

Lorentz violations of cosmic particles from string theory model of space-time foam

LI Chengyi (李成翊)

Based on [JHEP 03\(2023\)230](#); [PLB 835\(2022\)137543](#); [829\(2022\)137034](#);
[PRD 104\(2021\)063012](#); [PLB 819\(2021\)136443](#)

with Prof. MA Bo-Qiang (Peking Univ.)



2nd Int'l Conf on Axion Physics & Exp (Axion 2023 @ Xi'an) - 26.07.2023

Background

Light-speed variation in stringy D-foam

Implications of PeV- γ at LHAASO on Lorentz violation (LV)

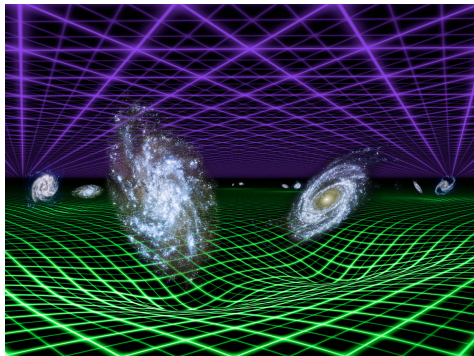
LHAASO PeV photon with LV

Crab Nebula constraint to electron LV & quantum gravity

CPT violating neutrino from strings

Closing

In a century from 1905



Einstein theory of time, space (SR) & gravity (GR)

Einstein theory of relativity

- relativistic principle
 - constant speed of light
- Lorentz symmetry as a foundation

- ★ Triumphs of relativity
- ★ Whether it works at every scales
 1. lengths $\lesssim 10^{-4}$ m $\rightarrow$ UV
 2. beyond Solar system $\rightarrow$ IR

grand unification? Einstein's dream

Hints for a failure of exact Lorentz symmetry?

- Noncompact group, QFT UV divergences, etc.
- Possible **deformation** (or **reduction**), and/or **violation of Lorentz invariance (LV)** within many well-motivated models for new physics beyond relativity

say, **Quantum Gravity (QG)**

- Dirac's new æther [Dirac'51]
- Wheeler's foam ($\delta\mathcal{E} \sim \hbar/\delta t$) [Wheeler'55, Hawking'78]

→ foaminess $\leftrightarrow$ quantum fluctuation of geometries $\leftrightarrow$ “*space-time foam*”

$$\delta g \sim \left(\frac{\ell_{\text{Pl}}}{\ell} \right)^\alpha \sim \mathcal{O}(1) \text{ as } \ell \sim \ell_{\text{Pl}}$$

Wheeler's $\alpha = 1$, also for D-foam, holographic foam $\alpha = \frac{2}{3}$, random-walk $\alpha = \frac{1}{3}$, etc.

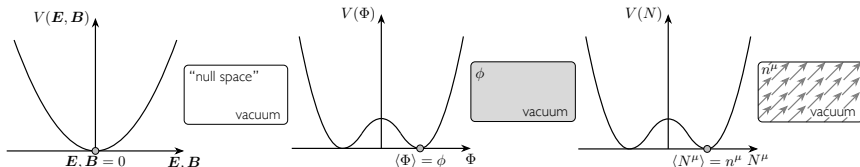
- QG with minimal length [Garay'95 IJMPA, see also Shao, Ma'11 SCPMA]
- discrete space-time? (from entropy bounds) [Xu, Ma'11 MPLA]

$$\delta t \sim \delta \ell \geq \left(\frac{128}{3645\pi} \right)^{\frac{1}{2}} \ell_{\text{Pl}} \simeq 0.1 \ell_{\text{Pl}}$$

Lorentz noninvariance [model-dep.]

- Lorentz-invariance violation from **strings** - **SLSB** by QG vacua

* Tensor condensate in bosonic open-string field theory [Kostelecký, Samuel'89 PRD]



→ effective target-space LV field theory - standard-model extension (SME)
[Colladay, Kostelecký'97, 98 PRD, Myers, Pospelov'03 PRL]

$$\mathcal{L}_{\text{SM}} + \delta^{\text{LV}} \mathcal{L} \supset \delta^{\text{LV}} \mathcal{L}_{\gamma}^{5\text{d}} = -\frac{\xi}{M_{\text{Pl}}} n^\mu F_{\mu\sigma} n_\nu n \cdot \partial \tilde{F}^{\nu\sigma} \Rightarrow \mathcal{E}^2 = \mathbf{k}^2 \pm \frac{2\xi}{M_{\text{Pl}}} \mathcal{E}^2 |\mathbf{k}|$$

