

QUARK MODEL WITH HIDDEN LOCAL SYMMETRY AND ITS APPLICATION TO THE HADRON SPECTRUM

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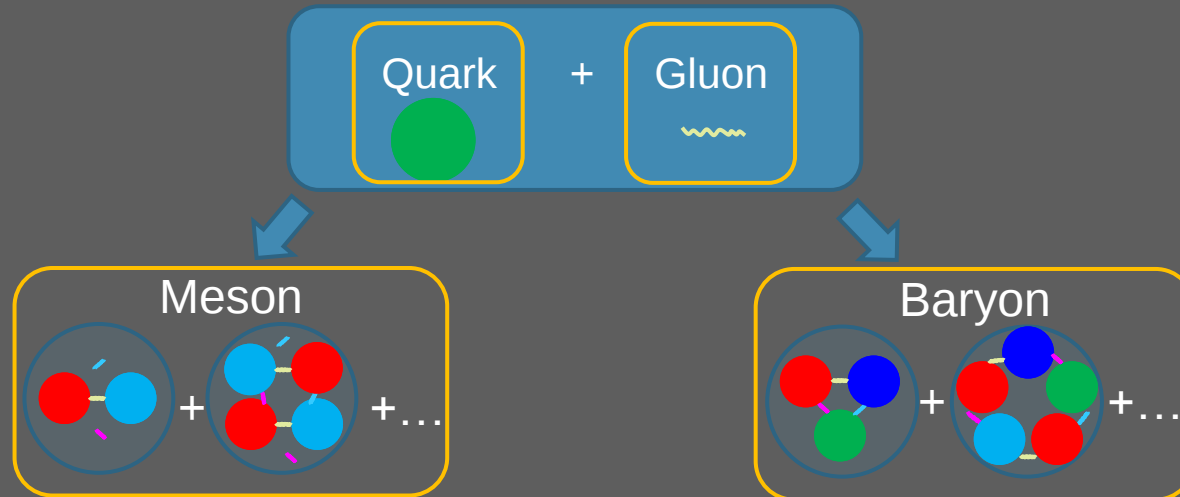
Outline

➤ Introduction

- ⊙ Chiral quark model with HLS
- ⊙ $SU2$ ground states + excited states
- ⊙ $SU3$ ground states
- ⊙ Future works

Introduction

Hadron are made by quarks and gluons



The dynamics of quarks and gluons are described by Quantum chromodynamics (QCD)

- QCD have two important features:
 - ◆ Color confinement
 - ◆ Asymptotic freedom
- In low energy region the perturbative calculation for QCD is impossible, alternatively:
 - ◆ Lattice QCD (non-perturbative calculation)
 - ◆ Effective models (chiral perturbation theory, quark model, etc...)

Meson Summary Table

See also the table of suggested $q\bar{q}$ quark model assignments in the Quark Model section.
 • Indicates particles that appear in the preceding Meson Summary Table. We do not regard the other entries as being established.

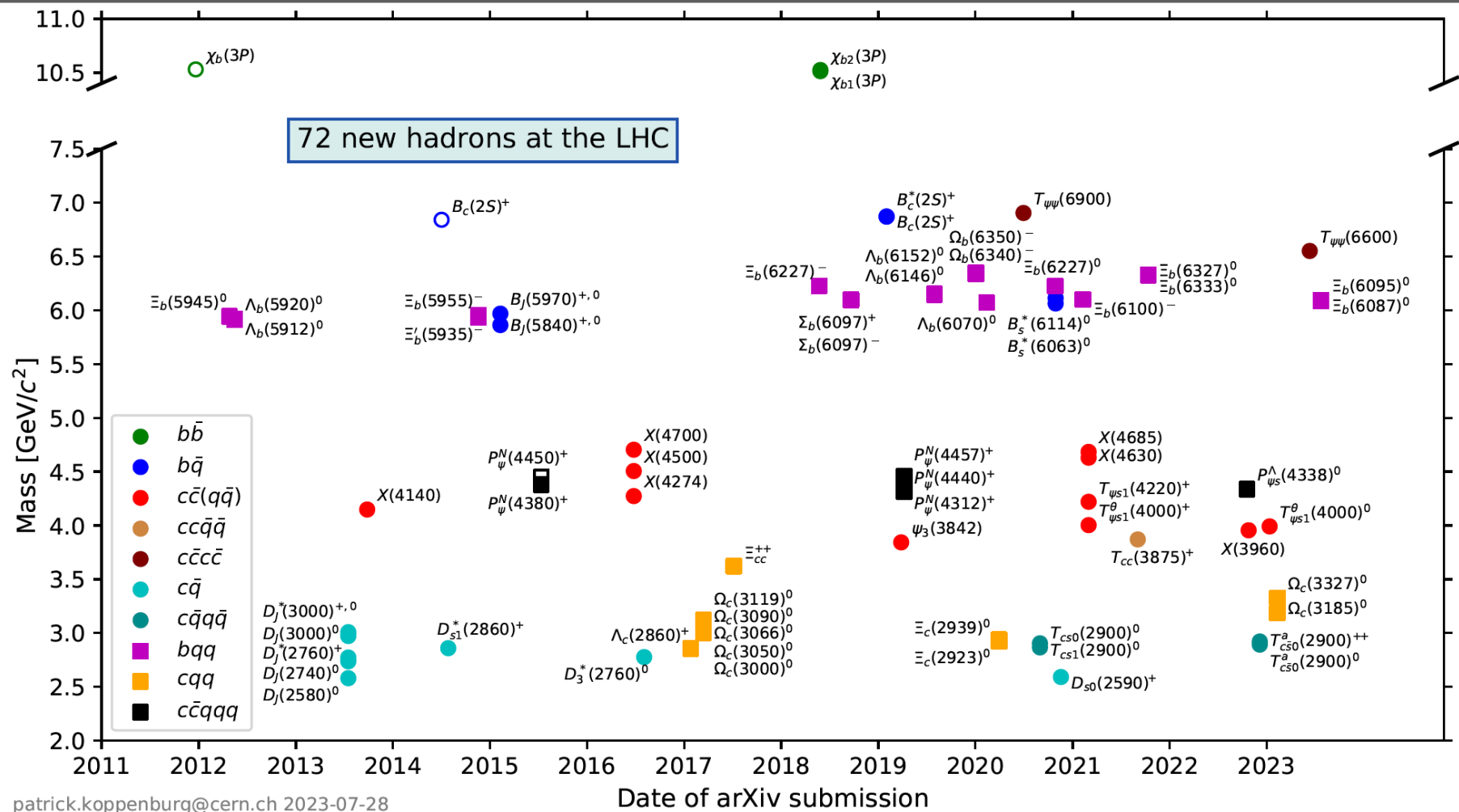
LIGHT UNFLAVORED ($S = C = B = 0$)		STRANGE ($S = \pm 1, C = B = 0$)	CHARMED, STRANGE ($C = \pm 1, S = \pm 1$) (+ possibly non- $q\bar{q}$ states)	$c\bar{c}$ continued $f^0(j^PC)$
$f^0(j^PC)$	$f^0(j^PC)$	$f^0(j^PC)$	$f^0(j^PC)$	$f^0(j^PC)$
$\pi^\pm$ $1^-(0^-)$ π^0 $1^-(0^-)$ η $0^+(0^-)$ $\eta(500)$ $0^+(0^+)$ $\rho(770)$ $1^+(1^-)$ $\omega(782)$ $0^-(1^-)$ $\eta(958)$ $0^+(0^+)$ $f_0(980)$ $0^+(0^+)$ $a_0(980)$ $1^-(0^+)$ $\phi(1020)$ $0^-(1^-)$ $h_1(1170)$ $0^+(1^+)$ $b_1(1235)$ $1^+(1^-)$ $a_1(1260)$ $1^-(1^+)$ $f_2(1270)$ $0^+(2^+)$ $f_1(1285)$ $0^+(1^+)$ $\eta(1295)$ $0^+(0^+)$ $\pi(1300)$ $1^-(0^+)$ $a_2(1320)$ $1^-(2^+)$ $f_0(1370)$ $0^+(0^+)$ $\pi_1(1400)$ $1^-(1^-)$ $\eta(1405)$ $0^+(0^+)$ $h_1(1415)$ $0^-(1^+)$ $f_1(1420)$ $0^+(1^+)$ $\omega(1420)$ $0^-(1^-)$ $f_2(1430)$ $0^+(2^+)$ $a_0(1450)$ $1^-(0^+)$ $\rho(1450)$ $1^+(1^-)$ $\eta(1475)$ $0^+(0^+)$ $f_0(1500)$ $0^+(0^+)$ $f_1(1510)$ $0^+(1^+)$ $f_2^*(1525)$ $0^+(2^+)$ $f_2(1565)$ $0^+(2^+)$ $\rho(1570)$ $1^+(1^-)$ $h_1(1595)$ $0^-(1^-)$ $\pi_1(1600)$ $1^-(1^-)$ $a_1(1640)$ $1^-(1^+)$ $f_2(1640)$ $0^+(2^+)$ $\eta_2(1645)$ $0^+(2^+)$ $\omega(1650)$ $0^-(1^-)$ $\omega_2(1670)$ $0^-(3^-)$	$\pi_2(1670)$ $1^-(2^+)$ $\phi(1680)$ $0^-(1^-)$ $\rho_2(1690)$ $1^+(3^-)$ $\rho(1700)$ $1^+(1^-)$ $a_2(1700)$ $1^-(2^+)$ $f_2(1710)$ $0^+(0^+)$ $X(1750)$ $?^-(1^-)$ $\eta(1760)$ $0^+(0^+)$ $\pi(1800)$ $1^-(2^+)$ $f_2(1810)$ $0^+(2^+)$ $X(1835)$ $?^-(0^+)$ $\phi_2(1850)$ $0^-(3^-)$ $\eta_2(1870)$ $0^+(2^+)$ $\pi_2(1880)$ $1^-(2^+)$ $\rho(1900)$ $1^+(1^-)$ $f_2(1910)$ $0^+(2^+)$ $a_0(1950)$ $1^-(0^+)$ $f_2(1950)$ $0^+(2^+)$ $a_2(1970)$ $1^-(4^+)$ $\rho_2(1990)$ $1^+(3^-)$ $\pi_2(2005)$ $1^-(2^+)$ $f_2(2010)$ $0^+(2^+)$ $f_2(2020)$ $0^+(0^+)$ $f_4(2050)$ $0^+(4^+)$ $\pi_2(2100)$ $1^-(2^-)$ $f_2(2100)$ $0^+(0^+)$ $f_2(2100)$ $0^+(2^+)$ $\rho(2150)$ $1^+(1^-)$ $\phi(2170)$ $0^-(1^-)$ $f_2(2200)$ $0^+(0^+)$ $f_2(2220)$ $0^+(2^+)$ - or 4^+ $\eta(2225)$ $0^+(0^+)$ $\rho_2(2250)$ $1^+(3^-)$ $f_2(2300)$ $0^+(2^+)$ $f_2(2300)$ $0^+(4^+)$ $f_2(2330)$ $0^+(0^+)$ $f_2(2340)$ $0^+(2^+)$ $\rho_2(2350)$ $1^+(5^-)$ $X(2370)$ $?