Lighting Electroweak-Violating ALP-Lepton Interactions at CEPC

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Ref: 2210.15648 [hep-ph]

26/07/2023

The Second International Conference on Axion Physics and Experiment (Axion 2023)

Content

- 1. Motivation
- 2. ALP-lepton interactions
- 3. Energy enhancement behaviors in $e^+e^- \rightarrow \nu_e a \overline{\nu_e}$
- 4. The signal-to-background analysis at CEPC
- 5. Conclusion

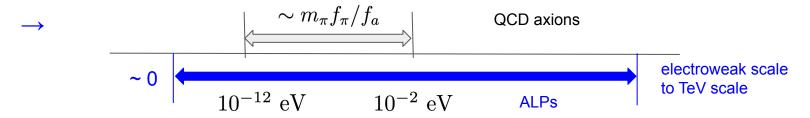
Content

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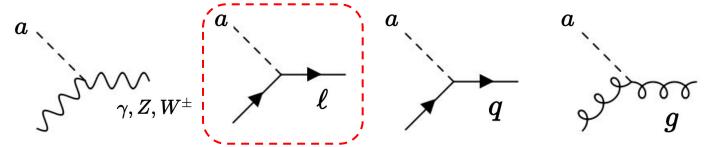
4 W + 1 H questions for axion-like particles (ALPs)

- 1. What does an ALP come from?
 - → An ALP is a light pseudoscalar with approximate shift symmetry.
- 2. Why we need ALPs?
 - \rightarrow (1) Strong CP problem, (2) DM candidates, (3) Hierarchy problem of the Higgs boson mass, (4) A hint of some string theories, ... etc.
- 3. Which is the mass range of ALPs?

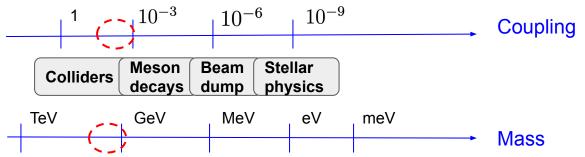


4 W + 1 H questions for axion-like particles (ALPs)

4. Who can interact with ALPs (SM particles only)?



5. How to search for ALPs?



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The global $U(1)_{PQ}$ \Longrightarrow pseudo Nambu-Goldstone bosons (ALPs) shift symmetry $a(x) \rightarrow a(x) + \text{const.}$ $\mathcal{L}_{\ell \text{ALP}} = \partial_{\mu} a J^{\mu}_{\text{PQ},\ell}$

$$\mathcal{L}_{\ell \text{ALP}} = \partial_{\mu} a \left[J^{\mu}_{\text{PQ},\ell} \right]$$
 dimensionless coupling
$$J^{\mu}_{\text{PQ},\ell} = \frac{\langle c^{\nabla}_{\ell} \rangle}{2 \Lambda} \bar{\ell} \gamma^{\mu} \ell + \frac{\langle c^{A}_{\ell} \rangle}{2 \Lambda} \bar{\ell} \gamma^{\mu} \gamma_{5} \ell + \frac{\langle c_{\nu} \rangle}{2 \Lambda} \bar{\nu}_{\ell} \gamma^{\mu} P_{L} \nu_{\ell}$$

$$U(1)_{\text{PQ}} \text{ new physics scale}$$

$$\mathcal{L}_{\ell ALP} = \partial_{\mu} a \left[J_{PQ,\ell}^{\mu} \right] \qquad \text{Are the previous statements in the literature correct?} \\ J_{PQ,\ell}^{\mu} = \left[\frac{c_{\ell}^{V}}{2\Lambda} \overline{\ell} \gamma^{\mu} \ell \right] + \left[\frac{c_{\ell}^{A}}{2\Lambda} \overline{\ell} \gamma^{\mu} \gamma_{5} \ell \right] + \left[\frac{c_{\nu}}{2\Lambda} \overline{\nu_{\ell}} \gamma^{\mu} P_{L} \nu_{\ell} \right] \\ \text{"The vector coupling is unphysical"}} \\ " \quad \frac{1}{2} \partial_{\mu} a \overline{\ell} \gamma^{\mu} \gamma_{5} \ell = m_{\ell} a \overline{\ell} i \gamma_{5} \ell \quad "$$

