

6th Numerical Lattice Field Theory Training Camp

Lattice QCD Data Analysis



Lattice Parton Collaboration

Outline

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- Theory on two-point function

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 - Programming language/packages
 - ``iog`` data format
 - Resampling
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- *Introduction to HDF5*

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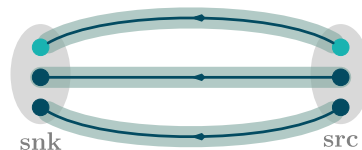
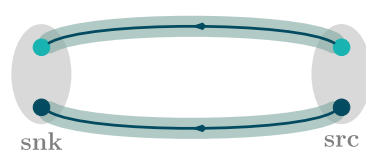
《格点量子色动力学导论》刘川, §20

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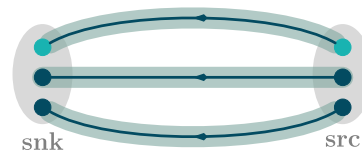
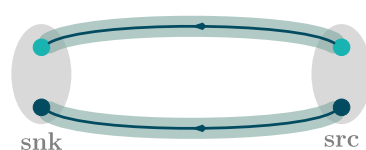


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- For large enough $\tau_f - \tau_i$, higher excited states decay faster

$$\langle \mathcal{O}(t_{\text{snk}}) \mathcal{O}(t_{\text{src}})^\dagger \rangle \approx$$

- $c_0 e^{-E_0 t} \Rightarrow$ one state analysis
- $c_0 e^{-E_0 t} + c_1 e^{-E_1 t} \Rightarrow$ two state analysis
- Determine the hadron mass spectrum from lagrangian (first-principle or ab initio calculation)

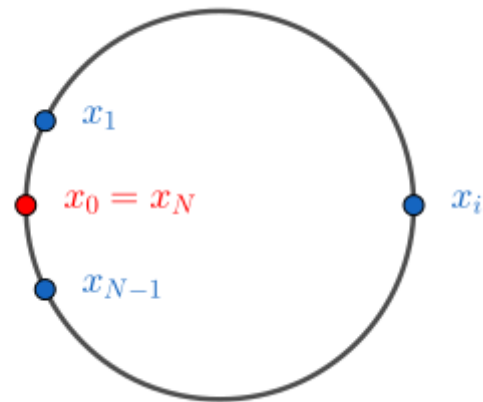
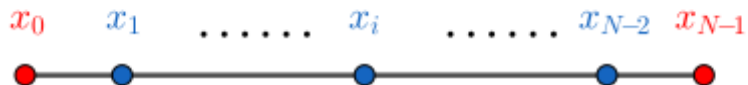
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 - $\phi_i = 0$ if $i \geq N$ or $i < N_0$
- Periodic/AntiPeriodic boundary condition
 - $\phi_N = \pm\phi_0, \phi_{N+i} = \pm\phi_i \Leftrightarrow \phi_{i+N} = \pm\phi_{(i+N) \bmod N}$



- Considering periodic boundary condition
- propagate in both $\pm t$ direction

$$C_2(t) \approx C_0 e^{-\frac{T}{2} E_0} \cosh \left[E_0 \left(\frac{T}{2} - t \right) \right]$$

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cosh

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- Determine hadron effective energy E_0 (m_{eff})

log

- A glance

- For $0 < t \ll T/2 \Rightarrow e^{-E_0 t} \gg e^{-E_0(T/2-t)} \Rightarrow \ln \frac{C_2(t)}{C_2(t+a)} \approx aE_0$
- $\frac{C_2(t)}{C_2(t+a)} = \frac{\cosh[E_0(T/2 - t)]}{\cosh[E_0(T/2 - (t+a))]} \text{ or } \frac{C_2(t+a) + C_2(t-a)}{2C_2(t)} = \cosh aE_0$
- More systematically way $\Rightarrow$ Fit (see sec. **Least χ^2 fit** for detail)

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 - Visualization: ``matplotlib``

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 - Regular expression (python package ``re``)

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- Useful but not mandatory
 - Regular expression (python package ``re``)
- Advanced
 - HDF5, ``h5py``
 - MPI

- Documentation

Library/Package	Documentation
pandas	<u>https://pandas.pydata.org/docs/</u>
numpy	<u>https://numpy.org/doc/stable/</u>
gvar	<u>https://gvar.readthedocs.io/en/latest/overview.html</u>
lsqfit	<u>https://lsqfit.readthedocs.io/en/latest/lsqfit.html</u>
Scipy	<u>https://scipy.org/</u>
HDF5	<u>https://portal.hdfgroup.org/display/support/documentation</u>
h5py	<u>https://docs.h5py.org/en/stable/</u>

- Installation
 - `pip3`: package installer for python
 - `pip3 install package_name --user`
 - `--user` install under current user environment, does not need root permission
- Python devel package (required by `iog.so`)
 - header `/usr/include/python3.6m/`

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2  # encoding: utf-8
3  from iog_reader import iog_read
4
5  iog_file = "./2pt_5350.dat.iog"
6  intrptr = ["cnfg", "hdrn", "t"]
7
8  iog = iog_read(iog_file, intrptr)
9  print(iog, '\n-----\n')
10
11 iog_pi=iog.loc[(iog['hdrn']=='0')]
12 print(iog_pi['Re'].to_numpy(), '\n-----\n')
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- Detailed usage of ``pandas.DataFrame.loc``: see documentation

- ``iog_reader.py` : `iog` ⇨ pandas.dataframe`

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3
4  from ctypes import *
5  import os
6  import numpy as np
7  import pandas as pd
8
9  lib = cdll.LoadLibrary(os.getcwd()+ '/iog.so')
10
11  def iog_read(iog_fl, intrprtrs):
12      iog_file = c_char_p(iog_fl.encode('utf-8'))
13      size = lib.getsize(iog_file)
14
15      class iog_type(Structure):
16          _fields_ = [('info_shape', POINTER(c_int)), ('info', POINTER(c_int)),
17                    ('Re', POINTER(c_double)), ('Im', POINTER(c_double))]
18
19      lib.getdat.restype = POINTER(iog_type)
20      iog = lib.getdat(iog_file)
21
22      info_shape = np.ctypeslib.as_array(iog.contents.info_shape, shape=[2])
23      info = np.ctypeslib.as_array(iog.contents.info, shape=[np.prod(info_shape)])
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- Source located under ``demo/iog``

- In case you need to compile `ioq.so` by yourself
- Source located under `demo/ioq`
- Set the value of `INCL` pointing to the path containing python develop tools header in `Makefile`

```
INCL = -I/dssg/opt/icelake/linux-centos8-icelake/gcc-8.3.1/python-3.9.12-  
omx7ttx5qbayml44yyhwifxuooiebv7/include
```

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```
- Execute ``make iog.so``

- Output of ``iog.py``

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```

1      cnfg hdnr  t      Re      Im
2  0    5350    0    0  591279.959489  0.000005
3  1    5350    0    1  522915.505562 -0.000003
4  2    5350    0    2  482360.005234 -0.000012
5  3    5350    0    3  440684.923986 -0.000002
6  4    5350    0    4  387859.756810  0.000004
7  ...    ...    ... ..      ...      ...
8 1147  5350    15   67   26763.208835  7141.283387
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15    -----
16
17    [591279.9594888687, 522915.5055618286,...
18    -----
19
20    [591279.95948887 522915.50556183 482360.00523376 ...

```

- Output of ``iog.py``