^-(??)$ $f_2(2510)$ $0^+(6^+)$	$K^\pm$ $1/2(0^-)$ K^0 $1/2(0^-)$ K_S^0 $1/2(0^-)$ K_L^0 $1/2(0^-)$ $K_S^*(700)$ $1/2(0^+)$ $K^*(892)$ $1/2(1^-)$ $K_1(1270)$ $1/2(1^+)$ $K_1(1400)$ $1/2(1^+)$ $K^*(1410)$ $1/2(1^-)$ $K_S^*(1430)$ $1/2(0^+)$ $K_S^*(1430)$ $1/2(2^+)$ $K_1(1460)$ $1/2(0^-)$ $K_2(1580)$ $1/2(2^-)$ $K(1630)$ $1/2(2^?)$ $K_1(1650)$ $1/2(1^+)$ $K^*(1680)$ $1/2(1^-)$ $K_S^*(1770)$ $1/2(2^-)$ $K_S^*(1780)$ $1/2(3^-)$ $K_2(1820)$ $1/2(2^-)$ $K(1830)$ $1/2(0^-)$ $K_S^*(1950)$ $1/2(0^+)$ $K_S^*(1980)$ $1/2(2^+)$ $K_S^*(2045)$ $1/2(4^+)$ $K_2(2250)$ $1/2(2^-)$ $K_2(2320)$ $1/2(3^+)$ $K_S^*(2380)$ $1/2(5^-)$ $K_2(2500)$ $1/2(4^-)$ $K(3100)$ $?^-(??)$	$D^\pm$ $1/2(0^-)$ D^0 $1/2(0^-)$ $D^*(2007)^0$ $1/2(1^-)$ $D^*(2010)^\pm$ $1/2(1^-)$ $D_S^*(2300)$ $1/2(0^+)$ $D_S^*(2420)$ $1/2(1^+)$ $D_1(2430)^0$ $1/2(1^+)$ $D_S^*(2460)$ $1/2(2^+)$ $D_0(2550)^0$ $1/2(0^-)$ $D_S^*(2600)^0$ $1/2(1^-)$ $D^*(2640)^\pm$ $1/2(2^?)$ $D_2(2740)^0$ $1/2(2^-)$ $D_S^*(2750)$ $1/2(3^-)$ $D_S^*(2760)^0$ $1/2(1^-)$ $D(3000)^0$ $1/2(2^?)$	$\psi_2(3823)$ $0^-(2^-)$ $\psi_2(3842)$ $0^-(3^-)$ $\chi_{c0}(3860)$ $0^+(0^+)$ $\chi_{c1}(3872)$ $0^+(1^+)$ $Z_c(3900)$ $1^+(1^+)$ $\chi_{c0}(3915)$ $0^+(0^+)$ $\chi_{c2}(3930)$ $0^+(2^+)$ $X(3940)$ $?^-(??)$ $X(4020)^\pm$ $1^+(?^-)$ $X(4040)$ $0^-(1^-)$ $X(4050)^\pm$ $1^-(?^-)$ $X(4055)^\pm$ $1^+(?^-)$ $X(4100)^\pm$ $1^-(?^-)$ $\chi_{c1}(4140)$ $0^+(1^+)$ $\psi(4160)$ $0^-(1^-)$ $X(4160)$ $?^-(??)$ $Z_c(4200)$ $1^+(1^+)$ $\psi(4230)$ $0^-(1^-)$ $R_{c0}(4240)$ $1^+(0^-)$ $X(4250)^\pm$ $1^-(?^-)$ $\chi_{c1}(4274)$ $0^+(1^+)$ $X(4350)$ $0^+(?^+)$ $\psi(4360)$ $0^-(1^-)$ $\psi(4415)$ $0^-(1^-)$ $Z_c(4430)$ $1^+(1^+)$ $\chi_{c0}(4500)$ $0^+(0^+)$ $X(4630)$ $0^+(?^+)$ $\psi(4660)$ $0^-(1^-)$ $\chi_{c1}(4685)$ $0^+(1^+)$ $\chi_{c0}(4700)$ $0^+(0^+)$
		BOT TOM ($B = \pm 1$)		$b\bar{b}$ (+ possibly non- $q\bar{q}$ states)
		$B^\pm$ $1/2(0^-)$ B^0 $1/2(0^-)$ $B^\pm/B^0$ ADMIXTURE $B^\pm/B^0/B_S^\pm/B$ baryon ADMIXTURE V_{bb} and V_{bb} CKM Matrix Elements B^* $1/2(1^-)$ $B_1(5721)$ $1/2(1^+)$ $B_2^*(5732)$ $?^-(?)$ $B_3^*(5747)$ $1/2(2^+)$ $B_J(5840)$ $1/2(2^?)$ $B_J(5970)$ $1/2(2^?)$		$\eta_b(1S)$ $0^+(0^-)$ $\Upsilon(1S)$ $0^-(1^-)$ $\chi_{b0}(1P)$ $0^+(0^+)$ $\chi_{b1}(1P)$ $0^+(1^+)$ $h_b(1P)$ $0^-(1^+)$ $\chi_{b2}(1P)$ $0^+(2^+)$ $\eta_b(2S)$ $0^+(0^-)$ $\Upsilon(2S)$ $0^-(1^-)$ $\Upsilon_2(1D)$ $0^-(2^-)$ $\chi_{b0}(2P)$ $0^+(0^+)$ $\chi_{b1}(2P)$ $0^+(1^+)$ $h_b(2P)$ $0^-(1^+)$ $\chi_{b2}(2P)$ $0^+(2^+)$ $\Upsilon(3S)$ $0^-(1^-)$ $\chi_{b1}(3P)$ $0^+(1^+)$ $\chi_{b2}(3P)$ $0^+(2^+)$ $\Upsilon(4S)$ $0^-(1^-)$ $Z_b(10610)$ $1^+(1^+)$ $Z_b(10650)$ $1^+(1^+)$ $\Upsilon(10753)$ $?^-(1^-)$ $\Upsilon(10860)$ $0^-(1^-)$ $\Upsilon(11020)$ $0^-(1^-)$
		BOT TOM, CHARMED ($B = C = \pm 1$)		
		$B_c^\pm$ $0(0^-)$ $B_c(2S)^\pm$ $0(0^-)$		
		$c\bar{c}$ (+ possibly non- $q\bar{q}$ states)		
		$\eta_c(1S)$ $0^+(0^-)$ $J/\psi(1S)$ $0^-(1^-)$ $\chi_{c0}(1P)$ $0^+(0^+)$ $\chi_{c1}(1P)$ $0^+(1^+)$ $h_c(1P)$ $0^-(1^+)$ $\chi_{c2}(1P)$ $0^+(2^+)$ $\eta_c(2S)$ $0^+(0^-)$ $\psi(2S)$ $0^-(1^-)$ $\psi(3770)$ $0^-(1^-)$		
		OTHER		
		Further States		

