# Near-threshold Production and Energy-Dependent Electromagnetic Form Factors of $\Lambda_c^+$

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# **Electromagnetic form factors (EMFFs)**

• Nucleons are composite objects with inner structure. At low Q, perturbative QCD does not work well (expansion of coupling constant  $\alpha_s$ )

⇒ Nucleon structure must be measured in experiments!



• Using photon as a probe, the coupling to nucleon can be expressed in terms EMFFs



# **Electromagnetic form factors**

#### □ Fundamental properties of the nucleon

N

- Connected to charge, magnetization distribution
- Crucial testing ground for models of the nucleon internal structure Space-like Time-like



The nucleon electromagnetic vertex  $\Gamma_{\mu}$  describing the hadron current:

$$\Gamma_{\mu}(p',p) = \gamma_{\mu}F_{1}(q^{2}) + \frac{i\sigma_{\mu\nu}q^{\nu}}{2m_{p}}F_{2}(q^{2})$$
Sachs FFs:  $G_{E}(q^{2}) = F_{1}(q^{2}) + \tau\kappa_{p}F_{2}(q^{2}), \ G_{M}(q^{2}) = F_{1}(q^{2}) + \kappa_{p}F_{2}(q^{2})$ 
Normalization of FF:  $q^{2} = 0$ :  $G_{E} = F_{1}(0), \ G_{M} = \mu_{N}$   $q^{2} = 4m_{N}^{2}$ :  $G_{E} = G_{M}$ 
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# Pair production of baryon

EMFFs parameterize the pair production cross section in  $e^+e^-$ 

$$\frac{d\sigma_{B\overline{B}}(s)}{d\Omega} = \frac{\alpha^2 \beta C}{4s} \left[ |G_M(s)|^2 \left(1 + \cos^2 \theta\right) + \frac{4m_B^2}{s} |G_E(s)|^2 \sin^2 \theta \right] \equiv N_0 (1 + \alpha_B \sin^2 \theta)$$

Ratio  $R_{em} = |G_E/G_M|$  reflects polar angle distribution of produced baryon!  $|G_E|$  and  $|G_M|$  can be separately evaluated after determining  $N_0$  and  $\alpha_B$ .

After the integration over the polar angle  $\boldsymbol{\theta}$ 

$$\sigma_{B\overline{B}}(s) = \frac{4\pi\alpha^2\beta C}{3s} \left[ |G_M(s)|^2 + \frac{2m_B^2}{s} |G_E(s)|^2 \right]$$

The so-called effective form factor could be defined in terms of EMFFs:

$$|G_{\rm eff}(s)| = \sqrt{\frac{\frac{\sigma_{B\bar{B}}(s)}{\frac{4\pi\alpha^2\beta C}{3s}\left(1 + \frac{2m_B^2}{s}\right)}}{\frac{1}{s}}} = \sqrt{\frac{|G_M(s)|^2 + \frac{2m_B^2}{s}|G_E(s)|^2}{1 + \frac{2m_B^2}{s}}}$$

Effective FF reflects the magnitude of production cross section of baryon!

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## **Experimental access of Time-like form factors**



	Energy Scan	Initial State Radiation	
E <sub>beam</sub>	discrete	fixed	
$\mathcal{L}$	low at each beam energy	high at one beam energy	
σ	$\frac{d\sigma_{\boldsymbol{p}\boldsymbol{\overline{p}}}}{d(\cos\theta)} = \frac{\alpha^2\beta C}{4q^2} [ G_M ^2 (1+\cos^2\theta)]$	$rac{d^2 \sigma_{p\overline{p}\gamma}}{dx d heta_{\gamma}} = W(s, x,  heta_{\gamma}) \sigma_{p\overline{p}}(q^2)$	
	$+ \frac{4m_p^2}{q^2}  G_E ^2 \sin^2 \theta$ ]	$W(s, x,  heta_{\gamma}) = rac{lpha}{\pi x} (rac{2-2x+x^2}{\sin^2  heta_{\gamma}} - rac{x^2}{2})$	
$q^2$	single at each beam energy	from threshold to s	

## **BEPCII** and **BESIII**





- Located at the BEPCII collider (Beijing/China)
- Symmetric beams (2-5 GeV C.M. Energy)
- Maximum Luminosity: 1 nb<sup>-1</sup>/s
- 93% coverage of the solid angle

## **Data collected at BESIII**



## **Proton form factors**

ISR approach with detected and undetected ISR photon using BESIII data corresponds to  $7.5 \text{ fb}^{-1}$  integrated luminosity.

