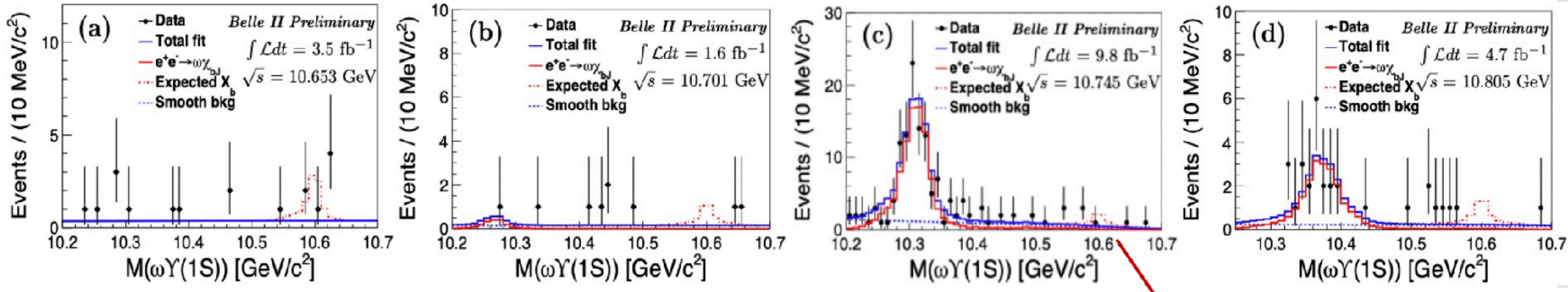
$$R_{02} = \frac{\mathcal{B}[\Upsilon(10753) \rightarrow \chi_{b0}\omega]}{\mathcal{B}[\Upsilon(10753) \rightarrow \chi_{b2}\omega]} = (0.55\text{--}0.63)$$

Sizable branching fractions



Search for $X_b \rightarrow \omega\Upsilon(1S)$ in $e^+e^- \rightarrow \gamma\omega\Upsilon(1S)$

[PRL 130, 091902 (2023)]



- No significant X_b signal is observed.
- The peaks are the reflections of $e^+e^- \rightarrow \omega\chi_{bJ}$.

From simulated events with $m(X_b) = 10.6 \text{ GeV}/c^2$
The yield is fixed at the upper limit at 90% C.L.

Upper limits at 90% C.L. on $\sigma_B(e^+e^- \rightarrow \gamma X_b) \cdot$ $\mathcal{B}(X_b \rightarrow \omega\Upsilon(1S))$ (pb)	\sqrt{s} (GeV)	10.653	10.701	10.745	10.805
	$m(X_b) = 10.6 \text{ GeV}/c^2$	0.45	0.33	0.10	0.14
	$m(X_b) = (10.45, 10.65) \text{ GeV}/c^2$	(0.14, 0.54)	(0.25, 0.84)	(0.06, 0.14)	(0.08, 0.36)