$$J_{\mathrm{PQ},\ell}^{\mu} = \frac{c_{\ell}^{V}}{2\Lambda} \overline{\ell} \gamma^{\mu} \ell + \frac{c_{\ell}^{A}}{2\Lambda} \overline{\ell} \gamma^{\mu} \gamma_{5} \ell + \frac{c_{\nu}}{2\Lambda} \overline{\nu_{\ell}} \gamma^{\mu} P_{L} \nu_{\ell}$$

More generally, each lepton coupling term in the above can arise independently in a electroweak invariant theory by including the following currents,

$$\overline{(HL)}\gamma_{\mu}(HL)$$
, $\overline{e}_{R}\gamma_{\mu}e_{R}$, and $\overline{(H^{\dagger}L)}\gamma_{\mu}(H^{\dagger}L)$,

Phys. Rev. Lett. 130, 241801 [arXiv: 2209.00665]

New Opportunities for Detecting Axion-Lepton Interactions

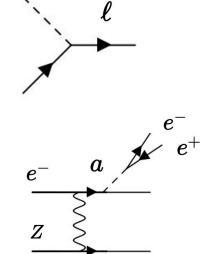
Wolfgang Altmannshofer, Jeff A. Dror, and Stefania Gori Phys. Rev. Lett. **130**, 241801 – Published 13 June 2023

ABSTRACT

We revisit the theory and constraints on axionlike particles (ALPs) interacting with leptons. We clarify some subtleties in the constraints on ALP parameter space and find several new opportunities for ALP detection. We identify a qualitative difference between weak-violating and weak-preserving ALPs, which dramatically change the current constraints due to possible "energy enhancements" in various processes. This new understanding leads to additional opportunities for ALP detection through charged meson decays (e.g., $\pi^+ \to e^+ \nu a$, $K^+ \to e^+ \nu a$) and W boson decays. The new bounds impact both weak-preserving and weak-violating ALPs and have implications for the QCD axion and addressing experimental anomalies using ALPs.

After integration by parts of $\partial_{\mu}a\ J^{\mu}_{PQ,\ell}$, the $\mathcal{L}_{\ell ALP}$ can be represented as

$$\begin{split} a \; \partial_{\mu} J^{\mu}_{\mathrm{PQ},\ell} = & i c_{\ell}^{A} \frac{m_{\ell}}{\Lambda} \; a \bar{\ell} \gamma_{5} \ell \bigg] \\ + \; \frac{\alpha_{\mathrm{em}}}{4\pi\Lambda} \bigg[\frac{c_{\ell}^{V} - c_{\ell}^{A} + c_{\nu}}{4s_{W}^{2}} \; a W_{\mu\nu}^{+} \tilde{W}^{-,\mu\nu} \\ + \; \frac{c_{\ell}^{V} - c_{\ell}^{A} (1 - 4s_{W}^{2})}{2s_{W} c_{W}} \; a F_{\mu\nu} \tilde{Z}^{\mu\nu} - c_{\ell}^{A} \; a F_{\mu\nu} \tilde{F}^{\mu\nu} + \\ \frac{c_{\ell}^{V} (1 - 4s_{W}^{2}) - c_{\ell}^{A} (1 - 4s_{W}^{2} + 8s_{W}^{4}) + c_{\nu}}{8s_{W}^{2} c_{W}^{2}} \; a Z_{\mu\nu} \tilde{Z}^{\mu\nu} \bigg] \\ + \; \frac{ig_{W}}{2\sqrt{2}\Lambda} (c_{\ell}^{A} - c_{\ell}^{V} + c_{\nu}) \; a (\bar{\ell} \gamma^{\mu} P_{L} \nu) W_{\mu}^{-} \; + \; \mathrm{h.c.} \; , \end{split}$$



After integration by parts of $\partial_{\mu}a\ J^{\mu}_{\mathrm{PQ},\ell}$, the $\mathcal{L}_{\ell\mathrm{ALP}}$ can be represented as