SA-ISR(un-tagged): PRD 99, 092002 (2019) LA-ISR(tagged): PLB 817, 136328 (2019)



> From threshold to  $q^2 = 4.0 \text{ GeV}^2$ , average cross section 840 pb

> Point-like cross section at threshold,  $\sigma_{\text{point}} = \frac{\pi \alpha^2}{3m_B^2 \tau} \left[ 1 + \frac{1}{2\tau} \right] = 845 \text{ pb}$ 

## **Proton form factors**

Scan technique from 2.00 to 3.08 GeV at BESIII, using data of 688.5 pb<sup>-1</sup>  $|G_E/G_M|$  is determined with high accuracy, comparable with space-like region.  $|G_E|$  and  $|G_M|$  are separated by analyzing the polar angle distribution.



PRL 124, 042001 (2020)

## Oscillation feature confirmed in $|G_{eff}|$



|G<sub>eff</sub>| data are fitted with the model: the monopole decrease with a damped oscillation : E. Tomasi-Gustafsson et al., PRL. 114, 232301 (2015), PRC 103, 035203 (2021)

$$|G_{\rm eff}|(s) = \frac{\mathcal{A}}{\left(1 + \frac{s}{a_0}\right) \left(1 - \frac{s}{0.71 \,\,{\rm GeV}^2}\right)^2} + b_0 e^{-b_1 p(s)} \cos[b_2 p(s) + b_3]$$

#### **Oscillation** feature in the cross section line-shape!

## Oscillation feature in $|G_E/G_M|$



 $|G_E/G_M|$  data can be well described by a function combining the monopole decrease with a damped oscillation

oscillation feature in the polar angle distribution of the outgoing proton!

 $|G_E/G_M|$  data are fitted with the model:

$$|G_E/G_M|(s) = \frac{1}{1 + \omega^2(s)/r_0} \Big[ 1 + r_1 e^{-r_2 \omega(s)} \sin(r_3 \omega(s)) \Big]$$

E. Tomasi-Gustafsson et al., PRL. 114, 232301 (2015), PRC 103, 035203 (2021)

## **Neutron form factors**

- > Scan technique from 2.00 to 3.08 GeV at BESIII, using data of  $647.9 \text{ pb}^{-1}$
- ➢ Unprecedented precision achieved, smaller than 8% at 2.396 GeV
- Clearly clarify the "puzzle" that photon-neutron coupling larger than photonproton coupling which exists over 20 years.





## Oscillation feature in $|G_{eff}|$

- ► Oscillation in addition to the dipole law:  $|G_{eff}^{p,n}(s)| = G_D^{p,n}(s) + G_{osc}^{p,n}(s)$
- Simultaneous fit on proton and neutron data with the same frequency but different phase:  $G_{osc}^{p,n}(s) = b_0^{p,n} e^{-b_1^{p,n} p(s)} \cos[b_2 p(s) + b_3^{p,n}]$
- > Fitted well but a phase shift around  $(125 \pm 12)^{\circ}$  is observed



## Oscillation feature in $|G_{eff}|$

#### **Recent SND** measurement suggests a different frequency:



#### Additional experimental and theoretical inputs are desired!

## $|G_E|$ and $|G_M|$ of neutron

- ▷  $|G_E|$  and  $|G_M|$  are obtained in 5 energy intervals due to the limited statistics,  $|G_E/G_M|$  distribution is not shown in the paper
- ▷ BESIII  $|G_M|$  values are smaller than that of FENICE by a factor of 2-3
- Data is compared with various models: pQCD, modified dipole, VMD and dispersion relations (DR), where the DR model gives good consistency