Baryon Summary Table

This short table gives the name, the quantum numbers (where known), and the status of baryons in the Review. Only the baryons with 3- or 4- star status are included in the Baryon Summary Table. Due to insufficient data or uncertain interpretation, the other entries in the table are not established baryons. The names with masses are of baryons that decay strongly. The spin parity J^P (when known) is given with each particle. For the strongly decaying particles, the J^P values are considered to be part of the names.

p	$1/2^+$	****	$\Delta(1232)$	$3/2^+$	****	Σ^+	$1/2^+$	****	Λ_c^+	$1/2^+$	****	Λ_b^0	$1/2^+$	***
n	$1/2^+$	****	$\Delta(1600)$	$3/2^+$	****	Σ^0	$1/2^+$	****	$\Lambda_c(2595)^+$	$1/2^-$	***	$\Lambda_b(5912)^0$	$1/2^-$	***
$N(1440)$	$1/2^+$	****	$\Delta(1620)$	$1/2^-$	****	Σ^-	$1/2^+$	****	$\Lambda_c(2625)^+$	$3/2^-$	***	$\Lambda_b(5920)^0$	$3/2^-$	***
$N(1520)$	$3/2^-$	****	$\Delta(1700)$	$3/2^-$	****	$\Sigma(1385)$	$3/2^+$	****	$\Lambda_c(2765)^+$	*		$\Lambda_b(6070)^0$	$1/2^+$	***
$N(1535)$	$1/2^-$	****	$\Delta(1750)$	$1/2^+$	*	$\Sigma(1580)$	$3/2^-$	*	$\Lambda_c(2860)^+$	$3/2^+$	***	$\Lambda_b(6146)^0$	$3/2^+$	***
$N(1650)$	$1/2^-$	****	$\Delta(1900)$	$1/2^-$	*	$\Sigma(1620)$	$1/2^-$	*	$\Lambda_c(2880)^+$	$5/2^+$	***	$\Lambda_b(6152)^0$	$5/2^+$	***
$N(1675)$	$5/2^-$	****	$\Delta(1905)$	$5/2^+$	****	$\Sigma(1660)$	$1/2^+$	***	$\Lambda_c(2940)^+$	$3/2^-$	***	Σ_b	$1/2^+$	***
$N(1680)$	$5/2^+$	****	$\Delta(1910)$	$1/2^+$	****	$\Sigma(1670)$	$3/2^-$	****	$\Sigma_c(2455)$	$1/2^+$	****	Σ_b^*	$3/2^+$	****
$N(1700)$	$3/2^-$	***	$\Delta(1920)$	$3/2^+$	****	$\Sigma(1750)$	$1/2^-$	****	$\Sigma_c(2520)$	$3/2^+$	***	$\Sigma_b(6097)^+$		***
$N(1710)$	$1/2^+$	****	$\Delta(1930)$	$5/2^-$	***	$\Sigma(1775)$	$5/2^-$	****	$\Sigma_c(2800)$		***	$\Sigma_b(6097)^-$		***
$N(1720)$	$3/2^+$	****	$\Delta(1940)$	$3/2^-$	**	$\Sigma(1780)$	$3/2^+$	*	Ξ_c^+	$1/2^+$	***	Ξ_b^0	$1/2^+$	***
$N(1860)$	$5/2^+$	**	$\Delta(1950)$	$7/2^+$	****	$\Sigma(1880)$	$1/2^+$	**	Ξ_c^0	$1/2^+$	****	Ξ_b^+	$1/2^+$	***
$N(1875)$	$3/2^-$	***	$\Delta(2000)$	$5/2^+$	**	$\Sigma(1900)$	$1/2^-$	**	Ξ_c^+	$1/2^+$	****	$\Xi_b^0(5935)^-$	$1/2^+$	***
$N(1880)$	$1/2^+$	***	$\Delta(2150)$	$1/2^-$	*	$\Sigma(1910)$	$3/2^-$	***	Ξ_c^0	$1/2^+$	***	$\Xi_b(5945)^0$	$3/2^+$	***
$N(1895)$	$1/2^-$	****	$\Delta(2200)$	$7/2^-$	****	$\Sigma(1915)$	$5/2^+$	****	$\Xi_c(2645)$	$3/2^+$	***	$\Xi_b(5955)^-$	$3/2^+$	***
$N(1900)$	$3/2^+$	****	$\Delta(2300)$	$9/2^+$	**	$\Sigma(1940)$	$3/2^+$	*	$\Xi_c(2790)$	$1/2^-$	***	$\Xi_b(6100)^-$	$3/2^-$	***
$N(1990)$	$7/2^+$	**	$\Delta(2350)$	$5/2^-$	*	$\Sigma(2010)$	$3/2^-$	*	$\Xi_c(2815)$	$3/2^-$	***	$\Xi_b(6227)^-$		***
$N(2000)$	$5/2^+$	**	$\Delta(2390)$	$7/2^+$	*	$\Sigma(2030)$	$7/2^+$	****	$\Xi_c(2923)$		**	$\Xi_b(6227)^0$		***
$N(2040)$	$3/2^+$	*	$\Delta(2400)$	$9/2^-$	**	$\Sigma(2070)$	$5/2^+$	*	$\Xi_c(2930)$		**	Ξ_b	$1/2^+$	***
$N(2060)$	$5/2^-$	***	$\Delta(2420)$	$11/2^+$	****	$\Sigma(2080)$	$3/2^+$	*	$\Xi_c(2970)$	$1/2^+$	***	$\Omega_b(6316)^-$		*
$N(2100)$	$1/2^+$	***	$\Delta(2750)$	$13/2^-$	**	$\Sigma(2100)$	$7/2^-$	*	$\Xi_c(3055)$		***	$\Omega_b(6330)^-$		*
$N(2120)$	$3/2^-$	***	$\Delta(2950)$	$15/2^+$	**	$\Sigma(2110)$	$1/2^-$	*	$\Xi_c(3080)$		***	$\Omega_b(6340)^-$		*
$N(2190)$	$7/2^-$	****				$\Sigma(2230)$	$3/2^+$	*	$\Xi_c(3123)$		*	$\Omega_b(6350)^-$		*
$N(2220)$	$9/2^+$	****	Λ	$1/2^+$	****	$\Sigma(2250)$		**	Ω_c^0	$1/2^+$	***			
$N(2250)$	$9/2^-$	****	$\Lambda(1380)$	$1/2^-$	**	$\Sigma(2455)$		**	$\Omega_c(2770)^0$	$3/2^+$	***	$P_c(4312)^+$		*
$N(2300)$	$1/2^+$	**	$\Lambda(1405)$	$1/2^-$	****	$\Sigma(2620)$		*	$\Omega_c(3000)^0$		***	$P_c(4380)^+$		*
$N(2570)$	$5/2^-$	***	$\Lambda(1520)$	$3/2^-$	****	$\Sigma(3000)$		*	$\Omega_c(3050)^0$		***	$P_c(4440)^+$		*
$N(2600)$	$11/2^-$	***	$\Lambda(1600)$	$1/2^+$	****	$\Sigma(3170)$		*	$\Omega_c(3065)^0$		***	$P_c(4457)^+$		*
$N(2700)$	$13/2^+$	**	$\Lambda(1670)$	$1/2^-$	****				$\Omega_c(3090)^0$		***			
			$\Lambda(1690)$	$3/2^-$	****	Ξ^0	$1/2^+$	****	$\Omega_c(3120)^0$		***			
			$\Lambda(1710)$	$1/2^+$	*	Ξ^-	$1/2^+$	****						
			$\Lambda(1800)$	$1/2^-$	***	$\Xi(1530)$	$3/2^+$	****	Ξ^+		*			
			$\Lambda(1810)$	$1/2^+$	***	$\Xi(1620)$		*	Ξ^0		***			
			$\Lambda(1820)$	$5/2^+$	****	$\Xi(1690)$		***	Ξ^+		***			
			$\Lambda(1830)$	$5/2^-$	****	$\Xi(1820)$	$3/2^-$	***	Ξ^0		***			
			$\Lambda(1890)$	$3/2^+$	****	$\Xi(1950)$		***	Ξ^+		***			
			$\Lambda(2000)$	$1/2^-$	*	$\Xi(2030)$	$\geq \frac{5}{2}^?$	***						
			$\Lambda(2050)$	$3/2^-$	*	$\Xi(2120)$		*						
			$\Lambda(2070)$	$3/2^+$	*	$\Xi(2250)$		**						
			$\Lambda(2080)$	$5/2^-$	*	$\Xi(2370)$		**						
			$\Lambda(2085)$	$7/2^+$	**	$\Xi(2500)$		*						
			$\Lambda(2100)$	$7/2^-$	****				Ξ^+		*			
			$\Lambda(2110)$	$5/2^+$	***	Ω^-	$3/2^+$	****	Ξ^0		*			
			$\Lambda(2325)$	$3/2^-$	*	$\Omega(2012)^-$	$?^-$	****	Ξ^+		***			
			$\Lambda(2350)$	$9/2^+$	***	$\Omega(2250)^-$		***	Ξ^0		***			
			$\Lambda(2585)$	*		$\Omega(2380)^-$		**	Ξ^+		***			
						$\Omega(2470)^-$		**	Ξ^0		***			

72 new hadrons at the LHC



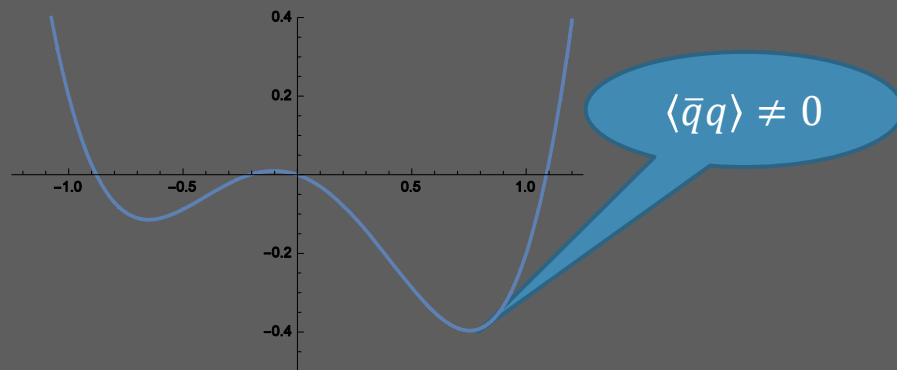
The chiral symmetry

The chiral symmetry:



Spontaneously breaking of chiral symmetry:

$$\langle \bar{q}q \rangle = \langle \bar{q}_L q_R + \bar{q}_R q_L \rangle \neq 0$$



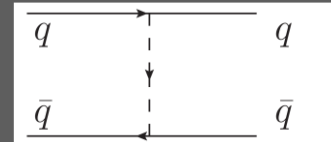
The effective theory based on chiral symmetry:

- Nonlinear sigma model
- Chiral perturbation theory

Chiral quark model

Naïve quark model:

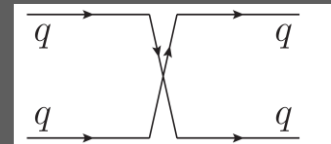
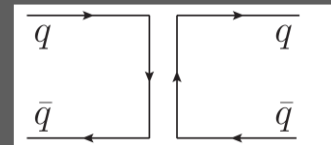
- Quark mass term
- Kinetic term
- Color confinement potential (CON)
- One gluon exchange (OGE)



- Gell-Mann, M., 1964, Phys. Lett. 8, 214.
- Zweig, G., 1964, CERN Reports No. 8182/TH. 401 and No. 8419/TH. 412).
- N. Isgur, G. Karl, Phys.Lett.B 72 (1977) 109.

The Nambu–Goldstone boson exchange:

- Chiral symmetry is spontaneously broken
- Pseudoscalars (π , K , η) are the Nambu–Goldstone (NG) bosons of chiral symmetry breaking
- Scalar meson σ as the chiral partner of NG bosons



- K. Shimizu, Phys. Lett. B 148, 418-422 (1984)
- L.Ya Glozman, Z. Papp, W. Plessas, Physics Letters B 381 (1996) 311-316
- Z.Y. Zhang, Y.W. Yu, P.N. Shen, L.R. Dai, A. Faessler, U. Straub, Nucl. Phys. A 625 (1997) 59.
- J. Vijande, F. Fernandez, A. Valcarce, J. Phys. G 31, 481(2005)

The Hamiltonian

$$H = \sum_{i=1}^n \left(m_i + \frac{p_i^2}{2m_i} \right) - T_{cm} + \sum_{j>i=1}^n (V_{ij}^{CON} + V_{ij}^{OGE} + V_{ij}^{\pi} + V_{ij}^K + V_{ij}^{\eta} + V_{ij}^{\sigma})$$

J . Vijande, F . Fernandez, A . Valcarce, J. Phys. G 31, 481(2005)

$$V_{ij}^{CON} = (\lambda_i^c \cdot \lambda_j^c) [-a_c (1 - e^{-\mu_c r_{ij}}) + \Delta],$$

$$V_{ij}^{OGE} = \frac{1}{4} \alpha_s (\lambda_i^c \cdot \lambda_j^c) \left[\frac{1}{r_{ij}} - \frac{1}{6m_i m_j} \frac{e^{-\frac{r_{ij}}{r_0(\mu_{ij})}}}{r_{ij} r_0^2(\mu_{ij})} \sigma_i \cdot \sigma_j \right],$$

$$V_{ij}^{\sigma} = -\frac{g_{ch}^2}{4\pi} \frac{\Lambda_{\sigma}^2}{\Lambda_{\sigma}^2 - m_{\sigma}^2} m_{\sigma} \left[Y(m_{\sigma} r_{ij}) - \frac{\Lambda_{\sigma}}{m_{\sigma}} Y(\Lambda_{\sigma} r_{ij}) \right],$$

$$V_{ij}^{\pi} = \frac{g_{ch}^2}{4\pi} \frac{m_{\pi}^2}{12m_i m_j} \frac{\Lambda_{\pi}^2}{\Lambda_{\pi}^2 - m_{\pi}^2} m_{\pi} \left[Y(m_{\pi} r_{ij}) - \frac{\Lambda_{\pi}^3}{m_{\pi}^3} Y(\Lambda_{\pi} r_{ij}) \right] \sigma_i \cdot \sigma_j \sum_{a=1}^3 \lambda_i^a \lambda_j^a,$$

$$V_{ij}^K = \frac{g_{ch}^2}{4\pi} \frac{m_K^2}{12m_i m_j} \frac{\Lambda_K^2}{\Lambda_K^2 - m_K^2} m_K \left[Y(m_K r_{ij}) - \frac{\Lambda_K^3}{m_K^3} Y(\Lambda_K r_{ij}) \right] \sigma_i \cdot \sigma_j \sum_{a=4}^7 \lambda_i^a \lambda_j^a,$$

$$V_{ij}^{\eta} = \frac{g_{ch}^2}{4\pi} \frac{m_{\eta}^2}{12m_i m_j} \frac{\Lambda_{\eta}^2}{\Lambda_{\eta}^2 - m_{\eta}^2} m_{\eta} \left[Y(m_{\eta} r_{ij}) - \frac{\Lambda_{\eta}^3}{m_{\eta}^3} Y(\Lambda_{\eta} r_{ij}) \right] \sigma_i \cdot \sigma_j (\lambda_i^8 \lambda_j^8 \cos \theta_p - \lambda_i^0 \lambda_j^0 \sin \theta_p).$$

