



西安交通大学
XI'AN JIAOTONG UNIVERSITY



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Experimental review of weak decays of heavy hadrons

(recent updated results)

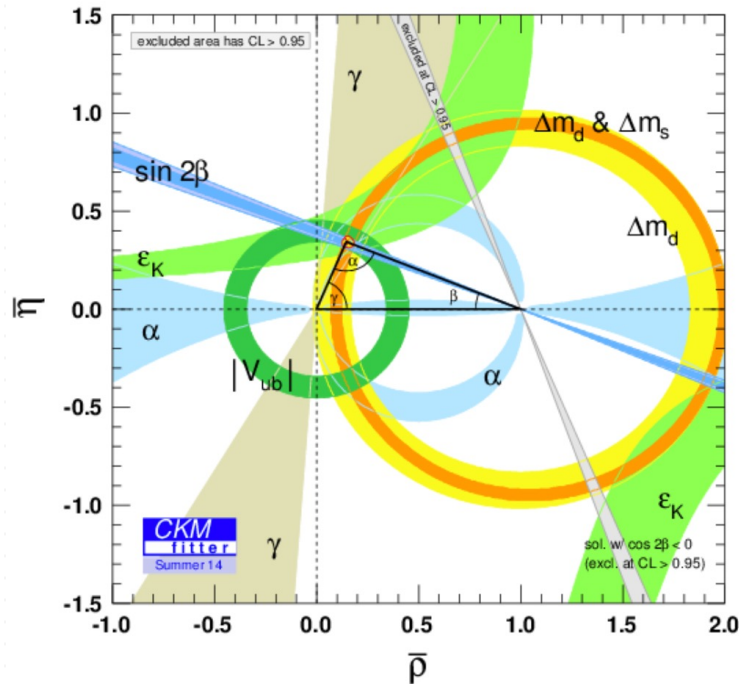
Yubo Li (李郁博)

第六届重味物理与量子色动力学研讨会

2023年8月

Why weak decay?

How do quarks participate in weak decays? -> CKM matrix

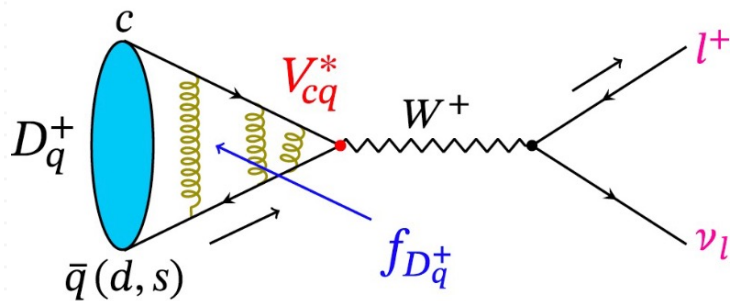


$$V = \begin{pmatrix} \begin{array}{c} d \\ n \end{array} \begin{array}{c} e^- \\ \bar{\nu} \\ p \end{array} & \begin{array}{c} s \\ K \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \\ \pi \end{array} & \begin{array}{c} b \\ B \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \\ \pi \end{array} \\ \hline \begin{array}{c} u \\ D \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \\ \pi \end{array} & \begin{array}{c} s \\ D \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \\ K \end{array} & \begin{array}{c} b \\ B \end{array} \begin{array}{c} \ell^- \\ \bar{\nu} \\ D \end{array} \\ \hline \begin{array}{c} t \\ B^0 \end{array} \begin{array}{c} \bar{B}^0 \end{array} & \begin{array}{c} s \\ B_s \end{array} \begin{array}{c} \bar{B}_s \end{array} & \begin{array}{c} t \\ W \end{array} \begin{array}{c} b \end{array} \end{pmatrix}$$

$$\alpha = \phi_2 \quad \beta = \phi_1 \quad \gamma = \phi_3$$

- ❖ $d \rightarrow u$: Nuclear physics (superaligned β decays)
- ❖ $s \rightarrow u$: Kaon physics (KLOE, KTeV, NA62)
- ❖ $c \rightarrow d, s$: Charm physics (CLEO-c, Babar, Belle, BESIII)
- ❖ $b \rightarrow u, c$ and $t \rightarrow d, s$: B physics (Babar, Belle, CDF, DØ, LHCb)
- ❖ $t \rightarrow b$: Top physics (CDF/DØ, ATLAS, CMS)

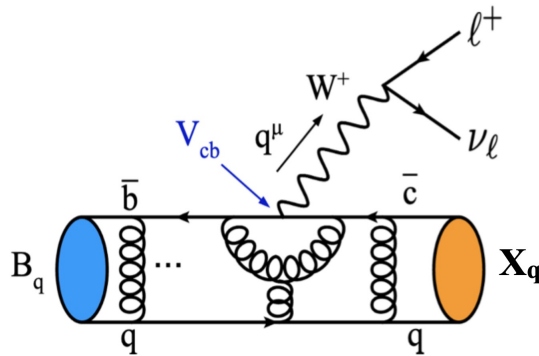
Why weak decay?



Leptonic decay

$$B[M \rightarrow l\nu_l]_{\text{SM}} = \frac{G_F^2 m_M m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_M^2}\right)^2 |V_{cq}|^2 f_M^2 \tau_M (1 + \delta_{em}^{Ml2})$$

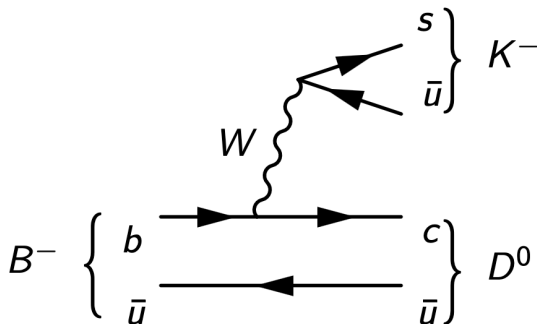
Semi-leptonic decay



$$\frac{d\Gamma(M \rightarrow Pl\nu)}{dq^2} = \frac{G_F^2 |V_{quqd}|^2 (q^2 - m_l^2)^2 \sqrt{E_P^2 - m_P^2}}{24\pi^3 q^4 m_H^2} \times \left[\left(1 + \frac{m_l^2}{2q^2}\right) m_M^2 (E_P^2 - m_P^2) |f_+(q^2)|^2 + \frac{3m_l^2}{8q^2} (m_M^2 - m_P^2)^2 |f_0(q^2)|^2 \dots \right]$$

	0^+	0^-	1^-	1^+	2^+
$B_{(l)} \rightarrow X \ell \bar{\nu}$	f_0	$-$	f_+	$-$	f_T
$B_{(l)} \rightarrow X^* \ell \bar{\nu}$	$-$	A_0	V_0	A_1, A_2	T_1, T_2, T_3

hadronic decay

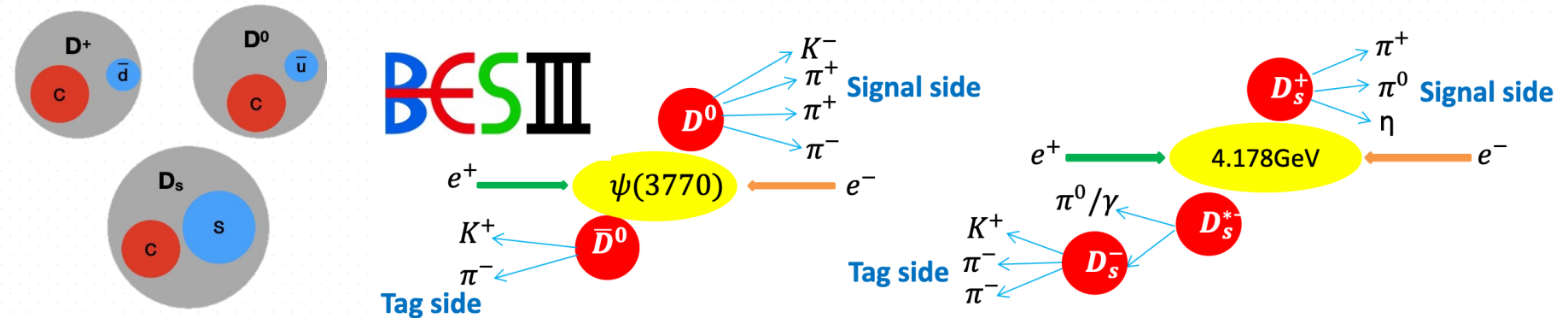


- ❖ Extract CKM Matrix parameters: $|V_{qq}|$, ϕ_i (test unitarity)
- ❖ CPV ❖ FCNC ❖ LFU (new physics)
- ❖ Decay constants and hadronic Form factor (LQCD)
- ❖ Decay parameters, Branching fraction, PWA (QCD, other hadrons)

❖

Charm Decays

leptonic decay of $D_{(s)}$



$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 f_{D_{(s)}}^2}{8\pi} |V_{cd(s)}|^2 m_l^2 m_{D_{(s)}} \left(1 - \frac{m_l^2}{m_{D_{(s)}}^2}\right)^2$$

Feynman diagram illustrating the leptonic decay of a D_q^+ meson. The meson consists of a c quark and a $\bar{q}(d, s)$ antiquark. The c quark transitions to a l^+ lepton via a W^+ boson, with a vertex factor V_{cq}^* . The $\bar{q}$ antiquark transitions to a ν_l neutrino via a W^+ boson, with a vertex factor $f_{D_q^+}$. The W^+ boson then decays into l^+ and ν_l .

$f_{D_{(s)}}$: extracted with $V_{cd(s)}$ taken from the CKM global fit -> Calibration of LQCD

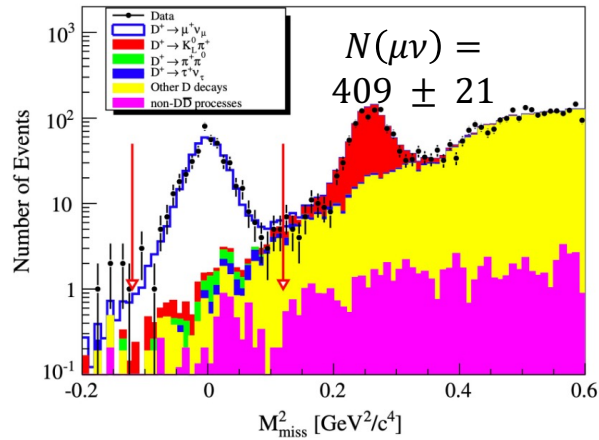
$V_{cd(s)}$: determined with $f_{D_{(s)}}$ taken from the LQCD -> test CKM unitary

Charm Decays

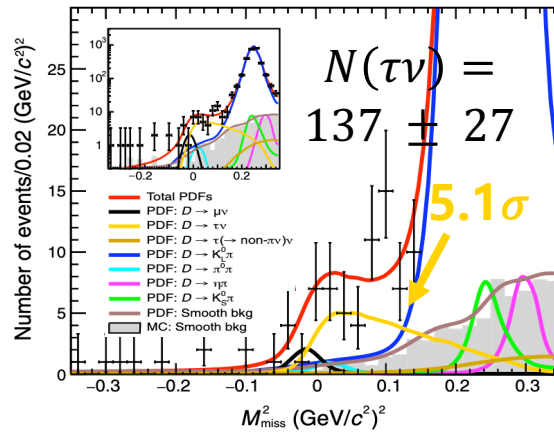
BESIII

leptonic decay of $D^+ \rightarrow l^+ \nu_l$

PRD 89, 051104 (2014)



PRL.123.211802 (2019)

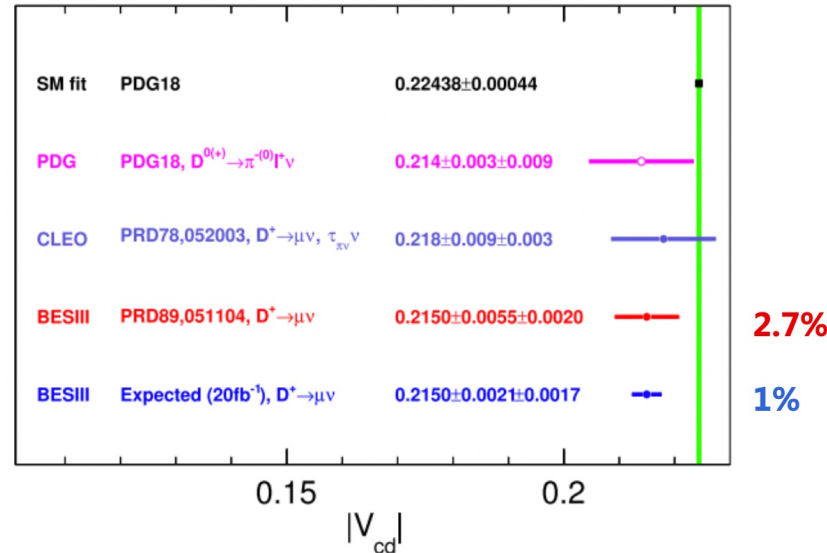
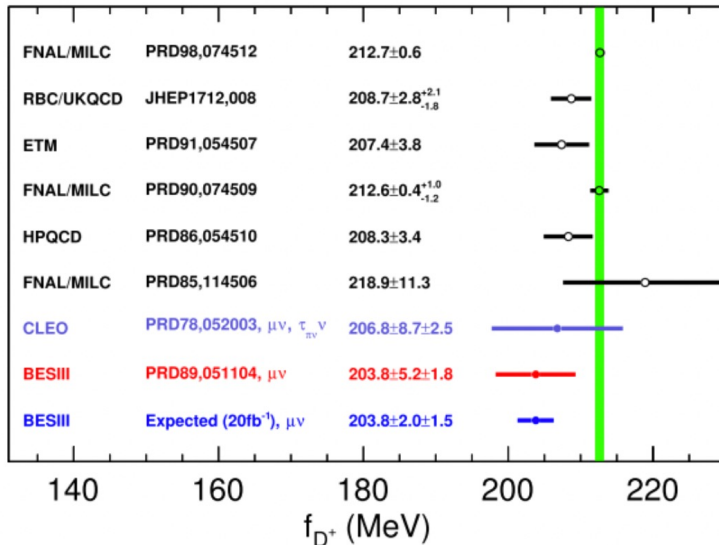


2.93 fb⁻¹ data
@ 3.773 GeV

$$R_{D^+} = \frac{\Gamma(D^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D^+ \rightarrow \mu^+ \nu_\mu)} = 3.21 \pm 0.64 \pm 0.43$$