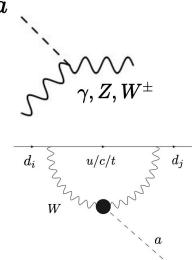
$$a \ \partial_{\mu} J_{\text{PQ},\ell}^{\mu} = i c_{\ell}^{A} \frac{m_{\ell}}{\Lambda} \ a \bar{\ell} \gamma_{5} \ell$$

$$\left(+ \frac{\alpha_{\text{em}}}{4\pi\Lambda} \left[\frac{c_{\ell}^{V} - c_{\ell}^{A} + c_{\nu}}{4s_{W}^{2}} \ aW_{\mu\nu}^{+} \tilde{W}^{-,\mu\nu} \right] \right)$$

$$+ \frac{c_{\ell}^{V} - c_{\ell}^{A} (1 - 4s_{W}^{2})}{2s_{W} c_{W}} \ aF_{\mu\nu} \tilde{Z}^{\mu\nu} - c_{\ell}^{A} \ aF_{\mu\nu} \tilde{F}^{\mu\nu} +$$

$$\left[\frac{c_{\ell}^{V} (1 - 4s_{W}^{2}) - c_{\ell}^{A} (1 - 4s_{W}^{2} + 8s_{W}^{4}) + c_{\nu}}{8s_{W}^{2} c_{W}^{2}} \ aZ_{\mu\nu} \tilde{Z}^{\mu\nu} \right]$$

$$+ \frac{ig_{W}}{2\sqrt{2}\Lambda} (c_{\ell}^{A} - c_{\ell}^{V} + c_{\nu}) \ a(\bar{\ell}\gamma^{\mu} P_{L}\nu) W_{\mu}^{-} + \text{h.c.},$$



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$$\left[\frac{c_{\ell}^{V} (1 - 4s_{W}^{2}) - c_{\ell}^{A} (1 - 4s_{W}^{2} + 8s_{W}^{4}) + c_{\nu}}{8s_{W}^{2} c_{W}^{2}} \ aZ_{\mu\nu} \tilde{Z}^{\mu\nu} \right]$$

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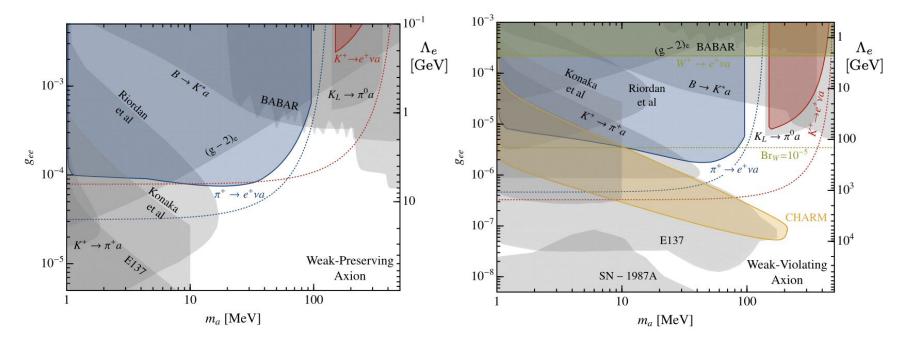
$$+ \frac{c_{\ell}^{V} - c_{\ell}^{A} (1 - 4s_{W}^{2})}{2s_{W} c_{W}} \ aF_{\mu\nu} \tilde{Z}^{\mu\nu} - c_{\ell}^{A} \ aF_{\mu\nu} \tilde{F}^{\mu\nu} +$$

$$\frac{c_{\ell}^{V} (1 - 4s_{W}^{2}) - c_{\ell}^{A} (1 - 4s_{W}^{2} + 8s_{W}^{4}) + c_{\nu}}{8s_{W}^{2} c_{W}^{2}} \ aZ_{\mu\nu} \tilde{Z}^{\mu\nu} \right]$$

$$+ \frac{ig_{W}}{2\sqrt{2}\Lambda} (c_{\ell}^{A} - c_{\ell}^{V} + c_{\nu}) \ a(\bar{\ell}\gamma^{\mu} P_{L}\nu) W_{\mu}^{-} + \text{h.c.},$$

$$(A)$$

$$\frac{P^{+}}{2\sqrt{2}\Lambda} (c_{\ell}^{A} - c_{\ell}^{V} + c_{\nu}) \ a(\bar{\ell}\gamma^{\mu} P_{L}\nu) W_{\mu}^{-} + \text{h.c.},$$