The Gaussian expansion method

$$\psi_{lm}(\mathbf{r}) = \sum_{n=1}^{n_{max}} c_n \psi_{nlm}^G(\mathbf{r}),$$

$$\psi_{nlm}^G(\mathbf{r}) = N_{nl} r^l e^{-\nu_n r^2} Y_{lm}(\hat{\mathbf{r}}),$$

$$N_{nl} = \left(\frac{2^{l+2} (2\nu_n)^{l+\frac{3}{2}}}{\sqrt{\pi} (2l+1)!!} \right)^{\frac{1}{2}},$$

$$\nu_n = \frac{1}{r_n^2}, r_n = r_{min} a^{n-1}, a = \left(\frac{r_{max}}{r_{min}} \right)^{\frac{1}{n_{max}-1}}.$$

E. Hiyama, Y. Kino, and M. Kamimura, Prog. Part. Nucl. Phys. 51 223 (2003).

Outline

- Introduction

- ***Chiral quark model with HLS***

- ⊙ $SU2$ ground states + excited states

- ⊙ $SU3$ ground states

- ⊙ Future works

Incorporate the vector meson contribution

The hidden local symmetry:

M. Bando, T. Kugo, K. Yamawaki.
Phys.Rept. 164 (1988) 217-314
M. Harada, K. Yamawaki.
Phys.Rept. 381 (2003) 1-233

$$U = \xi_L^\dagger \xi_R = e^{2i \frac{\pi(x)}{f_\pi}}$$

$$\xi_{L,R} \rightarrow h(x) \xi_{L,R} \cdot g_{L,R}^\dagger$$

$$h(x)^\dagger h(x) = 1$$

$$\xi_{L,R} = e^{i \frac{V(x)}{f_V}} e^{\mp i \frac{\pi(x)}{f_\pi}}$$

$$h(x) \in H_{\text{local}} , \quad g_{L,R} \in G_{\text{global}}$$

- The transformation for U do not changes, which seems that the freedom of vector meson is “hidden”

$$[SU(N_f)_L \times SU(N_f)_R]_{\text{global}} \times [SU(N_f)_V]_{\text{local}} \rightarrow [SU(N_f)_V]_{\text{global}}$$

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- ***SU2 ground states + excited states***
- ◎ *SU3* ground states
- ◎ Future works

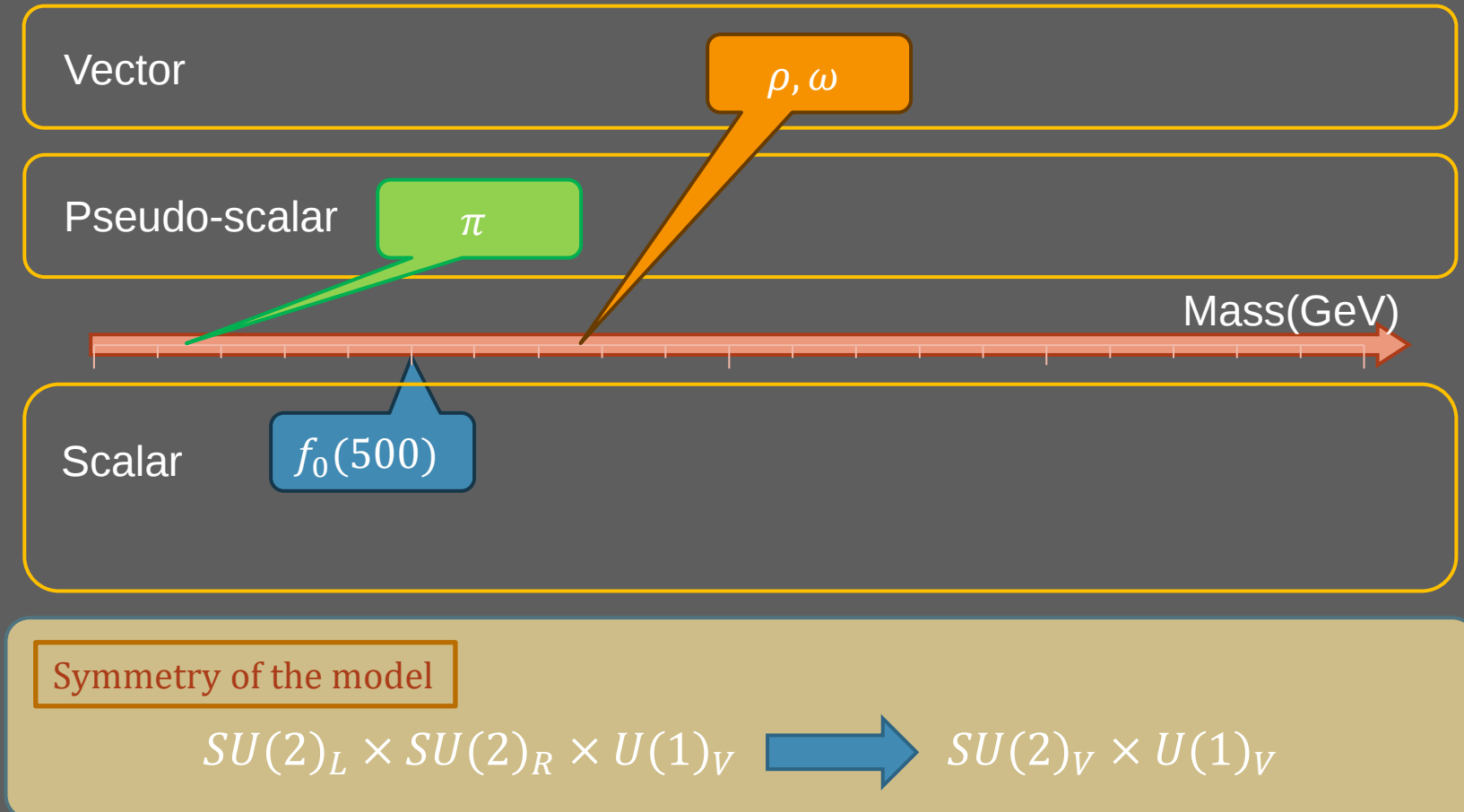
The Hamiltonian

$$H = \sum_{i=1} \left(m_i + \frac{p_i^2}{2m_i} \right) - T_{CM} + \sum_{j>i=1} (V_{ij}^{\text{CON}} + V_{ij}^{\text{OGE}} + V_{ij}^{\sigma} + V_{ij}^{\pi} + V_{ij}^{\omega} + V_{ij}^{\rho})$$

Bing-Ran He, Masayasu Harada,
Bing-Song Zou, 2306.03526

$$\begin{aligned} V_{ij}^v = & \frac{\Lambda_v^2}{\Lambda_v^2 - m_v^2} \left\{ \frac{g_v^2}{4\pi} m_v \left[Y(m_v r) - \left(\frac{\Lambda_v}{m_v} \right) Y(\Lambda_v r) \right] \right. \\ & + \frac{m_v^3}{m_i m_j} \left(\frac{g_v(2f_v + g_v)}{16\pi} + \frac{\boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j}{6} \frac{(f_v + g_v)^2}{4\pi} \right) \\ & \times \left[Y(m_v r) - \left(\frac{\Lambda_v}{m_v} \right)^3 Y(\Lambda_v r) \right] \\ & - \boldsymbol{S}_+ \cdot \boldsymbol{L} \frac{g_v(4f_v + 3g_v)}{8\pi} \frac{m_v^3}{m_i m_j} \\ & \times \left[G(m_v r) - \left(\frac{\Lambda_v}{m_v} \right)^3 G(\Lambda_v r) \right] \\ & - \boldsymbol{S}_{ij} \frac{(f_v + g_v)^2}{4\pi} \frac{m_v^3}{12m_i m_j} \\ & \left. \times \left[H(m_v r) - \left(\frac{\Lambda_v}{m_v} \right)^3 H(\Lambda_v r) \right] \right\} \end{aligned}$$