* Gravitational defects from noncritical strings [Ellis+'92 PLB, Amelino-Camelia+'97 IJMPA]

$$\mathcal{S}_0 + \mathcal{S}_L \left(\sim \int_{\Sigma} [(\pm)(\partial\phi)^2 - \mathcal{Q}\phi\mathcal{R}_{(2)}] \right) + \int_{\Sigma} \sqrt{\tilde{\gamma}} g_L^i(\phi) V_i \Rightarrow \mathcal{E} \sim |\mathbf{k}| + \rho \mathbf{k}^2 / M_{\text{Pl}}$$

→ D-brane LV models of string cosmology - "stringy space-time (D-)foam"

Lorentz noninvariance [model-indep.]

- Assume a Modified particle Dispersion Relation (MDR) w.r.t. $\mathcal{E}^2 = p^2 + m^2$
e.g., photon (or ultrarelativistic neutrino)

$$\mathcal{E}^2 \simeq \mathbf{p}^2 - s_n \mathcal{E}^2 \left(\frac{|\mathbf{p}|}{E_{LV,n}} \right)^n \longrightarrow v = \frac{\partial \mathcal{E}}{\partial |\mathbf{p}|} \simeq 1 - s_n \frac{1+n}{2} \left(\frac{\mathcal{E}}{E_{LV,n}} \right)^n$$

- it gives birth to Quantum-Gravity (QG) Phenomenology via LVs [See Shao, Ma'10 MPLA, for a review]

- vacuum dispersion & birefringence (via long-baseline exp.s)*
- anomalous/peculiar threshold reactions*
- shifting of existing thresholds, etc.*

...but, suppressed by $E_{LV} \sim \mathcal{O}(M_{Pl})$ v.s.

$$\Lambda_{EW}/M_{Pl} \sim 10^{-16}$$

[recall Bo-Qiang Ma's talk yesterday]

(LHC will probe Λ_{EW})

Can one see quantum gravity/space-time effect in the sky?

say, travel times affected by LV_{n=1}, $t_{LV} = K_1 \frac{(1+z)s}{E_{LV}} = t_o - (1+z)t_s$ (t_s - source-intrinsic lag)

$$K_1(z) = \frac{\mathcal{E}_h - \mathcal{E}_l}{(1+z)H_0} \int_0^z \frac{(1+\mathcal{Z})d\mathcal{Z}}{\sqrt{\Omega_\Lambda + \Omega_M(1+\mathcal{Z})^3}}$$

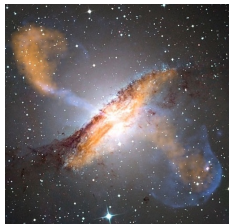
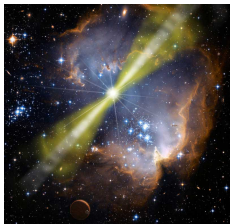
[Jacob, Piran'08 JCAP in Λ CDM, see also Zhu, Ma'22 PRD,
for a derivation in Finsler cosmology]

luckily, astrophysics by means of (multi)messengers play a leading role in making that job
e.g., **energetic** signal from **cosmologically remote** objects [Amelino-Camelia+, Nature393 (1998)]

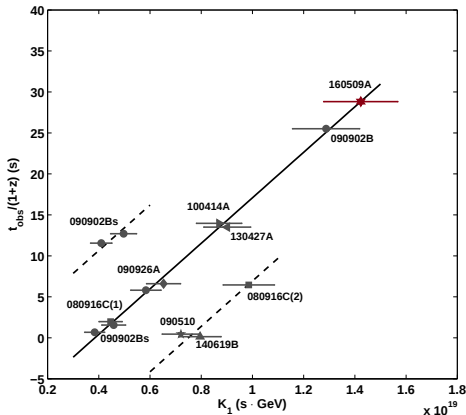
bright Gamma-Ray Burst (GRB)

vs.

Active Galactic Nucleus (AGN)



Light-speed variation in cosmic photons



[Xu, Ma'16 PLB, see also He, Ma'22 Universe, for a review on this suggestion]

- uncertainties: intrinsic lags $\mathcal{O}(\text{sec})$

Analysis on FERMI multi-GeV data

- GRB γ time delay suggests:

★ **light-speed variation**

$$v_{\gamma}(\mathcal{E}) = 1 - \mathcal{E}/E_{\text{LV}(\gamma)}$$

with $E_{\text{LV}} \gtrsim 3.6 \times 10^{17} \text{ GeV}$

[Shao, Xiao, Ma'10, Zhang, Ma'15, Xu, Ma'16 APP]

- re-examination

1. "too rare to be accidental!"