## **Production cross section of hyperons**



EMFF data of hyperon is limited due to the small statistics

## Production of charmed hyperon

#### BESIII measured the production of $\Lambda_c$ near-threshold:



- Precise non-zero cross section near the kinematic threshold, a significantly different energy-dependent trend from Belle's measurement
- $\geq |G_E/G_M|$  is consistent with 1 near the kinematic threshold
- ▶ Results are limited in a narrow c.m. energy region near threshold

A thorough study of the cross section and EMFFs is needed!

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## Cross section and EMFF measurements of $\Lambda_c^+$

#### A combined approach of the single tag (ST) and double tag (DT):

		-
$\sqrt{s}$ (GeV)	$\mathcal{L}_{int} \; (pb^{-1})$	-
4.6119	103.83	- Ve
4.6280	521.52	
4.6409	552.41	$\pi$
4.6612	529.63	$\Lambda^+_{\alpha} \longrightarrow e^+$
4.6819	1669.31	
4.6988	536.45	$e^ a^+$
4.7397	164.27	e e
4.7500	367.21	
4.7805	512.78	
4.8431	527.29	Only the decay channel
4.9180	208.11	<b>ST</b> $\stackrel{\text{IN}}{\longrightarrow}$ $\stackrel{\Lambda_c^+}{\longrightarrow} pK^-\pi^+$ and its
4.9509	160.37	charge-conjugate is used

#### Sufficient statistics enable a DT analysis to reduce uncertainty!

Significant positive and negative ST yields in the Y(4630) region:



Flat energy-dependent  $L_{int}$ , ST yields, and efficiency results in flat cross section

The Born cross section of channel  $\Lambda_c^+ \to p K^- \pi^+$  and  $\bar{\Lambda}_c^- \to \bar{p} K^+ \pi^-$ :

$$\sigma_{\pm} = \frac{N_{\text{ST}}^{\pm}}{\varepsilon_{\text{ST}}^{\pm} \mathcal{L}_{\text{int}} f_{\text{VP}} f_{\text{ISR}} \mathcal{B}_{\pm}}$$
$$N_{\text{ST}}^{\pm,n} = N_{\Lambda_c^+ \bar{\Lambda}_c^-}^n \varepsilon_{\text{ST}}^{\pm,n} \mathcal{B}_{\pm}, \quad N_{\text{DT}}^n = N_{\Lambda_c^+ \bar{\Lambda}_c^-}^n \mathcal{B}_+ \mathcal{B}_- \varepsilon_{\text{DT}}^n$$

Thus,

$$N_{\mathsf{DT}}^{n} = \mathcal{B}_{\pm} \frac{N_{\mathsf{ST}}^{\pm,n} \varepsilon_{\mathsf{DT}}^{n}}{\varepsilon_{\mathsf{ST}}^{\pm,n}}, \quad N_{\mathsf{DT}} = \sum_{n=1}^{9} N_{\mathsf{DT}}^{n} = \mathcal{B}_{\pm} \sum_{n=1}^{9} \left( \frac{N_{\mathsf{ST}}^{\pm,n} \varepsilon_{\mathsf{DT}}^{n}}{\varepsilon_{\mathsf{ST}}^{\pm,n}} \right)$$

As a result

$$\mathcal{B}_{\pm} = N_{\rm DT} \bigg/ \sum_{n=1}^{9} \bigg( \frac{N_{\rm ST}^{\pm,n} \varepsilon_{\rm DT}^{n}}{\varepsilon_{\rm ST}^{\pm,n}} \bigg)$$

Thus,

$$\sigma_{\pm} = \frac{N_{\text{ST}}^{\pm}}{\varepsilon_{\text{ST}}^{\pm} \mathcal{L}_{\text{int}} f_{\text{VP}} f_{\text{ISR}} N_{\text{DT}}} \sum_{n=1}^{9} \left( \frac{N_{\text{ST}}^{\mp, n} \varepsilon_{\text{DT}}^{n}}{\varepsilon_{\text{ST}}^{\mp, n}} \right)$$