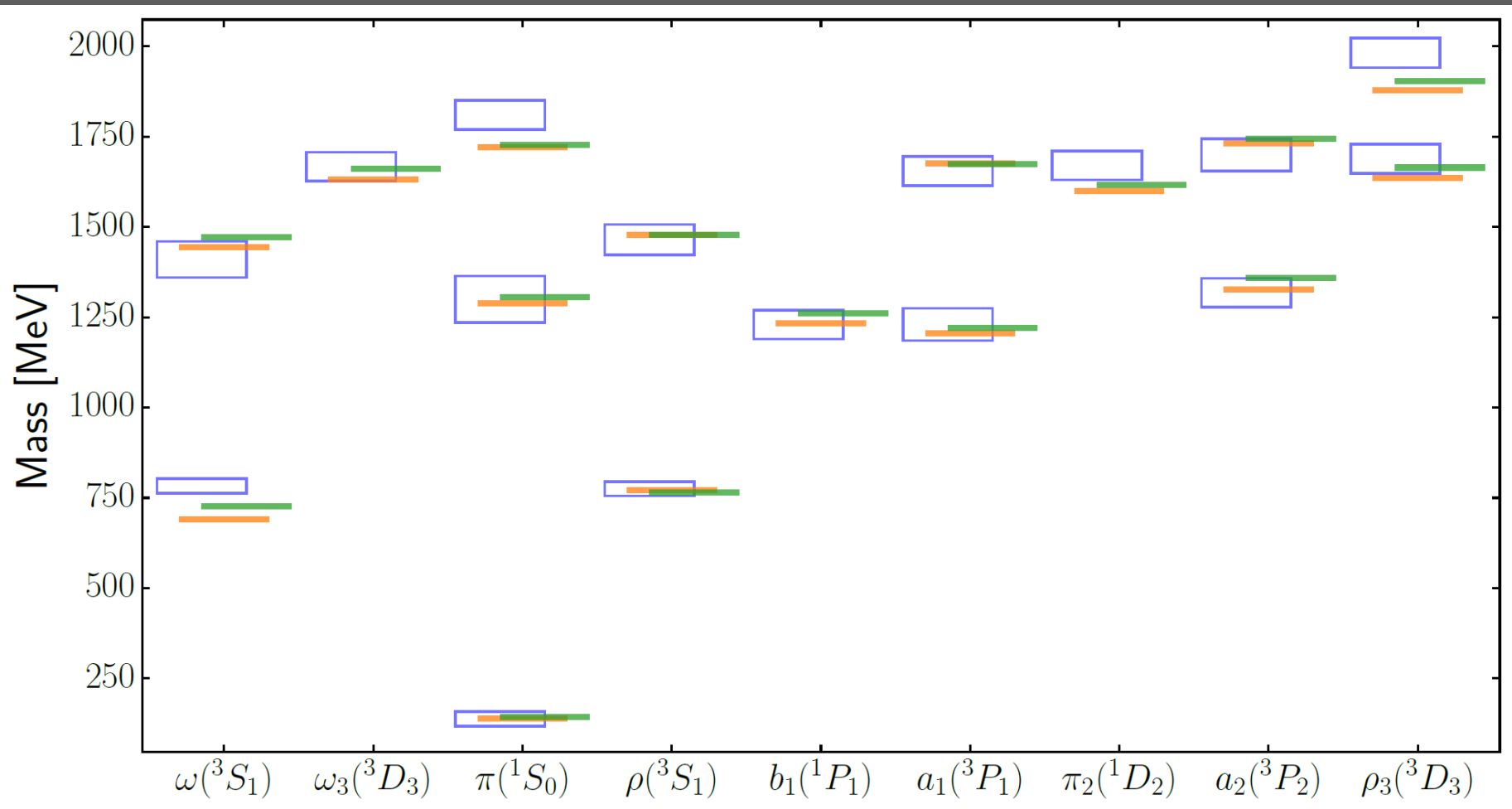
The exchanged mesons in $SU2$ model

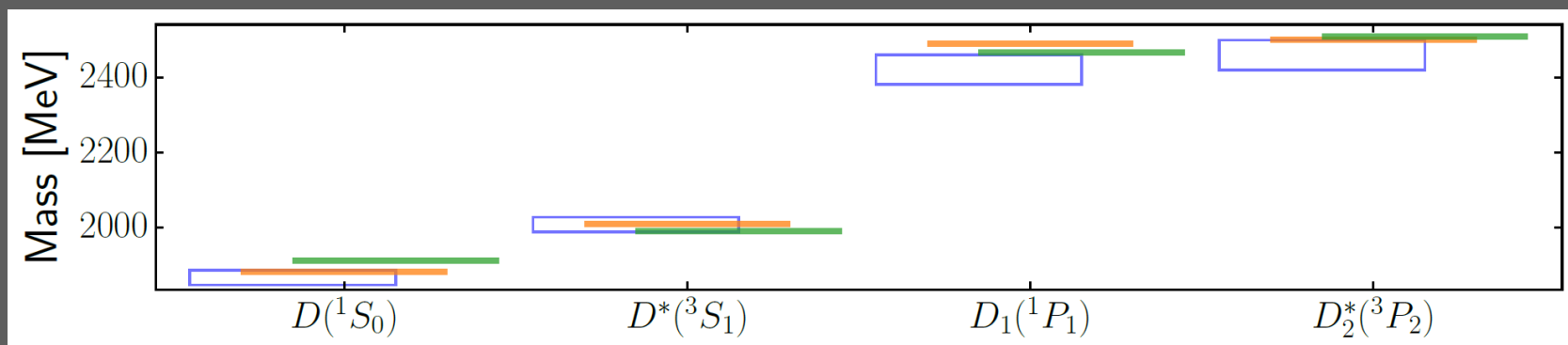
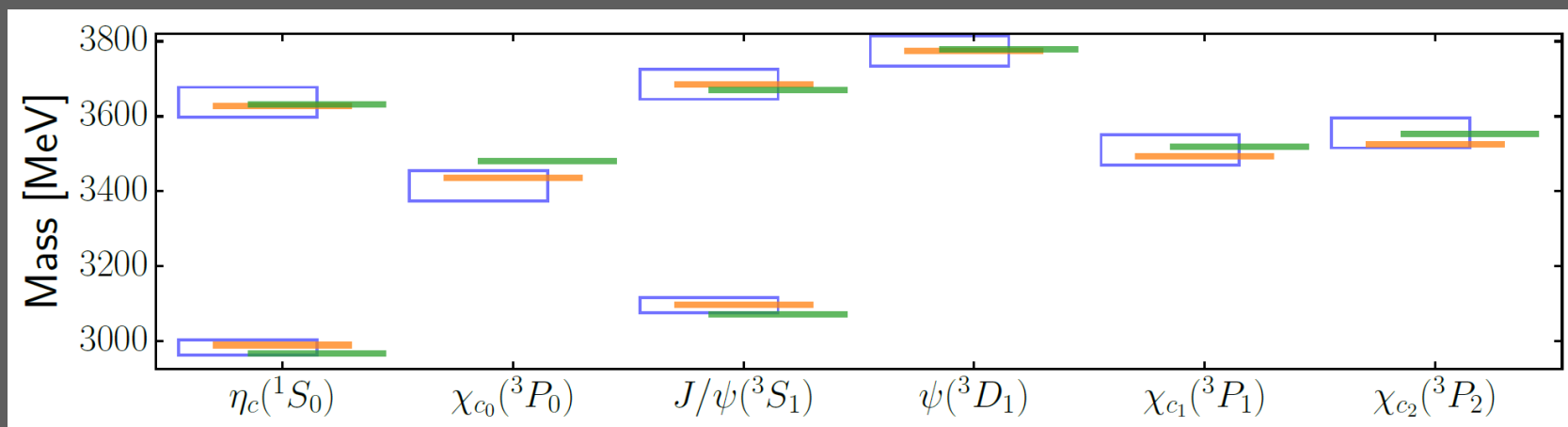


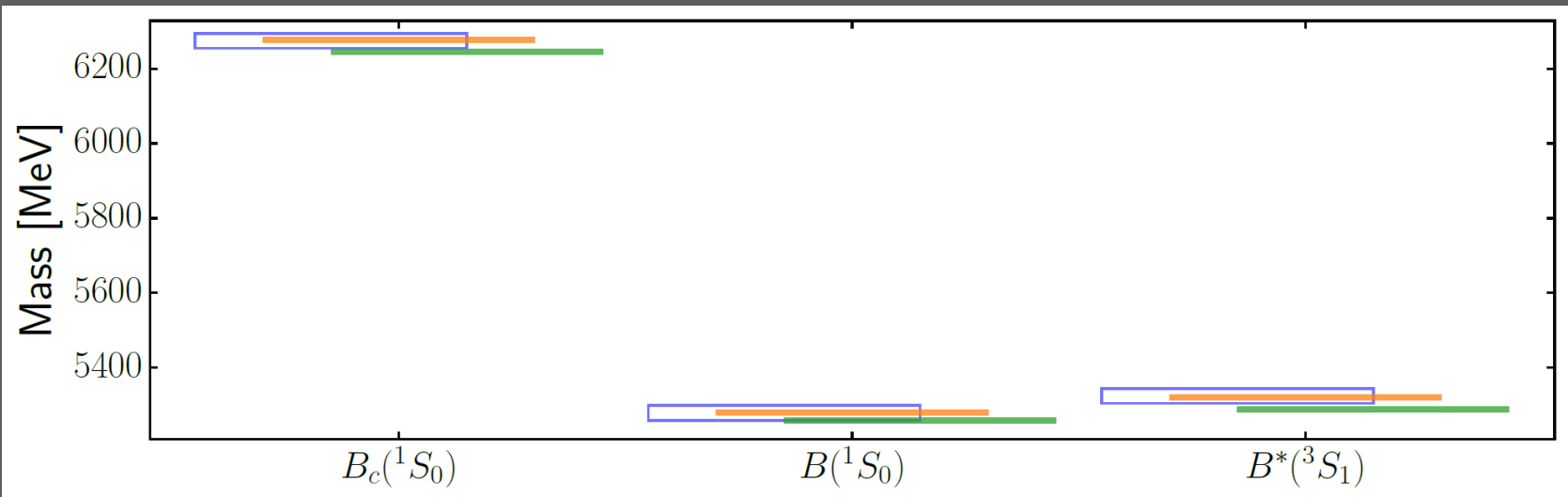
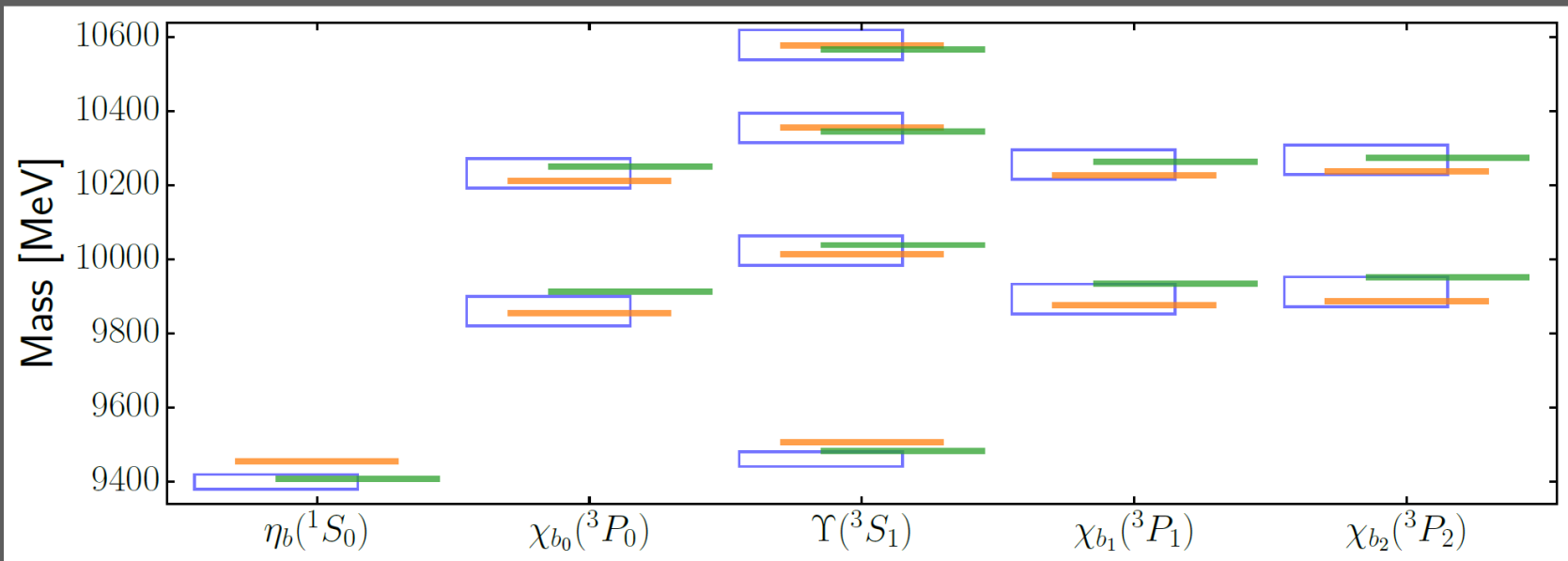
Wave functions