[Amelino-Camelia+'17 Nature Astron.]

2. *statistical significance 3-5 σ*

[Xu, Ma'18 JCAP, Liu, Ma'18 EPJC]

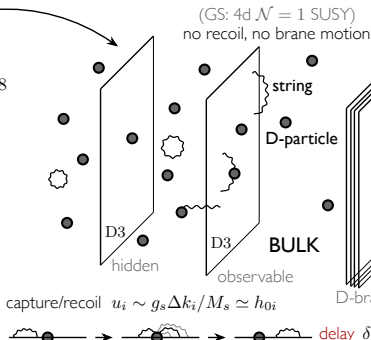
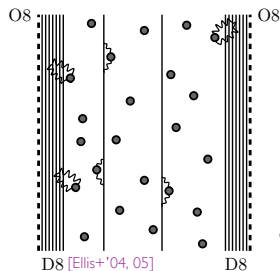
3. *supports from AGNs & others*

[Li, Ma'20 Sci. Bull., Zhu, Ma'21 PLB]

quantum space-time property, or just mimic?

D-brane/string inspired space-time foam

compactify on, e.g., $\text{AdS}_5 \times \mathbb{R}^5$
or $\mathbb{T}^5/\mathbb{Z}_2$ for I/IIA strings
[Ellis+'06]



string/D-foam cosmology:

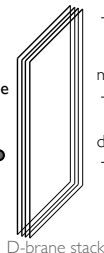
- dark energy budget
- inflation/early universe
- large-scale structure formation [Elghozi+'16; Mavromatos+'12, '13]

modified gravity:

- relativistic MOND (TeV-like models)

dark matter:

- sterile neutrino mass generation [Ellis+'19]
⇒ tiny SM neutrino mass through seesaw [Mavromatos+'11, '17]



$$c_g \simeq 1 - 2g_s \frac{\zeta_D |\mathbf{k}|}{M_s} \simeq 1 - \mathcal{O}\left(\frac{n_D \mathcal{E}}{M_D}\right) \quad \xleftrightarrow[\text{refractive index}]{\zeta_D = \langle \frac{\Delta k}{k} \rangle \geq 0} \quad \eta_{\text{vac}(\gamma)} = 1 + \mathcal{O}(\sqrt{\alpha'} \zeta_D |\mathbf{k}|) \geq 1, \quad M_D = 1/(g_s \sqrt{\alpha'})$$

delay $\delta t \sim \alpha' k^0$ [Seiberg+'99, 00; Ellis+'08]

(a) $\delta c_g := |c_g - 1|$ scales linearly with energy

(b) subluminal refractive index $\eta_{\text{vac}(\gamma)} - 1 > 0$

(c) photons are stable (i.e., do not decay away)

(d) helicity-blind/nonbirefringent foam vacuum

[CL, Ma, [PLB 819\(2021\)136443](#), see also [Results Phys. 26\(2021\)104380](#)]

Recoil distortion & time delay

- Models with (type I/IIA) 0-brane [Ellis+'99, 00 PRD, Ellis+'04 PRD]

- * Deformed σ model for recoiling D-brane [Ellis+'98 IJMPA, Mavromatos, Szabo'99 PRD]

- impulse operator (of LCFT) $V = \int_{\partial\Sigma} \epsilon u_i X^0 \Theta_\epsilon(X^0) \partial_n X^i$ $\Theta_{\epsilon \rightarrow 0+}(t) := \frac{1}{i} \int_{-\infty}^{\infty} \frac{dq}{q - i\epsilon} e^{iqt}$
- dressing of Liouville to restore conformality (criticality)

$$V^L \sim \int_{\Sigma} e^{\alpha^L \phi(z, \bar{z})} \varepsilon_{\alpha\beta} \partial^\beta (\epsilon u_i X^0 \Theta_\epsilon(X^0) \partial^\alpha X^i) \supset -\epsilon^2 u_i \int_{\Sigma} e^{\epsilon(\phi - X^0)} X^0 \Theta(X^0) \partial_\beta \phi \partial^\beta X^i$$

→ “foam-like” Finsler metrics $g_{0i}(X^0, u_i) \sim u_i \epsilon^2 X^0 \Theta(X^0) \sim u_i \sim \zeta k_i / M_D$ ($\zeta < 1$)

$$\mathbf{k}^2 - \mathcal{E}^2 \simeq 2\zeta_D g_s \ell_s \mathcal{E} \mathbf{k}^2 \text{ for } \langle\langle u_i \rangle\rangle \neq 0 \text{ (anisotropic foam)}$$