```

1      cnfg hdrn  t      Re      Im
2      0      5350   0   0 591279.959489  0.000005
3      1      5350   0   1 522915.505562 -0.000003
4      2      5350   0   2 482360.005234 -0.000012
5      3      5350   0   3 440684.923986 -0.000002
6      4      5350   0   4 387859.756810  0.000004
7      ...    ...   ... ..
8     1147    5350  15  67  26763.208835  7141.283387
9     1148    5350  15  68  42259.980047 12240.936307
10    1149    5350  15  69  79407.008466 17624.534133
11    1150    5350  15  70  141667.387280 25814.545022
12    1151    5350  15  71  245504.136076 36646.858214
13
14    [1152 rows x 5 columns]
15    -----
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17    [591279.9594888687, 522915.5055618286,...
18    -----
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20    [591279.95948887 522915.50556183 482360.00523376 ...

```

- Filter by value: ``iog.loc[18<=iog['t'].astype(int)]``
- Use logical operator: ``iog_pi=iog.loc[(iog['hdrn']=='0') & (iog['t'].astype(int)<18)]``

What is intrptr ? - iog convention

1		cnfg	hdrn	t		Re	Im
2	0	5350	0	0	591279.959489	0.000005	
3	1	5350	0	1	522915.505562	-0.000003	
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- ``hdrn`` (hadron) : ["PION", "KAON", "PROTON", "RHO", "D", "ETAS", "ETAC", "JPSI", "LAMBDA", "LAMBDAC", "SIGMA", "XI", "XIC", "OMEGA", "DELTA"]

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- ``t`` : time slice
- ``Re``, ``Im`` : real and imaginary part of two-point function

theoretically, 2pt should be real valued, but due to numerical errors, it may have a neglectable small imaginary part

more complicated iog convention (not in this traning camp)

1		cnfg	tsrc	lnk	snksmr	hdrn	mntm	t	Re	Im
2	0	2125	18	0	0	200505	505050	0	0.0	0.0
3	1	2125	18	0	0	200505	505050	1	0.0	0.0
4	...	...	...	..	...	...	...	...	...	...
5	4606	2125	18	0	1	100001515	505045	126	0.0	0.0
6	4607	2125	18	0	1	100001515	505045	127	0.0	0.0

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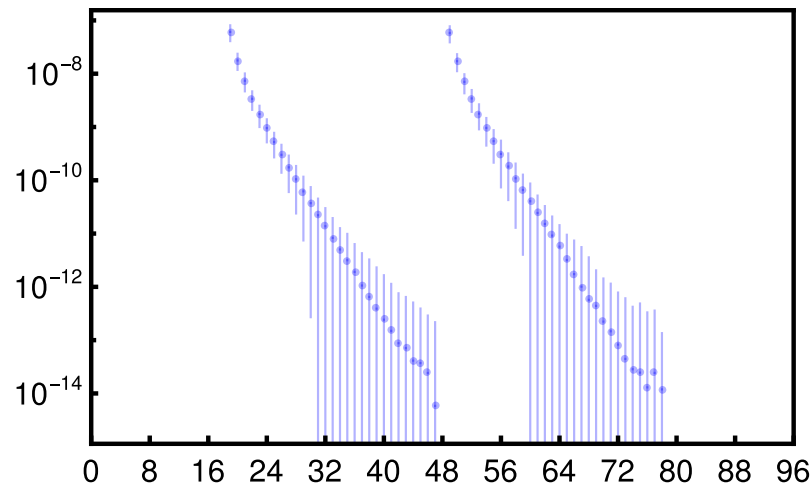
1		cnfg	tsrc	lnk	snksmr	hdrn	mntm	t	Re	Im
2	0	2125	18	0	0	200505	505050	0	0.0	0.0
3	1	2125	18	0	0	200505	505050	1	0.0	0.0
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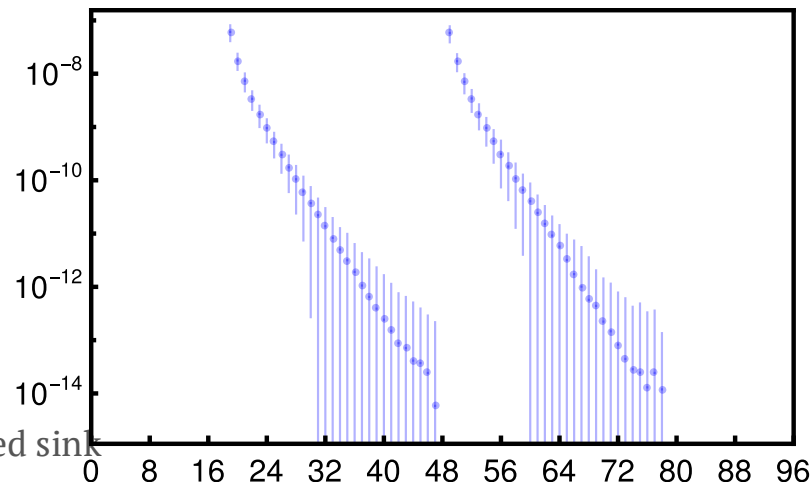
- ``cnfg``: configuration number
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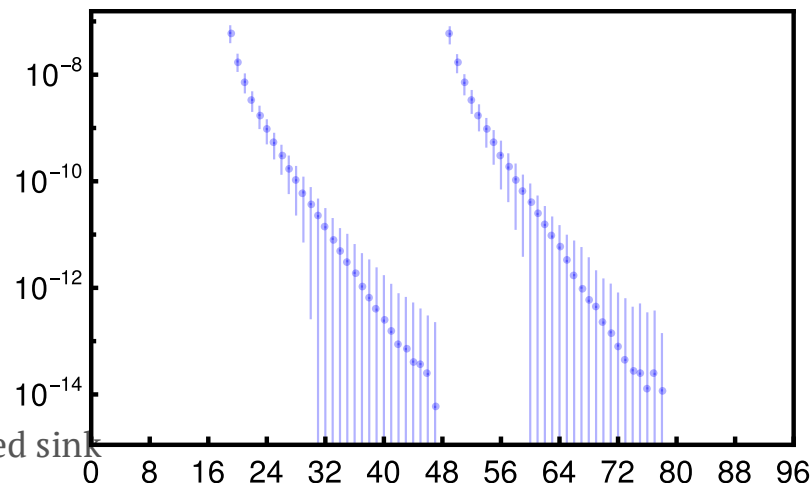
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- ``snksmr`` (sink smear): ``0`` $\Rightarrow$ unsmeared sink, ``1`` $\Rightarrow$ smeared sink



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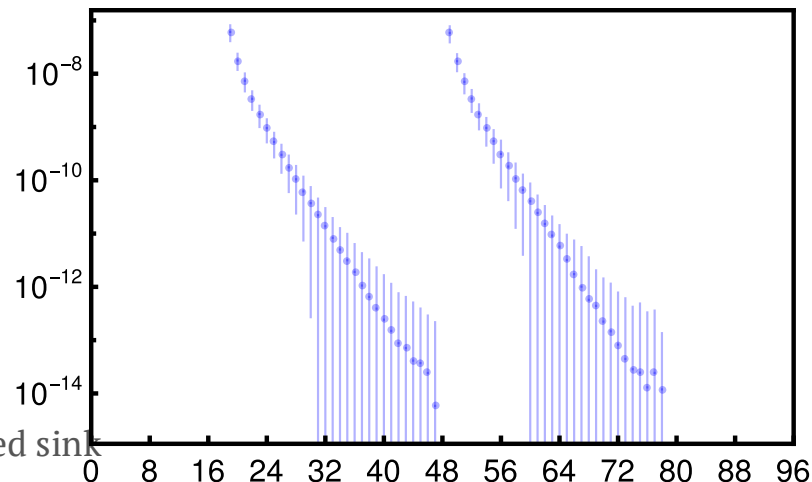
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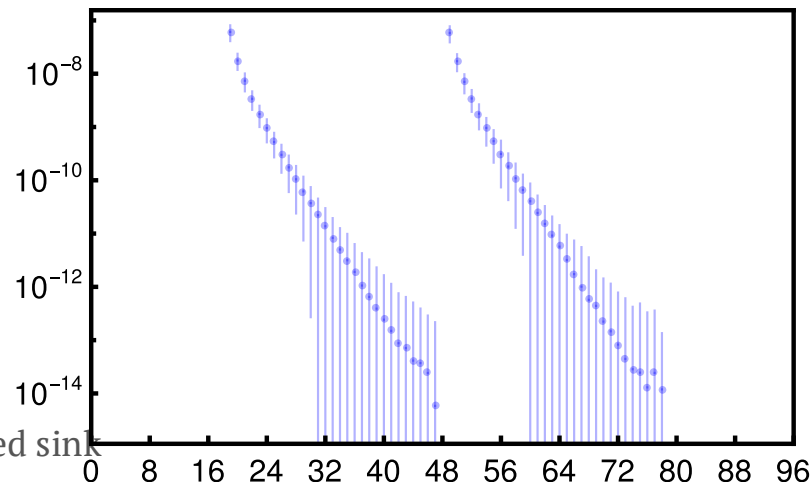
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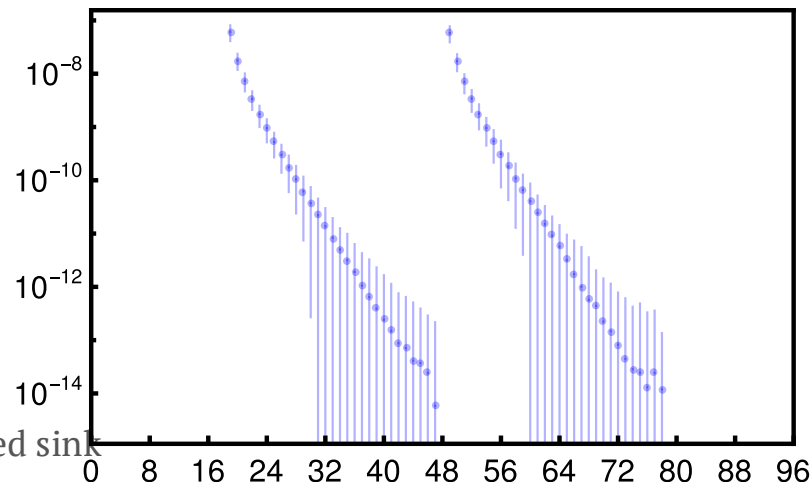
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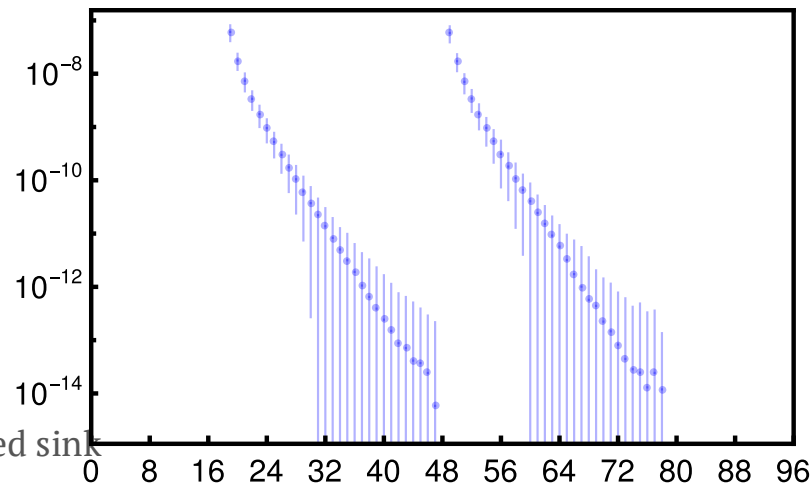
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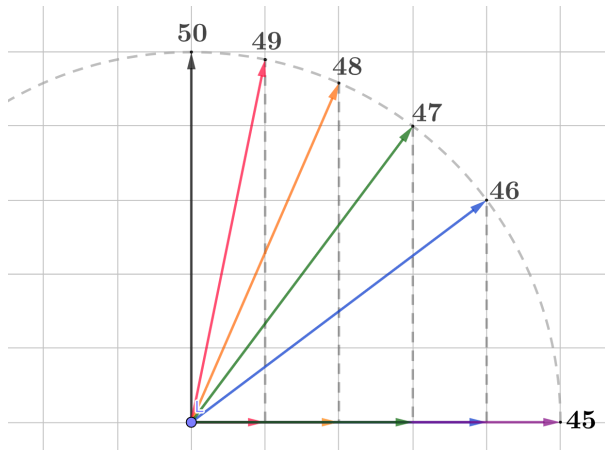
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- Momentum label (not used in this traning camp)

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- momentum : ``505050`` $\Leftrightarrow 50\ 50\ 50 \Leftrightarrow 0,0,0 \Leftrightarrow \vec{P} = (0,0,0)$
- lattice momentum unit: $\frac{2\pi}{L}, L = na$
Discretized Fourier transformation

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- lattice momentum unit: $\frac{2\pi}{L}, L = na$
Discretized Fourier transformation
- $\tilde{p}_x, \tilde{p}_y, \tilde{p}_z$, eg. 50 50 48
- $\vec{P} = [(50, 50, 50) - (\tilde{p}_x, \tilde{p}_y, \tilde{p}_z)] \times \frac{2\pi}{L} = (0, 0, 2) \times \frac{2\pi}{L} \Leftrightarrow 2 \text{ unit momentum in } z\text{-direction}$



Resampling

- Conventional resampling method
 - Jack-knife
 - Bootstrap

Why Resampling

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- Suppose $\mathcal{C}$ is directly calculate on the lattice, $\mathcal{O} = F(\langle \mathcal{C} \rangle)$ is what we are intrested in

F usually is a nonlinear function

- Usually, $\mathcal{O} = F(\langle \mathcal{C} \rangle) \neq \langle F(\mathcal{C}) \rangle$
- Error estimation of $\mathcal{O}$
 - usually, the target $\mathcal{O}$ has a complicate dependence (usually nonlinear) on lattice calculable $\mathcal{C}$
 - Error propagation $\sigma_{\mathcal{O}} \approx F'(\langle \mathcal{C} \rangle) \sigma_{\mathcal{C}}$?
 - 😭 F is nonlinear
 - 😭 $\sigma_{\mathcal{C}}$ is not small enough to neglect $\mathcal{O}(\sigma_{\mathcal{C}}^2)$ term

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Solution: Resampling

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- Original Datasets:
 - cnfg 1 $\Rightarrow \vec{C}^{(1)} = (C_0^{(1)}, \dots, C_t^{(1)})$
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 - cnfg $N \Rightarrow \vec{C}^{(N)} = (C_0^{(N)}, \dots, C_t^{(N)})$
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- $\tilde{C}^{(i)} = \frac{N}{N-1} \bar{C} - \frac{1}{N-1} \vec{C}^{(i)} \Rightarrow$ drop cnfg i , calculate mean value of the rest

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- i th Jack-knife sample
 - $\tilde{C}^{(i)} = \frac{N}{N-1} \bar{C} - \frac{1}{N-1} \vec{C}^{(i)} \Rightarrow$ drop cnfg i , calculate mean value of the rest
- Estimator
 - $\bar{C} = \frac{1}{N} \sum_i \vec{C}^{(i)} = \frac{1}{N} \sum_i \tilde{C}^{(i)}$
 - $\text{cov} = (N - 1) \times \tilde{\text{cov}}, \tilde{\text{cov}}$: covariance matrix of Jack-knife samples
 - $\sigma = \sqrt{N - 1} \times \tilde{\sigma}$

- Jackknife samples are highly correlated

- Mean of almost identical data

- $$\left(\tilde{C}^{(i)} - \bar{C}\right)^2 = \left(\frac{N}{N-1}\bar{C} - \frac{1}{N-1}\vec{C}^{(i)} - \bar{C}\right)^2 = \frac{1}{(N-1)^2} \left(\vec{C}^{(i)} - \bar{C}\right)^2$$

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2  # encoding: utf-8
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4  import numpy as np
5  from os import listdir
6  from iog_reader import iog_read
7  from re import match
8  import cProfile
9  from functools import reduce
10
11  iog_path = "./Data/"
12  T = 72
13
14  files = listdir(iog_path)
15  iogs = [file for file in files if match(r".*2pt.*.dat.iog",file)!=None]
16  Ncnfg = len(iogs)
17
18  c2pt = np.zeros((Ncnfg,T))
19  for indx in range(0,Ncnfg):
20      dat=iog_read(iog_path+iogs[indx],["cnfg","hdrn","t"])
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1  #!/usr/bin/env python3
2  # encoding: utf-8
3
4  import numpy as np
5  from os import listdir
6  from iog_reader import iog_read
7  from re import match
8  import cProfile
9  from functools import reduce
10
11  iog_path = "./Data/"
12  T = 72
13
14  files = listdir(iog_path)
15  iogs = [file for file in files if match(r".*2pt.*.dat.iog",file)!=None]
16  Ncnfg = len(iogs)
17
18  c2pt = np.zeros((Ncnfg,T))
19  for indx in range(0,Ncnfg):
20      dat=iog_read(iog_path+iogs[indx],["cnfg","hdrn","t"])
21      c2pt[indx] = dat.loc[(dat["hdrn"]=="0")]["Re"].to_numpy()
22
23  c2pt_jcknf_1 = np.zeros((Ncnfg,T))
24  c2pt_jcknf_2 = np.zeros((Ncnfg,T))
```