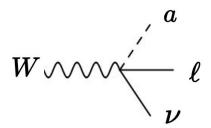
$$j^{\mu}_{
m PQ} = rac{ar{g}_{\ell\ell}}{2m_{\ell}}ar{\ell}\gamma^{\mu}\ell + rac{g_{\ell\ell}}{2m_{\ell}}ar{\ell}\gamma^{\mu}\gamma_5\ell + rac{g_{
u_{\ell}}}{2m_{\ell}}ar{
u}_{\ell}\gamma^{\mu}P_L
u_{\ell}\,.$$
 $\Lambda_e \equiv m_e/g_{ee}$

Wolfgang Altmannshofer, Jeff A. Dror, and Stefania Gori Phys. Rev. Lett. 130, 241801 - Published 13 June 2023

$$\Lambda_e \equiv m_e/g_{ee}$$

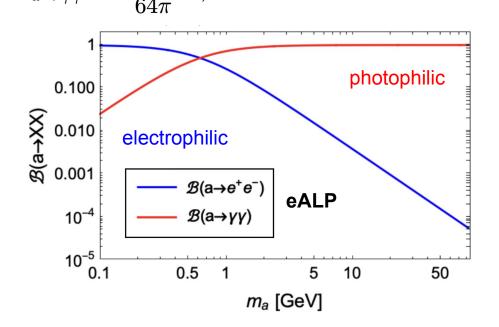
After integration by parts of $\partial_{\mu}a\ J^{\mu}_{\mathrm{PQ},\ell}$, the $\mathcal{L}_{\ell\mathrm{ALP}}$ can be represented as

$$\begin{split} a \; \partial_{\mu} J_{\mathrm{PQ},\ell}^{\mu} &= i c_{\ell}^{A} \frac{m_{\ell}}{\Lambda} \; a \bar{\ell} \gamma_{5} \ell \\ &+ \frac{\alpha_{\mathrm{em}}}{4\pi\Lambda} \left[\frac{c_{\ell}^{V} - c_{\ell}^{A} + c_{\nu}}{4s_{W}^{2}} \; a W_{\mu\nu}^{+} \tilde{W}^{-,\mu\nu} \right. \\ &+ \frac{c_{\ell}^{V} - c_{\ell}^{A} (1 - 4s_{W}^{2})}{2s_{W} c_{W}} \; a F_{\mu\nu} \tilde{Z}^{\mu\nu} - c_{\ell}^{A} \; a F_{\mu\nu} \tilde{F}^{\mu\nu} + \\ &\frac{c_{\ell}^{V} (1 - 4s_{W}^{2}) - c_{\ell}^{A} (1 - 4s_{W}^{2} + 8s_{W}^{4}) + c_{\nu}}{8s_{W}^{2} c_{W}^{2}} \; a Z_{\mu\nu} \tilde{Z}^{\mu\nu} \right] \\ &\left. \left. + \frac{i g_{W}}{2\sqrt{2}\Lambda} (c_{\ell}^{A} - c_{\ell}^{V} + c_{\nu}) \; a (\bar{\ell} \gamma^{\mu} P_{L} \nu) W_{\mu}^{-} \; + \; \mathrm{h.c.} \right], \end{split}$$



How about the scenario for heavy leptophilic ALPs?