- * Microscopic modeling of recoil/capture [Seiberg, Witten'99 JHEP, Susskind+'00 JHEP, Ellis+'08 PLB]

$$\delta t \sim \alpha' k^0 / (1 - \mathbf{u}^2) \sim \mathcal{E} \alpha' \text{ as } |u_i| \ll 1 \rightarrow \text{reduced-Lorentz symmetry}$$

- IIB (super)string model with wrapped 3-brane [Li+'09 PLB, Li, Nanopoulos'12 EPJC]

$$\mathcal{A}_{\text{scat}} \text{ comput} \rightarrow \delta t \sim \mathcal{E} \ell_s^2$$

Light-speed variation in a D-foam

- D-particle foam as a (stringy) origin for subluminal LV_γ

e.g., constraint to QG-foam parameter/scale

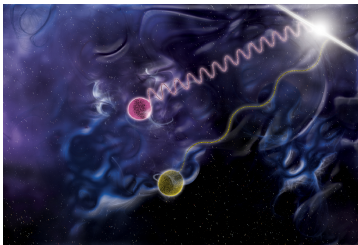
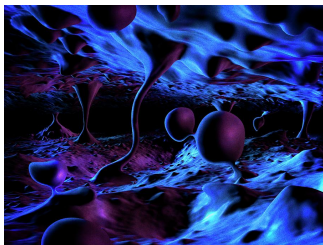
[CL, Ma [2105.06151](#) (PLB)]

$$\frac{\zeta_D g_s}{M_s} \simeq \frac{1}{2E_{LV}} \lesssim 1.4 \times 10^{-18} \text{ GeV}^{-1}$$

$$M_s \gtrsim 7.2 \times 10^{26} \zeta_D g_s \text{ eV} \gtrsim \mathcal{O}(\text{TeV})$$



light-speed variation of GRB/AGN, if plausible, *supports* stringy D(effect)-foam



photons travel through “foamy space-time” at different speeds!

[Credit: Mark Garlick'16(left), NASA/Sonoma State Univ., Aureore Simonnet(right)]

Escaping from other tight bounds

- (i) Lorentz violating γ -decay, $\gamma \rightarrow ee^+$

very-high-energy (VHE; $\mathcal{E} \gtrsim 0.1$ TeV) γ -ray bounds **superluminal** LV_γ

- * Crab Nebula 50-80 TeV- γ : $E_{\text{LV}} \gtrsim 10^{20}$ GeV [Martínez-Huerta, Peñáz-Lorenzana'17 PRD]
- * HAWC ~ 100 TeV photons: $E_{\text{LV}} > 2.2 \times 10^{22}$ GeV [Albert+(HAWC)'20 PRL]
- * Tibet AS γ Galactic γ -rays up to 957^{+166}_{-141} TeV [Amenomori+(Tibet AS γ)'21 PRL]

$$E_{\text{LV}}^{(\text{sup})} \gtrsim \mathcal{E}^3 / (4m_e^2) \sim 8 \times 10^{23} \text{ GeV}$$

- (ii) Vacuum birefringence - $\mathcal{O}(10^{11}) \times \gamma$ -decay limit $\sim E_{\text{LV}}^{(\text{bire})}$ for **birefringent** LV_γ

→ complementary **support** to string/D-brane foam scenario [CL, Ma'21 PLB & Results Phys.]

$$\underbrace{M_{\text{Pl}} \ll E_{\text{LV}}^{(\text{sup})}, E_{\text{LV}}^{(\text{bire})}}_{\text{natural with D-foam}} \not\rightarrow \frac{M_D}{\zeta_D} \quad (\zeta_D > 0 \text{ for } \gamma_{R,L})$$

- Future improvements with HAWC, Tibet AS γ & **LHAASO** !!

Large High Altitude Air Shower Observatory

- China's 3G mountain observatory - LHAASO

[See Cao'21 Nature Astron., Cao+'22 CPC, for LHAASO's objectives]

an ultrahigh-energy (UHE) cosmic-/ γ -ray “hunter” set on Tibetan Plateau!



[Credit: Institute of High Energy Physics/Chinese Academy of Sciences (IHEP/CAS)]

How to receive messengers from the sky?