Coding tips

- Vectorize your code instead of using loop

```
1      115780 function calls in 0.082 seconds
2      Ordered by: standard name
3      ncalls  tottime  percall  cumtime  percall filename:lineno(function)
4      4824    0.003    0.000    0.039    0.000 <__array_function__ internals>:177(delete)
5      4824    0.002    0.000    0.036    0.000 <__array_function__ internals>:177(mean)
6      .....
7      -----
8      1612 function calls in 0.001 seconds
9      Ordered by: standard name
10     ncalls  tottime  percall  cumtime  percall filename:lineno(function)
11     67     0.000    0.000    0.001    0.000 <__array_function__ internals>:177(delete)
12     67     0.000    0.000    0.001    0.000 <__array_function__ internals>:177(mean)
13     .....
14     -----
15     13 function calls in 0.000 seconds
16     Ordered by: standard name
17     ncalls  tottime  percall  cumtime  percall filename:lineno(function)
18     1     0.000    0.000    0.000    0.000 <__array_function__ internals>:177(sum)
19     1     0.000    0.000    0.000    0.000 <string>:1(<module>)
20     .....
21     -----
22     [ True  True  True  True  True  True  True  True  True  True  True  True  True .....
23
24     c2pt_jcknf_2 = np.zeros((Ncnfg,T))
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 - Randomly (uniformly) sample N cnfgs from original datasets, **allow repetition**,
 - $\tilde{C}^{(i)} \Rightarrow$ mean of previously sampled data
- Repeat resampling M times, $M > N$, usually $M \sim \mathcal{O}(10^3)$
 - resampled dataset $\Rightarrow (\tilde{C}^{(1)}, \dots, \tilde{C}^{(M)})$

- Estimator

- $\bar{C} = \frac{1}{N} \sum_i \vec{C}^{(i)} = \frac{1}{N} \sum_i \tilde{C}^{(i)}$

- $\text{cov} = \tilde{\text{cov}}, \tilde{\text{cov}}$: covariance matrix of bootstrap samples

- $\sigma = \tilde{\sigma}$

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- Central value $\bar{\mathcal{O}} = \bar{\tilde{\mathcal{O}}}$
- Error estimation
 - Jack-knife resample $\Leftrightarrow \sigma_{\mathcal{O}} = \sqrt{N-1} \times \sigma_{\tilde{\mathcal{O}}}$
 - Bootstrap resample $\Leftrightarrow \sigma_{\mathcal{O}} = \sigma_{\tilde{\mathcal{O}}}$

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- Parallel your code to do $F(\tilde{C}^{(i)})$
 - e.g. MPI: each process calculate one $F(\tilde{C}^{(i)})$

Least fit

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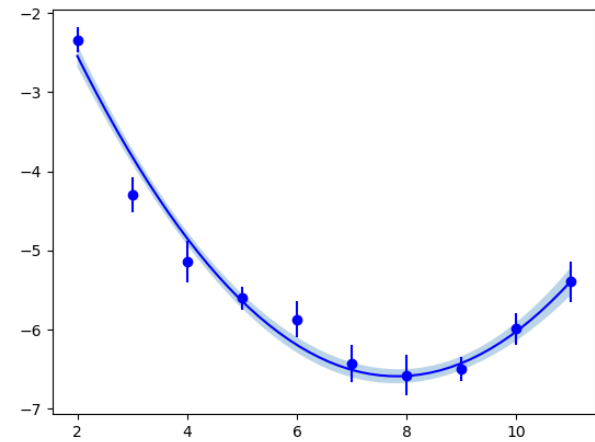
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 $\left[\begin{array}{l} 0 \dots T: \text{time slice indices} \\ 0 \dots N: \text{cnfg indices} \end{array} \right.$
- Model: $f(t, \{p_i\})$
 - t : time slices (w.r.t source)
 - $\{p_i\}$: fit parameters $\Rightarrow c_0, c_1, E_0, \Delta E$
 - e.g. For two-point function (two-state fit)

$$f(t, \{p_i\}) \implies c_0 e^{-E_0 t} (1 + c_1 e^{-\Delta E t})$$

χ^2 definition

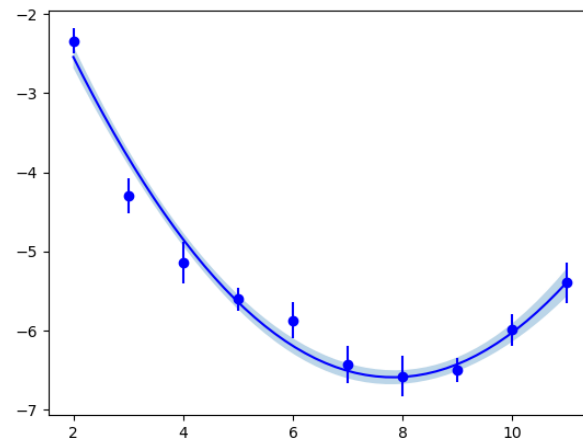


χ^2 definition

- Uncorrelated case

$$\chi^2 = \sum_t \frac{[\bar{C}_t - f(t, \{p_i\})]^2}{\sigma_t^2}$$

- $\bar{C}_t \Leftrightarrow$ mean value of the t -th timeslices
- $\sigma_t \Leftrightarrow$ standard deviation of the t -th timeslices
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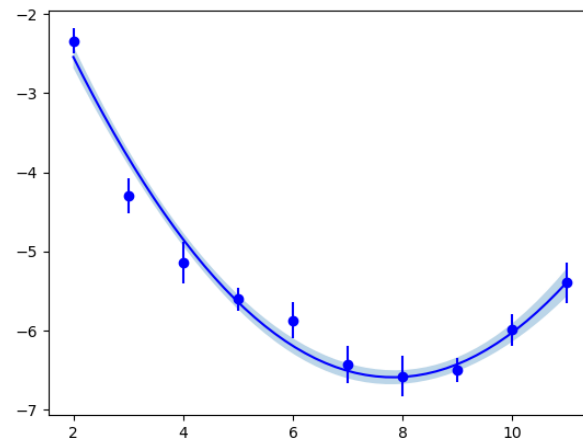
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$$\chi^2 = \sum_{t,t'} [\bar{C}_t - f(t, \{p_i\})] (\text{cov}^{-1})_{t,t'} [\bar{C}_{t'} - f(t', \{p_i\})]$$

- COV : covariance matrix

$$(\text{cov})_{t,t'} = \frac{1}{N-1} \sum_i (C_t^{(i)} - \bar{C}_t)(C_{t'}^{(i)} - \bar{C}_{t'})$$



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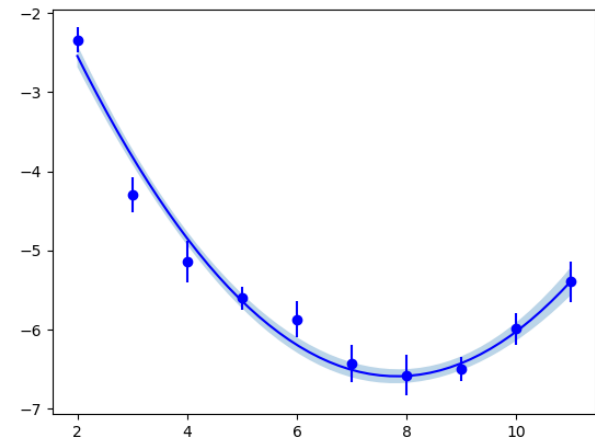
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- ``numpy``: ``numpy.mean``, ``numpy.std``, ``numpy.cov`` support high rank tensors
 - Set ``axis`` parameter in numpy function
 - e.g. $\mathbf{R} = R_{i,j,k,l}, i = 1, \dots, n_0, j = 1, \dots, n_1, k = 1, \dots, n_2, l = 1, \dots, n_3$
 - Assuming ``R, R'`` are ``numpy`` arrays
 - ``S=np.mean(R,axis=1)`` $\Leftrightarrow S_{i,k,l} = \frac{1}{n_1} \sum_j R_{i,j,k,l}$
 - ``R*R'`` $\Rightarrow (R * R')_{i,j,k,l} = R_{i,j,k,l} \times R'_{i,j,k,l}$

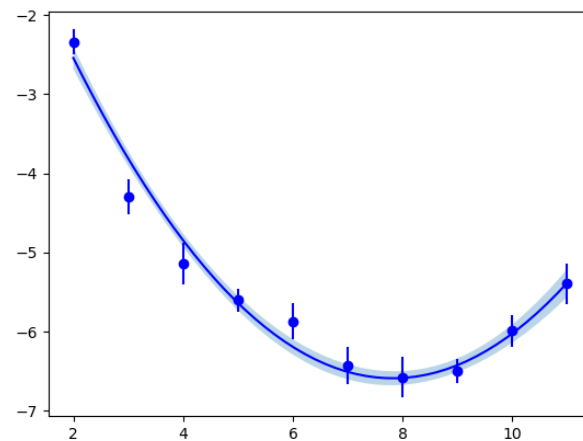
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- Not sure about which axis? Print out the shape of `R, S`: ``R.shape``, ``S.shape``

- $\chi^2 \Rightarrow$ measure the deviation between data and model



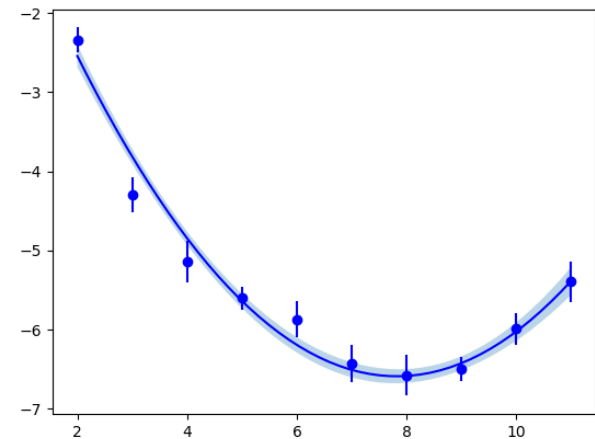
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- least χ^2 fit $\Rightarrow$ optimize $\{p_i\}$ for minimal **BUT resonable** χ^2
- ``lsqfit`` $\Rightarrow$ a python package perform *least χ -square fit*

```
1 fit = lsqfit.nonlinear_fit(data=(var_val, dat_val),
2                             fcn=model, prior=ini_val, debug=False)
```

- ``var_val`` : value of variables $\Rightarrow x$ -axis
- ``dat_val`` : value of datas (with erros) $\Rightarrow y$ -axis (with err/co ,
- ``model`` : fit model function
- ``ini_val`` : initial values of (also constrains on) fit parameters in ``model``



`lsqfit` - an example

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5  import lsqfit
6  import numpy as np
7  import matplotlib.pyplot as plt
8
9  c2pt_raw = np.load("./data_2pt.npy")
10 c2pt = c2pt_raw[:, 0, :, -2]
11 Ncnfg = c2pt.shape[0]
12 T = c2pt.shape[1]
13 T_hlf = T//2
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15 #? jack-knife resample
16 #! only used in plot , compare original data with fit
17 c2pt_sum = np.sum(c2pt,axis=0)
18 c2pt_jcknf = ((c2pt_sum) - c2pt)/(Ncnfg-1) # jack-knife resample
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20 c2pt_err = np.sqrt(Ncnfg-1)*np.std(c2pt_jcknf,axis=0) # jack-knife std
21
22 #? drop the first data point, normalized to c2[1] ~ 1
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1  #!/usr/bin/env python3
2  # encoding: utf-8
3
4  import gvar as gv
5  import lsqfit
6  import numpy as np
7  import matplotlib.pyplot as plt
8
9  c2pt_raw = np.load("./data_2pt.npy")
10 c2pt = c2pt_raw[:, 0, :, -2]
11 Ncnfg = c2pt.shape[0]
12 T = c2pt.shape[1]
13 T_hlf = T//2
14
15 #? jack-knife resample
16 #! only used in plot , compare original data with fit
17 c2pt_sum = np.sum(c2pt,axis=0)
18 c2pt_jcknf = ((c2pt_sum) - c2pt)/(Ncnfg-1) # jack-knife resample
19 c2pt_cntrl = np.mean(c2pt_jcknf,axis=0) # jack-knife mean
20 c2pt_err = np.sqrt(Ncnfg-1)*np.std(c2pt_jcknf,axis=0) # jack-knife std
21
22 #? drop the first data point, normalized to c2[1] ~ 1
23 t_ary = np.array(range(1,T))
24 c2pt_jcknf = c2pt_jcknf/c2pt_cntrl[1]
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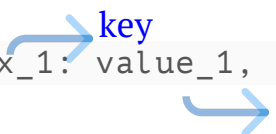
`lsqfit` - an example

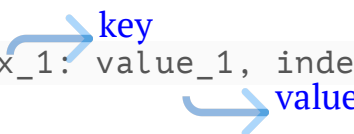
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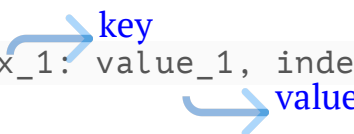
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- Example