SM : 2.67

Consistent



Charm Decays

BESIII

leptonic decay of $D_s^+ \rightarrow \ell \nu$

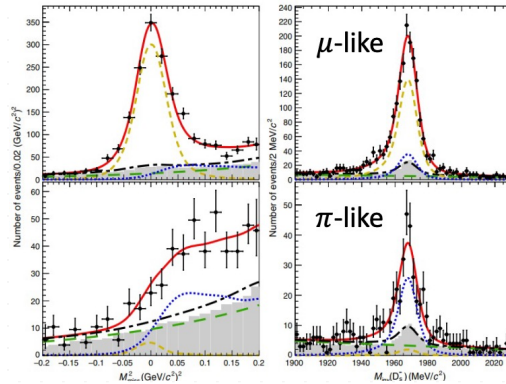
$$\text{SM: } R_{D_s^+} = \frac{\Gamma(D_s^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D_s^+ \rightarrow \mu^+ \nu_\mu)} = 9.75$$

❖ **6.32 fb^{-1} @ 4.18-4.23 GeV:**

$$\tau^+ \rightarrow \pi^+ \pi^0 \nu_e \bar{\nu}_\tau [\text{PRD 104, 052009 (2021)}]$$

$$\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau [\text{PRL 127, 171801 (2019)}]$$

$$B(\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau) = 17.82\%$$



$$D_s^+ \rightarrow \mu^+ \nu_\mu$$

$$D_s^+ \rightarrow \tau^+ (\pi^+ \bar{\nu}_\tau) \nu_\tau$$

$$\triangleright N_{sig} = 2198 \pm 55$$

$$\triangleright N_{sig} = 946 \pm 46$$

$$R_{D_s^+} = 9.72 \pm 0.7$$

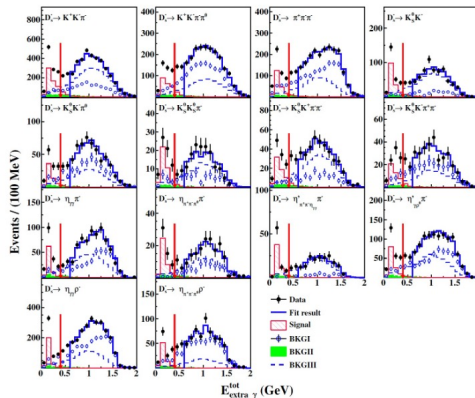
$$B(\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau) = 10.82\%$$

$$D_s^+ \rightarrow \mu \nu \text{ Updated in } 2307.14585$$

❖ **7.33 fb^{-1} @ 4.13-4.23 GeV:**

$$\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau [\text{arXiv:2303.12468}]$$

$$B(\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau) = 17.39\%$$

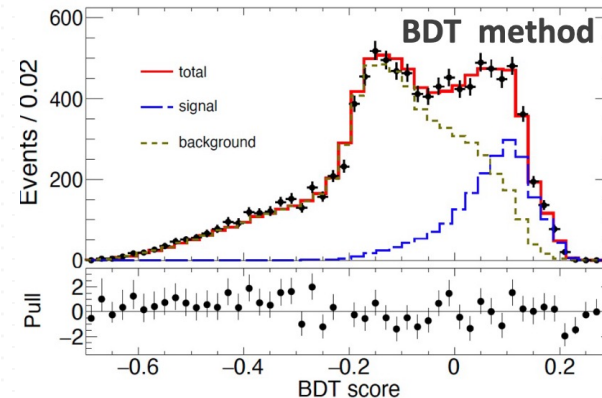


$$N_{sig} = 2714 \pm 64$$

$$R_{D_s^+} = 9.83 \pm 0.43$$

$$\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau [\text{arXiv:2303.12600}]$$

$$B(\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau) = 10.82\%$$



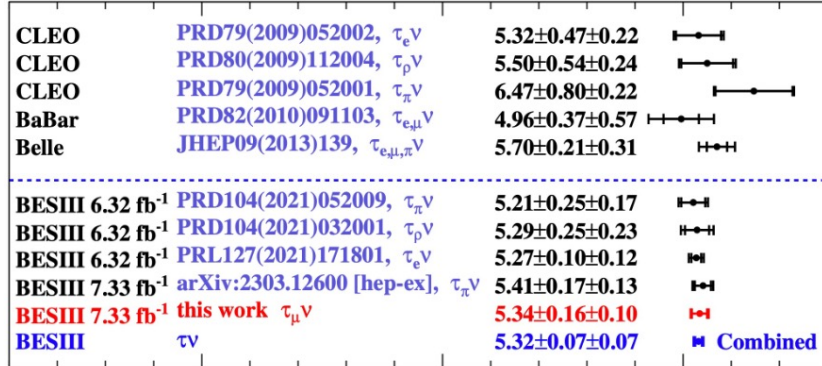
$$N_{sig} = 2731 \pm 74$$

$$R_{D_s^+} = 9.79 \pm 0.33$$

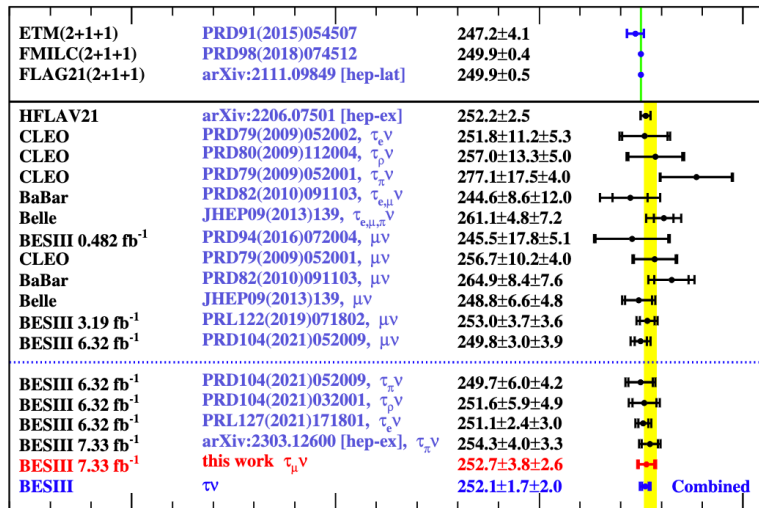
Charm Decays



leptonic decay of $D_s^+ \rightarrow \ell \nu$

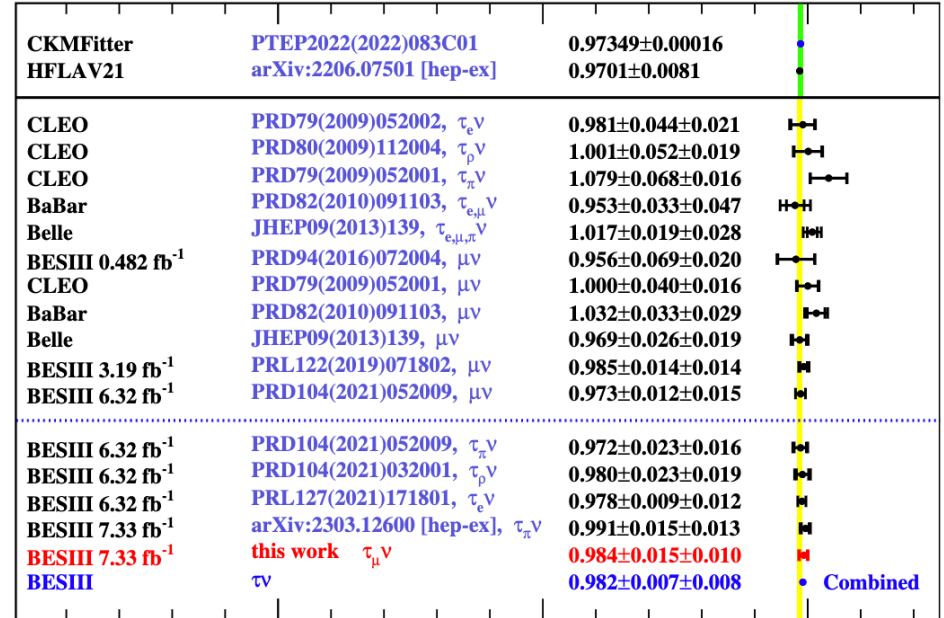


-5 0 5
 $B(D_s^+ \rightarrow \tau^+ \nu)$ (%)



0 100 200 300
 $f_{D_s^+}$ (MeV)

0.8σ



-1 0 1
 $|V_{cs}|$

0.14σ

Charm Decays

leptonic decay of $D_s^{*+} \rightarrow \ell \nu$ ❖ $7.33 \text{ fb}^{-1} @ 4.13\text{-}4.23 \text{ GeV}$:



$$B(D_s^{*+} \rightarrow e^+ \nu) = (2.1_{-0.9}^{+1.2}_{\text{stat}} \pm 0.2_{\text{syst}}) \times 10^{-5} \quad (2.9\sigma) \quad \text{Total width } \Gamma_{D_s^{*+}}^{\text{tot}} = (121.9_{-52.2}^{+69.6} \pm 11.8) \text{ eV}$$

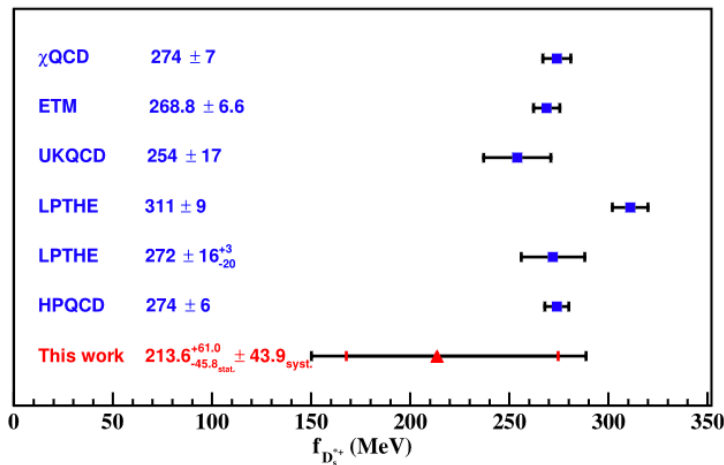
$$f_{D_s^{*+}} = (213.6_{-45.8}^{+61.0}_{\text{stat}} \pm 43.9_{\text{syst}}) \text{ MeV}$$

Theoretical prediction:

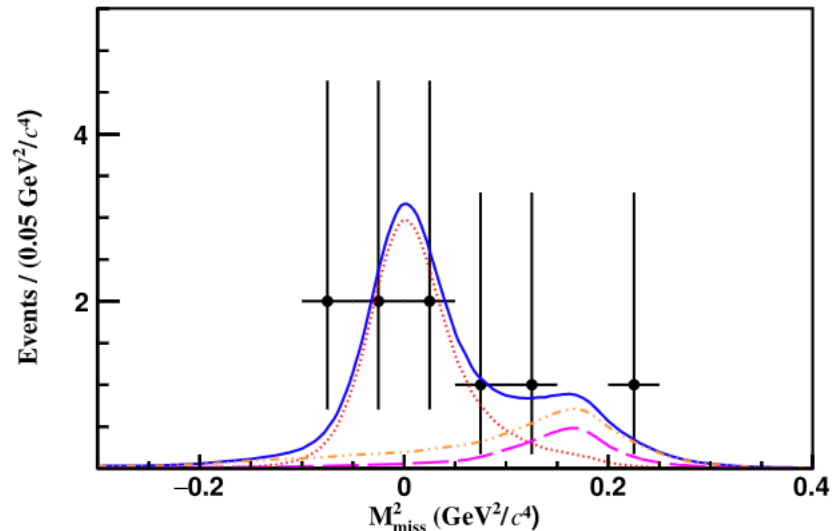
EPJC 82, 1037 (2022); PRL 112, 212002 (2022)

$$\bullet \quad \Gamma^{\text{tot}} = 2.4 \times 10^{-3} \times \left(\frac{f_{D_s^{*+}}}{f_{D_s^+}} \right)^2 / B(D_s^{*+} \rightarrow e^+ \nu_e) \text{ eV}$$

• Constrain the U.L. from MeV to KeV level



Arxiv:2307.14585



The first hint of leptonic decays of the excited D_s^{*+}

Charm Decays



Semi-leptonic decay of $D_s^+ \rightarrow f_0(980)e^+\nu_e$

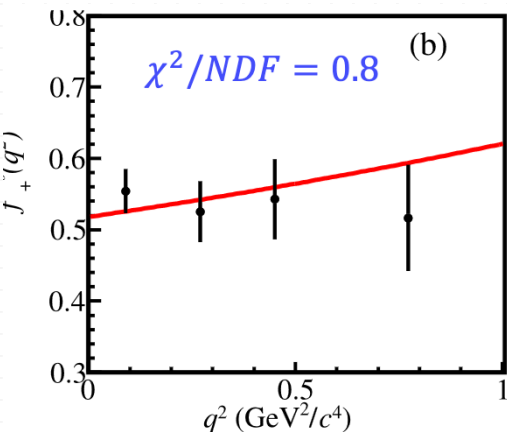
❖ 7.33 fb^{-1} @ 4.13-4.23 GeV :

$$\frac{d^2\Gamma(D_{(s)} \rightarrow S\ell^+\nu_\ell)}{dsdq^2} = \frac{G_F^2 |V_{cd(s)}|^2}{192\pi^4 m_{D_{(s)}}^3} \lambda^{3/2}(m_{D_s}^2, s, q^2) |f_+(q^2)|^2 P(s)$$

$$P(s) = \begin{cases} \frac{g_1 \rho_{\pi\pi}}{|m_0^2 - s - i(g_1 \rho_{\pi\pi} + g_1 \rho_{KK})|^2}, & \text{Flatte for } a_0(980)/f_0(980) \\ \frac{m_{f_0} \Gamma(s)}{(s - m_{f_0}^2)^2 + m_{f_0}^2 \Gamma^2(s)}, & \text{RBW for } f_0(500) \end{cases}$$

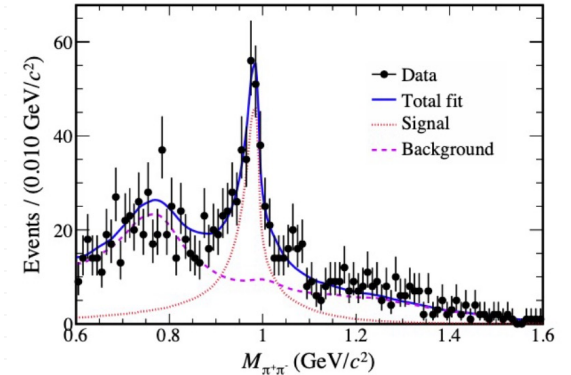
$f_0(980) \rightarrow \pi^+\pi^-$ arXiv:2303.12927

$$\mathcal{B}(D_s^+ \rightarrow f_0(980)e^+\nu_e) = (1.72 \pm 0.13_{\text{stat}} \pm 0.10_{\text{syst}}) \times 10^{-3}$$



	$f_+^{f_0(0)}$
This work	$0.518 \pm 0.018_{\text{stat}} \pm 0.036_{\text{syst}}$
CLFD [6]	0.45
DR [6]	0.46
QCDSR [7]	0.50 ± 0.13
QCDSR [8]	0.48 ± 0.23
LCSR [9]	0.30 ± 0.03
LFQM [11]	0.24 ± 0.05
CQCM [12]	0.39 ± 0.02

[6] Phys. Rev. D79, 076004 (2009). [7] Phys. Lett. B579, 59-66 (2004).
 [8] EPL90, 61001 (2010). [9] Phys. Rev. D81, 074001 (2010).
 [11] Phys. Rev. D80, 074030 (2009). [12] Phys. Rev. D102, 016013 (2020).