- Most of the uncertainties in  $\varepsilon_{ST}^{\pm}$  (due to tracking and PID) are reduced.
- The double counting between the uncertainties of  $\varepsilon_{ST}^{\pm}$  and  $\mathcal{B}_{\pm}$  is avoided.
- Data samples with  $\mathcal{L}_{int} > 350 \text{ pb}^{-1}$  is used in the double tag analysis. 2023/8/4 E4  $\pm 4$

Branching fraction and DT yield is determined by a simultaneous fit:



 $\succ$  A total of 9 data sets are used, small fraction of background events

▶  $\mathcal{B}_{\pm}$  is the shared parameter in the fit, and  $\mathcal{B}_{+}$  and  $\mathcal{B}_{-}$  are determined separately
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#### To verify the obtained $\mathcal{B}_\pm$ , its energy-dependency is checked:



 $\succ$  Systematic uncertainty is reduced by a factor of 2, i.e., from 6.0% to 3.2%

Our branching fraction result is consistent with that of Belle!

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The Born cross section:

$$\sigma_{\pm} = \frac{N_{\text{ST}}^{\pm}}{\varepsilon_{\text{ST}}^{\pm} \mathcal{L}_{\text{int}} f_{\text{VP}} f_{\text{ISR}} N_{\text{DT}}} \sum_{n=1}^{9} \left( \frac{N_{\text{ST}}^{\pm, n} \varepsilon_{\text{DT}}^{n}}{\varepsilon_{\text{ST}}^{\pm, n}} \right)$$

The average Born cross section:

$$\sigma = \sum_{i=\pm} \omega_i \sigma_i, \omega_i = (1/\Delta \sigma_i^2) \bigg/ \bigg( \sum_i 1/\Delta \sigma_i^2 \bigg)$$

and corresponding uncertainty takes the form

$$\Delta \sigma^2 = \sum_{i,j=\pm} \omega_i (\mathbf{M}^{\sigma})_{ij} \omega_j, \mathbf{M}^{\sigma} = \mathbf{M}_{\mathsf{stat}}^{\sigma} + \mathbf{M}_{\mathsf{syst}}^{\sigma}$$

or approximately

$$\Delta \sigma_{\mathsf{stat}}^2 = \sum_{i,j=\pm} \omega_i (\mathsf{M}_{\mathsf{stat}}^{\sigma})_{ij} \omega_j \quad \text{and} \quad \Delta \sigma_{\mathsf{syst}}^2 = \sum_{i,j=\pm} \omega_i (\mathsf{M}_{\mathsf{syst}}^{\sigma})_{ij} \omega_j$$

The covariance matrix  $\mathbf{M}^{\sigma}$  counts for independent and correlated uncertainties.

The i = +, - indexed results of tagging  $\Lambda_c^+ \to \rho K^- \pi^+$  and  $\bar{\Lambda}_c^- \to \bar{\rho} K^+ \pi^-$ , respectively.

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 $\blacktriangleright$  Typical uncertainty is less than 4.0%, which is dominated by that of  $\mathcal{B}_+$ 

- $\triangleright$  Cross sections at first four points are re-evaluated using updated  $\mathcal{L}_{int}$  and  $\mathcal{B}_{+}$
- $\blacktriangleright$  Near-threshold cross-section plateau is confirmed up to 4.68 GeV, and no resonance structure is observed around 4.64 GeV -- no charmed baryonium? 2023/8/4



#### Similar momentum-dependency with the proton and neutron

## Discussions in the theoretical point of view

#### **BESIII** data affects the parameterization of Y(4630):



## Discussions in the theoretical point of view

#### **BESIII** data affects the parameterization of Y(4630):



Xiang-Kun Dong, Feng-Kun Guo, and Bing-Song Zou, *Progr. Phys.* **41** (2021) 65-93