```
1  dct = {"a":1.0, "b":2.0}  
2  dct["a"]
```

- Why wrap data in dictionaries?
 - Consider the case of
 - fit 2 datasets with 2 models
 - 2 models may have shared parameters

Combined fit

- Combined fit: e.g. 2 data sets, 2 models (with shared parameters)

label	label1	label2
data	$(\vec{x}^{(1)}, \vec{y}^{(1)})$	$(\vec{x}^{(2)}, \vec{y}^{(2)})$
model	$f(x, \{\vec{p}, \vec{q}\})$	$g(x, \{\vec{p}, \vec{r}\})$
ini_val	$\vec{p}_0, \vec{q}_0$	$\vec{p}_0, \vec{r}_0$

- $\vec{p}$ denotes the shared parameters

- Wrapping data for combined fit

```

1  var_val = {'label1': [x1_1,x1_2,...], 'label2': [x2_1,x2_2,...]
2
3  dat_val = {'label1': [y1_1,y1_2,...], 'label2': [y2_1,y2_2,...]
4
5  prior = {'p_1': p_1, 'p_2': p_2, ..., 'q_1': q_1, 'q_2': q_2, ..., 'r_1': r_1, 'r_2': r_2}

```

- ``y_1,2`:gvar class`  $\Rightarrow$  ``y_1 = gvar(y_1_cntrl, y_1_cov)` ...`
- ``p_1,2`:gvar class`  $\Rightarrow$  ``p_1 = gvar(p_1_cntrl, p_1_err)` ...`
- Feed the ``var_val``, ``dat_val`` and ``prior`` to ``lsqfit.nonlinear_fit``

Wrapping model for combined fit

```

1  def fit_mdls(t_dctnry, p):
2      mdls = {}
3      mdls['label1'] = ...
4      mdls['label2'] = ...
5      return mdls

```

Multiple/Single source, Open/Periodic boundary condition

Multiple/Single source, Open/Periodic boundary condition

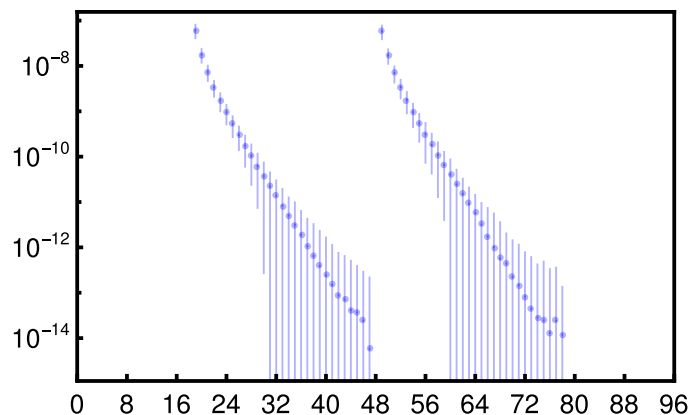
- Put multiple source in time direction to increase the statistics

Multiple/Single source, Open/Periodic boundary condition

- Put multiple source in time direction to increase the statistics
- Average over sources within each config (iog file)

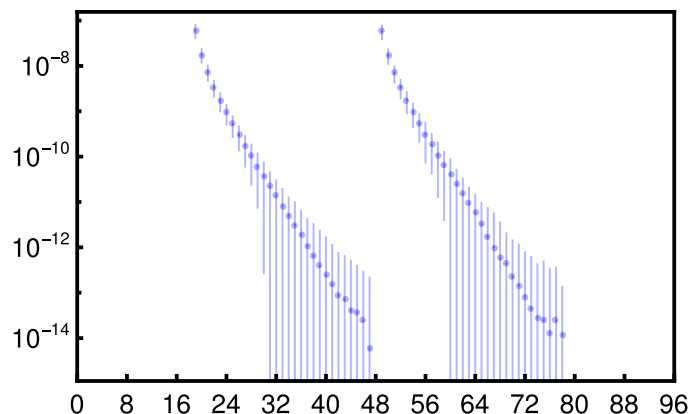
Multiple/Single source, Open/Periodic boundary condition

- Put multiple source in time direction to increase the statistics
- Average over sources within each config (iog file)
- Example of open boundary condition, two sources



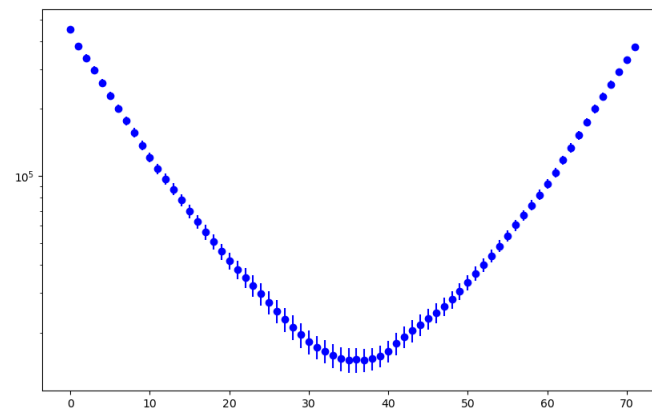
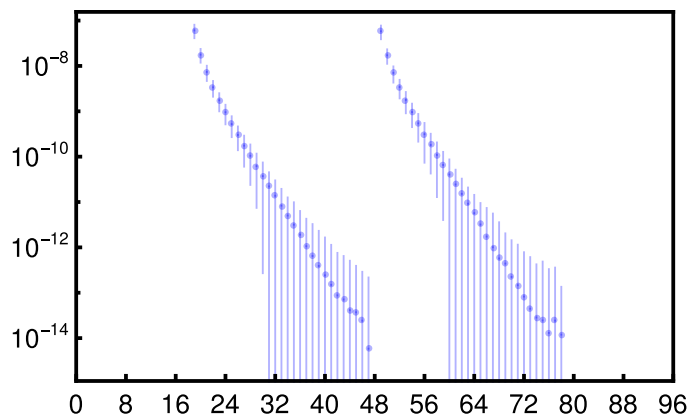
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- Put multiple source in time direction to increase the statistics
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- Example of open boundary condition, two sources
- Single source, periodic boundary condition
- Example
 - $C(T + a) = C(0)$
 - $C(t) \approx C_0 e^{-E_0 \frac{T}{2}} \cosh \left[E_0 \left(\frac{T}{2} - t \right) \right]$



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Fit Results - A glance

```
1 Least Square Fit:
2   chi2/dof [dof] = 0.96 [20]    Q = 0.5    logGBF = 116.43
3
4 Parameters:
5   c0      0.252 (10)    [ 0.0 (5.0) ]
6   E0      0.1090 (27)  [ 0.20 (50) ]
```

- Fences: two-point function data
- Bands: fitted model

Error has been magnified with factor of 5 in figure

- Fited effective mass: $E_0 =$
 - The fitted E_0 is in lattice unit.
 - $E_0 t$ in $e^{-E_0 t}$ must be dimensionless $\Rightarrow E_0 = \frac{E_{0,\text{latt.}} \times 0.1973}{a} [\text{GeV}]$

Output log

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8 Fit:
9     key          y[key]      f(p)[key]
10    -----
11    c2pt 0      0.277 (12)    0.2712 (79)
12           1      0.248 (11)    0.2435 (74)
13           2      0.223 (11)    0.2186 (69)
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23          12      0.0825 (68)    0.0773 (42)
24          13      0.0758 (66)    0.0703 (41)
```

Print this detailed log by setting `print(fit.format(True))`

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25          14      0.0701 (64)    0.0644 (39)
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Access the fitted model function

```
1  fit = lsqfit.nonlinear_fit(data=(tsep_dctnry, c2pt_dctnry),  
2  fcn=ft_mdls, prior=ini_prr, debug=True)  
3  
4  c2pt_fit_gvar = fit.fcn({'c2pt':t_lst}, fit.p)['c2pt']
```

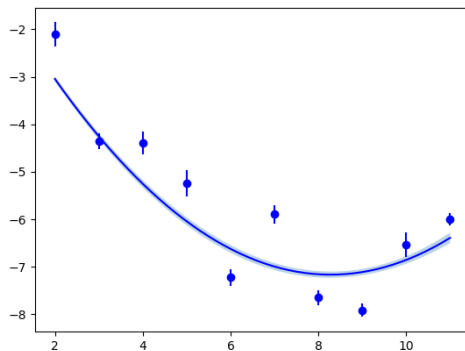
- `tsep_dctnry = {'c2pt':np.array(range(T_strt,T_end))}`
- `fit.p` $\Rightarrow$ fitting parameter, dictionary
 - `fit.p['E0']`

What is a reasonable fit?

Case 1

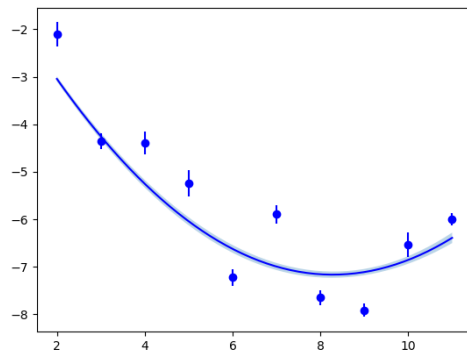
What is a reasonable fit?

Case 1



What is a reasonable fit?

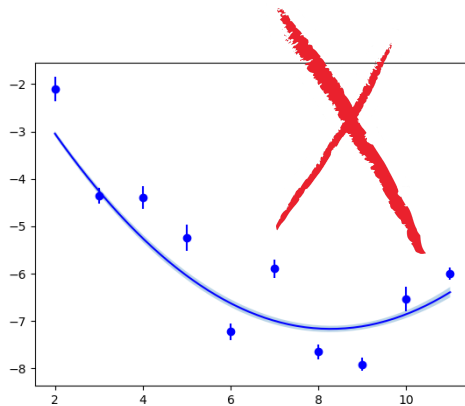
Case 1



```
1 Least Square Fit:
2   chi2/dof [dof] = 13 [10]
3   Q = 5.2e-24
4   logGBF = -74.281
```


What is a reasonable fit?

Case 1

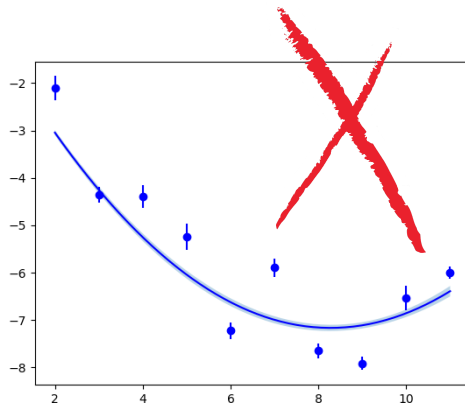


```
1 Least Square Fit:  
2 chi2/dof [dof] = 13 [10]  
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```

- Underfit
 - Model failed to describe data

What is a reasonable fit?

Case 1



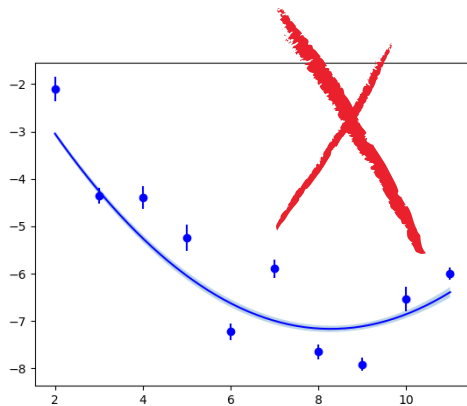
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- Underfit
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Case 2

What is a reasonable fit?

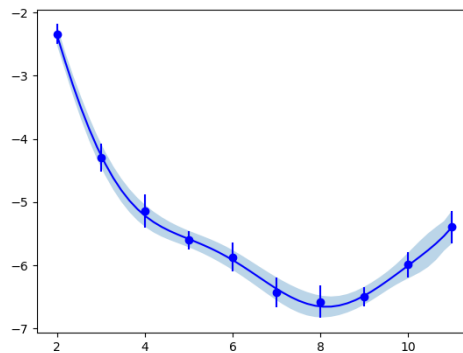
Case 1



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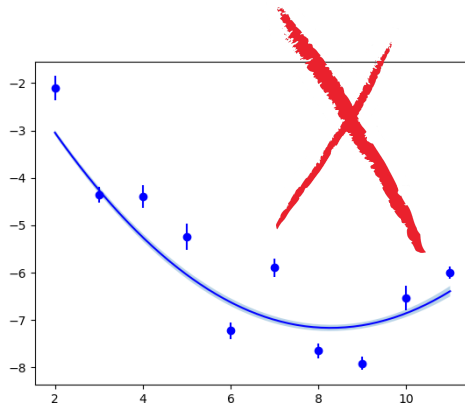
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Case 2



What is a reasonable fit?

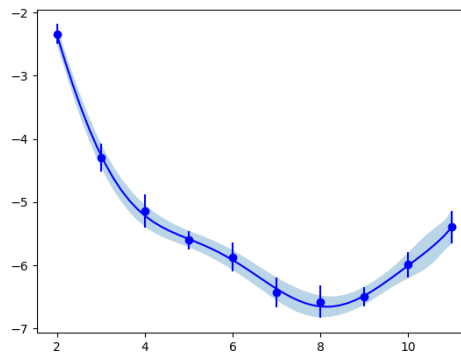
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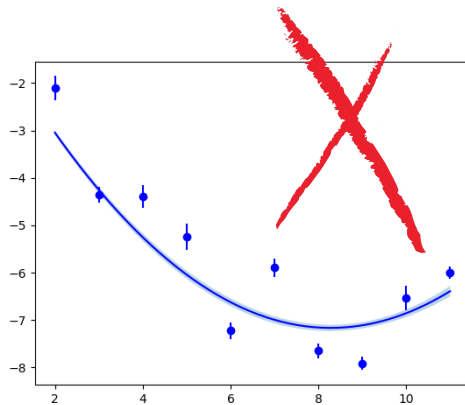
Case 2



