



中国科学院大学
University of Chinese Academy of Sciences



ICTP-AP
International Centre
for Theoretical Physics Asia-Pacific
国际理论物理中心-亚太地区

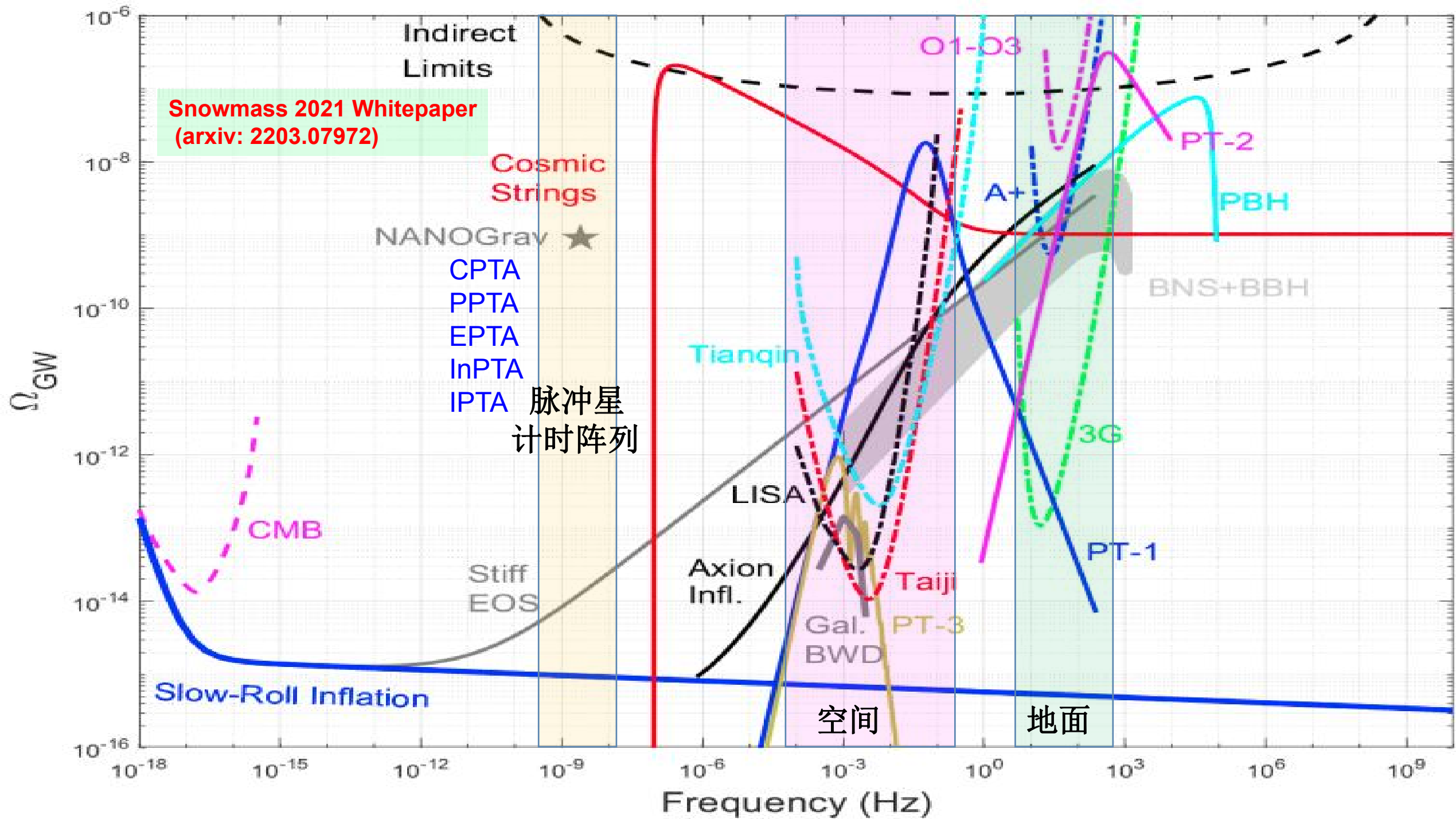
Some Particle Physics Studies with Gravitational Waves

Huaike Guo (郭怀珂)

UCAS (ICTP-AP)

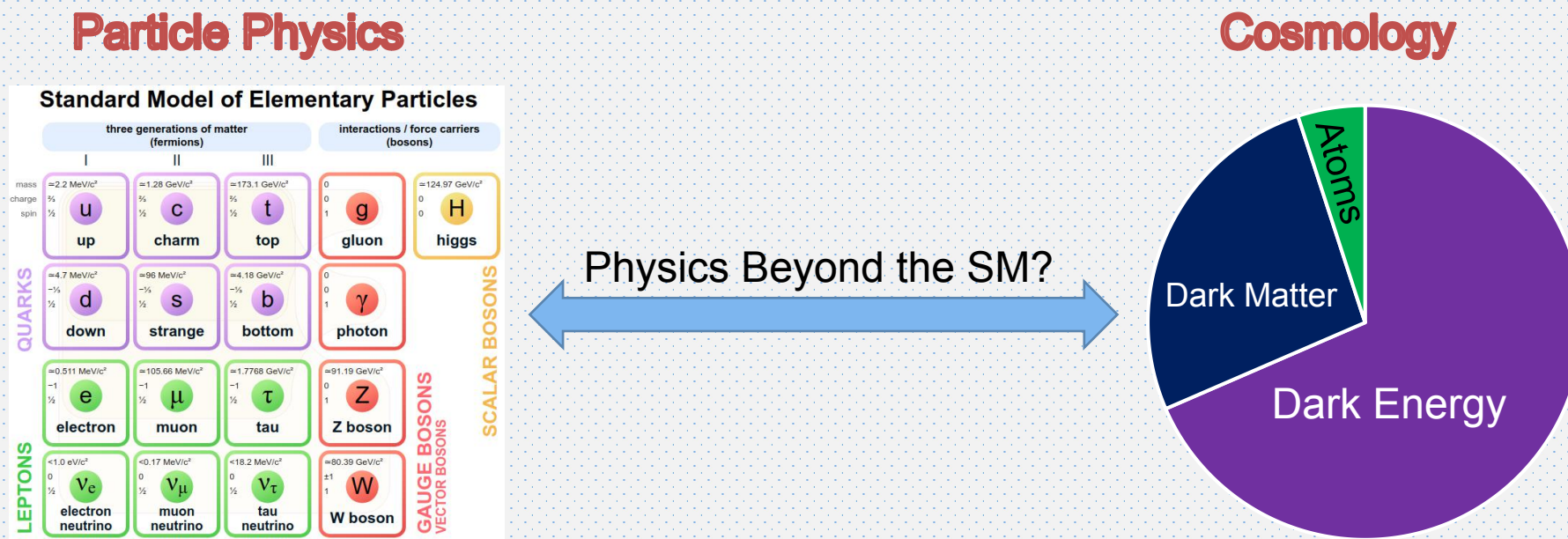
2023-8-8

第四届粒子物理前沿研讨会



New Perspectives?

How can we reconcile the standard models of particle physics and cosmology?



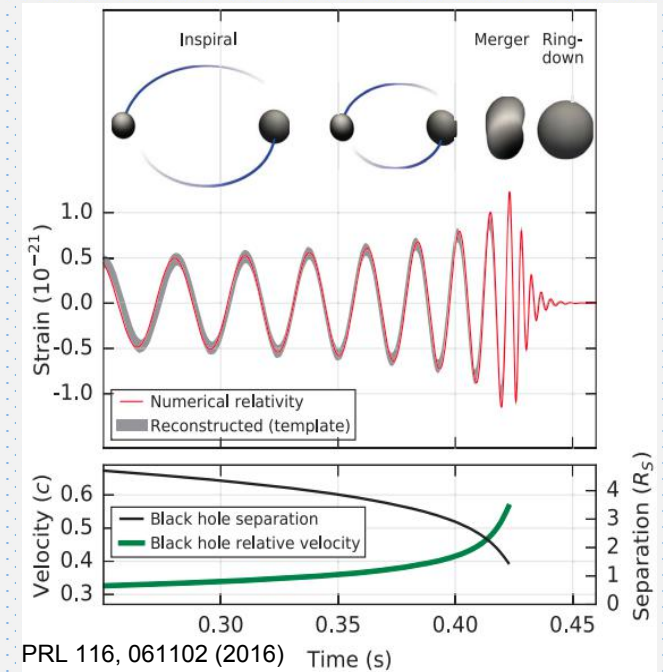
Why more matter than anti-matter? (phase transitions, solitons)

What is dark matter? (solitons, ultralight particles)

GWs from Particles?