$f_0 \rightarrow \pi^0\pi^0/K_S^0K_S^0$

PRD. 105, L031101 (2022)

➤ First BFs Measurement:

$$\mathcal{B}(D_s^+ \rightarrow f_0(980)e^+\nu_e, f_0(980) \rightarrow \pi^0\pi^0) = (7.9 \pm 1.4 \pm 0.4) \times 10^{-4}$$

➤ No significant signal and upper limit on BF @90% C.L. :

$$\mathcal{B}(D_s^+ \rightarrow f_0(500)e^+\nu_e, f_0(500) \rightarrow \pi^0\pi^0) < 7.3 \times 10^{-4}$$

$$\mathcal{B}(D_s^+ \rightarrow K_S^0K_S^0e^+\nu_e) < 3.8 \times 10^{-4}$$

Charm Decays

Semi-leptonic decay of $D_{(s)}^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$

arXiv: 2306.05194



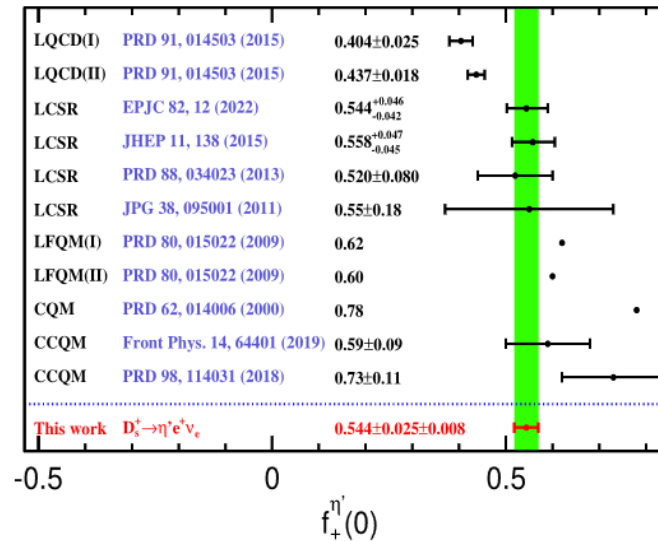
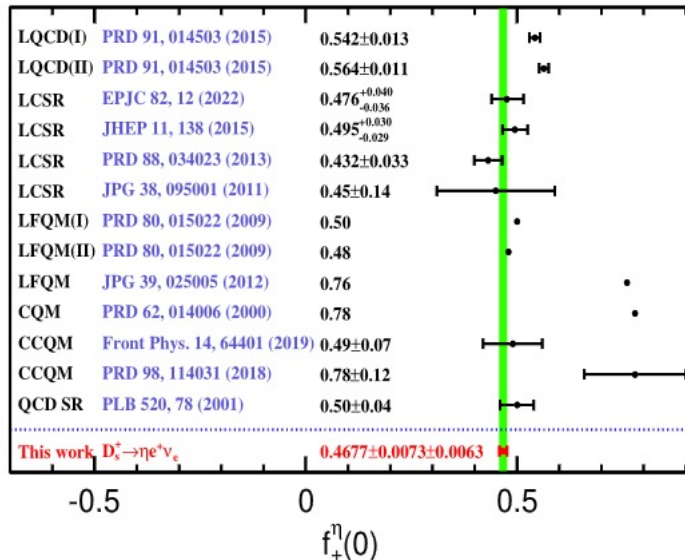
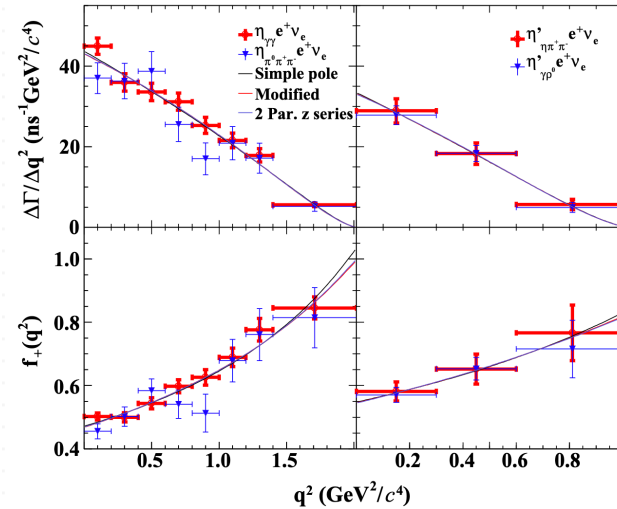
❖ 7.33 fb^{-1} @ 4.13-4.23 GeV :

$$\mathcal{B}_{\eta e^+ \nu_e} : (2.251 \pm 0.039_{\text{stat.}} \pm 0.051_{\text{syst.}}) \%$$

$$\mathcal{B}_{\eta' e^+ \nu_e} : (0.810 \pm 0.038_{\text{stat.}} \pm 0.024_{\text{syst.}}) \%$$

• $\eta - \eta'$ mixing angle: $\phi_P = (40.0 \pm 2.0_{\text{stat.}} \pm 0.6_{\text{syst.}})^\circ$

$$\cot^4 \phi_P = \frac{\Gamma_{D_s^+ \rightarrow \eta' e^+ \nu_e} / \Gamma_{D_s^+ \rightarrow \eta e^+ \nu_e}}{\Gamma_{D^+ \rightarrow \eta' e^+ \nu_e} / \Gamma_{D^+ \rightarrow \eta e^+ \nu_e}}.$$



Charm Decays

PWA of Semi-leptonic decay

❖ **7.33 fb⁻¹ @ 4.13-4.23 GeV :**

$D_s^+ \rightarrow K^+ K^- \mu^+ \nu$ [arXiv:2307.03024](https://arxiv.org/abs/2307.03024)

$$\mathcal{B}(D_s^+ \rightarrow \phi \mu^+ \nu_\mu) = (2.25 \pm 0.09 \pm 0.07) \times 10^{-2}$$

$$\mathcal{B}(D_s^+ \rightarrow \phi \mu^+ \nu_\mu) / \mathcal{B}(D_s^+ \rightarrow \phi e^+ \nu_e) = 0.94 \pm 0.08 \rightarrow \text{No LFU violation}$$

$$\mathcal{B}(D_s^+ \rightarrow f_0(980) \mu^+ \nu_\mu) \cdot \mathcal{B}(f_0(980) \rightarrow K^+ K^-) < 5.45 \times 10^{-4} @ 90\% \text{ C.L. } \sim 2.2\sigma$$

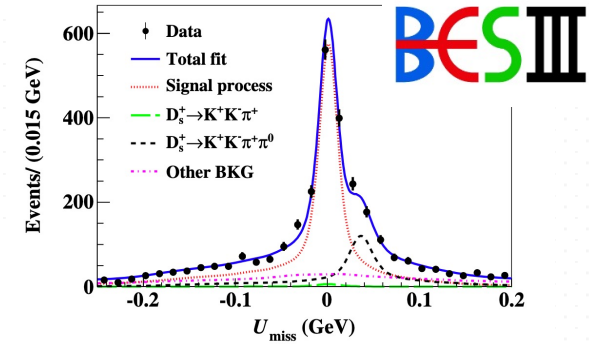
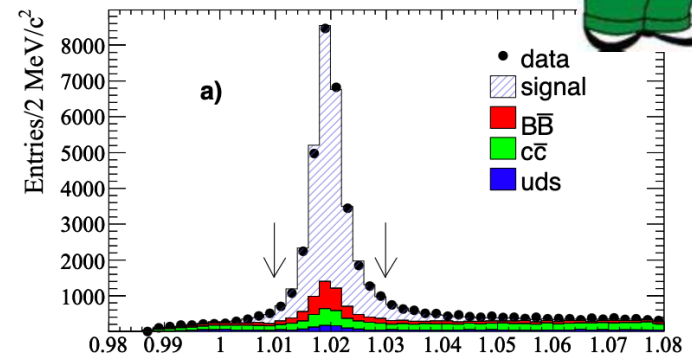


Table 5. Measured FF ratios and comparison with previous measurements.

Experiments	r_V	r_2
PDG [42]	1.80 ± 0.08	0.84 ± 0.11
This analysis	$1.58 \pm 0.17 \pm 0.02$	$0.71 \pm 0.14 \pm 0.02$
<i>BABAR</i> [25]	$1.807 \pm 0.046 \pm 0.065$	$0.816 \pm 0.036 \pm 0.030$
FOCUS [58]	$1.549 \pm 0.250 \pm 0.148$	$0.713 \pm 0.202 \pm 0.284$
Theory	r_V	r_2
CCQM [5]	1.34 ± 0.27	0.99 ± 0.20
CQM [6]	1.72	0.73
LFQM [7]	1.42	0.86
LQCD [3]	1.72 ± 0.21	0.74 ± 0.12
HM χ T [8]	1.80	0.52

BaBar 214 fb⁻¹:
PRD 78 (2008) 051101



Decay Mode	Exp/Year/Yield	BF/FF/Polarization	BESIII Status
$D_s^+ \rightarrow \phi(K^+K^-)e^+\nu_e$	BESIII/2018/26	Y/N/N	Internal Review@4.13 ~ 4.23GeV
	CLEO/2015/207	Y/N/N	
	BABAR/2008/25k	Y/Y/N	
	CLEO-II/1994/308	N/Y/Y	
$D_s^+ \rightarrow \phi(K^+K^-)\mu^+\nu_\mu$	BESIII/2018/22	Y/N/N	Internal Review@4.13 ~ 4.23GeV
	FOCUS/2004/793	N/Y/N	
	E687/1994/90	N/Y/Y	
$D^+ \rightarrow \bar{K}^{*0}(K^-\pi^+)e^+\nu_e$	BESIII/2016/18k	Y/Y/N	✓
	BABAR/2011/70k	Y/Y/N	
	CLEO/2010/5k	Y/Y/N	
$D^+ \rightarrow \bar{K}^{*0}(K^-\pi^+)\mu^+\nu_\mu$	CLEO/2010/5k	Y/Y/N	In process
	FOCUS/2002/15k	N/Y/N	
$D^+ \rightarrow \bar{K}^{*0}(\bar{K}^0\pi^0)e^+\nu_e$	N	N/N/N	In process
$D^+ \rightarrow \bar{K}^{*0}(\bar{K}^0\pi^0)\mu^+\nu_\mu$	N	N/N/N	In process
$D^0 \rightarrow K^{*-}(K^-\pi^0)e^+\nu_e$	CLEO/2005/94	Y/N/N	In process
$D^0 \rightarrow K^{*-}(K^-\pi^0)\mu^+\nu_\mu$	N	N/N/N	In process
$D^0 \rightarrow K^{*-}(\bar{K}^0\pi^-)e^+\nu_e$	BESIII/2019/3k	Y/Y/N	✓
	CLEO/2005/125	Y/N/N	
$D^0 \rightarrow K^{*-}(\bar{K}^0\pi^-)\mu^+\nu_\mu$	FOCUS/2005/175	Y/Y/N	In process
$D_s^+ \rightarrow K^{*0}(K^+\pi^-)e^+\nu_e$	CLEO/2015/32	Y/N/N	In process@4.13 ~ 4.23GeV
	BESIII/2019/155	Y/Y/N	
$D_s^+ \rightarrow K^{*0}(K^+\pi^-)\mu^+\nu_\mu$	N	N	In process@4.13 ~ 4.23GeV
$D^+ \rightarrow \rho^0(\pi^-\pi^+)e^+\nu_e$	CLEO/2013/447	Y/Y/N	✓
	BESIII/2019/1.7k	Y/Y/N	
$D^+ \rightarrow \rho^0(\pi^-\pi^+)\mu^+\nu_\mu$	FOCUS/2006/320	Y/N/N	In process
$D^+ \rightarrow \omega(\pi^-\pi^+\pi^0)e^+\nu_e$	BESIII/2016/491	Y/Y/N	✓
$D^+ \rightarrow \omega(\pi^-\pi^+\pi^0)\mu^+\nu_\mu$	BESIII/2020/194	Y/N/N	✓
$D^0 \rightarrow \rho^-(\pi^-\pi^0)e^+\nu_e$	CLEO/2013/305	Y/Y/N	✓
	BESIII/2019/1.1k	Y/Y/N	
$D^0 \rightarrow \rho^-(\pi^-\pi^0)\mu^+\nu_\mu$	BESIII/2021/570	Y/N/N	✓
$D^+ \rightarrow \phi(K^+K^-)e^+\nu_e$	BESIII/2016/-	Y/N/N	In process
$D^+ \rightarrow \phi(K^+K^-)\mu^+\nu_\mu$	N	N	In process

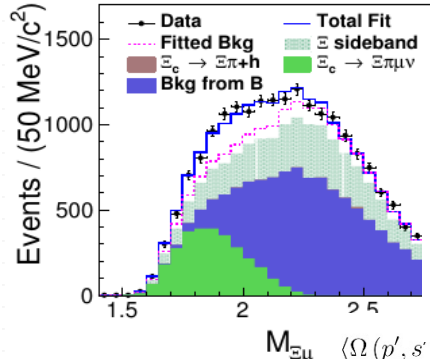
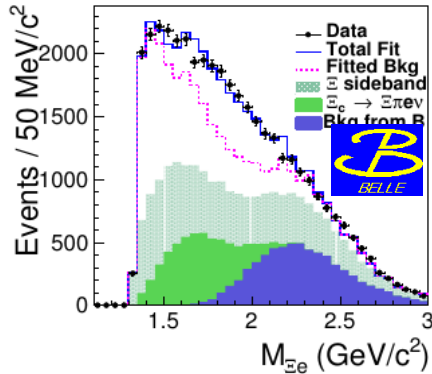
From Shulei Zhang
More can be seen in:
[Charm 2023](#)

Charm Decays

Semi-leptonic decay of charmed baryons

Λ_c Semi-leptonic decay will be reported by 张圣奇 in the next talk.