```
1 Least Square Fit:
2   chi2/dof [dof] = 0.07 [10]
3   Q = 1
4   logGBF = -46.654
```

What is a reasonable fit?

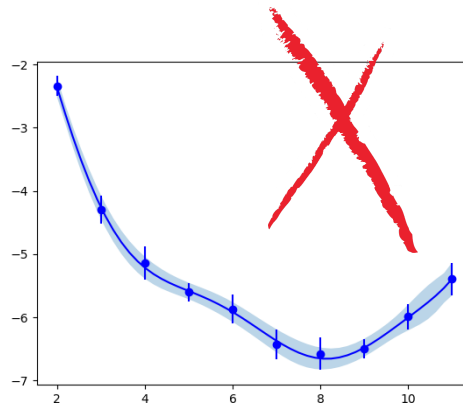
Case 1



```
1 Least Square Fit:
2   chi2/dof [dof] = 13 [10]
3   Q = 5.2e-24
4   logGBF = -74.281
```

- Underfit
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Case 2

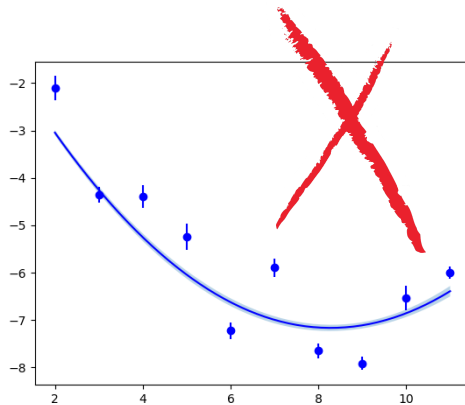


```
1 Least Square Fit:
2   chi2/dof [dof] = 0.07 [10]
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```

- Over fit
 - Try to extract too much info from data

What is a reasonable fit?

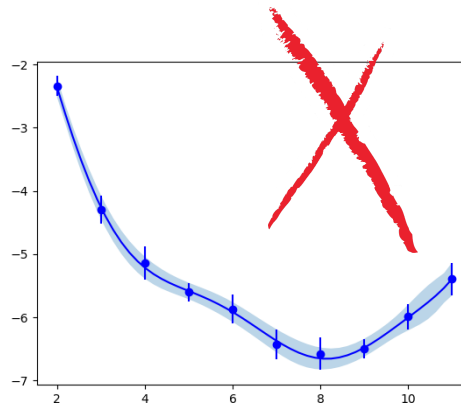
Case 1



```
1 Least Square Fit:
2   chi2/dof [dof] = 13 [10]
3   Q = 5.2e-24
4   logGBF = -74.281
```

- Underfit
 - Model failed to describe data

Case 2



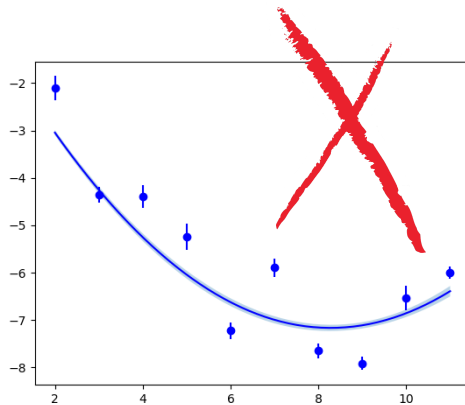
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```

- Over fit
 - Try to extract too much info from data

Case 3

What is a reasonable fit?

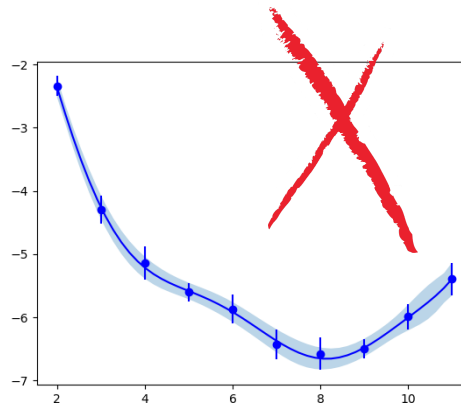
Case 1



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2   chi2/dof [dof] = 13 [10]
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- Underfit
 - Model failed to describe data

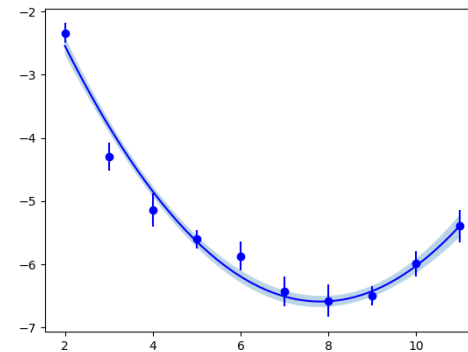
Case 2



```
1 Least Square Fit:
2   chi2/dof [dof] = 0.07 [10]
3   Q = 1
4   logGBF = -46.654
```

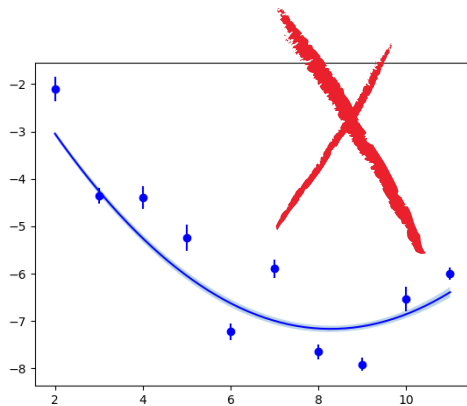
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Case 3



What is a reasonable fit?

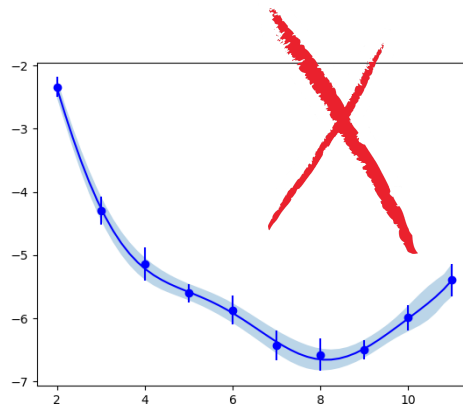
Case 1



```
1 Least Square Fit:
2 chi2/dof [dof] = 13 [10]
3 Q = 5.2e-24
4 logGBF = -74.281
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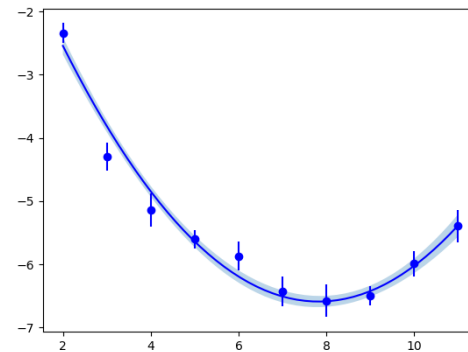
Case 2



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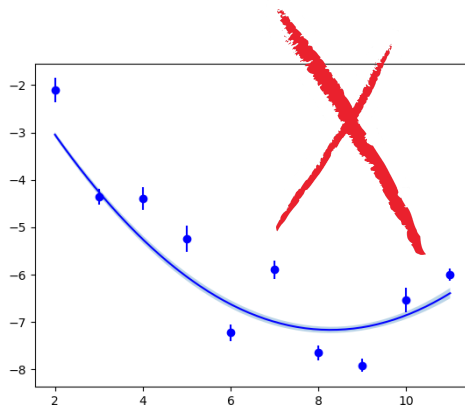
Case 3



```
1 Least Square Fit:
2 chi2/dof [dof] = 1 [10]
3 Q = 0.41
4 logGBF = -15.05
```


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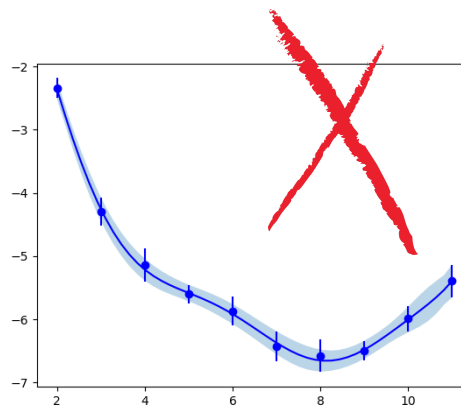
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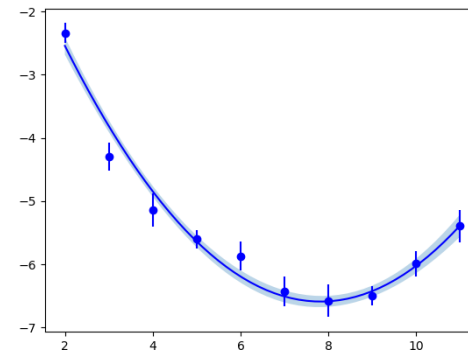
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- *Reasonable fit*

How good is a fit?

Interpretation of ``lsqfit`` log

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 - Good fits have Q values larger than 0.1 or so
- `logGBF`: $\ln P(\text{data}|\text{fit}) \Leftrightarrow$ Probability of obtaining the data by randomly sampling the fitted model
 - Useful for comparing fits of the same data to different models, with different priors and/or fit functions.
 - The model with the largest value of `logGBF` is the one preferred by the data.
 - Differences in `fit.logGBF` smaller than 1 are not very significant.

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 - e.g. in 2-point analysis demo
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- Version control (git, SVN)

Exercises

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For this exercise: lattice spacing: 0.108 fm , $m_\pi \approx 200 \text{ MeV}$

Hint:

Hint:

- ``iog_reader`, `pandas.DataFrame.loc`, `pandas.DataFrame.to_numpy`,
`numpy.mean`, `numpy.cov`, `numpy.std`, `lsqfit.nonlinear_fit``
- ``Data`` containing the 50 two-point function iog data files, from 50 configuration
- 72 lattice spacings in time direction
- ``iog_reader`` is provided in ``iog_read_demo.py``
- ``x=gvar.gvar('2(0.5)')`` : ``x.mean`` $\Rightarrow$ ``2.00``, ``x.sdev`` $\Rightarrow$ ``0.50``
- Construct gvar from tuple ``x=gvar.gvar((2.0.5))``

Notes

- `Python` indices starts from 0, *Mathematica*, Julia starts from 1
- `numpy.ndarray` slice, range do not include the last index e.g.
 - `a[2:5]` $\Leftrightarrow [a_2, a_3, a_4]$
 - `range(2, 5)` $\Leftrightarrow [2, 3, 4]$
- `iog_read.py` returns `pandas.DataFrame`, columns in this data frame are strings (not integers)

III. Linux Basics

- If windows

- try WSL

<https://docs.microsoft.com/zh-cn/windows/wsl/install>

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- Online forum

- <https://unix.stackexchange.com/>

- <https://stackoverflow.com/>

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- Autocomplete/suggestions
 - Press `Tab``

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- Similar for copy ``cp`` and move(rename) ``mv``

cat, grep, >

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- compress ``tar``
 - try ``tar --help``

SSH login

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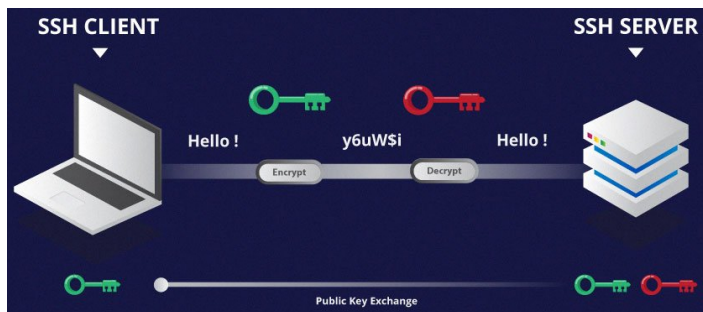
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- ``ssh usr@host``
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 - ``usr``: username, ``host``: remote machine
- Use ``key`` instead of password
 - ``ssh-keygen``: generate RSA key (public and private)
 - distribute pubkey ``id_rsa.pub`` to others
 - keep your private key ``id_rsa`` private
 - ``ssh-copyid usr@host``: install your pubkey to host



SSH login

- SSH config file

- `~/.ssh/config`