Leptophilic ALP decay modes



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Electroweak Violating and Electroweak Preserving scenarios

Electroweak Violating (**EWV**): $c_{\ell}^{V} = c_{\nu} = 0, c_{\ell}^{A} \neq 0,$

Electroweak Preserving (**EWP**): $c_{\nu} = 0, c_{\ell}^{V} = c_{\ell}^{A} \neq 0$

$$J^{\mu}_{\mathrm{PQ},\ell} = \frac{c_{\ell}^{V}}{2\Lambda} \overline{\ell} \gamma^{\mu} \ell + \frac{c_{\ell}^{A}}{2\Lambda} \overline{\ell} \gamma^{\mu} \gamma_{5} \ell + \frac{c_{\nu}}{2\Lambda} \overline{\nu_{\ell}} \gamma^{\mu} P_{L} \nu_{\ell}$$

EWP:

- 1. PQ charges are electroweak symmetric
- 2. The lepton current is pure right-handed coupling current

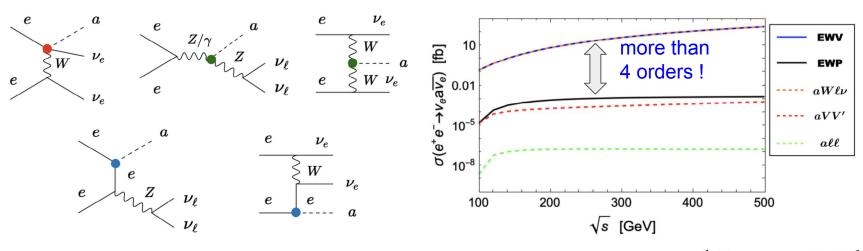
$$J_{\mathrm{PQ},\ell}^{\mu} = \frac{c_{\ell}^{A}}{\Lambda} \overline{\ell} \gamma_{\mu} P_{R} \ell$$

EWV:

- Generated through RG flow
- 2. Also by $\overline{(HL)}\gamma_{\mu}(HL)$
- The lepton current is pure axial-vector current

$$J_{\mathrm{PQ},\ell}^{\mu} = \frac{c_{\ell}^{A}}{2\Lambda} \overline{\ell} \gamma_{\mu} \gamma_{5} \ell$$

$$e^+e^- \to \nu_e a \overline{\nu_e}$$



 $c_e^A/\Lambda = 0.01 \text{ GeV}^{-1}$

$$e^+e^- \to \nu_e a \overline{\nu_e}$$

$$e^{-}(p_{1})e^{+}(p_{2}) \rightarrow \nu_{e}(q_{1})a(q_{2})\overline{\nu_{e}}(q_{3}), \quad \overline{|\mathcal{M}|^{2}} =$$

$$\frac{g_{W}^{4}\left(c_{\ell}^{A} - c_{\ell}^{V} + c_{\nu}\right)^{2}}{32\Lambda^{2}}\left(\frac{1}{k^{2} - M_{W}^{2}} + \frac{1}{k'^{2} - M_{W}^{2}}\right)^{2} \times \left(s - 2m_{e}^{2}\right)\left[s - m_{a}^{2} - 2q_{2}\cdot(q_{1} + q_{3})\right],$$

$$(3.$$

$$e$$
 v_e
 v_e

where $s = (p_1 + p_2)^2 = (q_1 + q_2 + q_3)^2$, $k = p_2 - q_3$ and $k' = p_1 - q_1$. It's clear to see this amplitude square can be enhanced when the momentum transferring in this t-channel process is large enough and it is estimated to be smaller than

$$|\overline{\mathcal{M}}|^2 < \frac{g_W^4 \left(c_\ell^A - c_\ell^V + c_\nu\right)^2}{16\Lambda^2 \left(s - M_{cr}^2\right)^2} \left(s - 2m_e^2\right) \left(\sqrt{s} - m_a\right)^2.$$