GW generation requires **macroscopic mass/energy**

$$\square^2 h_{\mu\nu} = -16\pi G S_{\mu\nu} \rightarrow \text{matter}$$



$$h \sim 10^{-22} \frac{M/M_{\odot}}{r/100\text{Mpc}} \left(\frac{v}{c}\right)^2 \rightarrow \text{huge mass/energy}$$

How to study particle physics with GWs?

GWs from Particles

Here will focus only on a collection of my personal works:

Extreme densities

disturbances in the early universe

As Macroscopic Objects

(non-) topological solitons

Environmental Effects

Faking GW signals (dark photon)

See also 蒋赞、樊琪琪、康召丰、丁然、
谢柯盼、余钊焕、张孟超、张阳's talks

GWs from Particles

Extreme densities



disturbances in the early universe

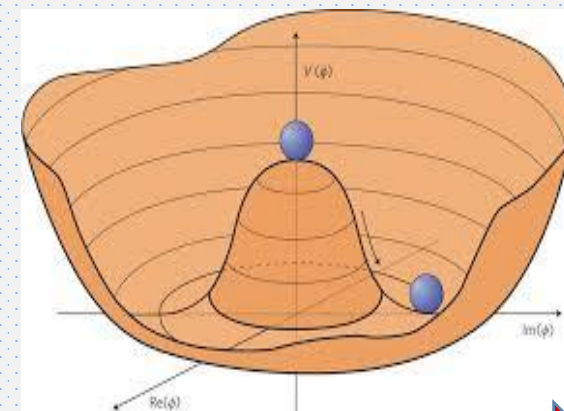
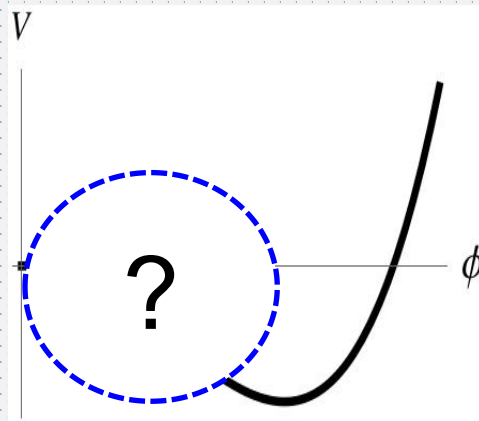
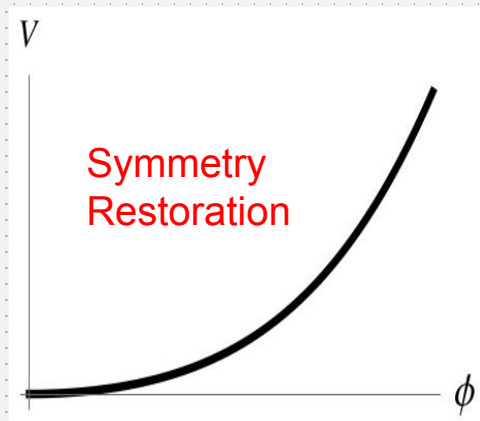
As Macroscopic Objects

(non-) topological solitons

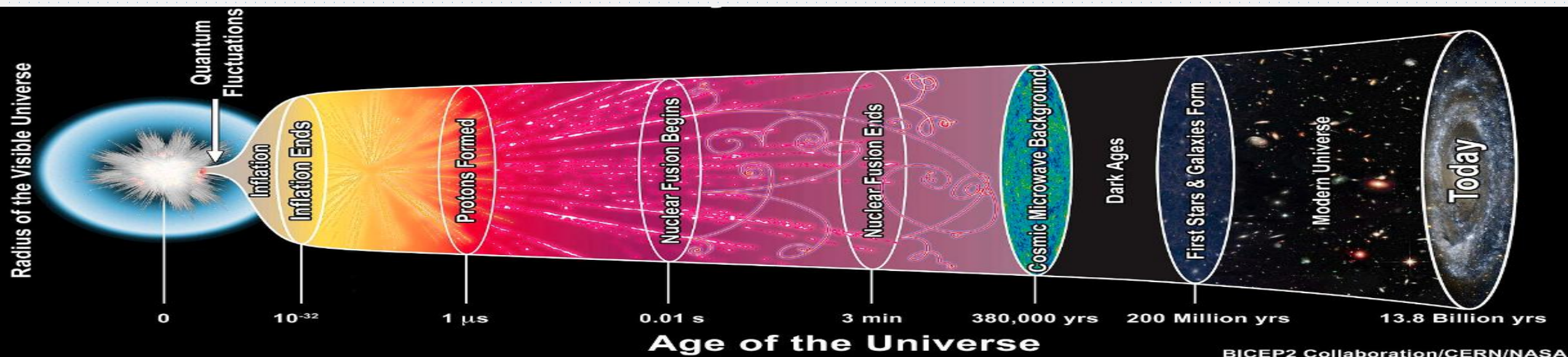
Environmental Effects

Faking GW signals (dark photon)

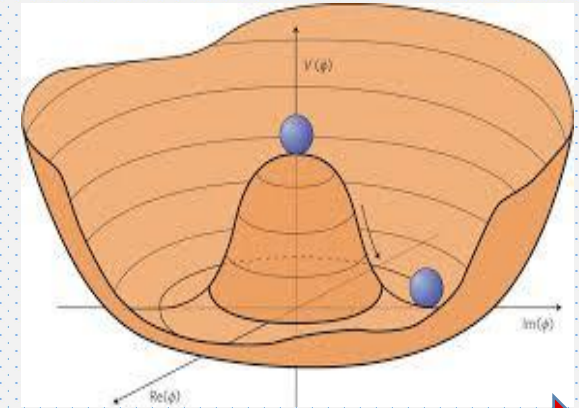
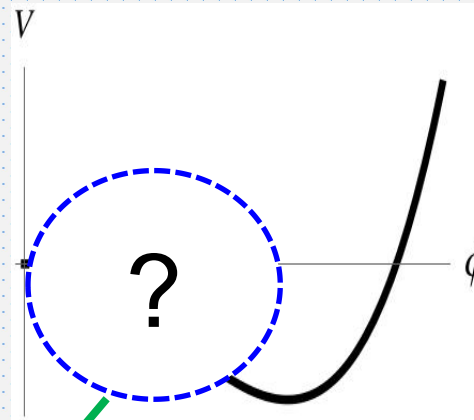
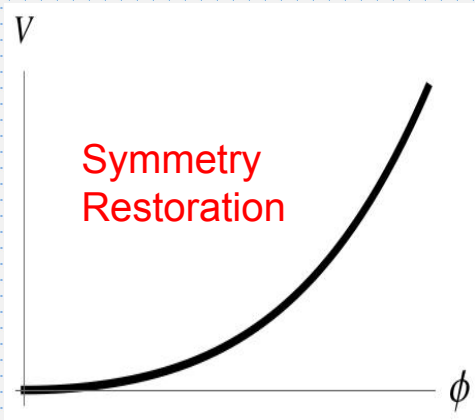
Electroweak Phase Transition