[Credit: IHEP/CAS]

WCDA



WFCTA



KM2A



(EDs + MDs)



3 major components of LHAASO

Opening the UHE γ window

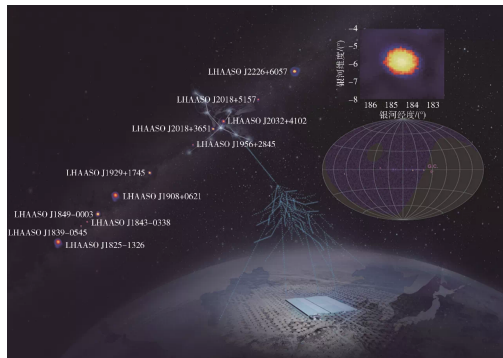
- Capture the *most-energetic* γ evt from the Cosmos! [Cao+(LHAASO), Nature594 (2021)]

[See also CL, Ma, *Sci. Bull.* 66(2021)2254,

for news & views, 李成翊, 马伯强, *现代物理知识*, 2022.34(1), p.33-37 (科普)]



Breakthrough discovery via LHAASO-KM2A



[Credit: LHAASO collab'21]

First results of LHAASO:

12 PeVatrons

- high significance $> 7\sigma$
- BG-free: CR BG rejection rate 10^{-5}
- large statistics: 530 UHE photons

★ LHAASO J2032+4102:

$$\mathcal{E}_{\max} = 1.42 \pm 0.13 \text{ PeV}$$

the highest-energy γ ever observed!

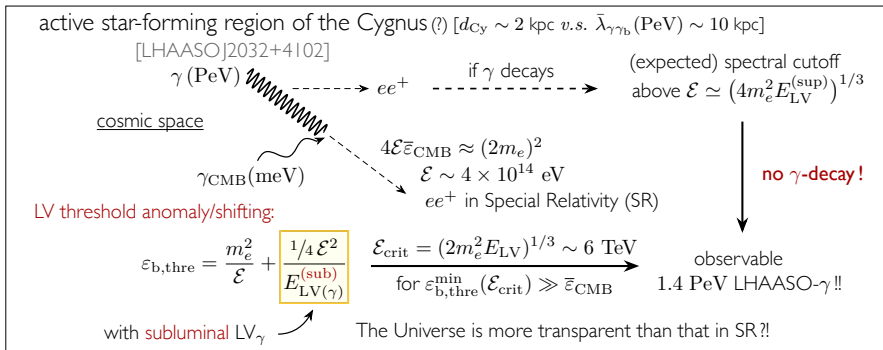
- multiple types of candidates

[Cao+(LHAASO)'21 Nature]

the Universe (incl. the Milky Way) is full of PeVatrons!

Implications for γ Lorentz violation

- Probing LV_γ via LHAASO PeV photon [CL, Ma, [PRD 104\(2021\)063012](#)]
 - stringent constraint on γ self-decay due to *superluminal* LV_γ
 - support for threshold anomaly of $\gamma\gamma_b \rightarrow ee^+$ induced by *subluminal* LV_γ



[See also CL, Ma [2109.07794 \(Sci. Bull.\)](#)]

- **Photon stability** against decay, $\gamma \rightarrow ee^+$

HAWC ~ 100 TeV $E_{LV\gamma} \gtrsim 2.2 \times 10^{22}$ GeV [Albert+(HAWC)'20 PRL]

Tibet AS γ up to sub-PeV scales $E_{LV\gamma} \geq 8 \times 10^{23}$ GeV [CL, Ma 2105.06151 (PLB)]

LHAASO 1.4 PeV evt (yielding **strongest** bound ever reported) [CL, Ma 2105.07967 (PRD)]

$$E_{LV\gamma}^{(\text{sup})} \gtrsim 9.57 \times 10^{32} \left(\frac{\mathcal{E}}{\text{PeV}} \right)^3 \text{ eV} \approx 2.74 \times 10^{24} \text{ GeV}$$

→ severely limits, e.g., SME [$\xi \ll \mathcal{O}(1)$] v.s. **supports** string/D-brane foam!

- **Necessity to modify $\gamma\gamma_b \rightarrow ee^+$ kinematics?** [CL, Ma'21 PRD]

$\gamma\gamma_b$ threshold anomaly “protects” above-threshold photons of LHAASO!

sources: **galactic** or **extragalactic**??

→ *extragalactic PeV γ as crucial test of subluminal LV_γ*
any observed γ of $\gtrsim 0.4$ PeV from outside of our galaxy as signal for new physics!

[Li, Ma'21 JHEAp, 23 APP + EPJC, Wang, Ma'23 PRD: **new supports of either LV or Axion** by GRB221009A]

“optical transparency” - $E_{LV\gamma}^{(\text{sub})} \lesssim \mathcal{O}(10^{23} \text{ GeV})$

[Luohan Wang's talk]

Petaelectronvolt γ from the “Standard Candle”

- Highest-energy messengers yet arrive from ancient Crab Nebula!