```
1 Host sjtu
2   HostName sylogin.hpc.sjtu.edu.cn
3   User stu1947
4   IdentityFile /home/chimaoshu/.ssh/id_rsa
5   AddKeysToAgent yes
```

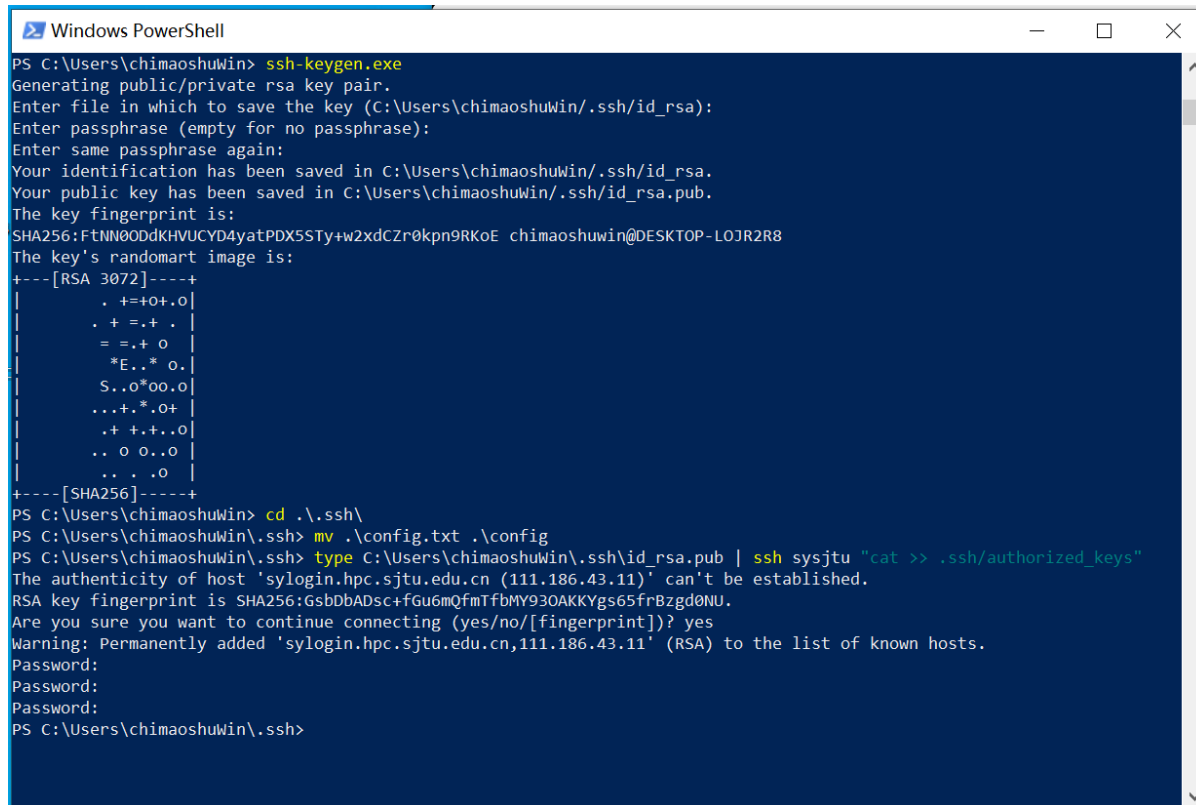
- After setting ssh config file $\Rightarrow$ `ssh sjtu`

SSH via Windows powershell (But recommend using vscode)

- `powershell` has built-in `ssh.exe`, `ssh-keygen.exe`, `scp.exe`

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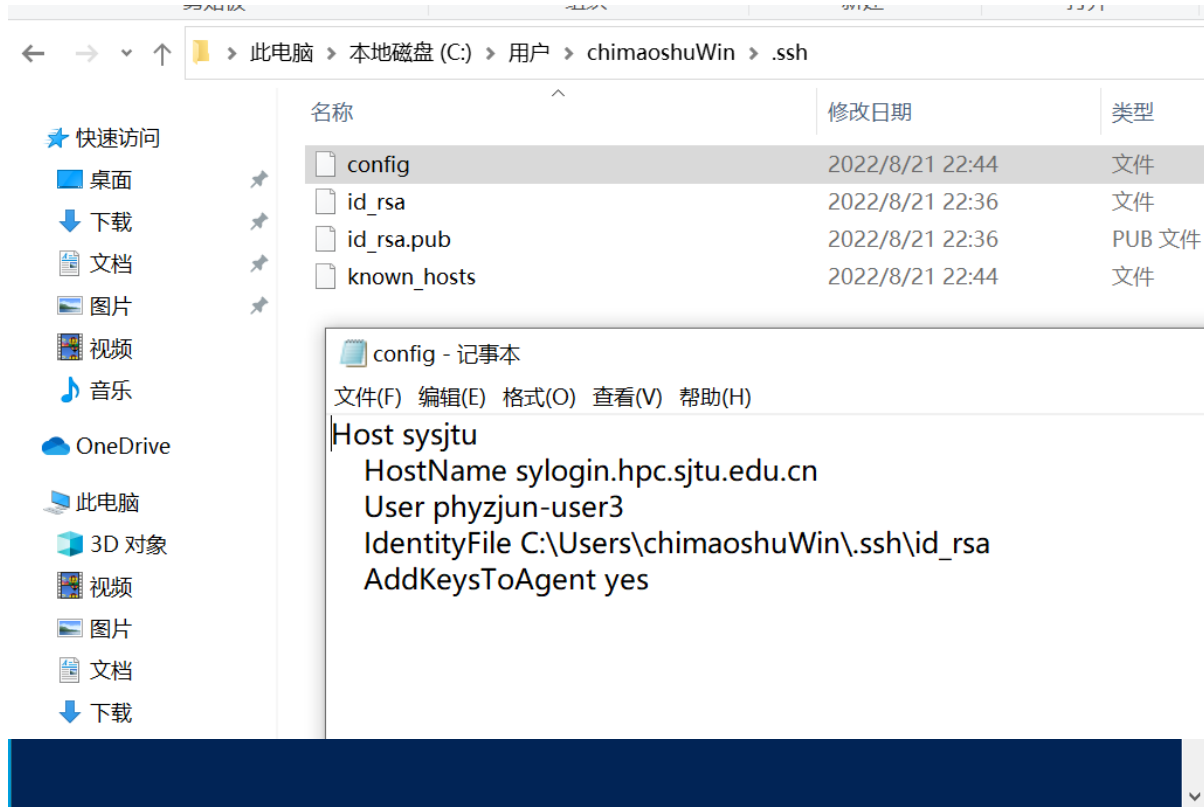
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```
Windows PowerShell
PS C:\Users\chimaoshuWin> ssh-keygen.exe
Generating public/private rsa key pair.
Enter file in which to save the key (C:\Users\chimaoshuWin/.ssh/id_rsa):
Enter passphrase (empty for no passphrase):
Enter same passphrase again:
Your identification has been saved in C:\Users\chimaoshuWin/.ssh/id_rsa.
Your public key has been saved in C:\Users\chimaoshuWin/.ssh/id_rsa.pub.
The key fingerprint is:
SHA256:FtNN0DDdKHVUCYD4yatPDX5STy+w2xdCZr0kpn9RKoE chimaoshuwin@DESKTOP-LOJR2R8
The key's randomart image is:
+---[RSA 3072]-----+
|  . +=+O+.O |
|  . + =.+ . |
|  = =.+ O |
|  *E..* O. |
|  S..O*oo.O |
|  ...+.*.O+ |
|  .+ +.+..O |
|  .. O O..O |
|  .. . .O |
+---[SHA256]-----+
PS C:\Users\chimaoshuWin> cd .\ssh\
PS C:\Users\chimaoshuWin\.ssh> mv .\config.txt .\config
PS C:\Users\chimaoshuWin\.ssh> type C:\Users\chimaoshuWin\.ssh\id_rsa.pub | ssh sysjtu "cat >> .ssh/authorized_keys"
The authenticity of host 'sylogin.hpc.sjtu.edu.cn (111.186.43.11)' can't be established.
RSA key fingerprint is SHA256:GsbDbADsc+fGu6mQfmTfbMY93OAKKYgs65frBzgd0NU.
Are you sure you want to continue connecting (yes/no/[fingerprint])? yes
Warning: Permanently added 'sylogin.hpc.sjtu.edu.cn,111.186.43.11' (RSA) to the list of known hosts.
Password:
Password:
Password:
PS C:\Users\chimaoshuWin\.ssh>
```

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```
OpenSSH SSH client
PS C:\Users\chimaoshuWin> ssh sysjtu
Password:
Last login: Sun Aug 21 23:12:52 2022 from 42.48.113.177
slurm常用指令:
  squeue 查看队列状态和信息
  sacct 显示用户作业历史
  squeue 显示当前作业状态
  sbatch 提交作业
  scancel 取消指定作业

集群设置以下队列，使用限制与说明如下：
    允许单作业CPU核数为1~60000，每核配比8G内存；单节点配置为64核，512G内存
    允许单作业GPU卡数为1~92，每卡配比CPU上限为16，每核配比8G内存；单节点配置为64核，512G内存，4块40G显存的A100 GPU卡
    仅用于短时间测试，请勿批量投递作业进行完整计算。作业最多申请2节点，运行60分钟，每核配比8G内存；单节点配置为64核，512G内存
    仅用于短时间测试，请勿批量投递作业进行完整计算。作业最多申请1节点，运行20分钟；单节点配置64核，512G内存，2块56G显存的虚拟GPU卡

用户帮助文档: https://docs.hpc.sjtu.edu.cn/

登陆节点禁止运行作业和并行编译，如需交互操作，请申请计算资源: $ srun -p 64c512g -n 4 --pty /bin/bash

登陆节点不适合进行大批量数据传输，请通过传输节点data.hpc.sjtu.edu.cn进行数据拷贝，参考 https://docs.hpc.sjtu.edu.cn/transport

邮件支持: hpc@sjtu.edu.cn
acct-phyzjun账户存储使用量为: 2.5T
phyzjun-user3用户存储使用量为: 2.0G

[phyzjun-user3@sylogin1 ~]$
```

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Password:
Last login: Sun Aug 21 23:12:52 2022 from 42.48.113.177
slurm常用指令:
  squeue 查看队列状态和信息
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    仅用于短时间测试，请勿批量投递作业进行完整计算。作业最多申请2节点，运行60分钟，每核配比8G内存；单节点配置为64核，512G内存
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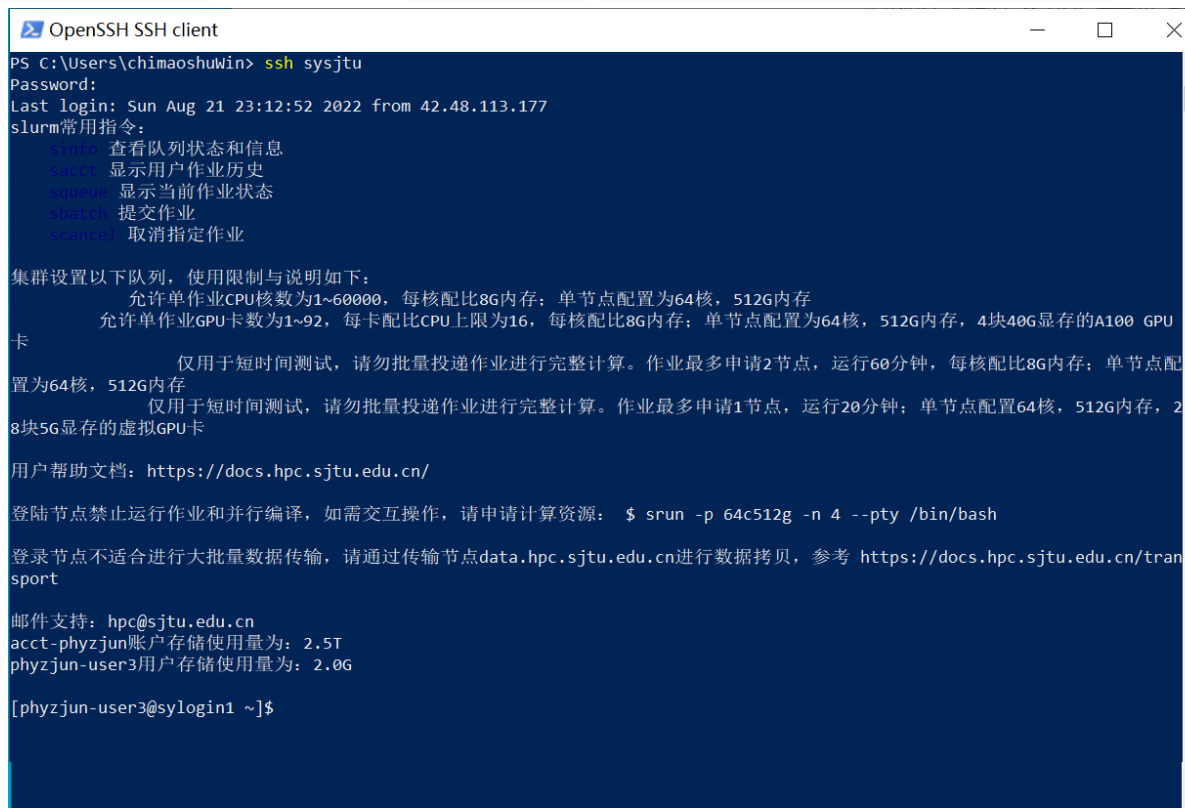
登陆节点不适合进行大批量数据传输，请通过传输节点data.hpc.sjtu.edu.cn进行数据拷贝，参考 https://docs.hpc.sjtu.edu.cn/transport

邮件支持: hpc@sjtu.edu.cn
acct-phyzjun账户存储使用量为: 2.5T
phyzjun-user3用户存储使用量为: 2.0G

[phyzjun-user3@sylogin1 ~]$
```