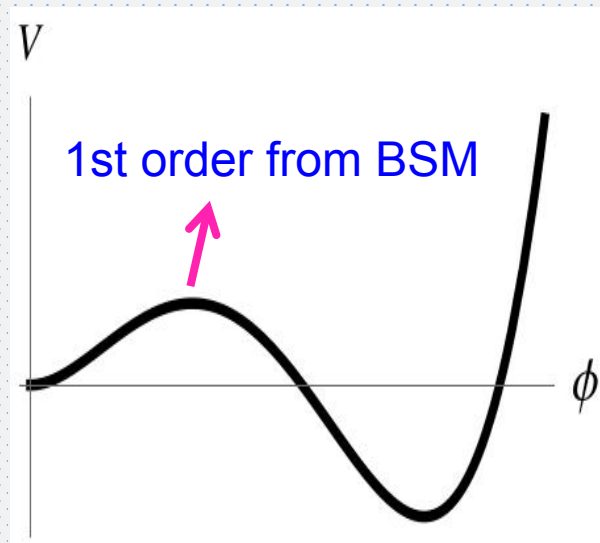
Temperature drops



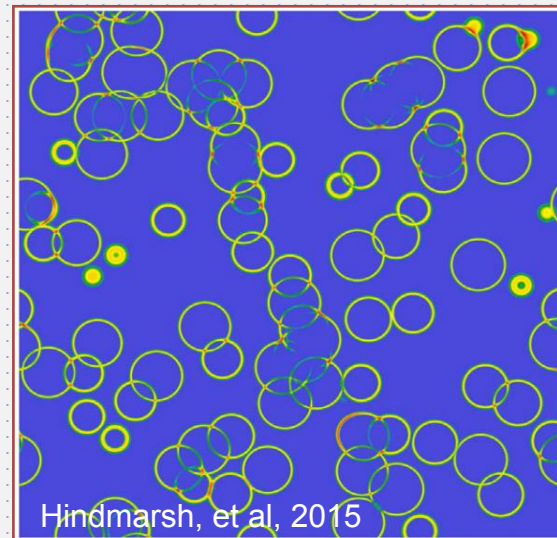
Electroweak Phase Transition



Temperature drops



bubbles, plasma, MHD



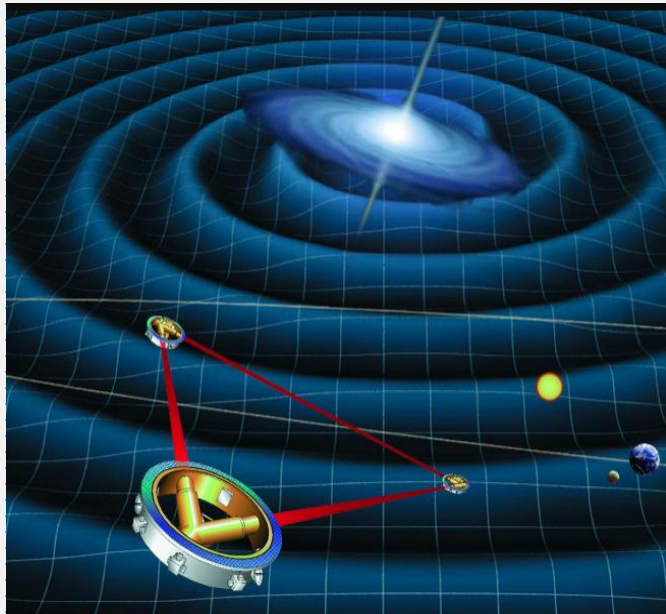
Electroweak Baryogenesis

- Modified Higgs potential (Higgs physics, GW)
- Extra CP-violation (EDM, LHC)
- B-violation: Sphaleron process (LHC, GW)

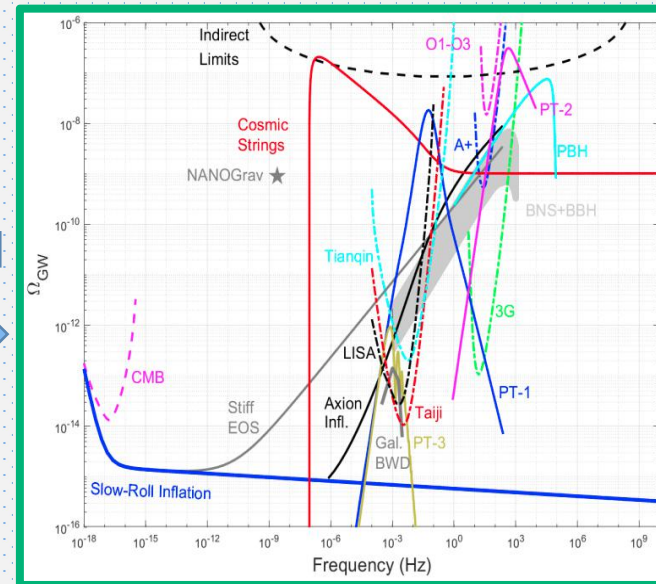
Morrissey, Ramsey-Musolf, NJP [1206.2942]

Flow of Studies

theoretical calculation of gravitational wave spectrum and detector simulation



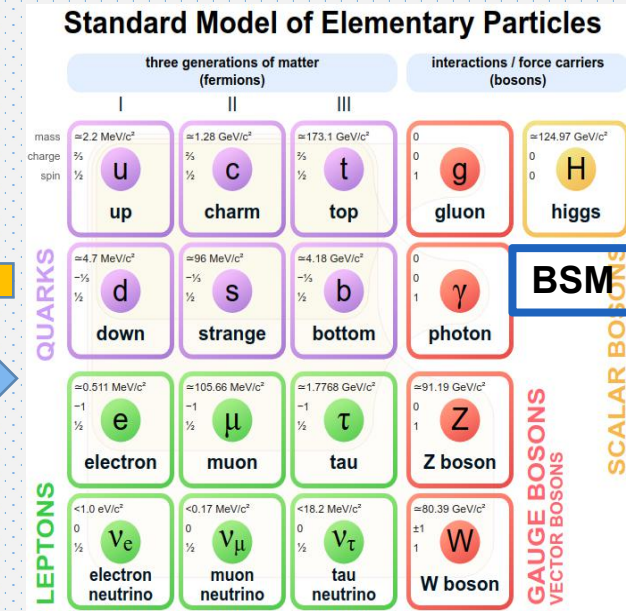
LIGO, LISA, Taiji, Tianqin...



Gravitational Wave Spectrum

α
 β
 v_w
 T_*
 g_s
...

Phase Transition Parameters



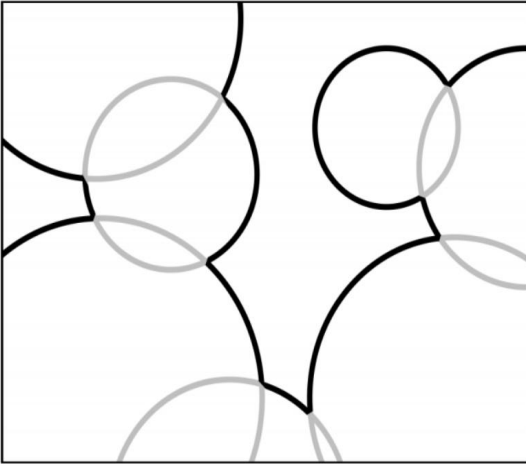
Particle Physics Model

data analysis, constraints or discovery(parameter estimation)



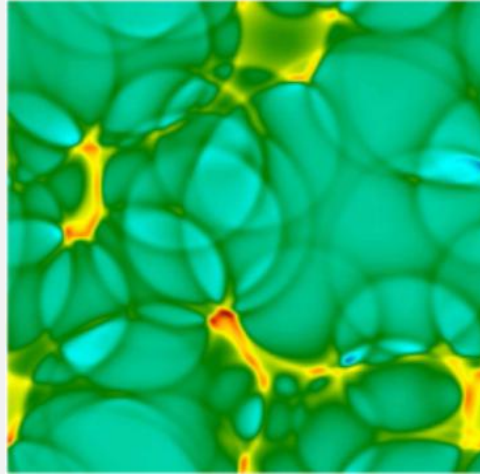
Gravitational Wave Sources

Bubble Collisions



energy concentrated at walls

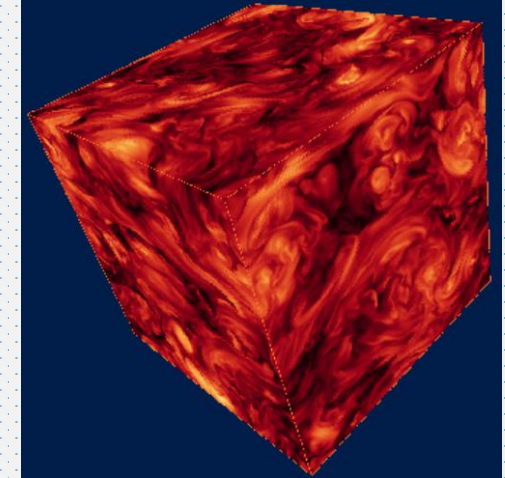
Sound Waves



Hindmarsh, et al, PRL 112, 041301 (2013)

acoustic production

MagnetoHydrodynamic Turbulence



<https://home.mpcdf.mpg.de/~wcm/projects/homog-mhd/mhd.html>

turbulent motion

New observables: primordial magnetic field, scalar perturbations, anisotropy, primordial black hole...

Di, Wang, Zhou, Bian, Cai, Liu, PRL 126 (2021) 25, 251102

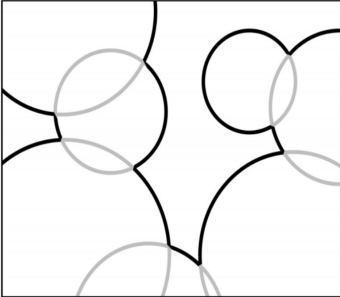
Jing, Bian, Cai, Guo, Wang, PRL 130 (2023) 051001

Li, Huang, Wang, Zhang, PRD 105 (2022) 083527

Huang, Xie, PRD 105 (2022) 11, 115033, JHEP 09 (2022) 052

The GW Observable

bubble collision

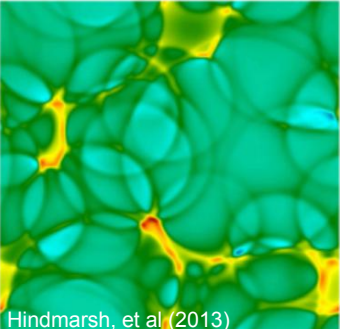


$$\Omega_{\text{coll}}(f)h^2 = 1.67 \times 10^{-5} \Delta \left(\frac{H_{\text{pt}}}{\beta} \right)^2 \left(\frac{\kappa_{\phi} \alpha}{1 + \alpha} \right)^2 \times \left(\frac{100}{g_*} \right)^{1/3} S_{\text{env}}(f),$$