$$\Xi_c^0 \rightarrow \Xi^- \ell^+ \nu:$$



Belle: PRL 127 (2021) 12, 121803

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) = (1.31 \pm 0.39)\%$$

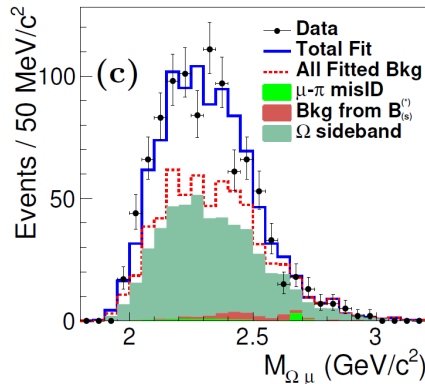
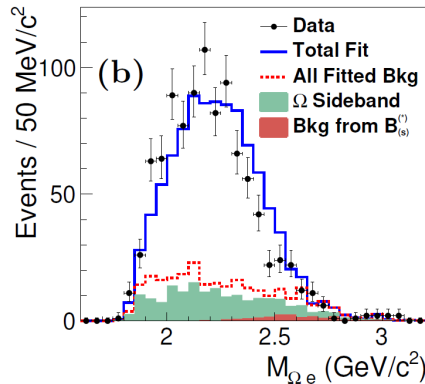
$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \mu^+ \nu_\mu) = (1.27 \pm 0.39)\%$$

PRL 127 (2021) 27, 272001

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- e^+ \nu_e) = (2.5 \pm 0.7)\%$$



$$\Omega_c^0 \rightarrow \Omega^- \ell^+ \nu:$$



$$\langle \Omega(p', s', s'_z) | V_\mu | \Lambda_c(p, s, s'_z) \rangle = \bar{u}(p', s'_z) \left[\frac{p^\alpha}{m_{\Omega_c}} (F_1^V \gamma_\mu + F_2^V \frac{p_\mu}{m_{\Omega_c}} + F_3^V \frac{p'_\mu}{m_\Omega}) + g^{\alpha\mu} F_4^V \right] \gamma_5 u(p, s_z)$$

$$\langle \Omega(p', s', s'_z) | A_\mu | \Omega_c(p, s, s'_z) \rangle = \bar{u}(p', s'_z) \left[\frac{p^\alpha}{m_{\Omega_c}} (F_1^A \gamma_\mu + F_2^A \frac{p_\mu}{m_{\Omega_c}} + F_3^A \frac{p'_\mu}{m_\Omega}) + g^{\alpha\mu} F_4^A \right] u(p, s_z)$$

$$\frac{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- e^+ \nu)}{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+)} = 1.98 \pm 0.15$$

$$\frac{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \mu^+ \nu)}{\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+)} = 1.94 \pm 0.21$$

Previous: 2.4 ± 1.2

PRD 105 (2022) 9, L091101

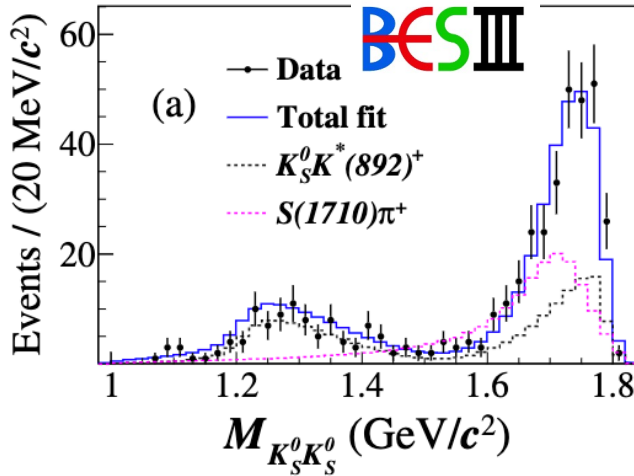


It is unlikely for us to extract BF vs q^2 for Ξ_c^0 and Ω_c^0 .

$\Xi_c^+ \rightarrow \Xi^0 \ell^+ \nu$: bkg/signal mixed due to contamination of gamma

Charm Decays

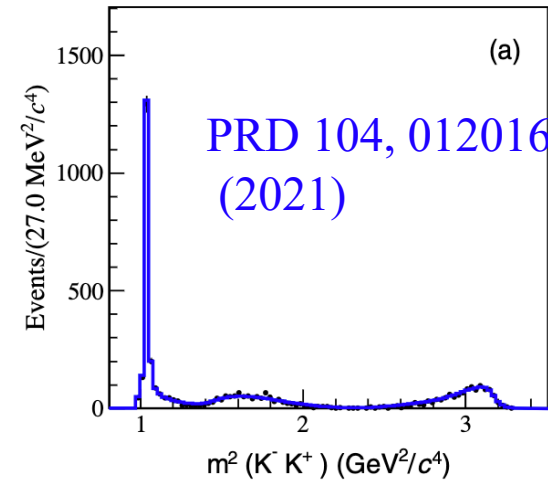
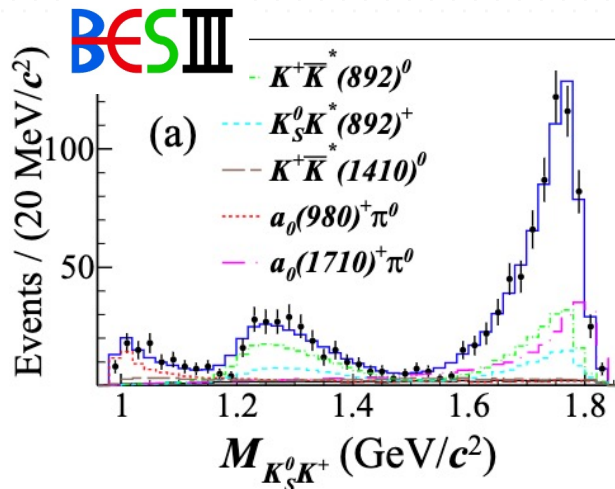
Hadronic decay of $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ PRD 105,L051103 (2022)



Amplitude	Phase	FF (%)
$D_s^+ \rightarrow K_S^0 K^*(892)^+$	0.0 (fixed)	$43.5 \pm 3.9 \pm 0.5$
$D_s^+ \rightarrow S(1710) \pi^+$	$2.3 \pm 0.1 \pm 0.1$	$46.3 \pm 4.0 \pm 1.2$

$f_0(1710)$ not seen in
 $D_s^+ \rightarrow K^+ K^- \pi^+$ decay
 -> $K^* \bar{K}^*$ molecule
 -> isospin one partner
 $a_0(1710)^0$

$D_s^+ \rightarrow K_S^0 K^+ \pi^0$ PRL 129 18 (2022)



Observation of $a_0^+(1710)$

Amplitude	Phase (rad)	FF (%)	BF (10^{-3})	σ
$D_s^+ \rightarrow K^*(892)^0 K^+$	0.0(fixed)	$32.7 \pm 2.2 \pm 1.9$	$4.77 \pm 0.38 \pm 0.32$	> 10
$D_s^+ \rightarrow K^*(892)^+ K_S^0$	$-0.16 \pm 0.12 \pm 0.11$	$13.9 \pm 1.7 \pm 1.3$	$2.03 \pm 0.26 \pm 0.20$	> 10
$D_s^+ \rightarrow a_0(980)^+ \pi^0$	$-0.97 \pm 0.27 \pm 0.25$	$7.7 \pm 1.7 \pm 1.8$	$1.12 \pm 0.25 \pm 0.27$	6.7
$D_s^+ \rightarrow \bar{K}^*(1410)^0 K^+$	$0.17 \pm 0.15 \pm 0.08$	$6.0 \pm 1.4 \pm 1.3$	$0.88 \pm 0.21 \pm 0.19$	7.6
$D_s^+ \rightarrow a_0(1710)^+ \pi^0$	$-2.55 \pm 0.21 \pm 0.07$	$23.6 \pm 3.4 \pm 2.0$	$3.44 \pm 0.52 \pm 0.32$	> 10

Charm Decays

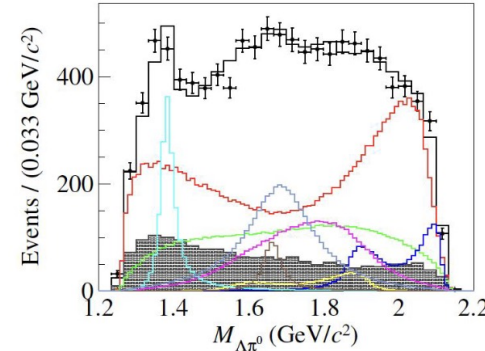
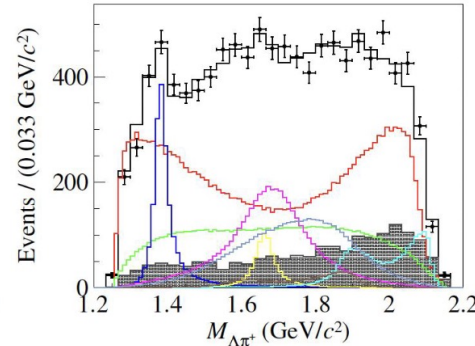
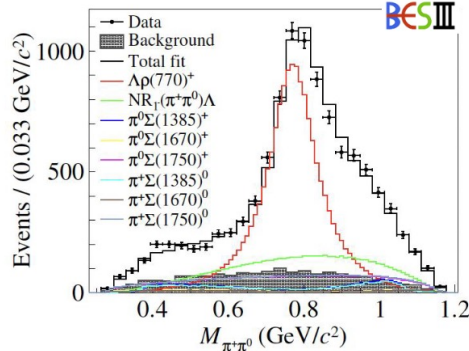
Decay mode	Paper	comment
$D_S^+ \rightarrow K^+ K^- \pi^+ \pi^0$	PRD104,032011(2021)	
$D_S^+ \rightarrow K_S^0 K^- \pi^+ \pi^+$	PRD103,092006 (2021)	Mainly $K^*(892)^+ K^*(892)^0$
$D_S^+ \rightarrow \pi^+ \pi^- \pi^+ \eta$	PRD104,L071101(2021)	W-annihilation $\rightarrow a_0(980)\rho$
$D_S^+ \rightarrow K_S^0 \pi^+ \pi^0$	JHEP 06,181(2021)	
$D_S^+ \rightarrow K_S^0 K^+ \pi^0$	PRL129,182001(2022)	$a_0^+(1710)$
$D_S^+ \rightarrow K_S^0 K_S^0 \pi^+$	PRD105,L051103(2022)	
$D_S^+ \rightarrow \pi^+ \pi^0 \eta'$	JHEP04,058(2022)	$\rho^+ \eta'$ dominant
$D_S^+ \rightarrow \pi^+ \pi^- \pi^+$	BESIII: PRD 106,112006(2022) LHCb: JHEP 06 (2023) 044	$\pi^+ \pi^-$ S-wave dominant
$D_S^+ \rightarrow \pi^+ \pi^0 \pi^0$	JHEP 01,052 (2022)	
$D_S^+ \rightarrow K^+ \pi^+ \pi^-$	JHEP 08,196 (2022)	
$D_S^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$	JHEP 07,051(2022)	$a_1(1260)^+ \phi$ dominant
$D_S^+ \rightarrow K^+ \pi^+ \pi^- \pi^0$	JHEP 09 242 (2022)	
$D_S^+ \rightarrow \omega \pi^+ \eta$	arXiv: 2302.04670	First observation

Charm Decays

Decay mode	Paper	comment
$D^0 \rightarrow \omega \phi$	BESIII: PRL 128 011803 (2022)	$\omega \phi$ transversely polarized
$D^0 \rightarrow K_L \pi \pi$	BESIII: arXiv:2212.09048	
$D^0 \rightarrow K_S K^+ K^-$	BESIII: arXiv:2006.02800	
$D^0 \rightarrow K^+ \pi^- \pi^0,$ $\rightarrow K^+ \pi^- \pi^0 \pi^0$	BESIII: PRD 105,112001 (2022)	No signal for $K^+ \pi^- \pi^0 \pi^0$
$D^+ \rightarrow \pi^+ \pi^- \pi^+ X$	BESIII: PRD 167, 032802 (2023)	Important for $R_{D^{(*)}}$
$D_S^+ \rightarrow \pi^+ \pi^- \pi^+ X$	BESIII: PRD 108, 032001 (2023)	
$D^+ \rightarrow K^+ K^- \pi^+ \pi^0$ $D_{(s)}^+ \rightarrow K^+ \pi^- \pi^+ \pi^0,$	Belle: PRD 107,033003 (2023)	

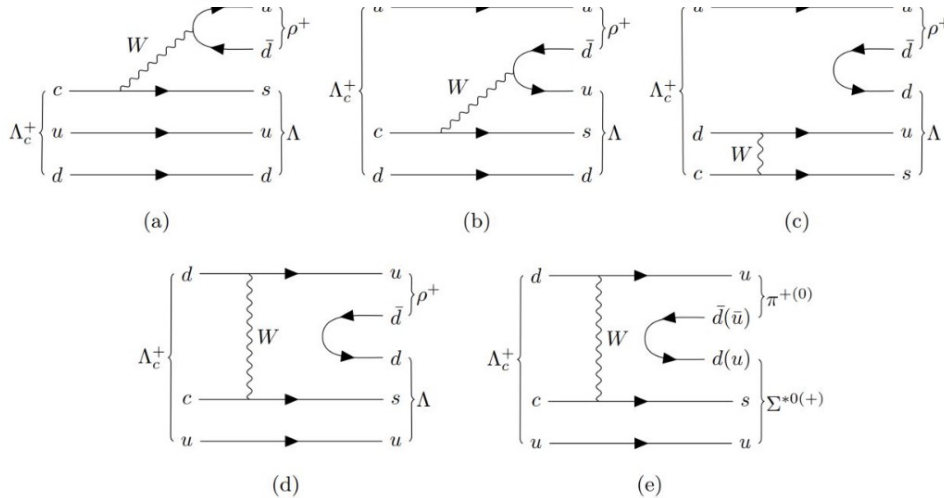
Charm Decays

$$\Lambda_c \rightarrow \Lambda \pi^+ \pi^0$$



JHEP12 (2022) 033

BES III



$\Lambda_c^+ \rightarrow \Lambda \rho^+$ consists of both factorizable(a) and non-factorizable(b-d) contributions.

$\Lambda_c^+ \rightarrow \Sigma(1385)\pi$ consists of pure non-factorizable(e) contribution.

- Decay asymmetry parameters: relevant to the interference of the internal partial wave amplitudes.
- Provide important inputs to the theoretical calculations for non-factorizable.