SSH via Windows powershell (But recommend using vscode)

- `powershell` has built-in `ssh.exe`, `ssh-keygen.exe`, `scp.exe`



```
OpenSSH SSH client
PS C:\Users\chimaoshuWin> ssh sysjtu
Password:
Last login: Sun Aug 21 23:12:52 2022 from 42.48.113.177
slurm常用指令:
  squeue 查看队列状态和信息
  sacct 显示用户作业历史
  squeue 显示当前作业状态
  sbatch 提交作业
  scancel 取消指定作业

集群设置以下队列，使用限制与说明如下:
  允许单作业CPU核数为1~60000，每核配比8G内存；单节点配置为64核，512G内存
  允许单作业GPU卡数为1~92，每卡配比CPU上限为16，每核配比8G内存；单节点配置为64核，512G内存，4块40G显存的A100 GPU卡
  仅用于短时间测试，请勿批量投递作业进行完整计算。作业最多申请2节点，运行60分钟，每核配比8G内存；单节点配置为64核，512G内存
  仅用于短时间测试，请勿批量投递作业进行完整计算。作业最多申请1节点，运行20分钟；单节点配置64核，512G内存，2块56G显存的虚拟GPU卡

用户帮助文档: https://docs.hpc.sjtu.edu.cn/

登录节点禁止运行作业和并行编译，如需交互操作，请申请计算资源: $ srun -p 64c512g -n 4 --pty /bin/bash

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```

- `ssh-copy-id` equivalent: `type path_to_id_rsa.pub | ssh sjtu "cat >> ~/.ssh/authorized_keys"`

Copy between local and remote machines

- ``scp source target`,(`scp` = `s`(ssh) + `cp`)` e.g.

- ``scp ./demo/lsqfit_2pt.py sysjtu:~/demo``

- ``scp -r sjtu:~/demo /home/chimaoshu``

``sjtu`` could be replaced by ``usr@host`` if ``.ssh/config`` is not set

Modify files on remote machine

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- vi, vim

🔗 Q: How do you generate a random string?

A: Put a Windows user in front of vi, and tell them to exit



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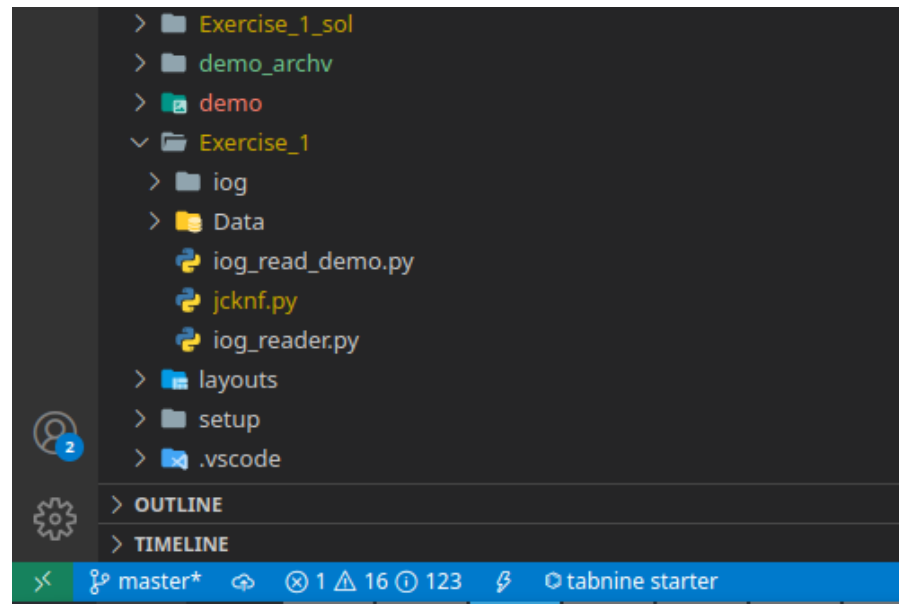
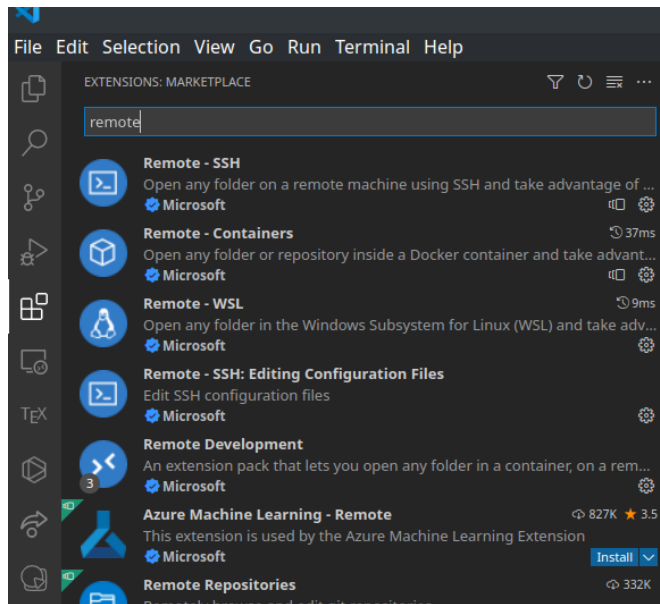
- Download to local $\Rightarrow$ edit locally $\Rightarrow$ upload to remote $\Rightarrow$ compile/execute $\Rightarrow$ download to local,...
- Recommended: vscode + remote development extension

<https://code.visualstudio.com/docs/remote/ssh-tutorial>

```
better set `ssh/config`
```

vscode

- <https://code.visualstudio.com/Download>
- Extensions
 - Remote Development



vscode

- <https://code.visualstudio.com/Download>
- Extensions
 - Python by Microsoft
 - Pylint by Microsoft
 - C/C++ by Microsoft
 - Kite
 - ...

Enviornmental Modules

- ``module avail``: list available modules
- ``module load mod``: load mod
- ``module list``: list currently loaded modules
- ``module purge``: unload all modules
- ...

Setup Python Enviroment

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- Use `export` to set the relavent enviroment variables (`PATH` and `PYTHONPATH`)
 - `export PATH=$PATH:/dssg/home/acct-phyww/phyww/qazhang/packages/anaconda3/bin`
 - `export PYTHONPATH=/dssg/home/acct-phyww/phyww/.local/lib/python3.7/site-packages`
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- Or excute them everytime after login/reconnect...

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 - `h5glance h5_file [path]`
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- Advanced usage:
 - show attributes: `h5glance --attrs h5_file [path]`
 - peek data: `h5glance --attrs h5_file path`
 - slice data: `h5glance -s slice --attrs h5_file path`
 - `slice`: `numpy` like slice, e.g: `2,10:15`

IV. Introduction to HDF5

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- HDF5: Hierarchical Data Format Version 5

High-performance data management and storage suite Utilize the HDF5 high performance data software library and file format to manage, process, and store your heterogeneous data. HDF5 is built for fast I/O processing and storage.

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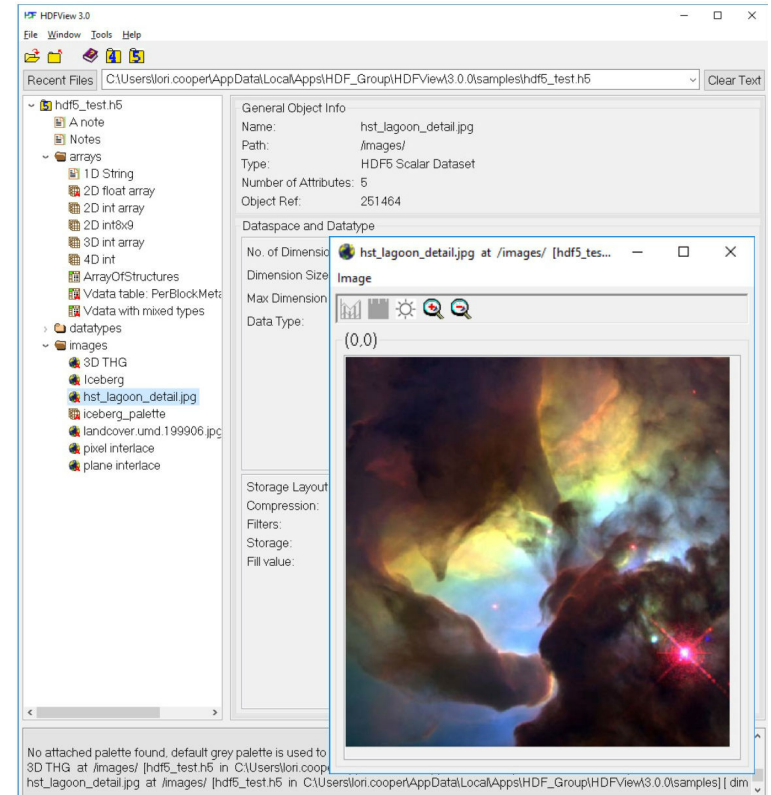
- Sell sheet : <https://www.hdfgroup.org/wp-content/uploads/2017/12/HDF512-17.pdf>
- Open source library
- Supported by C/C++, Julia, Mathematica, Python ...
- HDF5 does not provide native complex type, different software may have different interpretation of complex type
 - e.g. Interpreted as association (dictionary) in Mathematica