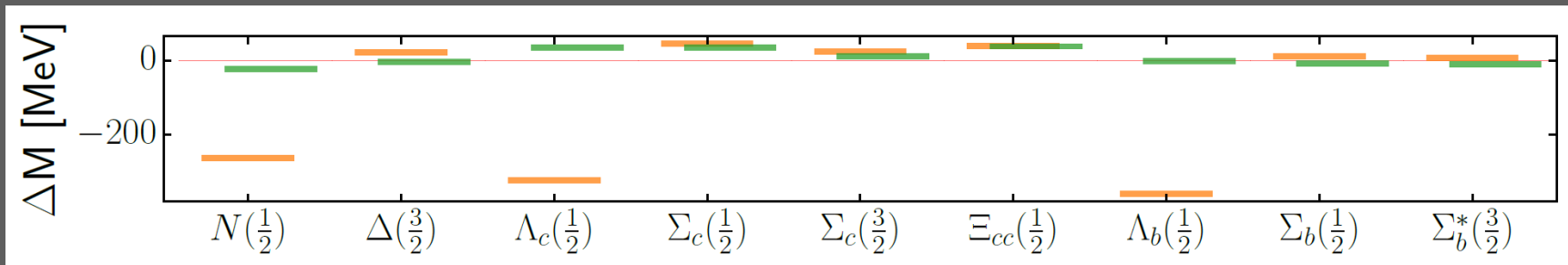
- Orbital (SO(3)): (ψ_L)
- Spin (SU(2)): (χ_S^σ)
- Flavor (SU(2)): (χ_I^f)
- Color (SU(3)): (χ^c)

$$\Psi_{JM_J IM_I}^{ijk} = \mathcal{A} \left[[\psi_L \chi_S^{\sigma i}]_{JM_J} \chi_I^{fj} \chi_k^c \right]$$









	1	$\tau_i \tau_j$	$\sigma_i \sigma_j$	$\sigma_i \sigma_j \cdot \tau_i \tau_j$
σ	-/-			
π				+/-
a_0		-/+		
OGE	-/-		+/+	
CON	+/+			
ω (This work)	+/-		+/-	
ρ (This work)		+/+		+/+

$qq/q\bar{q}$

Channel	E_B		Channel	E_B	
$[DD^*]_{1\otimes 1}$	6.2	39%	$[BB^*]_{1\otimes 1}$	0.5	12%
$[D^*D]_{1\otimes 1}$	6.2	39%	$[B^*B]_{1\otimes 1}$	0.5	12%
$[D^*D^*]_{1\otimes 1}$	83.1	5%	$[B^*B^*]_{1\otimes 1}$	31	32%
$[DD^*]_{8\otimes 8}$	383.1	0%	$[BB^*]_{8\otimes 8}$	253.6	0%
$[D^*D]_{8\otimes 8}$	383.1	0%	$[B^*B]_{8\otimes 8}$	253.6	0%
$[D^*D^*]_{8\otimes 8}$	337.3	0%	$[B^*B^*]_{8\otimes 8}$	233.3	0%
$[(cc)(\bar{q}\bar{q})^*]_{6\otimes \bar{6}}$	337.5	0%	$[(bb)(\bar{q}\bar{q})^*]_{6\otimes \bar{6}}$	233.7	0%
$[(cc)^*(\bar{q}\bar{q})]_{\bar{3}\otimes 3}$	120.3	17%	$[(bb)^*(\bar{q}\bar{q})]_{\bar{3}\otimes 3}$	-37.8	44%
Mixed	-4.9		Mixed	-88.2	

	r_{cc}	$r_{\bar{q}c}$	$r_{\bar{q}\bar{q}}$	$r_{\bar{q}b}$	r_{bb}
T_{cc}	1.56	1.24	1.70		
T_{bb}			0.75	0.65	0.37

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The Hamiltonian

$$H = \sum_{i=1} \left(m_i + \frac{p_i^2}{2m_i} \right) - T_{CM} + \sum_{j>i=1} (V_{ij}^{\text{CON}} + V_{ij}^{\text{OGE}} + V_{ij}^{\bar{\sigma}} + V_{ij}^{\eta} + V_{ij}^{\eta'} + V_{ij}^{\pi} + V_{ij}^K + V_{ij}^{\omega} + V_{ij}^{\phi} + V_{ij}^{\rho} + V_{ij}^{K*})$$

Bing-Ran He, Masayasu Harada,
Bing-Song Zou, 2307.16280

$$\begin{aligned} V_{ij}^{\bar{\sigma}} &= V_{ij}^{s=\bar{\sigma}, g_s=g_{\bar{\sigma}q}} \lambda_i^q \lambda_j^q + V_{ij}^{s=\bar{\sigma}, g_s=g_{\bar{\sigma}s}} \lambda_i^s \lambda_j^s, \\ V_{ij}^{\eta} &= V_{ij}^{p=\eta, g_p=g_{\eta q}} \lambda_i^q \lambda_j^q + V_{ij}^{p=\eta, g_p=g_{\eta s}} \lambda_i^s \lambda_j^s, \\ V_{ij}^{\eta'} &= V_{ij}^{p=\eta', g_p=g_{\eta'q}} \lambda_i^q \lambda_j^q + V_{ij}^{p=\eta', g_p=g_{\eta's}} \lambda_i^s \lambda_j^s, \end{aligned}$$

$$V_{ij}^{\pi} = V_{ij}^{p=\pi, g_p=g_{\pi}} \sum_{a=1}^3 \lambda_i^a \lambda_j^a,$$

$$V_{ij}^K = V_{ij}^{p=K, g_p=g_K} \sum_{a=4}^7 \lambda_i^a \lambda_j^a,$$

$$V_{ij}^{\omega} = V_{ij}^{v=\omega, g_v=g_{\omega q}} \lambda_i^q \lambda_j^q + V_{ij}^{v=\omega, g_v=g_{\omega s}} \lambda_i^s \lambda_j^s,$$

$$V_{ij}^{\phi} = V_{ij}^{v=\phi, g_v=g_{\phi q}} \lambda_i^q \lambda_j^q + V_{ij}^{v=\phi, g_v=g_{\phi s}} \lambda_i^s \lambda_j^s,$$

$$V_{ij}^{\rho} = V_{ij}^{v=\rho, g_v=g_{\rho}} \sum_{a=1}^3 \lambda_i^a \lambda_j^a,$$

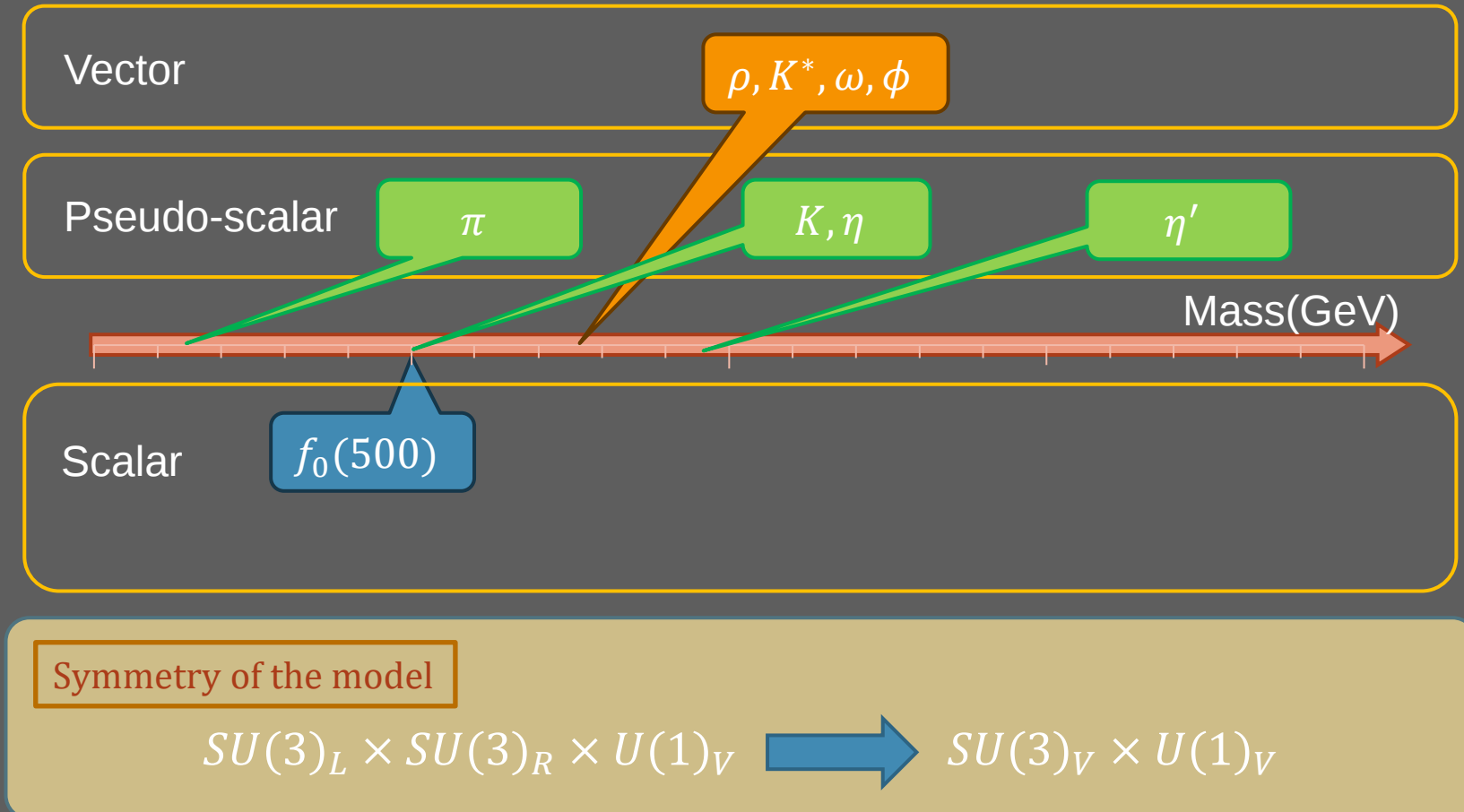
$$V_{ij}^{K*} = V_{ij}^{v=K^*, g_v=g_{K^*}} \sum_{a=4}^7 \lambda_i^a \lambda_j^a$$

$$\lambda^q = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \lambda^s = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

The coupling have relations based on $SU3$ flavor symmetry:

$$\begin{aligned} g_{\eta s} &= g_{\eta q} - \sqrt{3} \cos \theta_p g_{\pi} \\ g_{\eta' q} &= -\cot \theta_p g_{\eta q} + \frac{1}{\sqrt{3} \sin \theta_p} g_{\pi} \\ g_{\eta' s} &= -\cot \theta_p g_{\eta q} + \frac{\cos \theta_p \cot \theta_p - 2 \sin \theta_p}{\sqrt{3}} g_{\pi} \\ g_{\pi} &= g_K \\ g_{\omega s} &= g_{\omega q} - g_{\rho} \\ g_{\phi q} &= -\sqrt{\frac{1}{2}} (g_{\omega q} - g_{\rho}) \\ g_{\phi s} &= -\sqrt{\frac{1}{2}} (g_{\omega q} + g_{\rho}) \\ g_{\rho} &= g_{K^*} \text{ and } f_{\omega s} = f_{\omega q} - f_{\rho} \\ f_{\phi q} &= -\sqrt{\frac{1}{2}} (f_{\omega q} - f_{\rho}) \\ f_{\phi s} &= -\sqrt{\frac{1}{2}} (f_{\omega q} + f_{\rho}) \\ f_{\rho} &= f_{K^*} \end{aligned}$$