LHAASO measurement

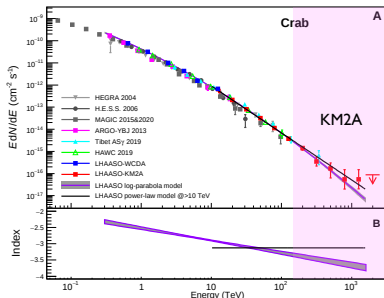
[Cao+(LHAASO), Science373 (2021) July 8th]

- unique UHE SED; a PeVatron without ambiguity
- clear origin - a well-known Pulsar Wind Nebula (PWN)
- record-breaking Crab γ ($\gtrsim 100$ TeV since 2019!)

$$\mathcal{E}_{\text{max}}^{\text{Crab}} = 1.12 \pm 0.09 \text{ PeV}$$



remnant of SN explosion (“guest star”) witnessed in 1054 AD



[Credit: NASA, ESA, NRAO/AUI/NSF, Buenos Aires Univ.(left), LHAASO collab'21(right)]

Does electron (or, its antiparticle counterpart) have nontrivial properties *in vacuo*?

say, it possesses a modified canonical dispersion relation [CL, Ma, [PLB 829\(2022\)137034](#)]

$$\mathcal{E}_e^2 = m_e^2 + \mathbf{p}_e^2 (1 + \delta_e^{(2)}) - s_{e,n} \mathcal{E}_e^2 \left(\frac{|\mathbf{p}_e|}{E_{\text{LVe},n}} \right)^n \quad |\delta_e|^{\text{LEP}} \lesssim 10^{-15} \quad [\text{Altschul'10 PRD}]$$

so vacuum Čerenkov (VČ) effect by charged leptons, if being superluminal, occurs (e.g., efficient decay via VČ of electron/positron, $e \rightarrow e\gamma$) [Jacobson+'04 PRL]

→ electron of some high $\mathcal{E}_e$ is no longer stable in a vacuum!

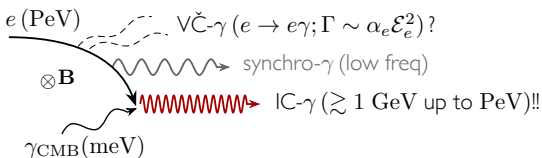
Stability against IC Čerenkov effect

→ Crab Nebula as an ideal laboratory for constraining, or even ruling out LV_e

- Assume an electronic origin (synchro + *inverse-Compton (IC)*)

inside the nebula

no $e^\mp$ Čerenkov!



- IC Čerenkov bound**

50 TeV photons $E_{LV_e} \gtrsim 10^{21}$ GeV

HEGRA up to ~ 75 TeV strengthened by $(3/2)^3 \approx 3$

Tibet AS γ up to ~ 450 TeV (near-PeV $e^\mp$ is inferred) [CL, Ma [2204.02956](#)]

$$E_{LV_e}^{(\text{sup})} > 2\mathcal{E}_e^3/m_e^2 \sim 7 \times 10^{23} \text{ GeV}$$

Stability against IC Čerenkov effect

→ Crab Nebula as an ideal laboratory for constraining, or even *ruling out* LV_e

- IC Čerenkov bound via LHAASO

[CL, Ma 2204.02956 (PLB)]

$$E_{\text{LV}_e}^{(\text{sup})} \gtrsim 7.21 \times 10^{25} \left(\frac{\mathcal{E}^{\text{Crab}}}{\text{PeV}} \right)^{2.38} \text{ GeV}$$

$$\geq (7.7 \times 10^6) \times M_{\text{Pl}}$$

$$\sim 9.4 \times 10^{25} \text{ GeV (improved by } \gtrsim 10^4)$$

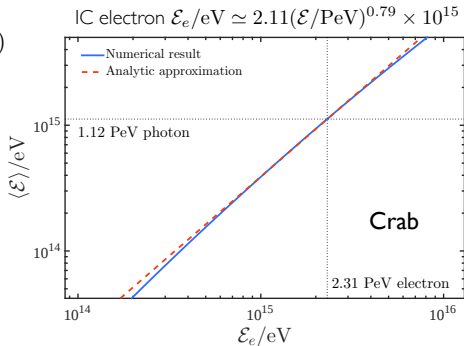
$$\sim \mathcal{O}(10^{35} \text{ eV})$$

it severely *limits*, e.g., SME $\eta \ll \mathcal{O}(1)$

$$\delta^{\text{LV}} \mathcal{L}_{\text{QED}} \supset \frac{1}{M_{\text{Pl}}} \bar{\psi} (\chi_1 \not{n} + \chi_2 \not{n} \gamma_5) (n \cdot \partial)^2 \psi$$

$$\text{with } 2(\chi_1 \pm \chi_2) =: \eta_{R/L} \lesssim 1.3 \times 10^{-7}$$

[See also He, Ma'22 PLB,
for a joint analy for param plane]