```
1 In[1]:= c = 1 + 0.2*I;  
2 In[2]:= Export["cmplx.h5", "/cmplx" -> c];  
3 In[3]:= Import["cmplx.h5", {"Datasets", "/cmplx"}]  
4 Out[4] = <|"Re" -> 1., "Im" -> 0.2|>
```

Other Features

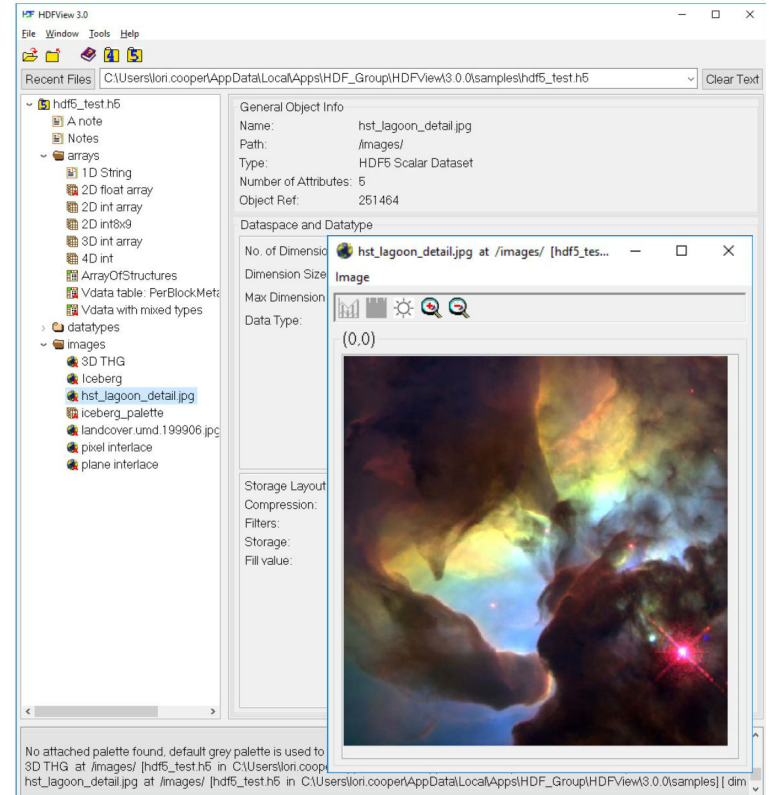
Other Features

- Float, integer, string, array, image ... all in a single h5 file



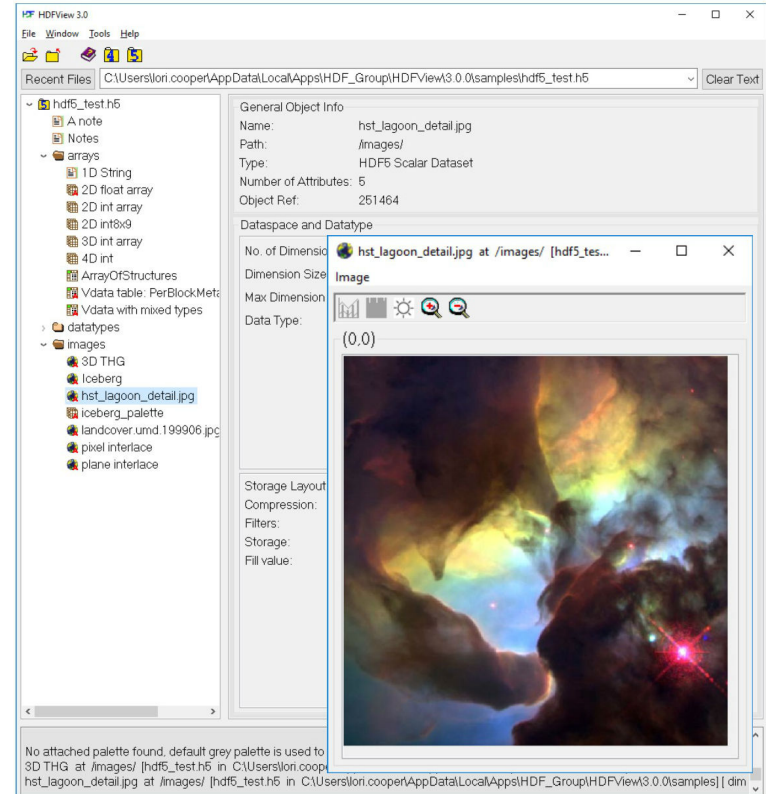
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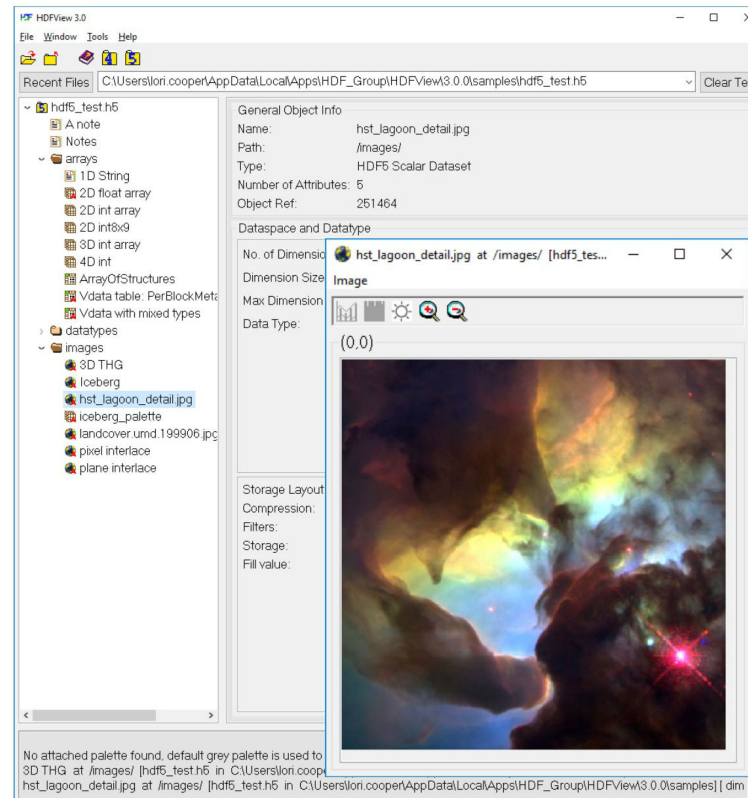
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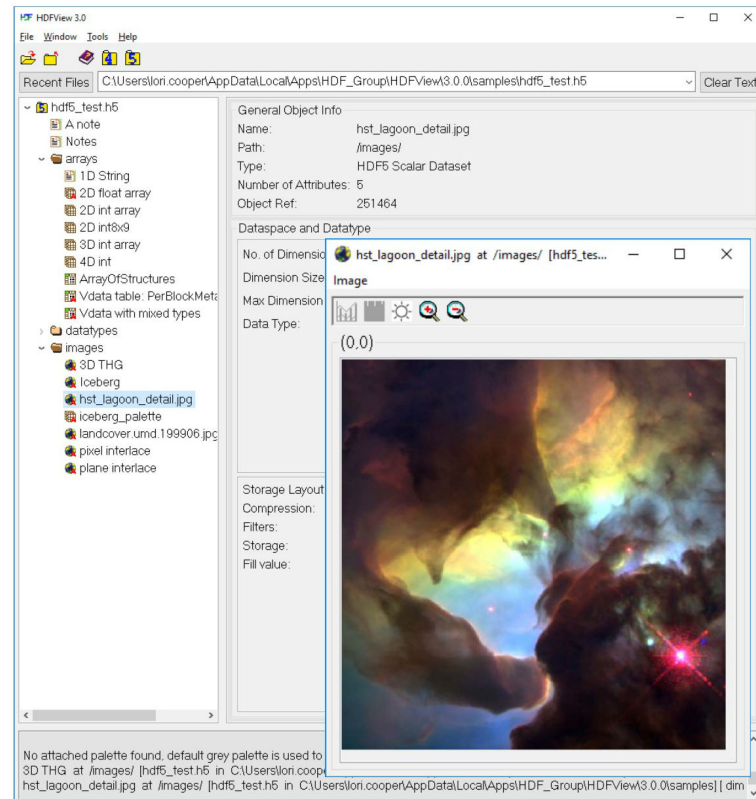
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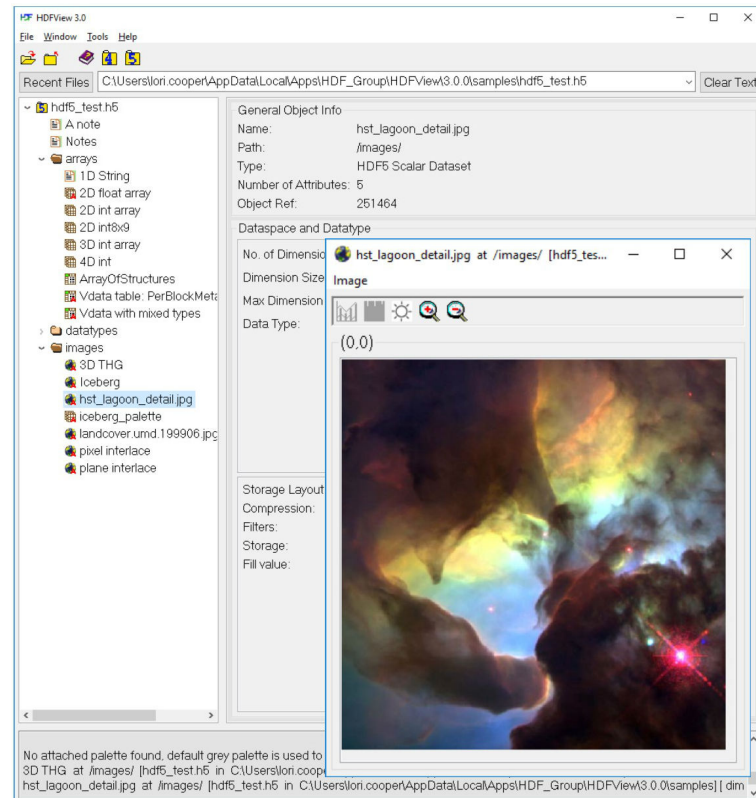
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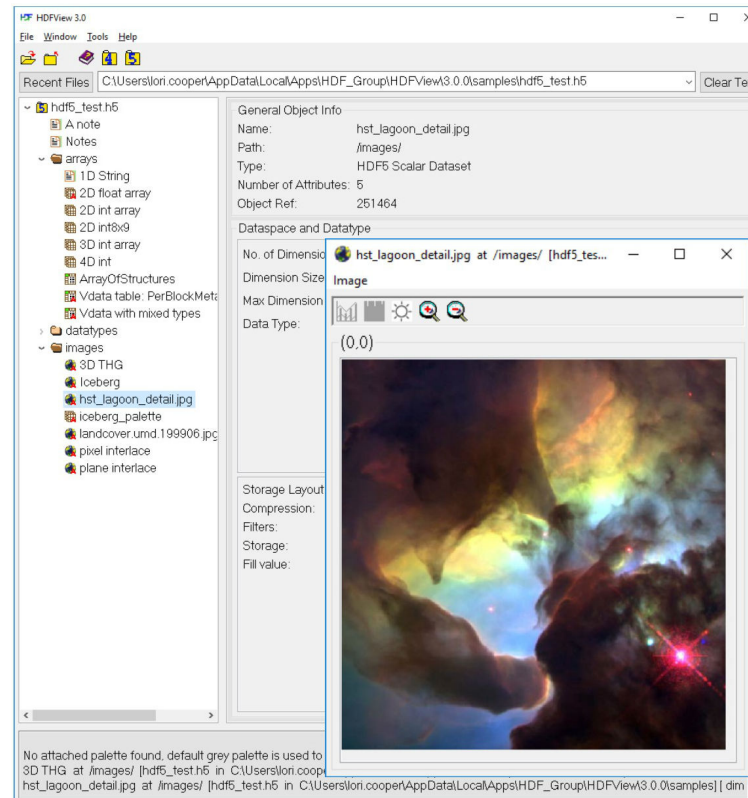
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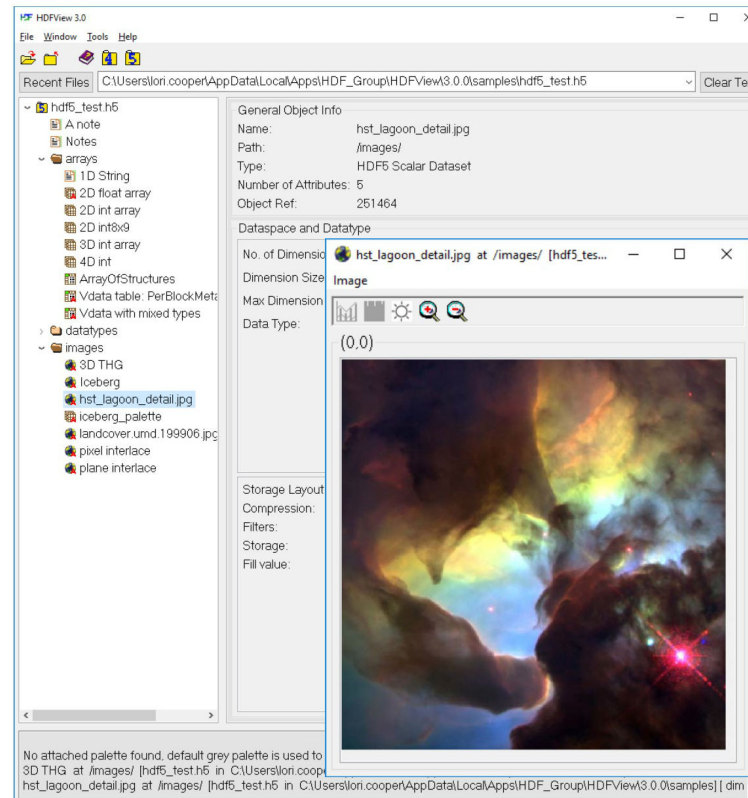
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- *Python and HDF5*, Andrew Collette, ISBN: 9781449367831 (2013)



iog to h5

- Based on ``iog.so``, ``iog_reader.py``, requiring ``h5py`` python package
 - `iog2h5_2pt.py`: convert 2pt iog files to h5
 - `iog2h5_3pt.py`: convert 3pt iog files to h5

provided on demand