Energy density Spectrum

$$\Omega_{\text{GW}}(f) = \frac{d\rho_{\text{GW}}}{\rho_c d \log f}$$

sound waves



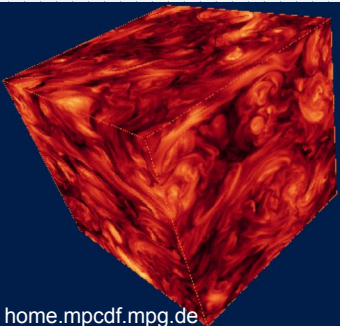
Hindmarsh, et al (2013)

$$\Omega_{\text{sw}}(f)h^2 = 2.65 \times 10^{-6} \left(\frac{H_{\text{pt}}}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 \left(\frac{100}{g_*} \right)^{1/3} \times v_w \left(\frac{f}{f_{\text{sw}}} \right)^3 \left(\frac{7}{4 + 3(f/f_{\text{sw}})^2} \right)^{7/2} \Upsilon(\tau_{\text{sw}}),$$

$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}} H_{\text{pt}})^{-1/2} \quad (\text{RD})$$

HG, Sinha, Vagie, White, JCAP 01 (2021) 001

MHD



home.mpcdf.mpg.de

$$h^2 \Omega_{\text{turb}}(f) = 3.35 \times 10^{-4} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{\frac{3}{2}} \left(\frac{100}{g_*} \right)^{1/3} v_w S_{\text{turb}}(f)$$

THE SPECTRUM OF GRAVITATIONAL WAVES

Observatories
& experiments

Ground-based
experiment



Space-based observatory



Pulsar timing array



Cosmic microwave
background polarisation



Timescales

milliseconds

seconds

hours

years

billions of years

Frequency (Hz)

100

1

10^{-2}

10^{-4}

10^{-6}

10^{-8}

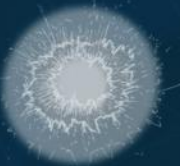
10^{-16}

PeV-EeV

$\sim 100\text{GeV}$ Cosmic fluctuations in the early Universe

$\sim 100\text{MeV}$

Cosmic
sources



Supernova



Pulsar



Compact object falling
onto a supermassive
black hole



Merging supermassive black holes



Merging neutron
stars in other galaxies



Merging stellar-mass black holes
in other galaxies



Merging white dwarfs
in our Galaxy



LIGO Search Result

O1+O2+O3@LIGO (H1, L1), Virgo

- No Evidence for Broken Power Law Signal
- No Evidence for Bubble Collision Domination Signal
- No Evidence for Sound Waves Domination Signal

Broken Power Law

95% CL UL (CBC+BPL)

$$\Omega_{\text{ref}} = 6.1 \times 10^{-9}$$

$$\Omega_* = 5.6 \times 10^{-7}$$

$$\Omega_{\text{BPL}}(25 \text{ Hz}) = 4.4 \times 10^{-9}$$

Bubble Collision

95% CL UL with fixed T_{pt} and β/H_{pt}

Phenomenological model (bubble collisions)

$\Omega_{\text{coll}}^{95\%}(25 \text{ Hz})$

$\beta/H_{\text{pt}} \backslash T_{\text{pt}}$	10^7 GeV	10^8 GeV	10^9 GeV	10^{10} GeV
0.1	9.2×10^{-9}	8.8×10^{-9}	1.0×10^{-8}	7.2×10^{-9}
1	1.0×10^{-8}	8.4×10^{-9}	5.0×10^{-9}	...
10	4.0×10^{-9}	6.3×10^{-9}

no sensitivity

Sound Waves

95% CL UL

$$\Omega_{\text{sw}}(25 \text{ Hz}) = 5.9 \times 10^{-9}$$

$$\beta/H_{\text{pt}} < 1 \text{ and } T_{\text{pt}} > 10^8 \text{ GeV}$$

First result from gravitational wave data!

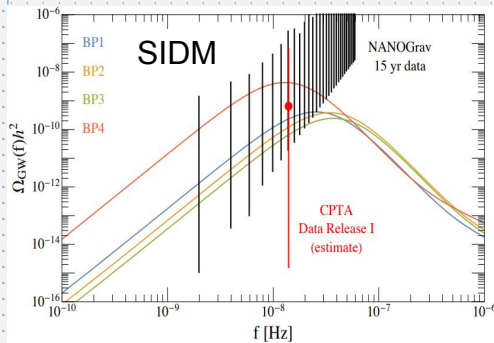
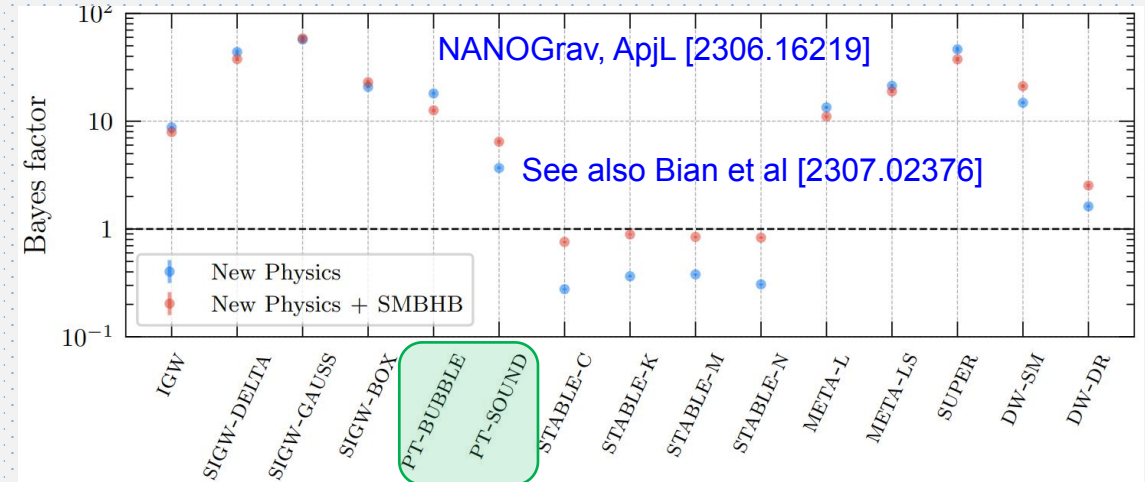
What possible PTA discovery implies?

- Once discovered, firstly needs to know its origin
- Can be the next “CMB” (spectral shape, anisotropy, etc)
- Can be from first order QCD-scale PT

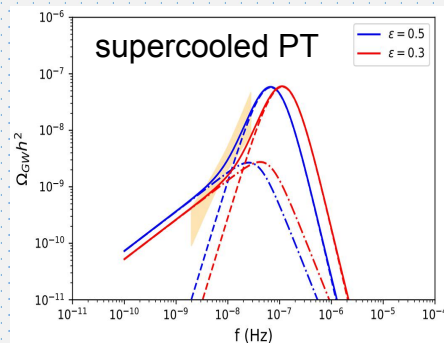
PPTA: Xue et al, PRL [2110.03096]

NANOGrav (12.5-year): Arzoumanian et al, PRL [2104.13930]

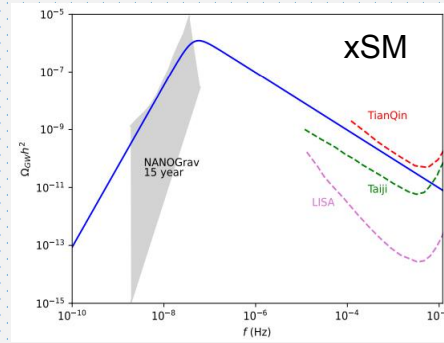
...



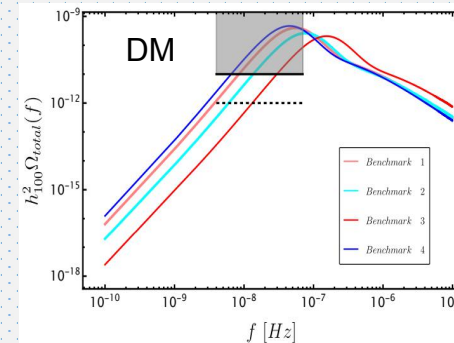
Han,Xie,Yang,Zhang [2306.16966]



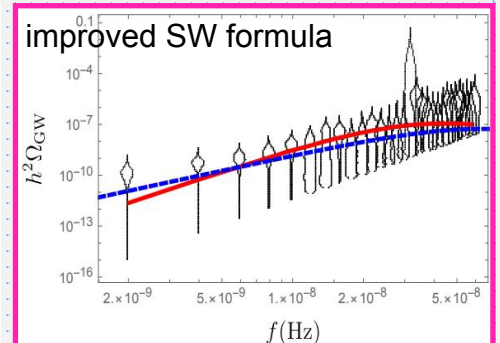
Zu,Zhang,Li,Gu,Tsai,Fan [2306.17239]



Xiao,Yang,Zhang [2307.01072]



Yang,Ma,Jiang,Huang [2306.17827]



Ghosh et al [2307.02259]

and more...