Crab radiation & Quantum Gravity

- **Synchrotron constraint** [Jacobson+'03 Nature]

critical freq $\omega_c = 3|e\mathbf{B}|\mathcal{E}_e^2/(2m_e^3)$ affected by **subluminal** LV_e

$$\omega_o \sim \mathcal{O}(.1 \text{ GeV}) \lesssim \omega_c \leq \frac{5^{5/6}}{9\sqrt[3]{2}} \frac{|e\mathbf{B}|}{m_e} (m_e/E_{LV_e}^{(\text{sub})})^{-\frac{2}{3}}$$

maximal at $\mathcal{E}_e = (2m_e^2 E_{LV_e}/5)^{1/3}$

$$E_{LV_e} \gtrsim 10^{24} \text{ GeV}$$

[Maccione+'07 JCAP]

- Pheno preferred LV-feature_{QED}

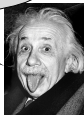
1. *In vacuo γ speed variation (as catalyzed by D-foam)*

2. *No electron/positron LV below Planck*

➡ LV_e may not be permitted by nature?

[CL, Ma [2204.02956](#) (Phys. Lett. B)]

No $e^\mp$ Lorentz violation ?!



Crab radiation & Quantum Gravity

- Synchrotron constraint [Jacobson+'03 Nature]

critical freq $\omega_c = 3|e\mathbf{B}|\mathcal{E}_e^2/(2m_e^3)$ affected by **subluminal** LV_e

$$\omega_o \sim \mathcal{O}(1 \text{ GeV}) \lesssim \omega_c \leq \frac{5^{5/6}}{9\sqrt[3]{2}} \frac{|e\mathbf{B}|}{m_e} (m_e/E_{LV_e}^{(\text{sub})})^{-\frac{2}{3}} \quad E_{LV_e} \gtrsim 10^{24} \text{ GeV}$$

- Pheno preferred LV-feature_{QED}
- Crab discriminates between models of QG?** [CL, Ma'22 PLB]

* D-foam transparency to charged fields! D-particle: no "hair" - (electric) neutrality

$$S_{\text{endpoint}} = \int_{\partial\Sigma} d\tau A_a(X) (dX^a/d\tau)$$

[“such a cutting is not allowed, due to charge conservation ($U(1)_{em}$ gauge inv.)”, Ellis+'04 APP, Nature, IJMPA]

- no (tree-level) effect on probes carrying conserved charges (say, electric, or color flux)
- $e^\mp$ has usual in-vacuo behavior ➡ evasion of any limit from soft/hard $V\check{C}$

CPT violation in cosmic neutrinos

Analysis on IceCube TeV & PeV data

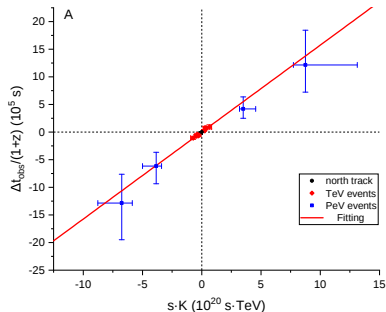
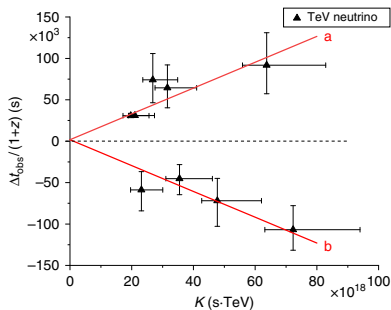
[Huang, Ma'18 Commun. Phys.]

- association of ν evts with GRBs (delay + advance):

★ neutrino-speed variation

$$v_\nu(\mathcal{E}_\nu) = 1 \mp \mathcal{E}_\nu / E_{LV\nu} \quad E_{LV\nu} \sim 6 \times 10^{17} \text{ GeV}$$

- additional supports [Huang, Li, Ma'19 PRD, see also Huang, Ma'22 Fund. Res.]