## Effective form factor of $\Lambda_c^+$

The effective form factors spectrum is fitted with a three-pole model:

$$G_{3p}(s) = \frac{\mathcal{G}}{\left(1 + \frac{s}{g_a}\right) \left(1 - \frac{s}{g_b}\right)^2}$$

where

$$p = \sqrt{\left(\frac{s}{2m_{\Lambda_c^+}} - m_{\Lambda_c^+}\right)^2 - m_{\Lambda_c^+}^2}$$





The residual between effective form factors data and the three-pole model is obtained:

$$\Delta |G_{\rm eff}|(p) = |G_{\rm eff}|(p) - G_{3p}(p)$$

and fitted to a damped oscillation model:

 $|G_{\rm osc}|(p) = Ae^{-Bp}\cos(Cp + D)$ 

 $C = (0.03 \pm 0.14) \ (\text{GeV}/c)^{-1}$ 

No oscillation feature is discerned in the effective form-factor spectrum of  $\Lambda_c^+$ 

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## Electromagnetic form factor of $\Lambda_c^+$

The  $|G_E/G_M|$  of  $\Lambda_c^+$  is studied by analyzing the polar angle distribution:



One-photon exchange process is assumed

An ISR correction is considered due to the contribution from ISR returned events

Polar angle spectra is fitted with formula:

 $f(\cos\theta) \propto N_0 (1 + \alpha_{\Lambda_c} \cos^2 \theta)$ 

$$|G_E/G_M|^2 = \frac{s}{4m_{\Lambda_c^+}^2} \left(\frac{1-\alpha_{\Lambda_c}}{1+\alpha_{\Lambda_c}}\right)$$

The reversal of the angular distribution leads to  $|G_E/G_M| < 1$ 

## Electromagnetic form factor of $\Lambda_c^+$

#### Additional efforts are made to verify the angular analysis:

Contribution from two-photon exchange (TPE) process is studied via the formula

 $f(\cos\theta) \propto N_0 (1 + c_0 \cos\theta + \alpha_{\Lambda_c} \cos^2\theta)$ 

*E. Tomasi-Gustafsson et al., PRC 103, 035203 (2021)* where  $c_0$  reflects the contribution from two-photon exchange process. Vanishing  $c_0$  is obtained at each c.m. energy, no contribution from TPE process

- > Cross feed between different  $\cos\theta$  bins are considered via performing an unfolding based on the signal MC samples, negligible effects to  $|G_E/G_M|$
- > Different binning scheme in terms of  $\cos\theta$  is tested, including 8, 12, 16, 26, 32, and 40, no systematic deviation from the nominal case (20) is observed
- Sufficient input-output checks are carried out based on larger-statistic signal MC samples, the angular-analysis approach is valid
- ➢ A plenty of systematic effects are considered, the total uncertainty is dominated by the statistical one

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## Electromagnetic form factor of $\Lambda_c^+$



➢ Fitted to a function combining monopole decrease with damped oscillation

 $\succ$  Oscillation feature is unambiguously discerned for the charmed baryon  $\Lambda_c^+$ 

## Where is the oscillation from?

#### Dispersion theory: broad poles above threshold in nucleon

Yong-Hui Lin, Hans-Werner Hammer, and Ulf-G. Meißner, Phys. Rev. Lett. 128, 052002 (2022)





May not applicable for  $\Lambda_c^+$  be since no oscillation feature is observed  $|G_{eff}|$  data

## Where is the oscillation from?

#### A prediction of $|G_E|$ and $|G_M|$ based on the **modified VMD model** :



 $\triangleright$   $|G_E|$  and  $|G_M|$  are parameterized separately with the modified VMD model

- $\blacktriangleright$  Contribution from the vector charmed mesons and their excitations are included
- ➢ Phenomenology parameters are determined by fitting BESIII and Belle cross section data and BESIII  $|G_E/G_M|$  data

Maybe difficult to simultaneously reproduce new BESIII cross section and  $|G_E/G_M|$  data