Decay mode	Paper	comment
$\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^- \pi^+$	Belle : PRL 130, 151903 (2023)	Peaks at 1434 MeV $M_{\Lambda \pi^\pm}$
$\Lambda_c^+ \rightarrow \Lambda \eta^{(\prime)}$	Belle : PRD 107, 032003 (2023) BESIII : PRD 106,072002(2022)	
$\Lambda_c^+ \rightarrow \Lambda h, \Sigma^0 h$	Belle : 科学通报 68 583 (2023) BESIII : PRD 106,L111101(2022) PRD106,052003(2022)	CPV measurement for Belle
$\Lambda_c^+ \rightarrow p K_s K_s, p K_s \eta$	Belle : PRD 107, 032004 (2023)	
$\Lambda_c^+ \rightarrow \Sigma^+ \gamma, \Xi_c^0 \rightarrow \Xi^0 \gamma$	Belle : PRD 107, 032001 (2023) BESIII : arXiv 2212.07214	no evident signal
$\Lambda_c^+ \rightarrow p K^+ \pi^-$	Belle : PRD 108 3 (2023) LHCb : PRD 108 012023 (2023)	Amplitude analysis from LHCb, observe $\Lambda(2000)$
$\Lambda_c^+ \rightarrow \Sigma^+ K^+ K^-, \Sigma^+ \phi$ $\rightarrow \Sigma^+ K^+ \pi^- (\pi^0)$	BESIII : arXiv 2304.09405	no evidence $\Sigma^+ K^+ \pi^- \pi^0$
$\Lambda_c^+ \rightarrow n + X$	BESIII : PRD 108 L031101(2023)	
$\Lambda_c^+ \rightarrow n \pi^+$	BESIII : PRL 128,142001(2022)	Less Non-factorization contributions
$\Lambda_c^+ \rightarrow n \pi^+ \pi^0,$ $n \pi^+ \pi^- \pi^+, n K^+ \pi^- \pi^+$	BESIII : CPC 47 023001 (2023)	
$\Lambda_c^+ \rightarrow p \eta, p \omega$	BESIII : arXiv 2307.09266 Belle : PRD 104, 072008 (2021)	
$\Lambda_c^+ \rightarrow p \pi^0$	Belle : PRD 103, 072004 (2021)	
$\Lambda_c^+ \rightarrow p \eta'$	Belle : JHEP 03 2022, 090 (2022)	
$\Xi_c^+ \rightarrow \Lambda K_S, \Sigma^0 K_S, \Sigma^+ K^-$	Belle : PRD 105, L011102 (2022)	
$\Omega_c^0 \rightarrow \Xi^- \pi^+, \Xi K^+, \Omega^- K^+$	Belle : JHEP 01 055 (2023) LHCb : arXiv 2308.08512	No evidence of CS decay from Belle CS decay observed by LHCb

Charm Decays

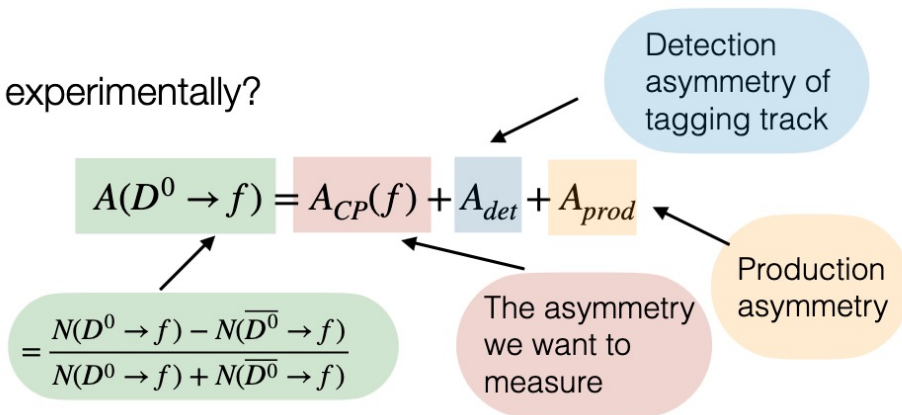
CP violation effects are small at charm sector $\leq \mathcal{O}(10^{-3})$

- Only bound HF system made of up-type quarks, high sensitivity to NP effect wrt K and B_s
- difficult for the observation

The only observation of CPV of D is $D \rightarrow KK, \pi\pi$ PRL 122 211803 (2019)

$$A_{CP}(f) = \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow f)}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow f)}$$

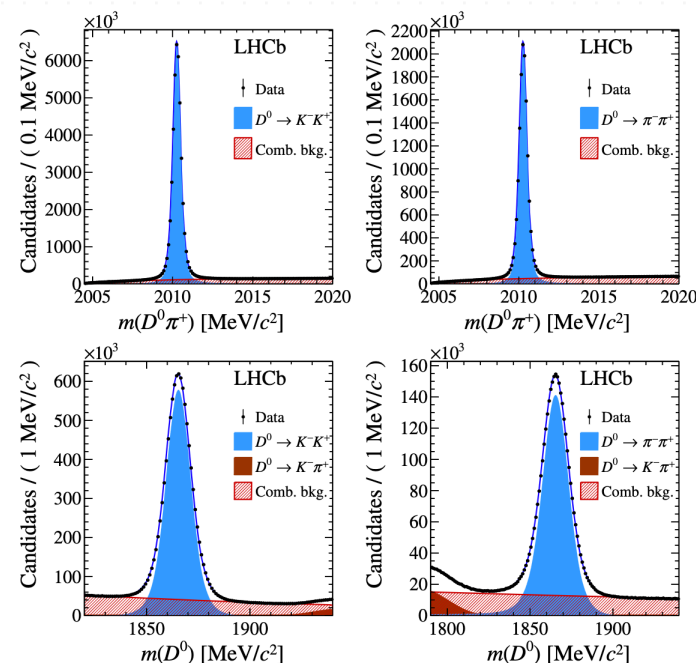
How experimentally?



to cancel Detection and production asymmetry

$$\begin{aligned} \Delta A_{CP} &= A(D \rightarrow K^+ K^-) - A(D \rightarrow \pi^+ \pi^-) \\ &= (-15.4 \pm 2.9) \times 10^{-4} \end{aligned}$$

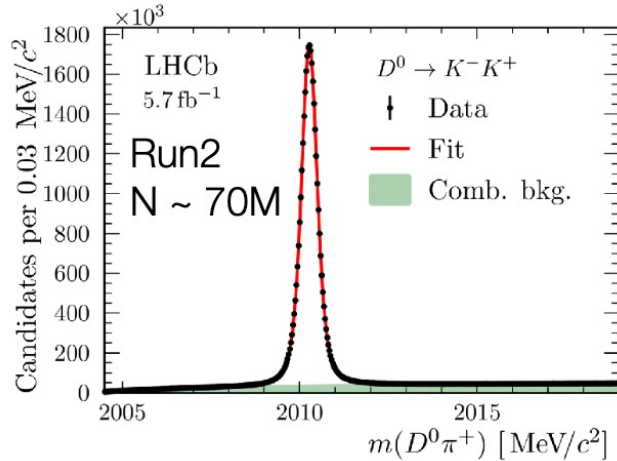
Run 2 (5.6fb⁻¹) data



See M. Piscopo's talk
@ BEAUTY 2023 for theory review.

Charm Decays

observation of CPV of $D \rightarrow hh$: [arXiv:2209.03179](https://arxiv.org/abs/2209.03179)

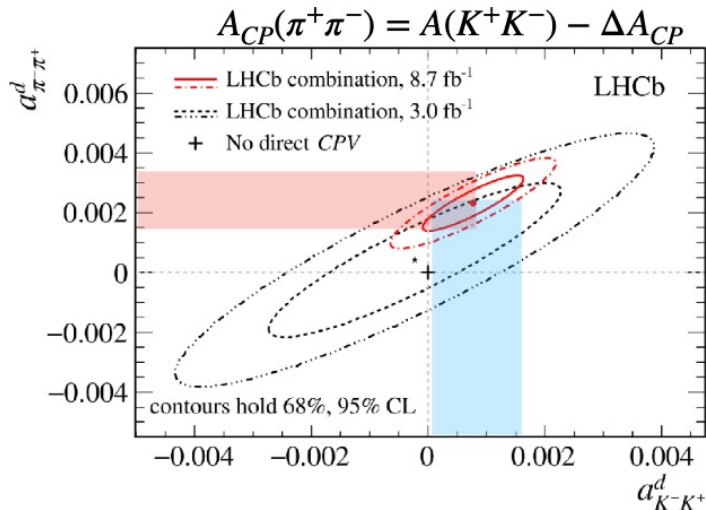


Run 2 (5.6fb⁻¹) only:

$$A_{CP}(K^+K^-) = [6.8 \pm 5.4(\text{stat}) \pm 1.6(\text{sys})] \times 10^{-4}$$

$$a_f^d = A_{CP}(f) - \frac{\langle \tau_f \rangle}{\tau_D} \Delta Y_f$$

Indirect term,
asymmetries in effective
width, lifetimes



Run1+Run2:

$$a_{CP}^d(K^+K^-) = [7.7 \pm 5.7] \times 10^{-4}$$

$$a_{CP}^d(\pi^+\pi^-) = [23.2 \pm 6.1] \times 10^{-4}$$

First evidence (3.8 σ) of CPV in $D \rightarrow \pi^+\pi^-$

Charm Decays

Other recent search for CPV in Charm sector: **not see CPV in all cases**

Decay mode	Paper
$D_{(s)}^+ \rightarrow K^+ K^- K^+$	LHCb: JHEP 07 067 (2023)
$D^0 \rightarrow \pi^+ \pi^- \pi^+$	LHCb: arXiv:2306.12746
$D_{(s)}^+ \rightarrow \eta^{(\prime)} \pi^+$	LHCb: JHEP 04 081 (2023)
$D_{(s)}^+ \rightarrow K^+ K^- \pi^+ \pi^0,$ $\quad \rightarrow K^+ \pi^- \pi^+ \pi^0$ $D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0$	Belle: arXiv 2305.12806
$D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$	Belle: PRD 107, 052001 (2023)
$D_{(s)}^+ \rightarrow K^+ K_S^0 h^+ h^-$ $D_s^+ \rightarrow K^+ K^- K_S^0 \pi^+$	Belle: arXiv 2305.11405
$D^0 \rightarrow h^+ h^- \mu^+ \mu^-$	LHCb: PRL 128, 221801 (2022)

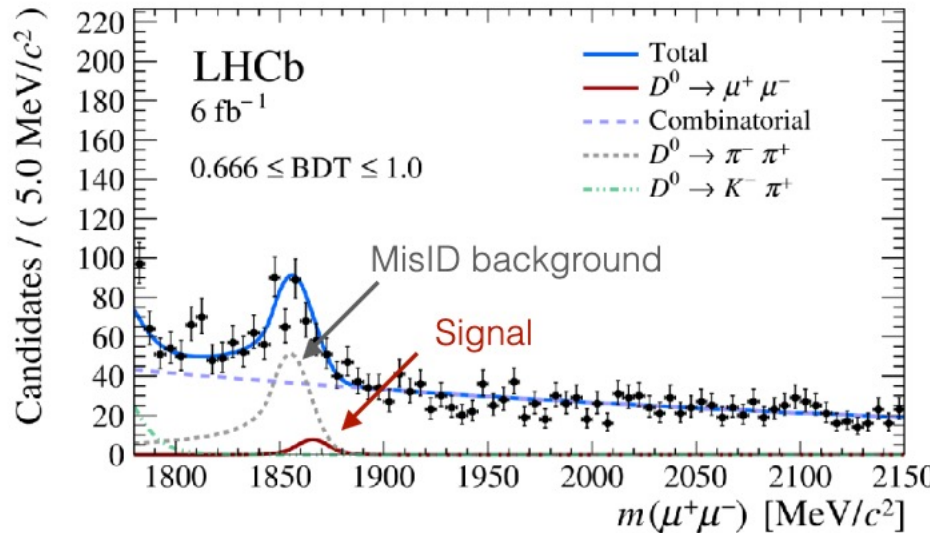
Angular analysis

Charm Decays

Rare decays:



•PRL 131 041804 (2023)



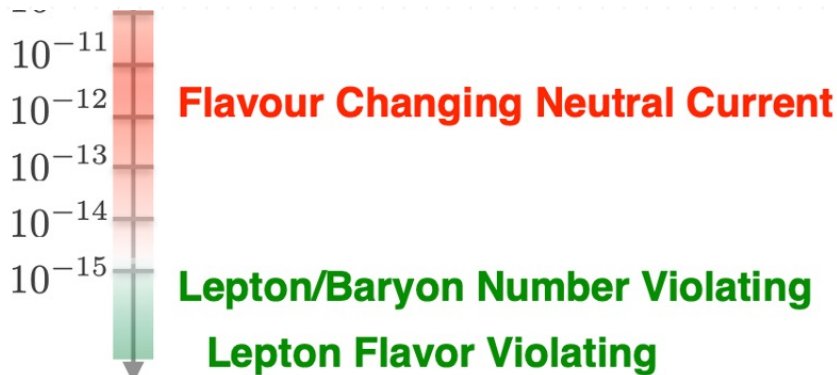
$$B(D^0 \rightarrow \mu^+ \mu^-) < 2.94 \times 10^{-9} @ 90 \% \text{ CL}$$

(LHCb 9/fb Run1+2)

Most stringent
limit on charm FCNC!

$$B(D^{0*}(2007) \rightarrow \mu^+ \mu^-) < 2.6 \times 10^{-8} @ 90 \% \text{ CL}$$

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$$\begin{array}{ll} D^0 \rightarrow \mu^- \mu^+ & D \rightarrow h \ell^+ \ell^- \\ D^0 \rightarrow e^- e^+ & D \rightarrow h h' \ell^- \ell^+ \\ & D \rightarrow V \ell^+ \ell^- \end{array}$$