The exchanged mesons in $SU3$ model



Wave functions

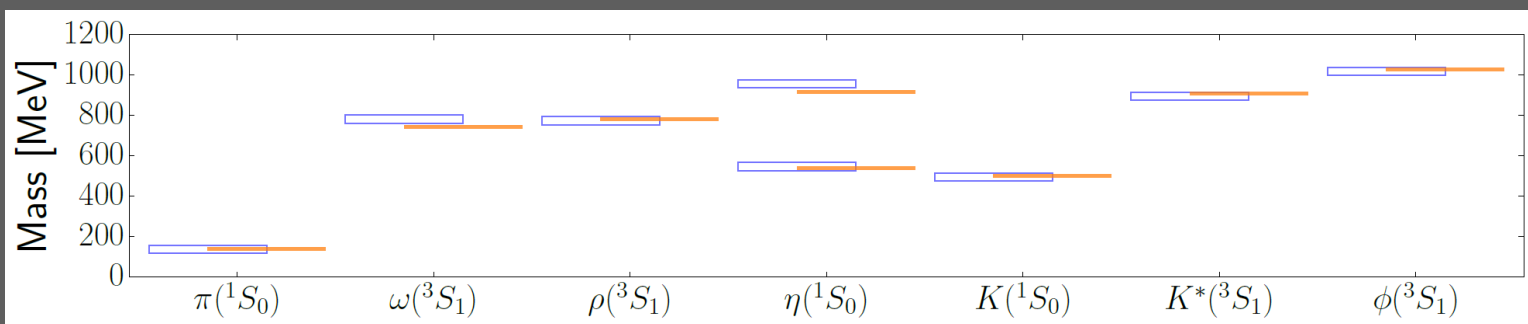
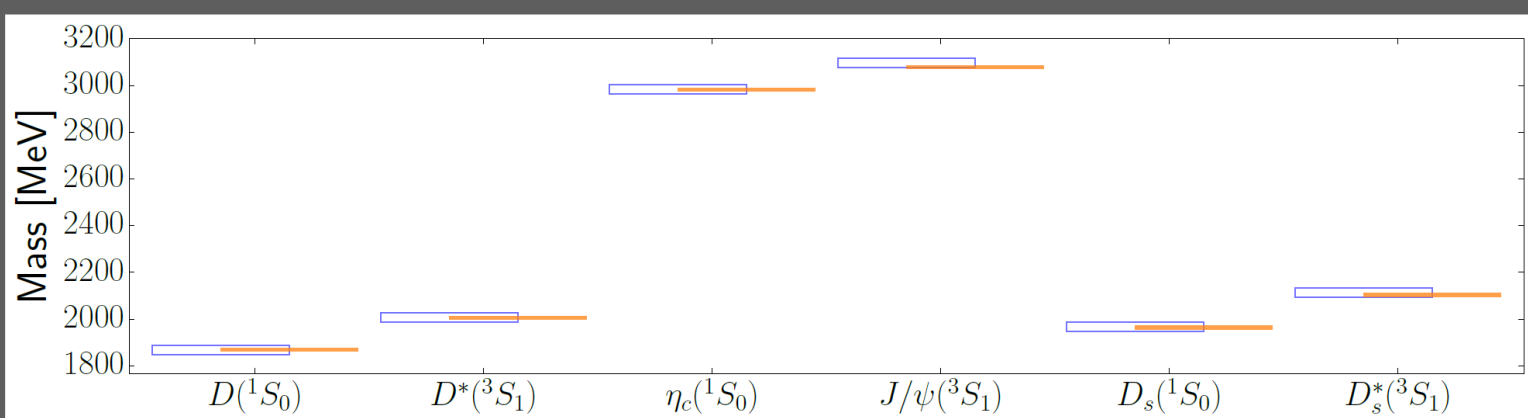
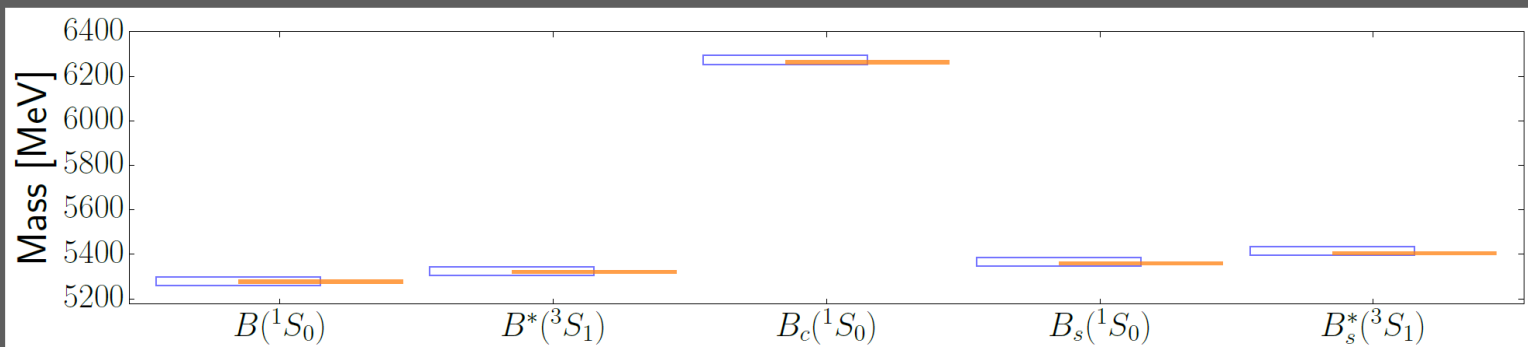
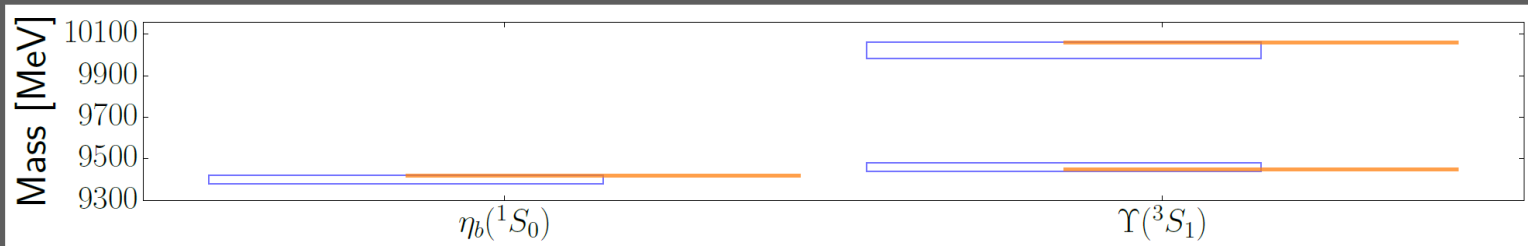
- Orbital (SO(3)): (ψ_L)
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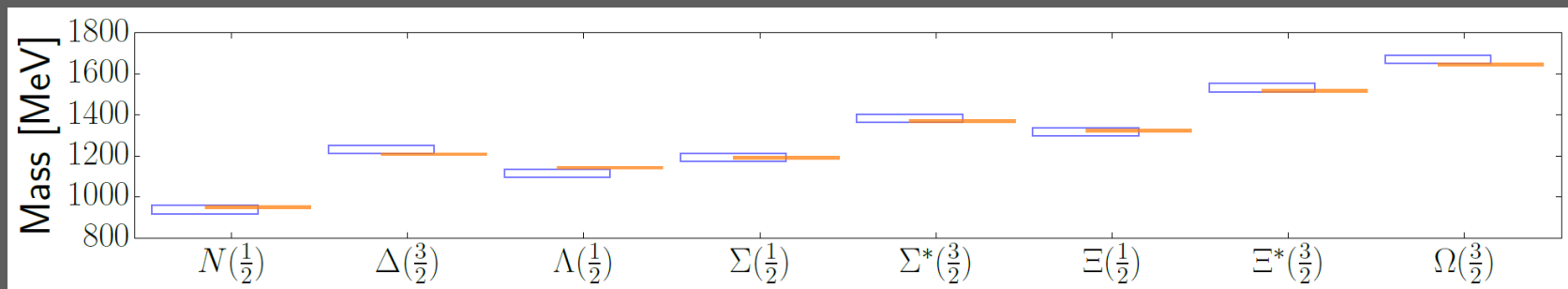
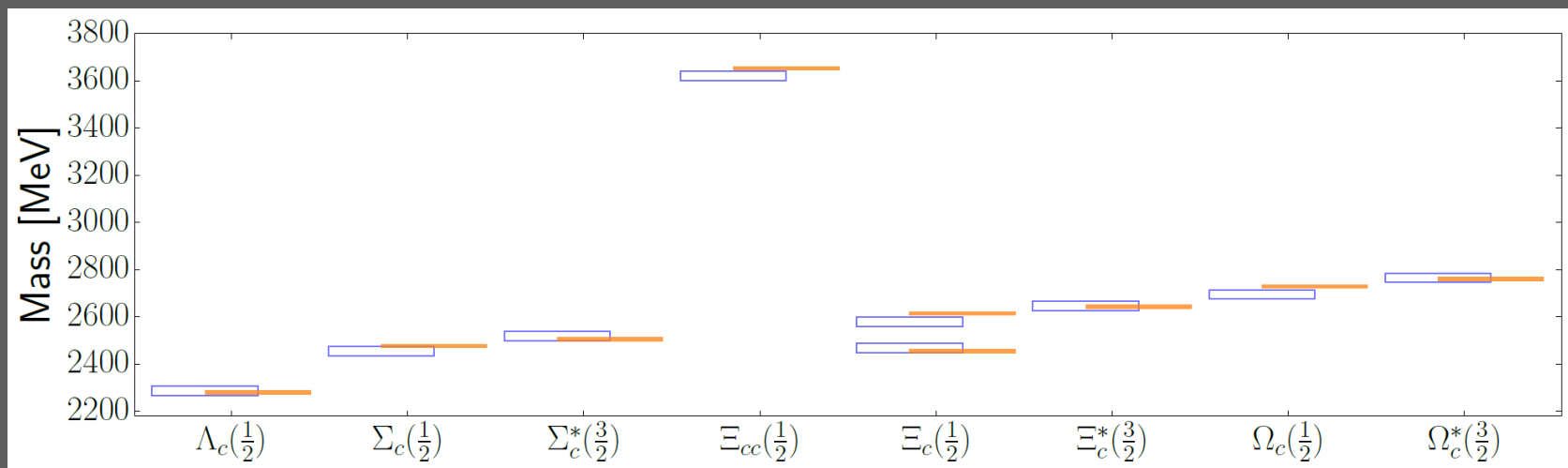
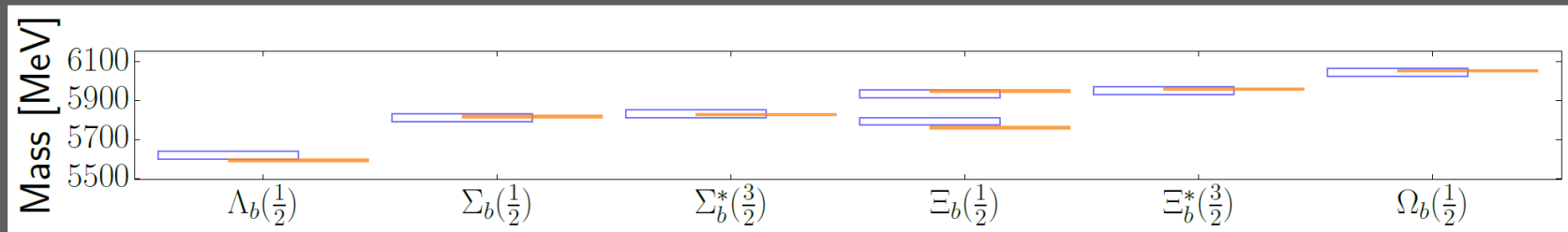
$$\Psi_{JM_J IM_I}^{ijk} = \mathcal{A} \left[[\psi_L \chi_S^{\sigma i}]_{JM_J} \chi_I^{fj} \chi_k^c \right]$$