CPT breaking neutrino from strings

- Asymmetric $\nu/\bar{\nu}$ -dispersion due to D-foam [CL, Ma, [PLB 835\(2022\)137543](#)]
- isotropic $\langle\langle \frac{\Delta k}{k} \rangle\rangle = \langle\langle \zeta \rangle\rangle = 0$; but stochastic $\langle\langle \zeta^2 \rangle\rangle =: \zeta_D^2 < 1$ [Mavromatos, Sarkar'05 PRD]

$$\begin{aligned}\mathcal{E}_\nu(\mathbf{k}) &= \underbrace{\sqrt{\mathbf{k}^2 + m_\nu^2} \left(1 + \frac{g_s^2}{2M_s^2} \zeta_D^2 \mathbf{k}^2\right)}_{\text{geometric origin}} - \underbrace{\zeta_D^2 g_s \frac{\mathbf{k}^2}{2M_s}}_{\text{kinematic origin}} + \mathcal{O}(1/M_D^4) \\ \mathcal{E}_{\bar{\nu}}(\mathbf{k}) &= \underbrace{\sqrt{\mathbf{k}^2 + m_\nu^2} \left(1 + \frac{g_s^2}{2M_s^2} \zeta_D^2 \mathbf{k}^2\right)}_{\text{geometric origin}} + \underbrace{\zeta_D^2 g_s \frac{\mathbf{k}^2}{2M_s}}_{\text{kinematic origin}} + \mathcal{O}(1/M_D^4)\end{aligned}$$

- CPT-violating (CPTV) neutrino propagation *in vacuo*

* Only subluminal ν is present, while superluminality of $\bar{\nu}$ is established

$$\delta_{\bar{\nu}} := v_{\bar{\nu}} - 1 = \zeta_D^2 |\mathbf{k}| / M_D > 0 \quad \delta_\nu = -\zeta_D^2 |\mathbf{k}| / M_D$$

➡ different propagation properties between ν 's & $\bar{\nu}$'s at IceCube!

[See also CL, Ma [2303.04765 \(JHEP\)](#)]

$$\zeta_D^2 \simeq 1.6 \times 10^{-18} \left(\frac{M_s}{g_s} \right) \text{ GeV}^{-1}$$

Suppressing $\bar{\nu}$ -decay

- Cohen-Glashow v.s. OPERA “phantom”: $\nu \rightarrow \nu ee^+$ [Cohen, Glashow'11 PRL]
e.g., limits on superluminal velocities

$$\delta_{>} := \mathcal{E}_{\nu}/E_{\text{LV}\nu} < 10^{-18} \text{ to } \sim 5 \times 10^{-19} \quad \longrightarrow \quad E_{\text{LV}\nu}^{(\text{sup})} \geq (10^3 - 10^5) \times M_{\text{Pl}}$$

- Plausible violation of energy conservation **inhibits** $\bar{\nu}$ -decay? [CL, Ma'22 PLB, 23 JHEP]
- * Stochastic loss $\delta\mathcal{E}_D$ of $(\varsigma_I/M_D)p^2$ ($\varsigma_I > 0$) in particle reaction in D-foam [Ellis+'01 PRD]
affects **decay threshold** for, e.g., most efficient $\bar{\nu} \rightarrow \bar{\nu} ee^+$ channel:

$$\mathcal{E}_{\bar{\nu}} > \frac{2m_e}{\sqrt{\Delta}} \quad \Delta := \left(1 - \frac{4\varsigma_I}{\dot{\varsigma}_D^2}\right) \delta_{\bar{\nu}}$$

- for observing $\mathcal{O}(\text{PeV})$ superluminal evt (#35, or #20)

$$(\dot{\varsigma}_D^2 - 4\varsigma_I) \lesssim \mathcal{O}(10^{-7}) \text{ or, with assignment } \varsigma_I \geq \dot{\varsigma}_D^2/2$$

Conclusions

Take home message

- Consistent LV_γ (incl. LHAASO obs) via D-foam [CL, Ma 2105.06151 (PLB) + 2105.07967 (PRD)]
- In accordance with Crab Nebula limits on LV_e [CL, Ma 2204.02956 (PLB)]
- CPTV for IceCube neutrino from strings [CL, Ma 2303.04765 (JHEP) + 2211.00900 (PLB)]

Open question

what is the fate of UV Lorentz symmetry (say, LV as essential ingredient of nature?)

→ unraveling quantum gravity - “Holy Grail”

*the situation starts to become exciting and,
time will show if QG can be finally confirmed by exp.s*

Thanks for your attention !