See also 丁然、谢柯盼、余钊焕、张孟超's talks

GWs from Particles

Extreme densities

disturbances in the early universe

As Macroscopic Objects

(non-) topological solitons



Environmental Effects

Faking GW signals (dark photon)

Solitons

- Localized
- Associated with nonlinear problem

Found in:

- ✓ Optics
- ✓ Hydrodynamics
- ✓ Condensed matter systems
- ✓ Quantum field theory

...



Solitons in Quantum Field Theory

- **Topological solitons**: symmetry breakings in the early universe (new physics, baryon asymmetry)
- **Non-Topological solitons**: as DM candidates (ultralight DM, macroscopic DM)

	Topological Solitons	Non-Topological Solitons
Definition	<p>Static Solution (Theory with Spontaneously Broken Symmetry)</p> <ul style="list-style-type: none">● Global symmetry (Skyrmion, Cosmic String)● Discrete symmetry (Domain wall)● Local symmetry (Monopole, Cosmic String or Vortex line...)● Pure gauge theory (Instanton)	<p>Bose-Einstein Condensate (of Ultralight particles)</p> <ul style="list-style-type: none">● Galactic scale (DM Halo)● Stellar scale (Boson stars)
Boundary	Non-Trivial (needs degenerate vacuum states)	Trivial vacuum state
Stabilized by	Topology (boundary field values)	<p>Conserved Charge, and Balancing</p> <ul style="list-style-type: none">● quantum pressure● gravity (or not, Q-balls etc)● self-interactions (or not)

Topological Solitons in the Early Universe

- Firstly proposed to form in the early universe (Kibble, 1976)
(None observed)
- Later proposed to form in condensed matter systems (Zurek, 1985)
(already observed)

Name variant:
Topological Defects

The Cosmological Kibble Mechanism in the Laboratory: String Formation in Liquid Crystals
[Science, 263 \(1994\)](#)
Mark J. Bowick,* L. Chandar, E. A. Schiff, Ajit M. Srivastava

Can we detect the (cosmic) topological solitons?

Topology of cosmic domains and strings

T W B Kibble

[J.Phys.A 9 \(1976\) 1387-1398](#)

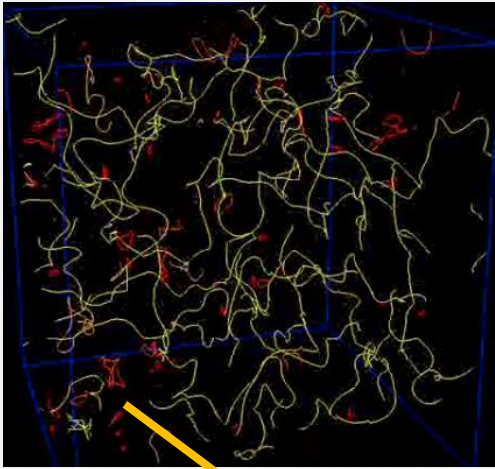
Blackett Laboratory, Imperial College, Prince Consort Road, London

Received 11 March 1976

www.theguardian.com



Cosmic String



Example: the Abelian Higgs Model

$$\mathcal{L} = |(\partial_\mu - igA_\mu)\Phi|^2 - \frac{1}{4}\lambda(|\Phi|^2 - \eta^2)^2 - \frac{1}{4}F_{\mu\nu}F^{\mu\nu}$$

closed string
(loop)

cosmological scale

>>

$O(1/\eta)$

degenerate vacua
with nontrivial topology

LIGO Search Result of Cosmic Strings

Symmetry breakings at scales higher than $O(10^{11})$ GeV
with Cosmic String production are excluded

Caveat (loop distribution model)

GW measurement tells
scale (η) of symmetry breaking

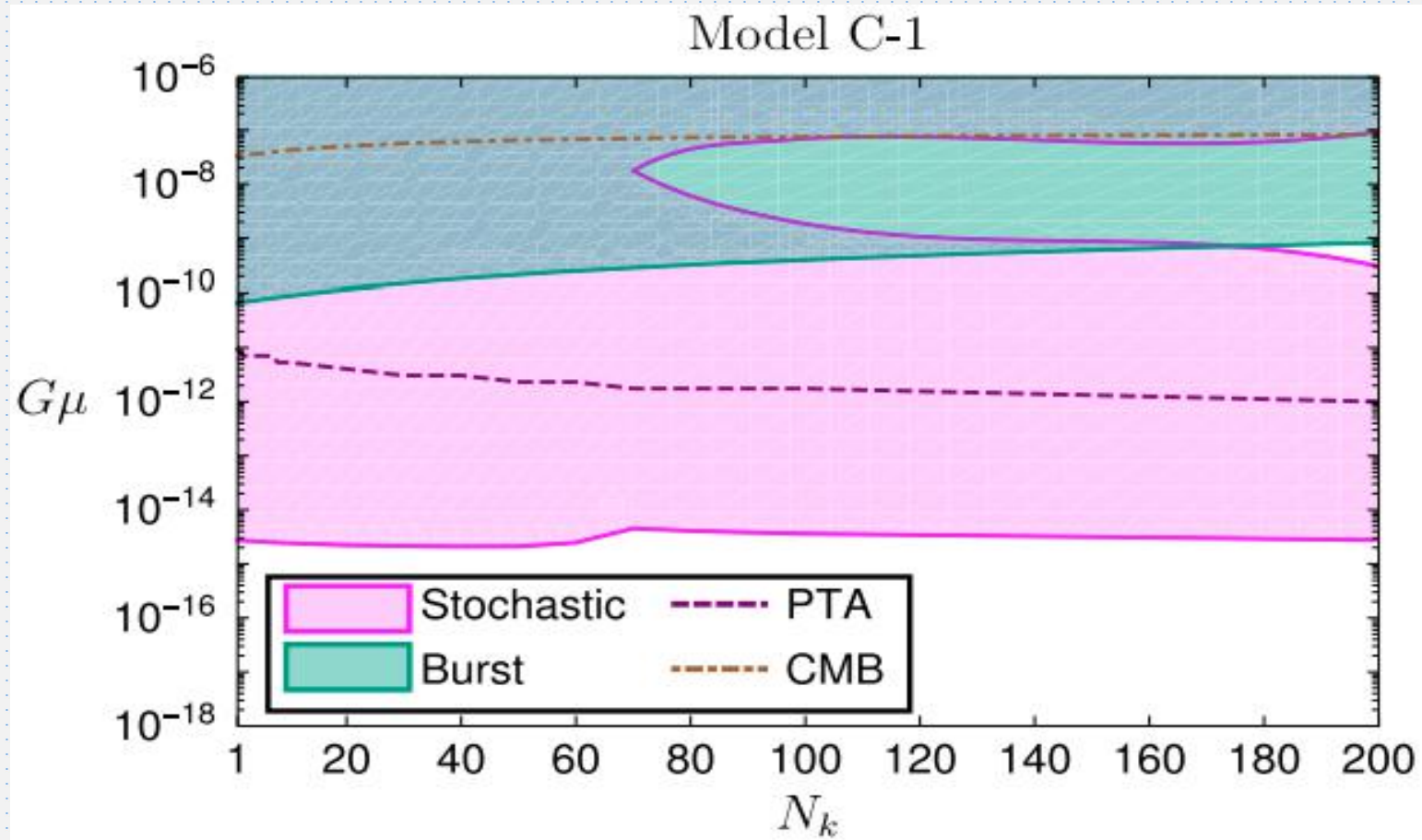
$$G\mu \sim \left(\frac{\eta}{10^{19} \text{GeV}} \right)^2$$

μ : line mass density

Results from PTA Measurements

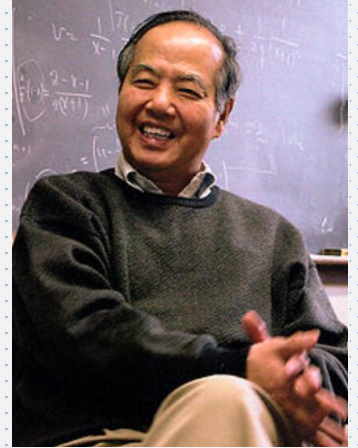
Bian, Cai, Liu, Yang, Zhou, PRD (Letter) 103 (2021) 8

Blasi, Brdar, Schmitz, PRL 126, 041305 (2021)