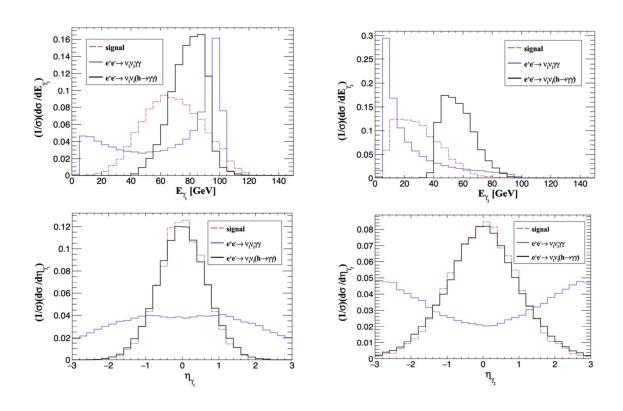
Content

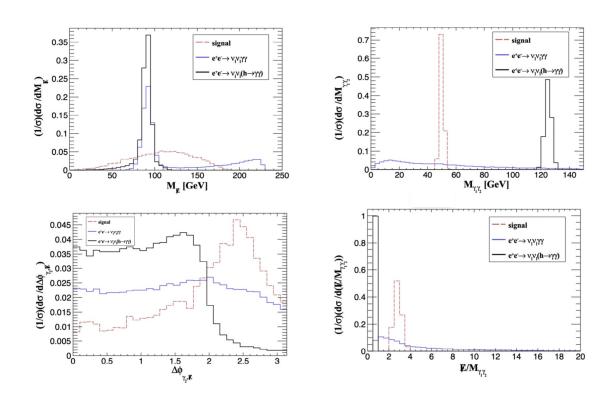
- 1. Motivation
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- 1. We choose the CEPC with $\sqrt{s}=240~{\rm GeV}$
- 2. Benchmark point : $m_a = 50 \text{ GeV with } c_e^A/\Lambda = 1 \text{ TeV}^{-1}$.
- 3. The signal process $e^+e^- \to \nu_e a \overline{\nu_e}$, $a \to \gamma \gamma$ signature : 2 isolated photons plus missing energy
- 4. Possible SM backgrounds:

$$e^+e^-
ightarrow \gamma\gamma
u_\ell\overline{
u_\ell}$$
 $e^+e^-
ightarrow
u_\ell\overline{
u_\ell}h
ightarrow
u_\ell\overline{
u_\ell}(\gamma\gamma)$

- (1) $N(\gamma) \ge 2$ with $30 < E_{\gamma_1} < 90$ GeV, $E_{\gamma_2} > 15$ GeV, $|\eta_{\gamma_1}| < 1.5$ and $|\eta_{\gamma_2}| < 2.0$,
- (2) $E > 120 \text{ GeV} \text{ and } |\eta_{E}| < 2.0,$
- (3) Veto $85 < M_{E} < 95 \text{ GeV}$,
- (4) $|M_{\gamma_1\gamma_2} m_a| < 3 \text{ GeV},$
- (5) $\Delta \phi_{\gamma_1, E} > 2.5 \text{ and } \Delta \phi_{\gamma_2, E} > 1.8$,
- (6) $2.2 < E/M_{\gamma_1 \gamma_2} < 3.6$,





cut flow in σ [fb]	signal	$ u_\ell \overline{ u_\ell} \gamma \gamma$	$ u_\ell \overline{ u_\ell}(h o \gamma \gamma) $
Generator	0.11	263.60	7.67×10^{-2}
cut-(1)	7.10×10^{-2}	32.23	5.47×10^{-2}
cut-(2)	6.62×10^{-2}	21.85	3.84×10^{-5}
cut-(3)	6.02×10^{-2}	12.62	3.84×10^{-5}
cut-(4)	5.96×10^{-2}	1.17	7.67×10^{-7}
cut-(5)	5.01×10^{-2}	0.68	0
cut-(6)	4.99×10^{-2}	0.64	0

pre-selection cuts $(E_{\gamma} > 5 \text{ GeV and } |\eta_{\gamma}| < 3.0)$

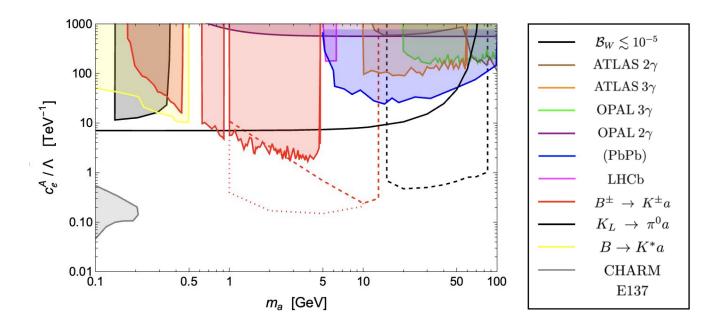
When the ALP is light, it will be highly boosted, generating two photons in the final state that are too collimated to pass the photon isolation criteria, resulting in a novel 'photon-jet' signature. Additionally, the light ALP can become a long-lived particle (LLP). Further details on these studies can be found in my paper.