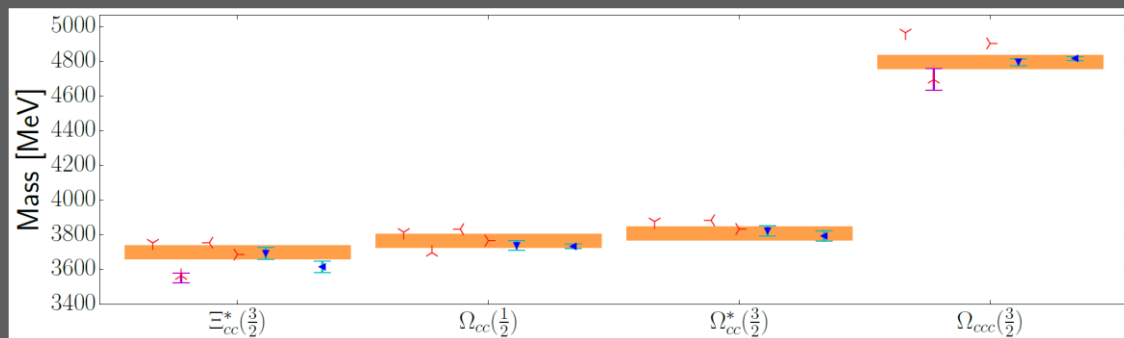
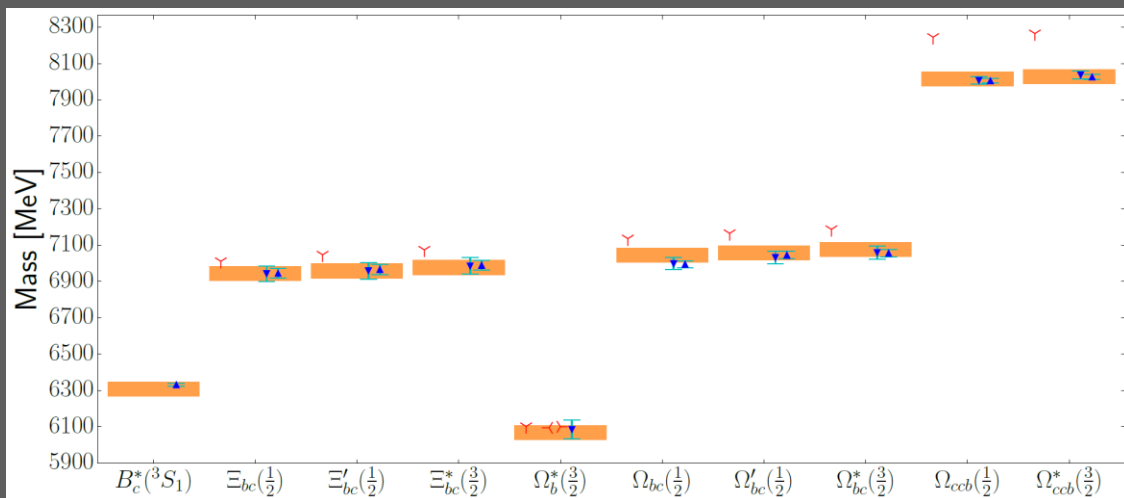
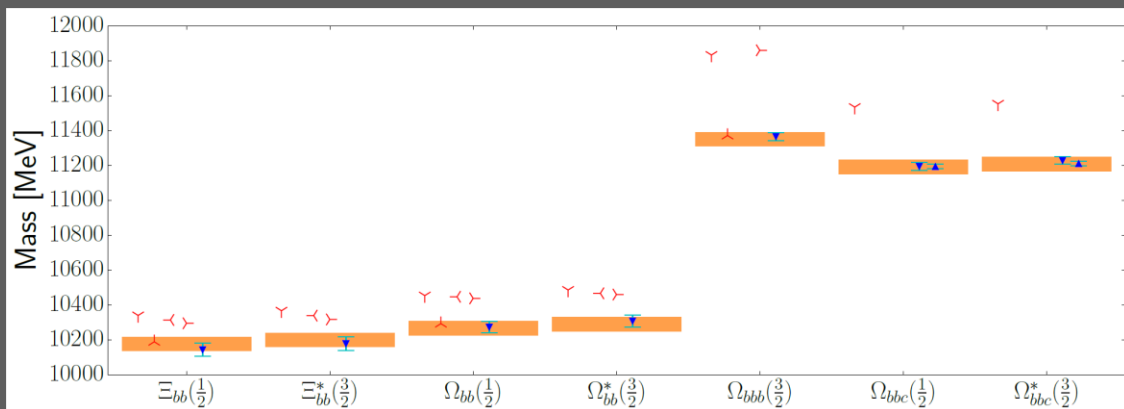
	1	$\lambda_i \lambda_j$	$\sigma_i \sigma_j$	$\sigma_i \sigma_j \cdot \lambda_i \lambda_j$
$\bar{\sigma}$	-/-			
η/η'			+/+	
π/K				+/-
ω/ϕ	+/-		+/-	
ρ/K^*		+/+		+/+
OGE	-/-		+/+	
CON	+/+			

$qq/q\bar{q}$

	No vector J . Vijande, F . Fernandez, A . Valcarce, J. Phys. G 31, 481(2005)	su2 vector 2306.03526	su3 vector 2307.16280
$\alpha_s(qq)$	0.536	0.880	0.456
$\alpha_s(qs)$	0.479		0.426
$\alpha_s(qc)$	0.426	0.774	0.363
$\alpha_s(qb)$	0.409	0.749	0.339
$\alpha_s(ss)$	0.419		0.388
$\alpha_s(sc)$	0.360		0.308
$\alpha_s(sb)$	0.340		0.279
$\alpha_s(cc)$	0.288	0.510	0.205
$\alpha_s(cb)$	0.260	0.447	0.168
$\alpha_s(bb)$	0.223	0.366	0.128



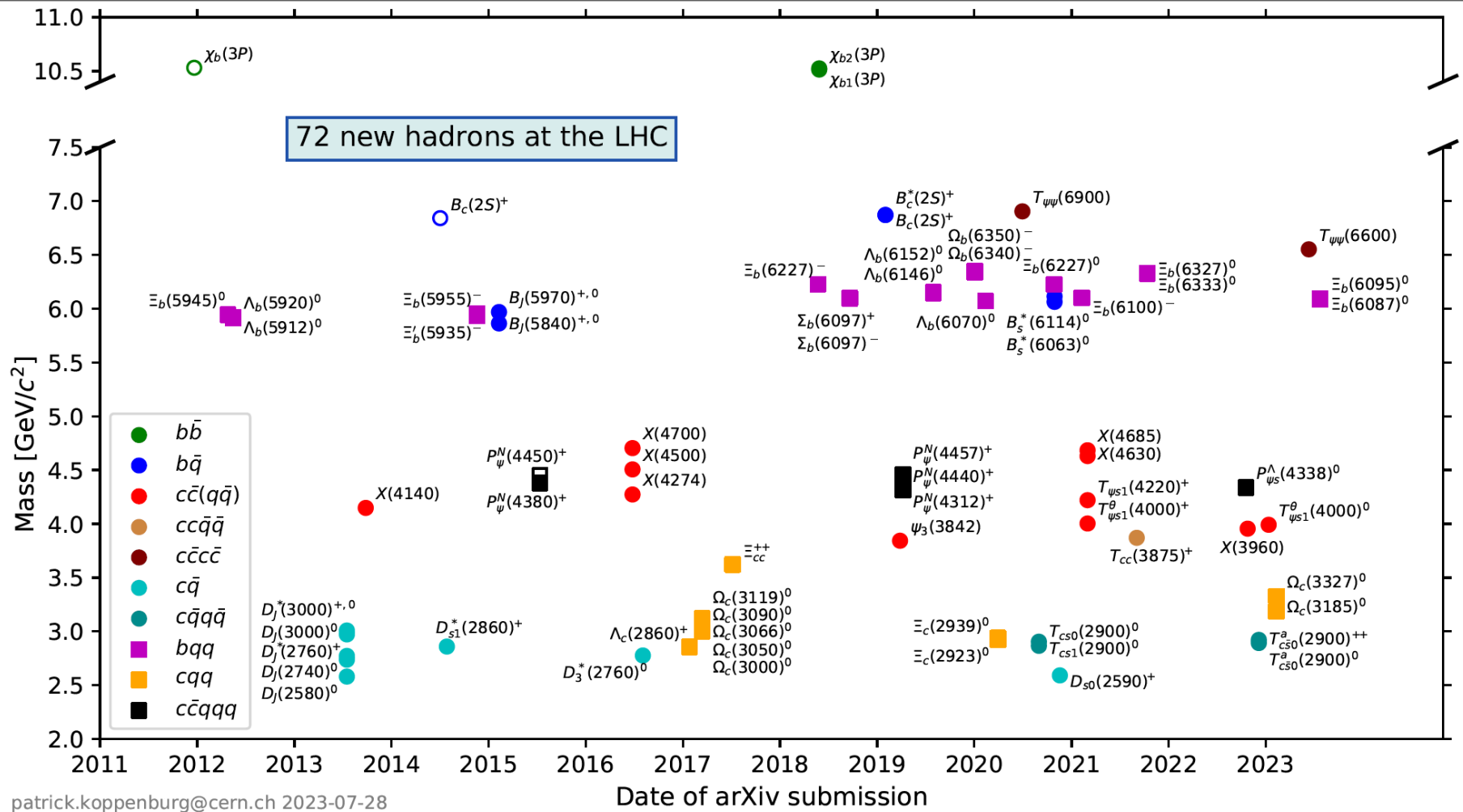




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72 new hadrons at the LHC



Thank you for your attention!