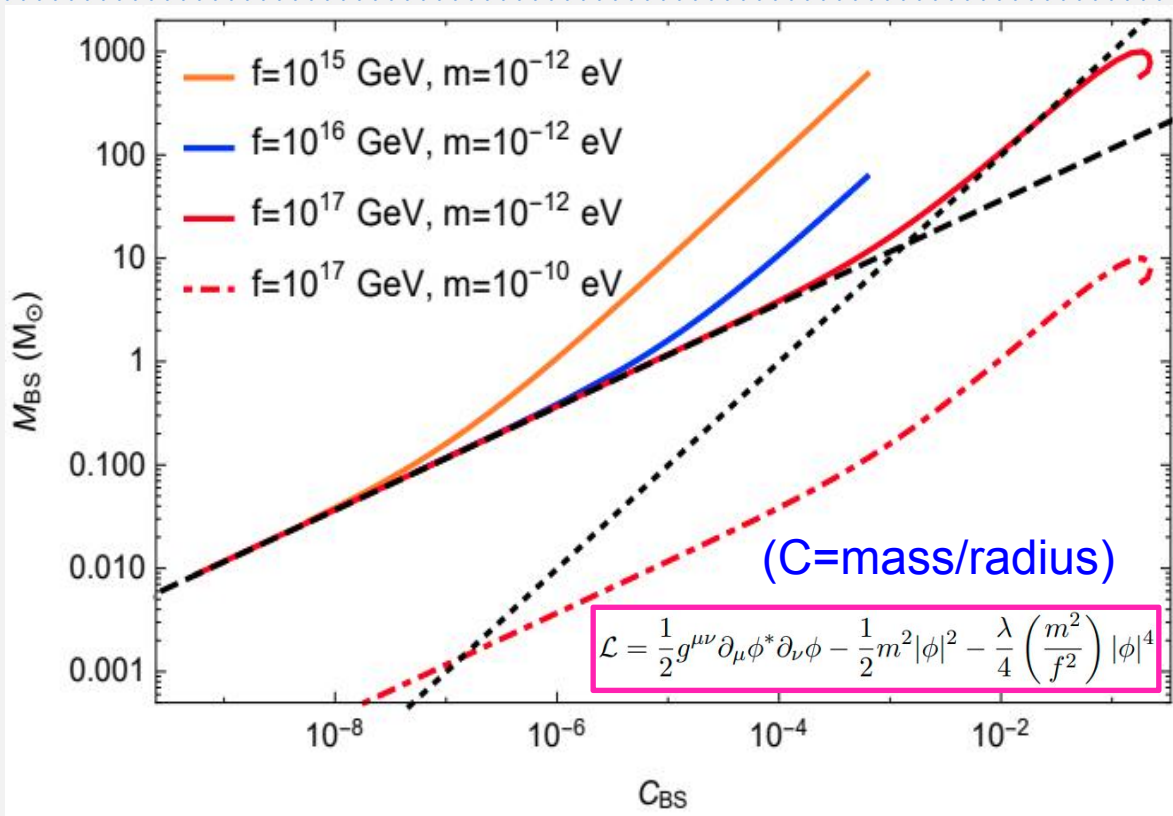


LIGO-Virgo-KAGRA collaborations, PRL 126, 241102 (2021)

Non-Topological Solitons as Boson Stars



- Macroscopic Bose-Einstein condensate of ultralight particles
- Boson stars can be very massive and compact



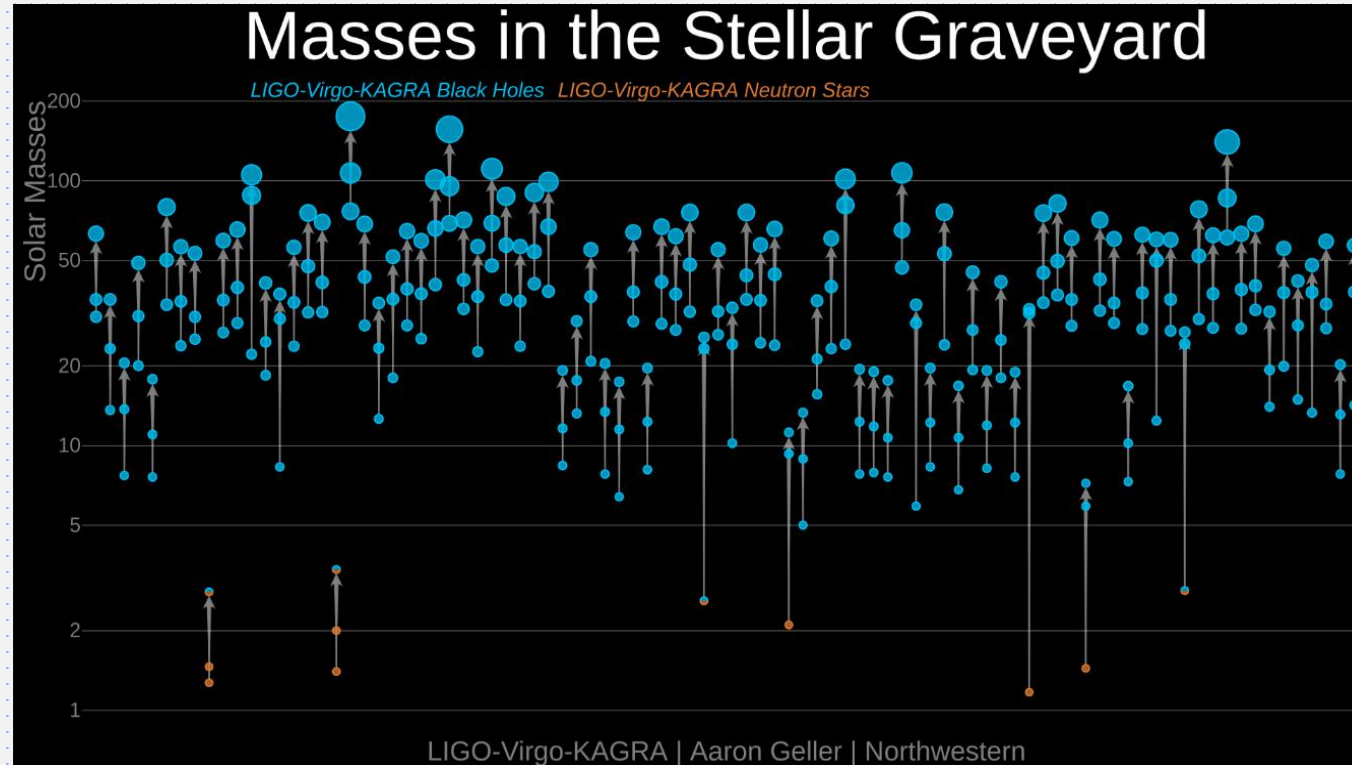
- ❖ Mini-Boson Star (without self-interaction)
- ❖ Solitonic Boson Star (specific potential)
- ❖ Oscillaton (real scalar field)
- ❖ Proca Star (massive complex vector)
- ❖ Axion Stars (dense, dilute)

See, e.g., Liebling, Palenzuela, Living Rev Relativ (2017) 20:5

Lee, Pang, Phys.Rept (1992)

Did LIGO detect Boson Stars?

- Difficult to distinguish
- Mass as discriminator
(SBH cannot be subsolar)



PRL **116**, 201301 (2016)

PHYSICAL REVIEW LETTERS

week ending
20 MAY 2016

Did LIGO Detect Dark Matter?

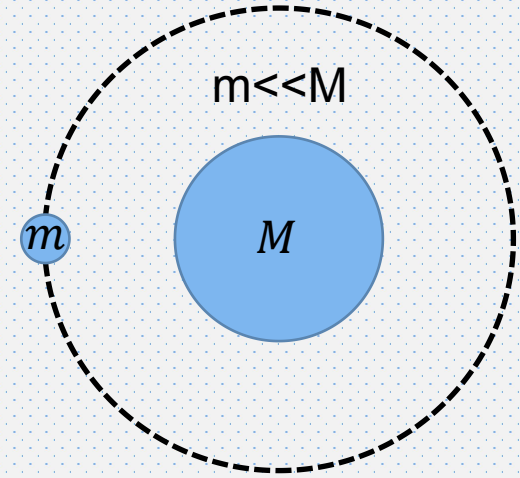
Simeon Bird,^{*} Ilias Cholis, Julian B. Muñoz, Yacine Ali-Haïmoud, Marc Kamionkowski,
Ely D. Kovetz, Alvise Raccanelli, and Adam G. Riess
*Department of Physics and Astronomy, Johns Hopkins University,
3400 North Charles Street, Baltimore, Maryland 21218, USA*
(Received 4 March 2016; published 19 May 2016)

GW190521 as a Merger of Proca Stars: A Potential New Vector
Boson of 8.7×10^{-13} eV