Lighting Electroweak-Violating ALP-Lepton Interactions at e^+e^- and ep Colliders

Chih-Ting Lu (Nanjing Normal U.) (Oct 27, 2022)

e-Print: 2210.15648 [hep-ph]

Main results and existing bounds



---- 2γ CEPC_5 ab^{-1} ---- J_{γ} CEPC_5 ab^{-1} ····· Displaced J_{γ} CEPC_5 ab^{-1}

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Conclusion

1. The less discussed four-point interaction, W-l-v-a, in electroweak-violating (EWV) scenario plays an important role to explore leptophilic ALPs:

Light eALPs: charged mesons and W boson exotic decays.

Heavy eALPs : t-channel ALP production modes : $\,e^+e^ightarrow
u_e a\overline{
u_e}$

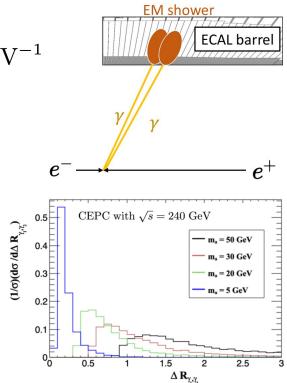
2. Taking CEPC with $\mathcal{L}=5ab^{-1}$ as an examples, we find the possible future bounds of c_e^A/Λ can be lower than about $0.1-1.0~{\rm TeV^{-1}}~{\rm for}~1~{\rm GeV}\leqslant m_a\lesssim M_W$ which is much stronger than existing bounds.

Thank you for your attention

Back-up

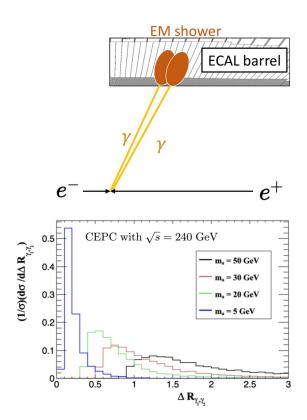
- 1. We choose the CEPC with $\sqrt{s}=240~{
 m GeV}$
- 2. Benchmark point : $m_a=5~{
 m GeV}~{
 m with}~c_e^A/\Lambda=1~{
 m TeV}^{-1}$
- 3. The signal process $e^+e^- \to \nu_e a \overline{\nu_e}$, $a \to \gamma \gamma$ signature : A photon-jet plus missing energy
- 4. Possible SM backgrounds:

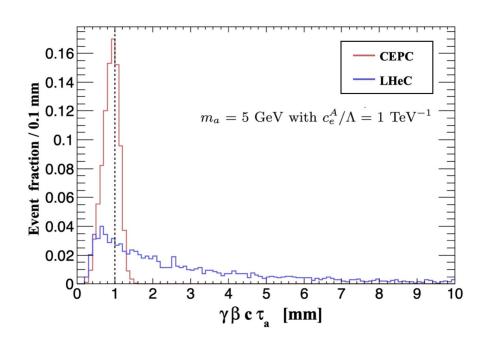
$$e^+e^- \rightarrow \nu_\ell \overline{\nu_\ell} \gamma$$