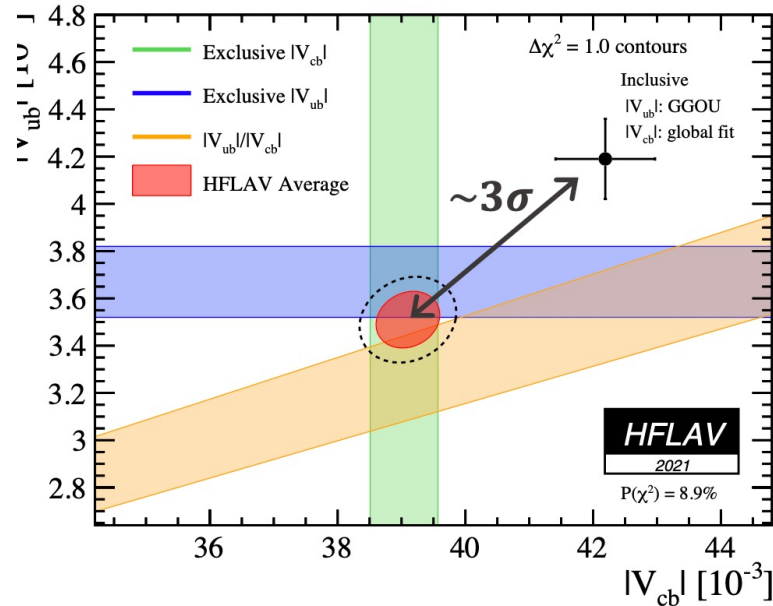
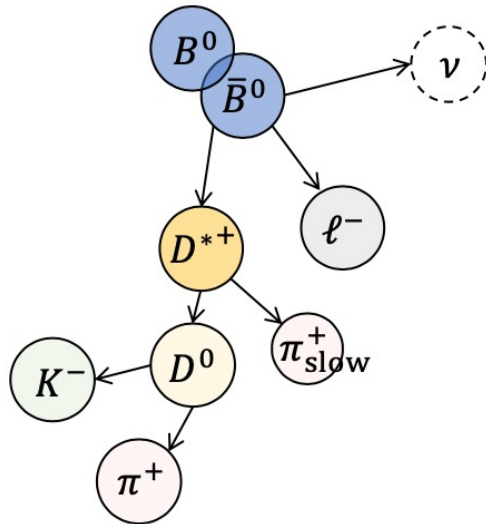
$$\begin{array}{l} D \rightarrow (h) e^- \mu^+ \\ D \rightarrow (h) \ell^+ \ell^+ \end{array}$$

Beauty Decays

Semileptonic B Decays

- ❖ determine the CKM elements $|V_{cb}|$ and $|V_{ub}|$
- ❖ Tests of lepton universality, $R(D^{(*)}), R(K^{(*)})$

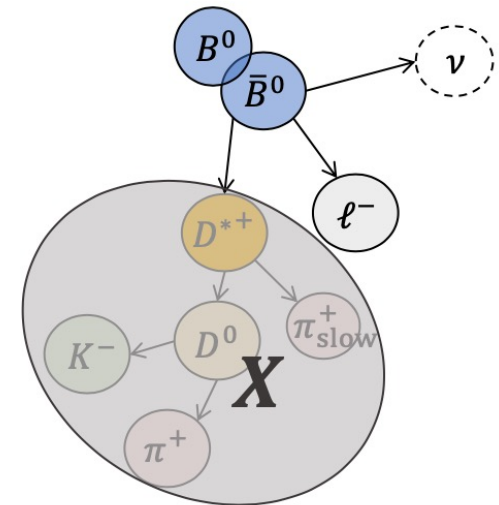
Exclusive



Reconstruct all daughters through specific channels exclusively.

The current experimental focus is on understanding the origin of this discrepancy.

Inclusive

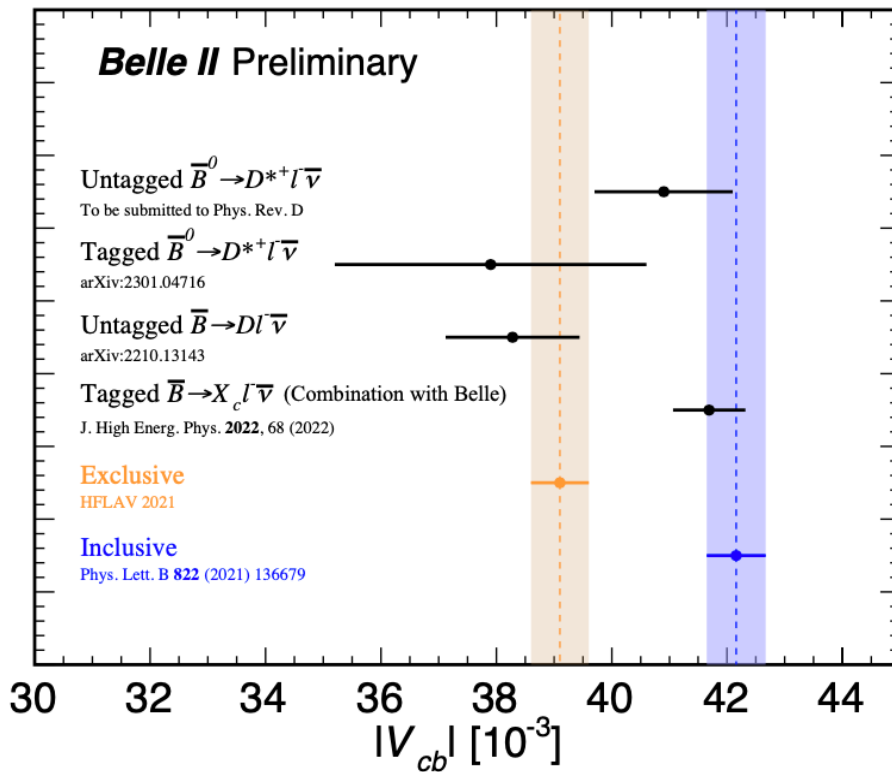


Reconstruct a lepton and assign other tracks and clusters as an inclusive daughter X .

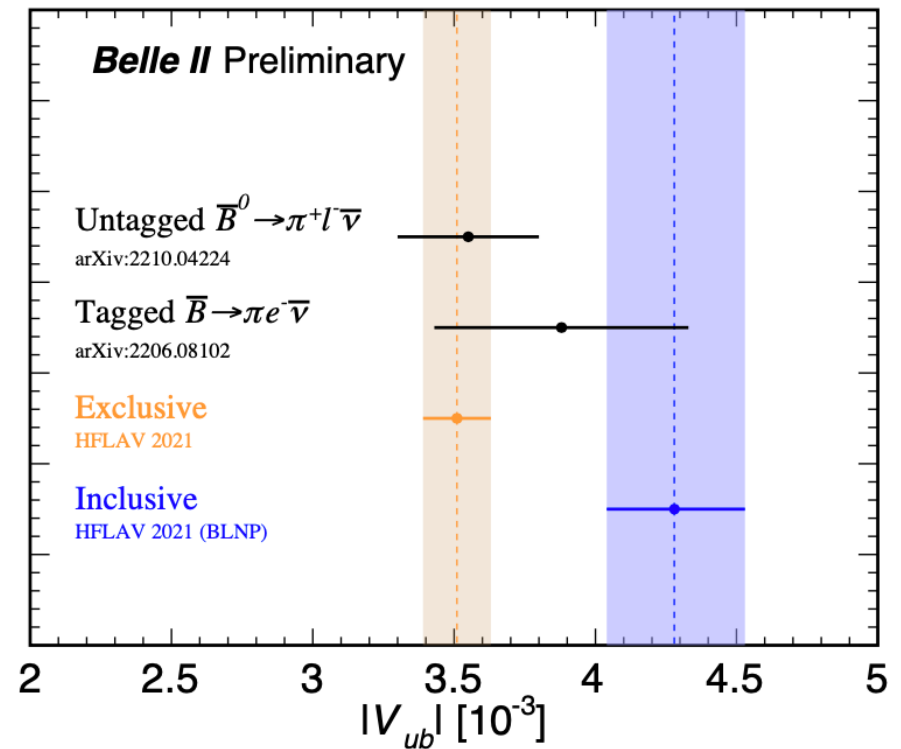
Beauty Decays

Semileptonic B Decays

$|V_{cb}|$ from $B \rightarrow D^* l \bar{\nu} (l = e, \mu)$:



$|V_{ub}|$ from $B \rightarrow \pi l \bar{\nu} (l = e, \mu)$:

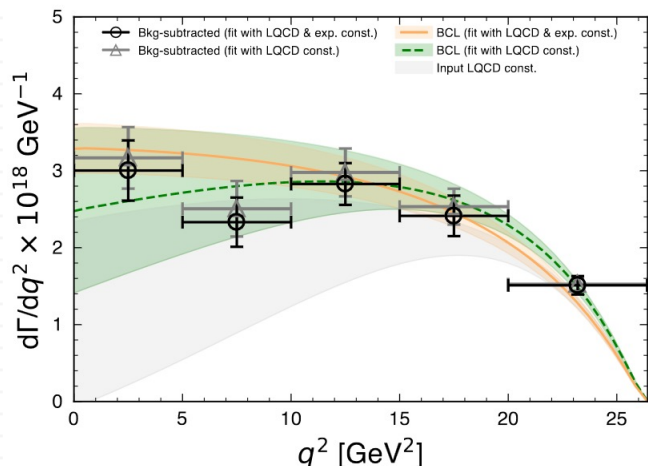


Beauty Decays



First Simultaneous Determination of Inclusive and Exclusive $|V_{ub}|$

arXiv:2303.17309

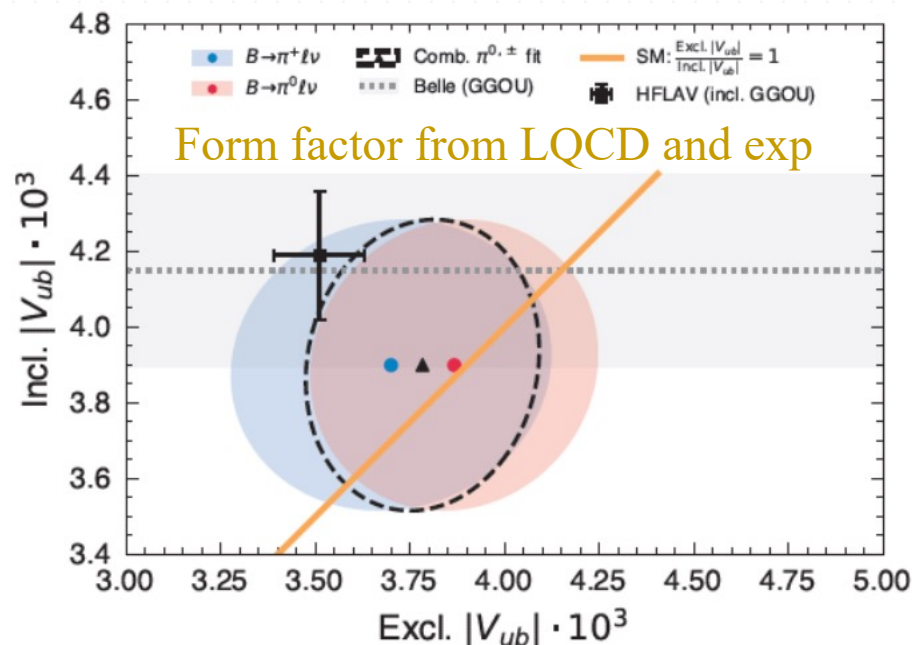
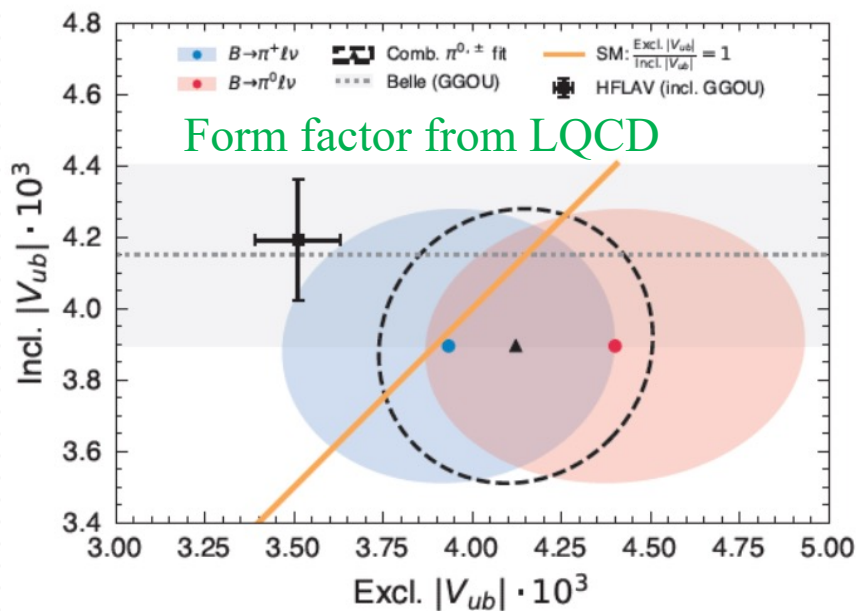


$$|V_{ub}^{\text{excl.}}| = (3.78 \pm 0.23^{\text{stat}} \pm 0.16^{\text{syst}} \pm 0.14^{\text{theo}}) \times 10^{-3}$$

$$|V_{ub}^{\text{incl.}}| = (3.90 \pm 0.20^{\text{stat}} \pm 0.32^{\text{syst}} \pm 0.09^{\text{theo}}) \times 10^{-3}$$

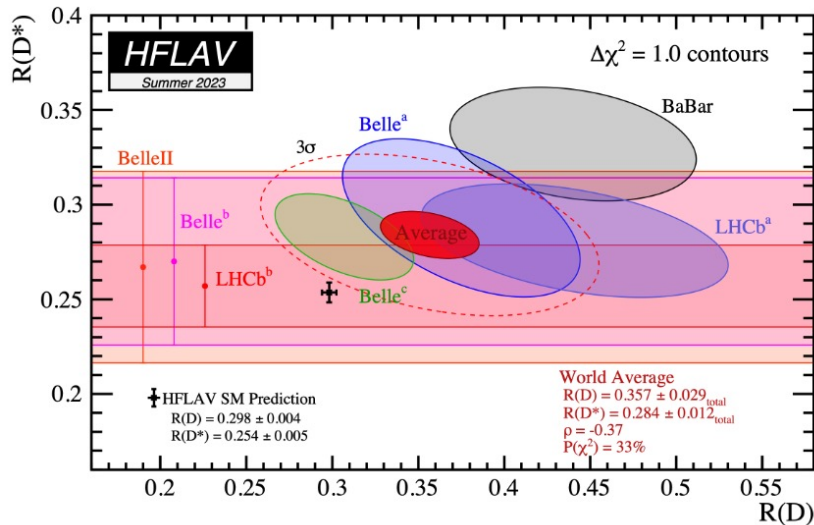
Correlation = 0.10

$$|V_{ub}^{\text{excl.}}| / |V_{ub}^{\text{incl.}}| = 0.97 \pm 0.12^{\text{exp}}$$