- → BESIII measured the cross section and electromagnetic form factors of  $e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$  with unprecedented precision
- → The cross-section plateau is confirmed up to 4.66 GeV and the decay process  $Y(4630) \rightarrow \Lambda_c^+ \overline{\Lambda_c^-}$  is not observed
- ▷ Contradict to the case in proton and neutron, the oscillation feature is not observed in the  $|G_{eff}|$  spectrum of  $\Lambda_c^+$
- > Oscillation is discerned in  $|G_E/G_M|$  distribution of  $\Lambda_c^+$ , but with a significantly different frequency from that of proton

It is likely that these two oscillations come from different origins

# ► BESIII will collect data at energies up to 5.6 GeV, more charmed baryons, such as $\Lambda_c^*$ , $\Sigma_c$ , $\Xi_c$ and $\Omega_c$ , could be studied Chin. Phys. C 44, 04001 (2020)

Table 7.1: List of data samples collected by BESIII/BEPCII up to 2019, and the proposed samples for the remainder of the physics program. The most right column shows the number of required data taking days in current ( $T_{\rm C}$ ) or upgraded ( $T_{\rm U}$ ) machine. The machine upgrades include top-up implementation and beam current increase.

Energy	Physics motivations	Current data	Expected final data	$T_{ m C}$ / $T_{ m U}$
1.8 - 2.0 GeV	R values	N/A	$0.1 { m ~fb^{-1}}$	60/50  days
	Nucleon cross-sections		(fine scan)	
2.0 - 3.1 GeV	R values	Fine scan	Complete scan	250/180  days
	Cross-sections	(20  energy points)	(additional points)	
$J/\psi$ peak	Light hadron & Glueball	$3.2 \text{ fb}^{-1}$	$3.2 \text{ fb}^{-1}$	N/A
	$J/\psi$ decays	(10  billion)	(10  billion)	
$\psi(3686)$ peak	Light hadron & Glueball	$0.67 { m ~fb^{-1}}$	$4.5 { m fb}^{-1}$	150/90  days
	Charmonium decays	(0.45  billion)	(3.0  billion)	
$\psi(3770)$ peak	$D^0/D^{\pm}$ decays	$2.9 { m fb}^{-1}$	$20.0 \text{ fb}^{-1}$	610/360  days
3.8 - 4.6  GeV	R values	Fine scan	No requirement	N/A
	XYZ/Open charm	(105  energy points)		
4.180  GeV	$D_s$ decay	$3.2 { m ~fb^{-1}}$	$6  {\rm fb}^{-1}$	140/50  days
	XYZ/Open charm			
	XYZ/Open charm			
$4.0$ - $4.6~{\rm GeV}$	Higher charmonia	$16.0 { m ~fb^{-1}}$	$30 \text{ fb}^{-1}$	770/310  days
	cross-sections	at different $\sqrt{s}$	at different $\sqrt{s}$	
4.6 - 4.9 GeV	Charmed baryon/ $XYZ$	$0.56 { m ~fb^{-1}}$	$15 { m fb}^{-1}$	1490/600  days
	cross-sections	at $4.6 \mathrm{GeV}$	at different $\sqrt{s}$	
$4.74  {\rm GeV}$	$\Sigma_c^+ \bar{\Lambda}_c^-$ cross-section	N/A	$1.0 \text{ fb}^{-1}$	100/40 days
$4.91 \mathrm{GeV}$	$\Sigma_c \overline{\Sigma}_c$ cross-section	N/A	$1.0 { m  fb^{-1}}$	120/50 days
$4.95~{\rm GeV}$	$\Xi_c$ decays	N/A	$1.0 {\rm ~fb^{-1}}$	130/50 days

A refined energy-scan will always help for the study of the  $e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$  process!

EESIII will collect data at energies up to 5.6 GeV, more charmed baryons, such as  $\Lambda_c^*$ ,  $\Sigma_c$ ,  $\Xi_c$  and  $\Omega_c$ , could be studied



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# Thank you!

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