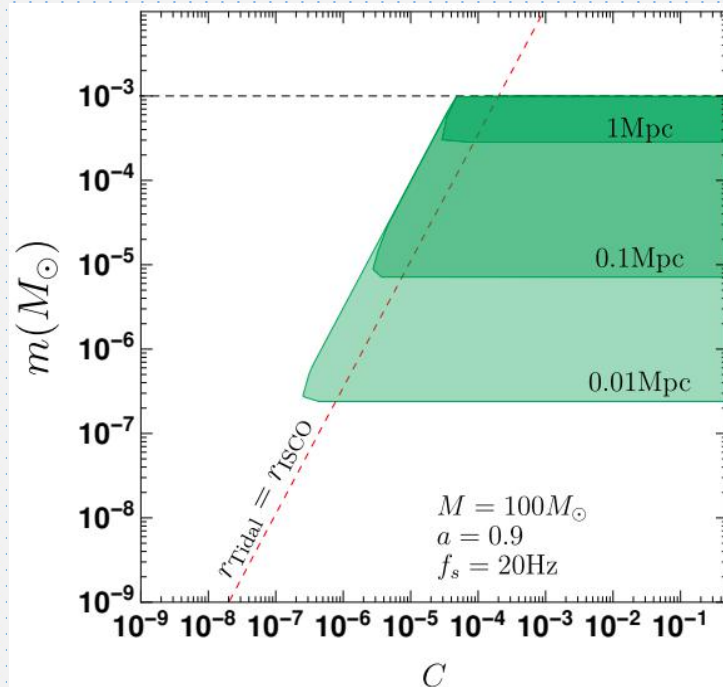
Juan Calderón Bustillo, Nicolas Sanchis-Gual, Alejandro Torres-Forné, José A. Font, Avi Vajpeyi, Rory Smith,
Carlos Herdeiro, Eugen Radu, and Samson H. W. Leong
Phys. Rev. Lett. **126**, 081101 – Published 24 February 2021

Detection with EMRI and mini-EMRI

- By making one object much heavier, one can probe much lighter companion object
- Ideal systems: extreme mass ratio inspirals (EMRIs), key target of Taiji, Tianqin, LISA.
- LIGO can detect mini-EMRIs (extreme mass ratio, but lighter objects)

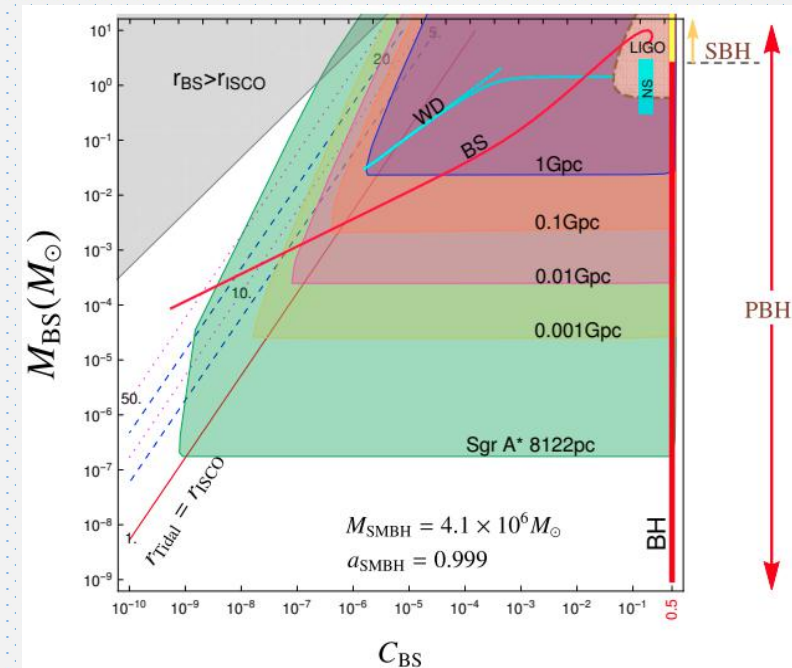


LIGO ("mini-EMRI")



HG, A. Miller, arxiv:2205.10359

LISA, Taiji, Tianqin (EMRI)



HG, Sinha, Sun, JCAP 09 (2019) 032

HG, Shu, Zhao, PRD 99 (2019) 023001

GWs from Particles

Extreme densities

disturbances in the early universe

As Macroscopic Objects

(non-) topological solitons

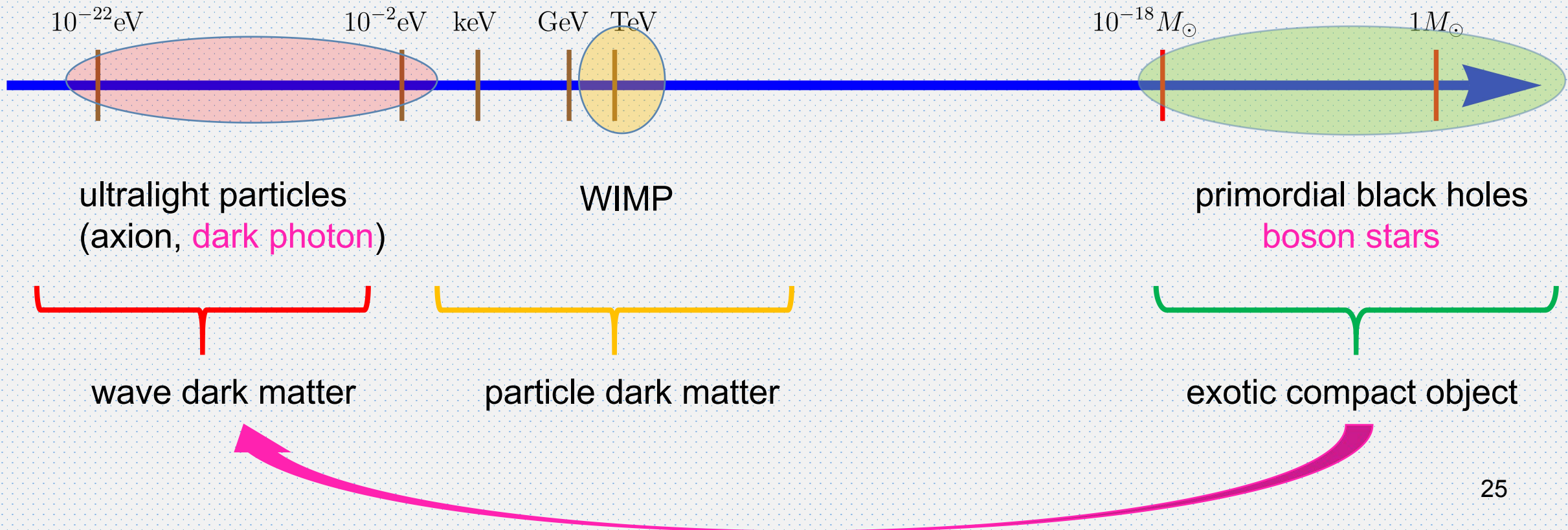
Environmental Effects

Faking GW signals (dark photon)



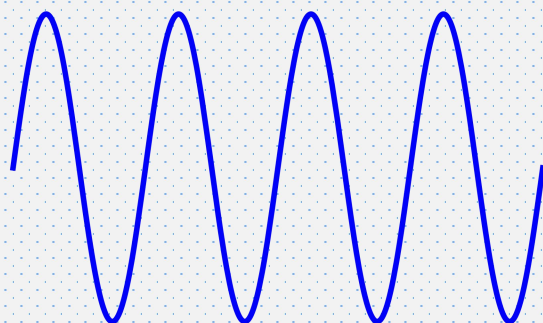
Ultralight Dark Matter

- Boson stars serve as macroscopic dark matter candidate
- So does the ultralight particle making up the boson stars