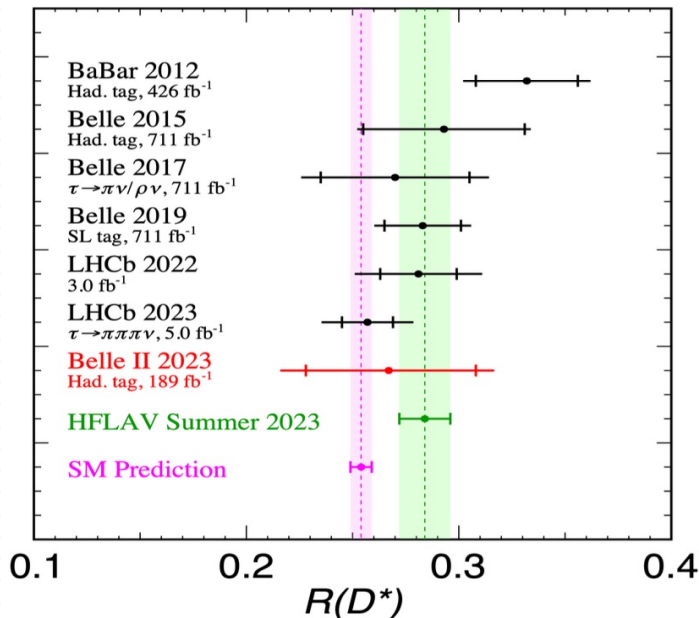
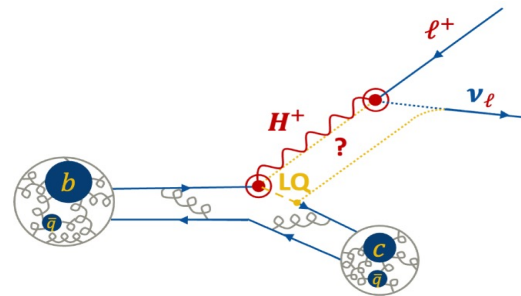


Beauty Decays

❖ Tests of lepton universality, $R(D^{(*)}), R(K^{(*)})$



$$R(D^{(*)}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \ell^- \bar{\nu}_\ell)}, (\ell = e \text{ or } \mu)$$

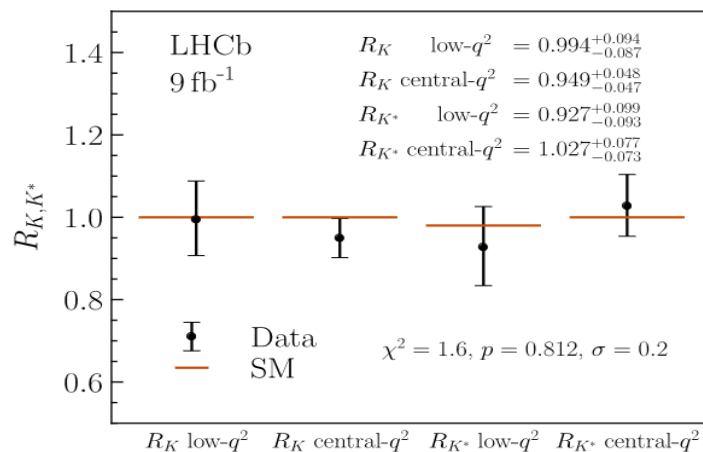
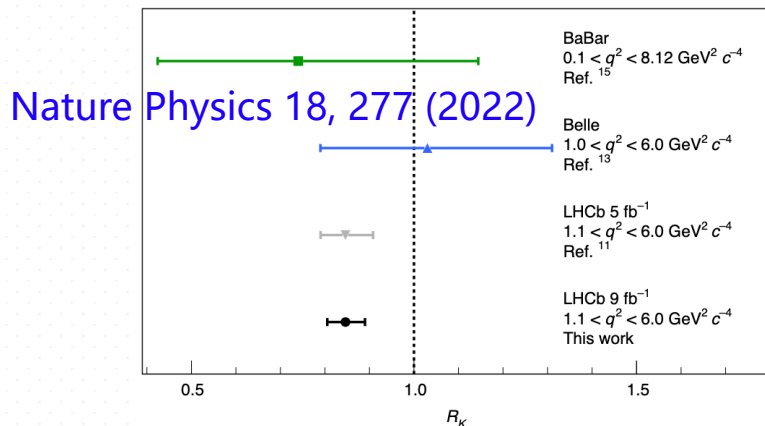


- LHCb: [PRD 108 012018 \(2023\)](#)
=> reduce tension $2.49\sigma \rightarrow 2.15\sigma$
 - Belle II: [PRD 108 012018 \(2023\)](#)
=> 40% improvement in statistical precision over Belle at the same sample size
- LHCb: [arXiv 2302.02886](#)
=> simultaneous measurement of $R(D)$ and $R(D^*)$, 1.9σ tension

Beauty Decays

❖ Other recent checks:

LHCb: PRL 131 051803 (2023), Phys. Rev. D 108, 032002 (2023)



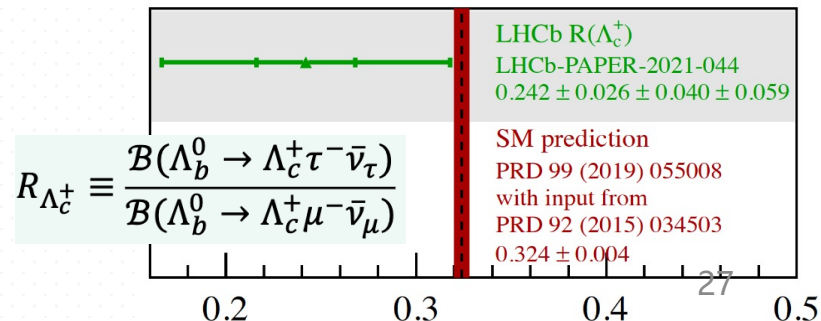
$$R_H \equiv \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow H\mu^+\mu^-)}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow He^+e^-)}{dq^2} dq^2}$$

$$R_{K,K^*}(q_a^2, q_b^2) = \frac{\int_{q_a^2}^{q_b^2} \frac{d\Gamma(B^{(+,0)} \rightarrow K^{(+,0)}\mu^+\mu^-)}{dq^2} dq^2}{\int_{q_a^2}^{q_b^2} \frac{d\Gamma(B^{(+,0)} \rightarrow K^{(+,0)}e^+e^-)}{dq^2} dq^2}$$

BelleII: Phys. Rev. Lett. 131, 051804 (2023)

LHCb: Phys. Rev. Lett. 128, 191803 (2022)

$$\begin{aligned}
 R(X_{e/\mu}) &= \mathcal{B}(B \rightarrow X e \nu) / \mathcal{B}(B \rightarrow X \mu \nu) \\
 &= 1.007 \pm 0.009 \pm 0.019
 \end{aligned}$$



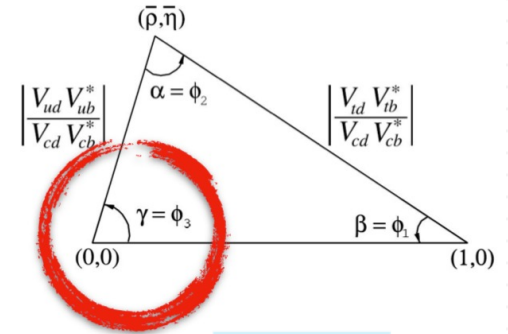
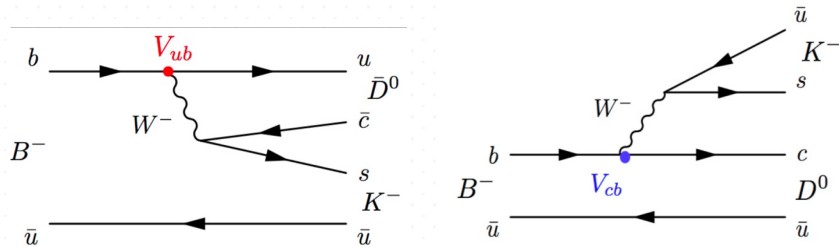
Beauty Decays

Hadronic decay (Measurement of CKM angle $\phi_3 = \arg\left[\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right]$)

⊙ Theoretical uncertainty on measurement is $\frac{\delta\phi_3}{\phi_3} \sim 10^{-7}$

⊙ Test physics beyond SM

⊙ CPV in the interference $b \rightarrow c\bar{u}s$ and $b \rightarrow u\bar{c}s$:



-- $B^0 \rightarrow D(\rightarrow K_S h^+ h^-) K^{*0}$

LHCb-PAPER-2023-009

- Limited statistics,
- CPV still observed in some bins

$$\phi_3 = (49_{-18}^{+23})^\circ$$

-- $B^- \rightarrow D^*(\rightarrow D(\rightarrow K_S h^+ h^-) \pi^0 / \gamma) h^-$

LHCb-PAPER-2023-012

$$\phi_3 = (69 \pm 14)^\circ$$

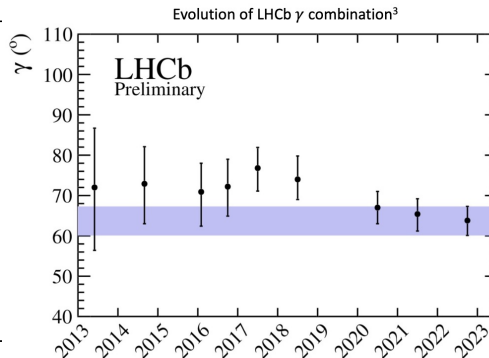
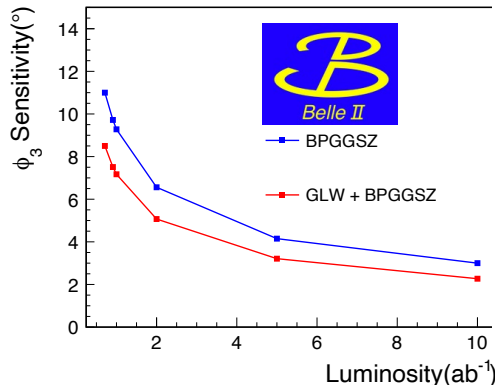
-- $B^- \rightarrow D(\rightarrow K^+ K^- \pi^+ \pi^-) h^-$

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$$\phi_3 = (116_{-14}^{+12})^\circ$$

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$$\phi_3 = (78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ$$



$\sim 1.5^\circ$ (50 ab^{-1} @ Belle II)

Data limited!

Precision in 2013	LHCb 2018	Upgrade I (50 fb^{-1})	Upgrade II (300 fb^{-1})
$\sim 10-12^\circ$	4°	1°	0.35°

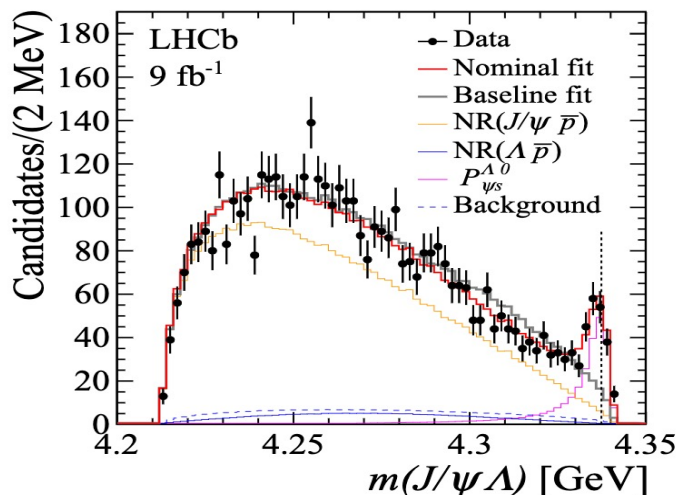
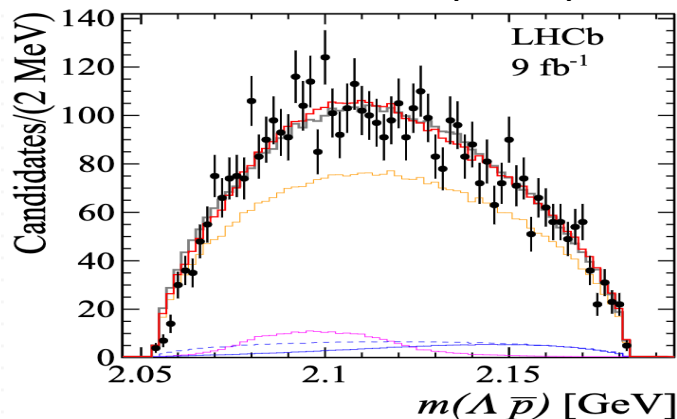
Beauty Decays

Hadronic decay (exotic, light hadron states)



$$B^- \rightarrow J/\psi \Lambda \bar{p}$$

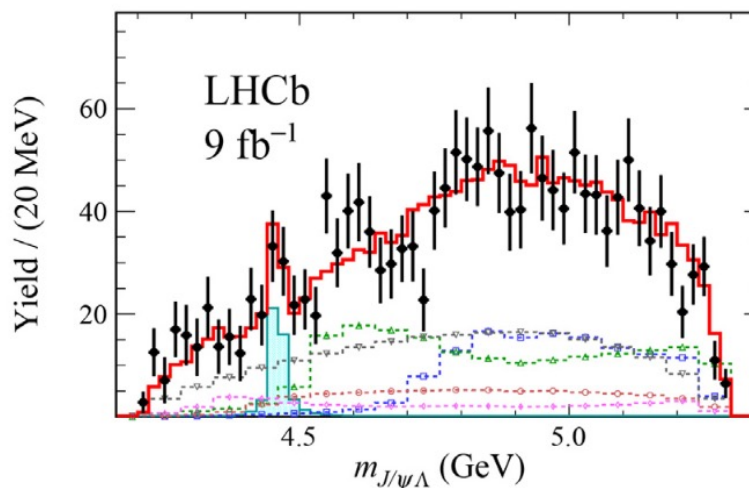
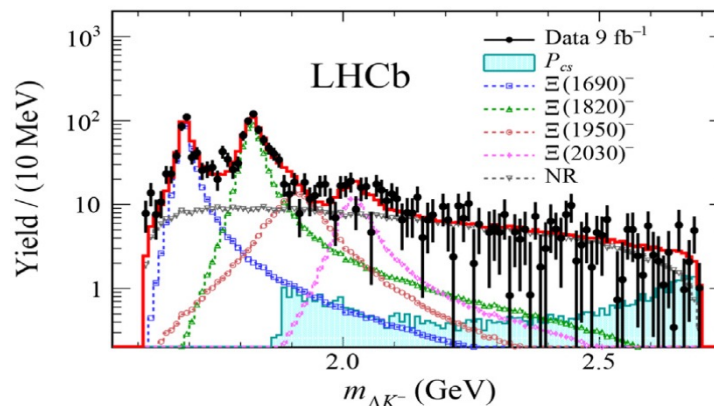
PRL 131 031901 (2023)