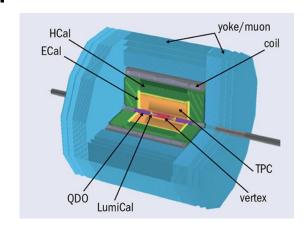
- We apply the C/A jet clustering algorithm with a cone size R = 0.4 for a photon-jet candidate.
- 2. Then the hadronic energy fraction is required to satisfy $log heta_J < -2$

$$\theta_J = \frac{E_{J, \text{HCAL}}}{E_J},$$

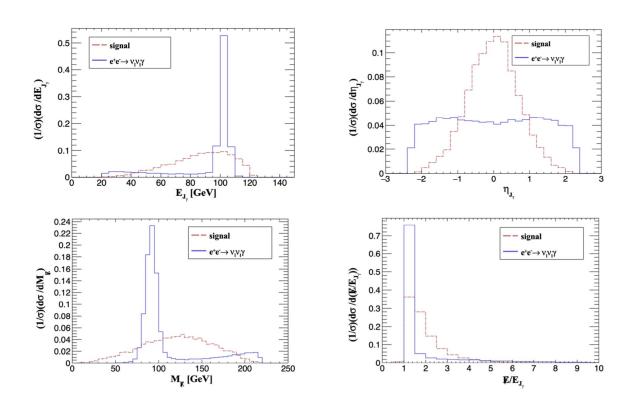


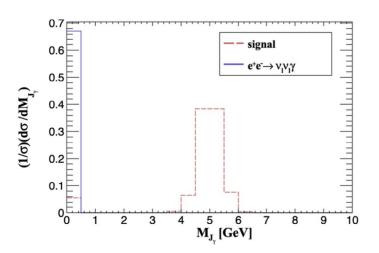


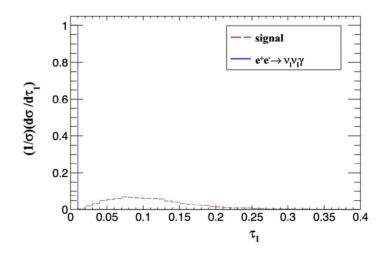
- 1. $16 \leqslant R_{\text{vertex}} \leqslant 60 \text{ mm}$,
- 2. $0.15 \leqslant R_{\text{ECAL}} \leqslant 1.81 \text{ m},$
- 3. $2.30 \leqslant R_{\text{HCAL}} \leqslant 3.34 \text{ m},$
- 4. $2.30 \le R_{\text{muon}} \le 3.34 \text{ m}$



- (1) $N(J_{\gamma}) \ge 1$ with $log\theta_J < -2$, $30 < E_{J_{\gamma}} < 100$ GeV, and $|\eta_{J_{\gamma}}| < 1.5$,
- (2) $E > 140 \text{ GeV} \text{ and } |\eta_{E}| < 1.5,$
- (3) Veto $75 < M_{E} < 105 \text{ GeV}$,
- (4) $E/E_{J_{\gamma}} > 1.5$,
- (5) $|M_{J_{\gamma}} m_a| < 1 \text{ GeV},$
- (6) $\tau_1(J_{\gamma}) > 0.03$.







cut flow in σ [fb]	signal	$oxedsymbol{ u_\ell \overline{ u_\ell} \gamma}$
Generator	0.16	4266.80
$\gamma \beta c \tau_a < 1 \text{ mm}$	0.10	_
cut-(1)	8.49×10^{-2}	520.29
cut-(2)	8.49×10^{-2}	520.29
cut-(3)	8.10×10^{-2}	387.77
cut-(4)	7.92×10^{-2}	373.39
cut-(5)	7.76×10^{-2}	0
cut-(6)	7.67×10^{-2}	0
	$Senerator$ $\gamma \beta c \tau_a < 1 \text{ mm}$ $cut-(1)$ $cut-(2)$ $cut-(3)$ $cut-(4)$ $cut-(5)$	Generator 0.16 $\gamma\beta c\tau_a < 1 \text{ mm}$ 0.10 cut-(1) 8.49×10^{-2} cut-(2) 8.49×10^{-2} cut-(3) 8.10×10^{-2} cut-(4) 7.92×10^{-2} cut-(5) 7.76×10^{-2}

The pre-selection cuts in parton-level are similar as before, except for $E_{\gamma} > 1$ GeV ($E_{\gamma} > 10$ GeV) for the signal (background).