Dark Photon Detection at LIGO

a single dark photon



$$\vec{A}_{n,0} \sin(\omega_n t - \mathbf{k}_n \cdot \mathbf{x} + \phi_n)$$

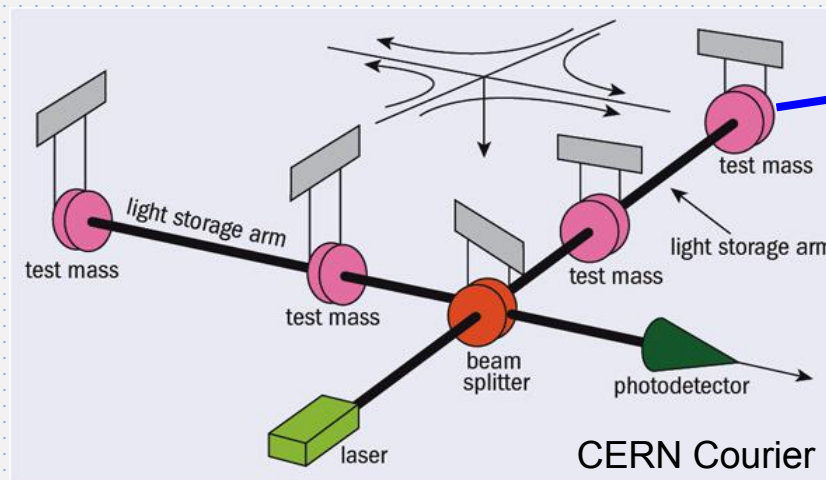
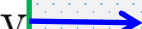


$$\omega_n = m_A \left(1 + \frac{1}{2} v_n^2\right) = 2\pi \times (100 \text{ Hz}) \approx 4 \times 10^{-13} \text{ eV}$$

typical LIGO frequency



typical dark photon mass
LIGO is sensitive to



silicon mirror

$$U(1)_B: 1/\text{GeV}$$

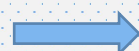
$$U(1)_{B-L}: 1/2\text{GeV}$$



$$\mathbf{a}_i(t, \mathbf{x}_i) \simeq \epsilon e \frac{q_{D,i}}{M_i} \partial_t \mathbf{A}(t, \mathbf{x}_i)$$

acceleration

$$v_0 \sim \mathcal{O}(10^{-3})$$

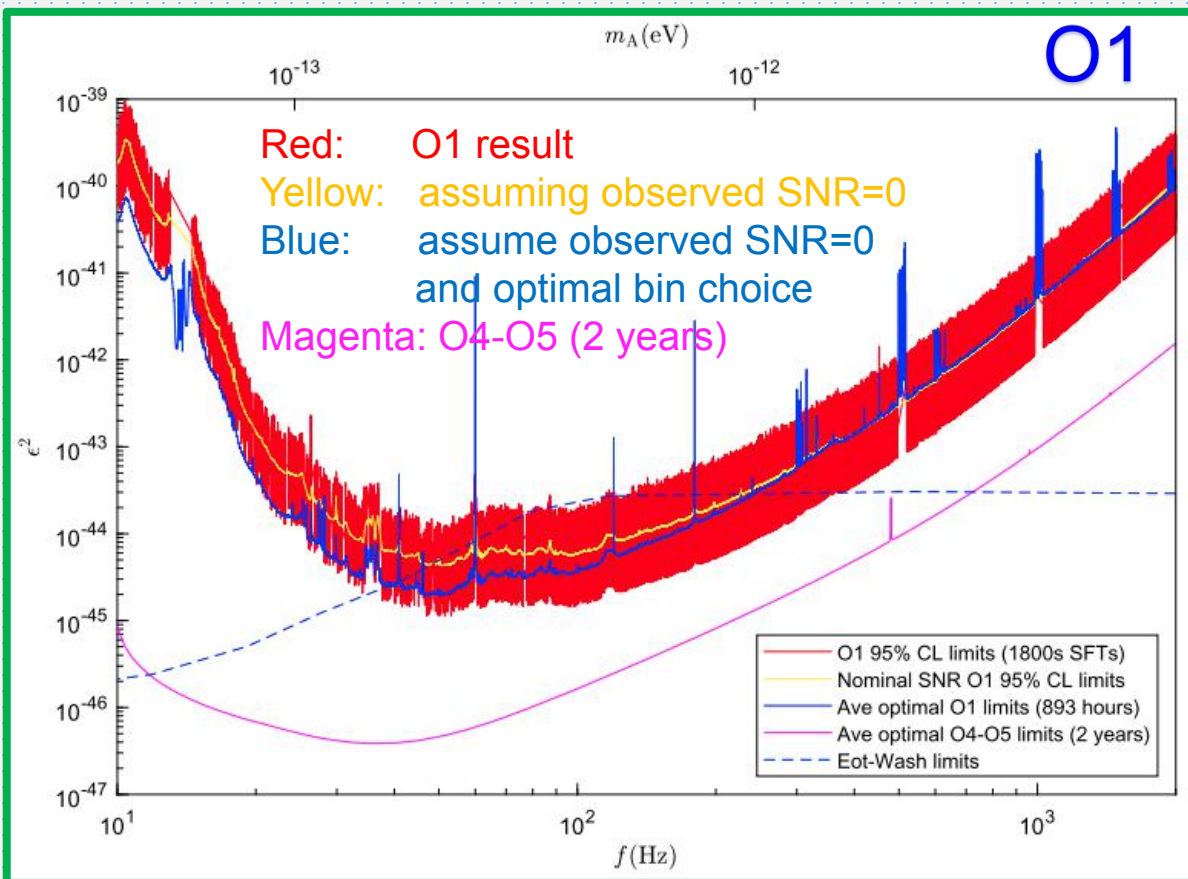


$$\Delta f / f = 10^{-6}$$

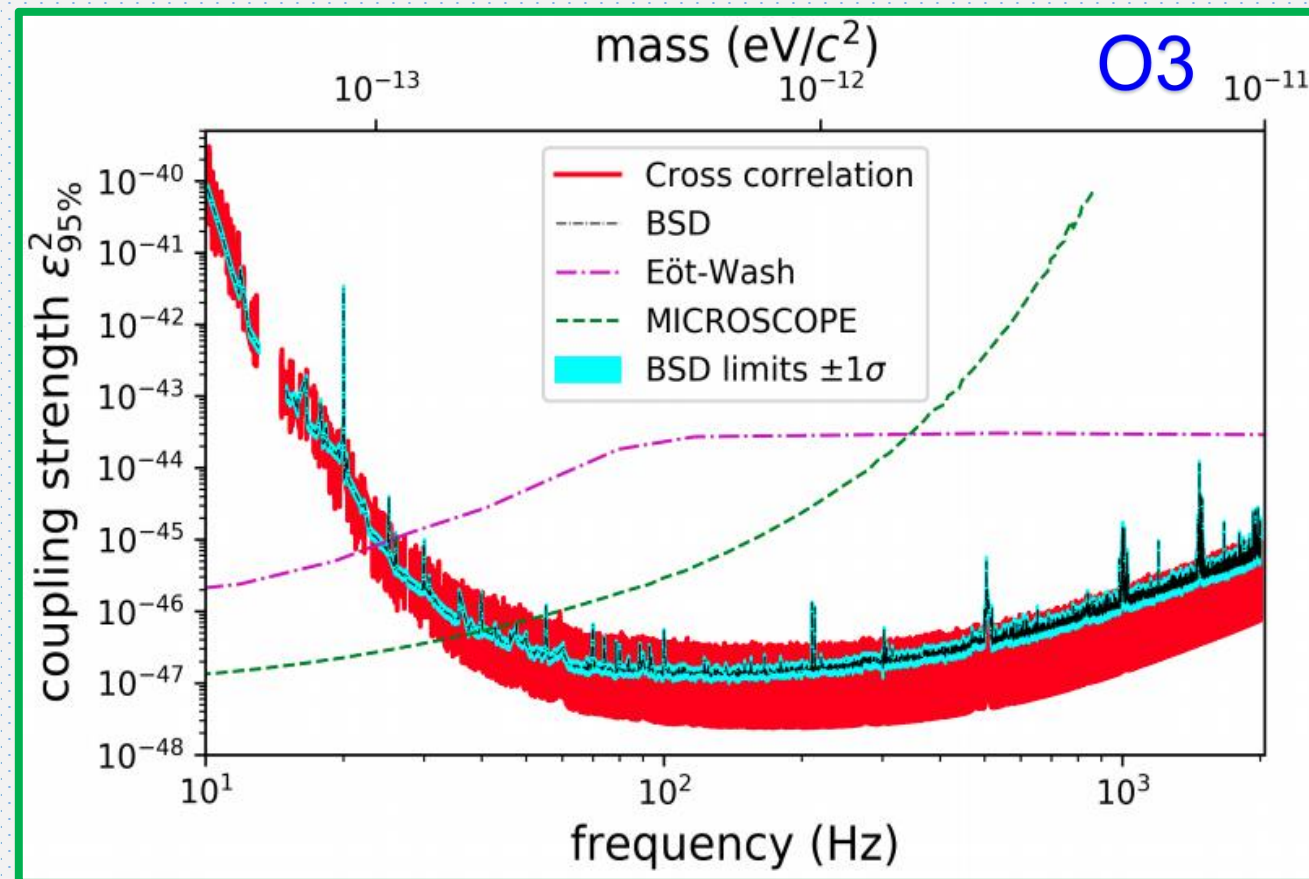


Signal: a narrow peak in frequency domain

Search Results



(Nature) Commun.Phys. 2 (2019) 155, [HG](#), Riles, Yang, Zhao



Phys.Rev.D 105 (2022) 6, LIGO-Virgo-KAGRA Collaborations

See also Yuan,Jiang,Huang, PRD [2204.03482], Yu,Yao,Tang,Wu [2307.09197]

Summary

GWs as a new important tool in particle physics studies

- Early universe symmetry breakings (phase transitions)
- Macroscopic solitons (topological and nontopological)
- Dark photon (environmental effects)

Thanks!