$P_{CS}(4338) : \Xi_c^+ D^-$ threshold

$$\Xi_b^- \rightarrow J/\psi \Lambda K^-$$

Science Bulletin 66 (2021) 1278



$P_{CS}(4459) : \sim < \Xi_c^0 \bar{D}^{*0}$ threshold

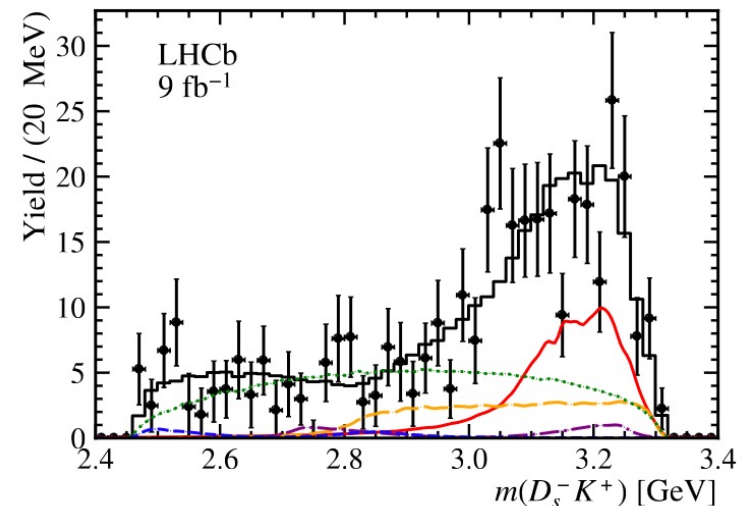
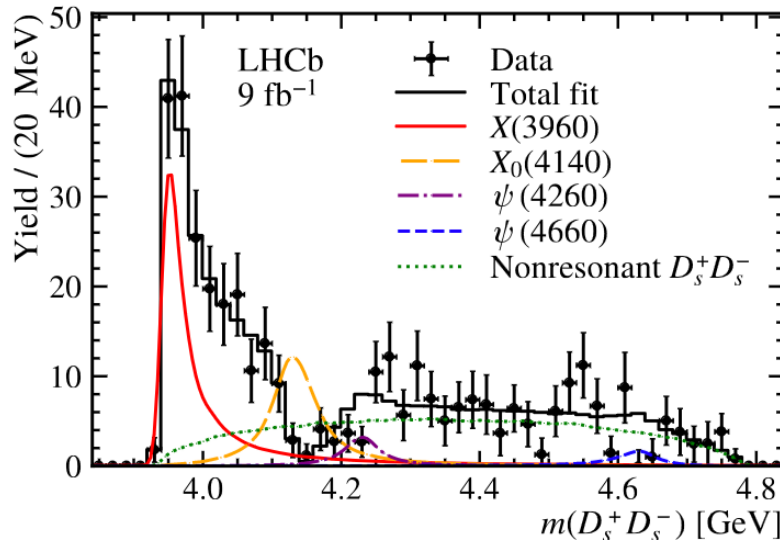
Beauty Decays

Hadronic decay (exotic, light hadron states)



$$B^+ \rightarrow D_s^+ D_s^- K^+$$

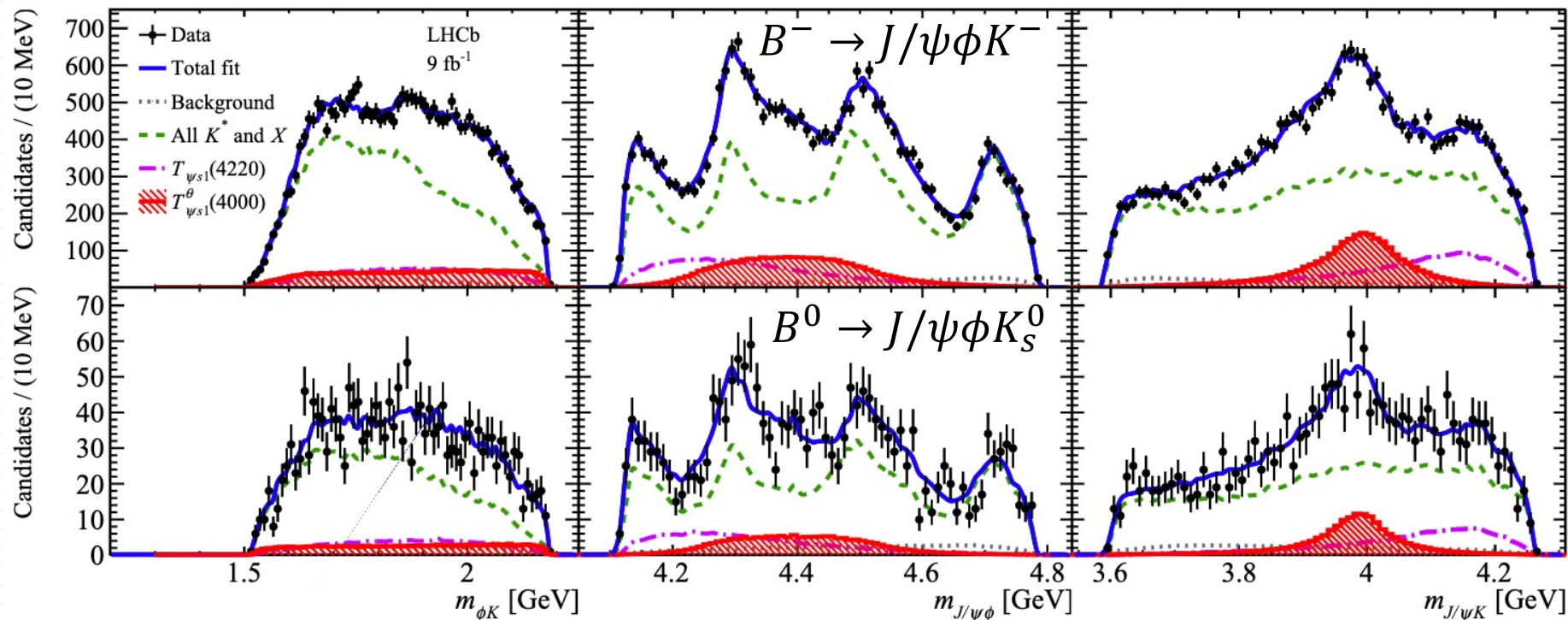
PRL 131, 071901 (2023)



Component	J^{PC}	M_0 (MeV)	Γ_0 (MeV)	$\mathcal{F}$ (%)	$\mathcal{S}$ (σ)
X(3960)	0^{++}	$3956 \pm 5 \pm 11$	$43 \pm 13 \pm 8$	$25.4 \pm 7.7 \pm 8.0$	12.6 (14.3)
X ₀ (4140)	0^{++}	$4133 \pm 6 \pm 11$	$67 \pm 17 \pm 7$	$16.7 \pm 4.7 \pm 7.5$	3.7 (3.9)
ψ(4260)	1^{--}	4230	55	$3.6 \pm 0.4 \pm 3.0$	3.1 (3.3)
ψ(4660)	1^{--}	4633	64	$2.2 \pm 0.2 \pm 0.5$	2.9 (3.2)
NR	S-wave	-	-	$46.1 \pm 13.2 \pm 11.1$	3.1 (3.4)

Beauty Decays

Hadronic decay (exotic, light hadron states) [arXiv 2301.04899](https://arxiv.org/abs/2301.04899)



State	Mass (MeV)	Width (MeV)	Fit fraction (%)	ΔM (MeV)
$T_{\psi s1}^\theta(4000)^0$	$3991^{+12}_{-10} {}^{+9}_{-17}$	$105^{+29}_{-25} {}^{+17}_{-23}$	$7.9 \pm 2.5 {}^{+3.0}_{-2.8}$	$-12^{+11}_{-10} {}^{+6}_{-4}$

$T_{\psi s1}^\theta(4000)^0$: **4.0 σ**

Change to **5.4 σ** when isospin symmetry imposed on $T_{\psi s1}^\theta(4000)^{0,\pm}$

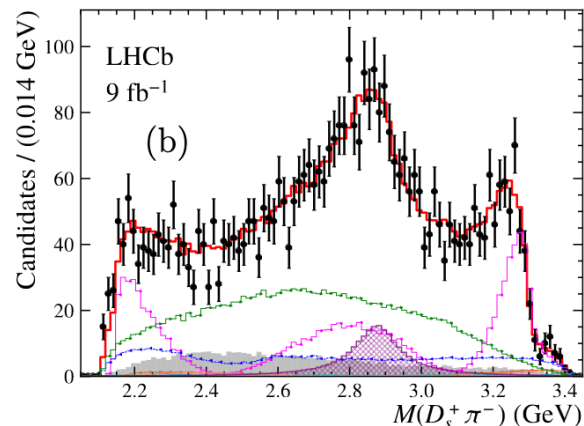
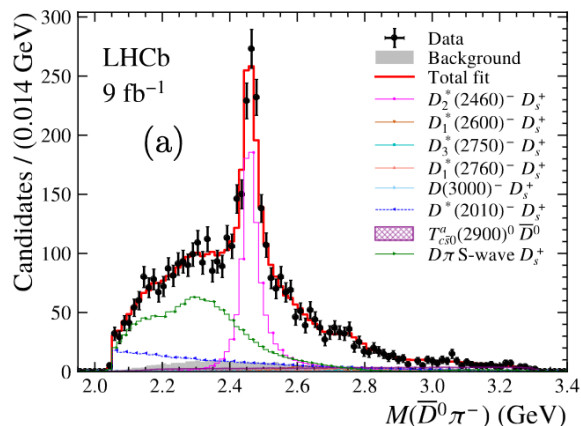
Beauty Decays

Hadronic decay (exotic, light hadron states)

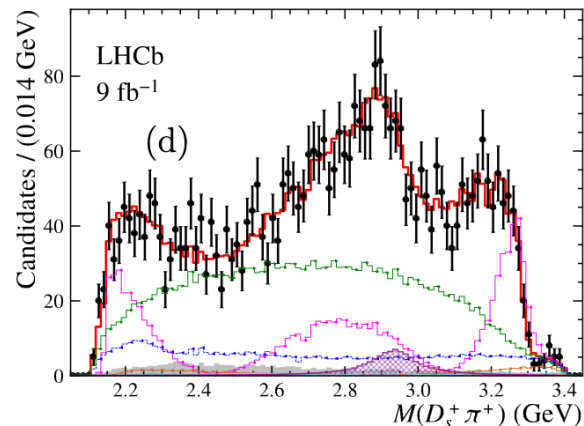
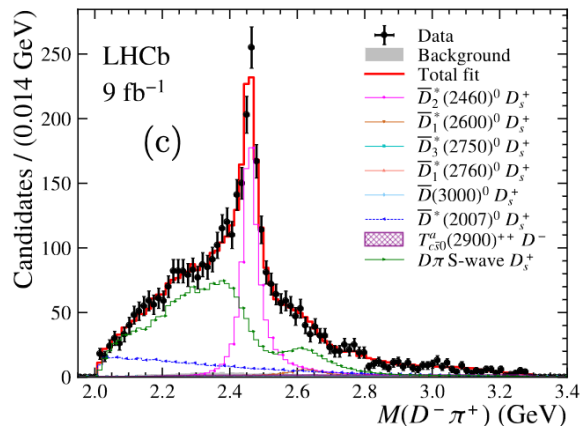


PRD PRD 108 (2023) 012017

$$B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$$



$$B^+ \rightarrow D^- D_s^+ \pi^+$$



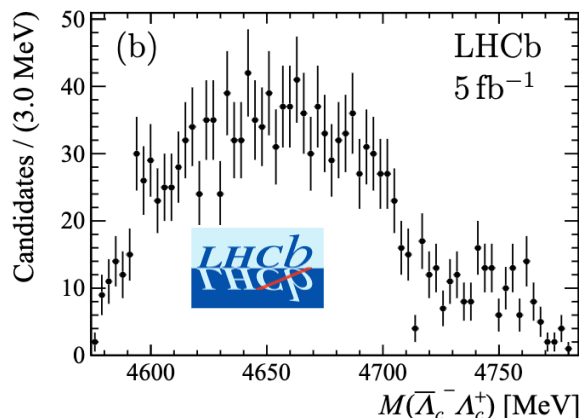
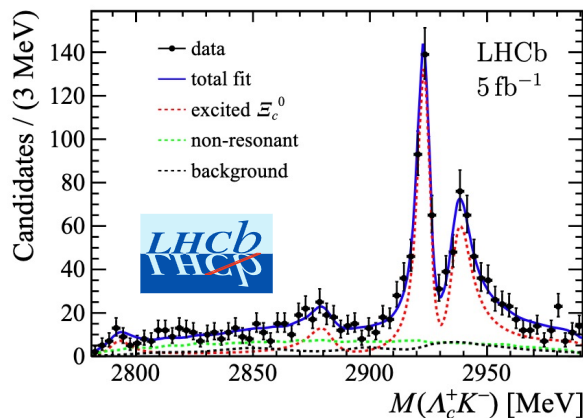
	Particle	Mass (GeV)	Width (GeV)
6.6 σ	$T_{c\bar{s}0}^a(2900)^0$	$2.879 \pm 0.017 \pm 0.018$	$0.153 \pm 0.028 \pm 0.020$
4.8 σ	$T_{c\bar{s}0}^a(2900)^{++}$	$2.935 \pm 0.021 \pm 0.013$	$0.143 \pm 0.038 \pm 0.025$

Beauty Decays

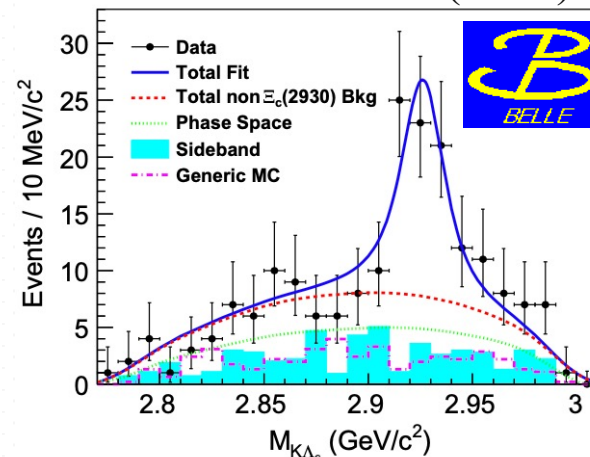
Hadronic decay (heavy hadrons)

$$B^+ \rightarrow \Lambda_c^+ \bar{\Lambda}_c^- K^+$$

LHCb: PRD 108, 012020 (2023)

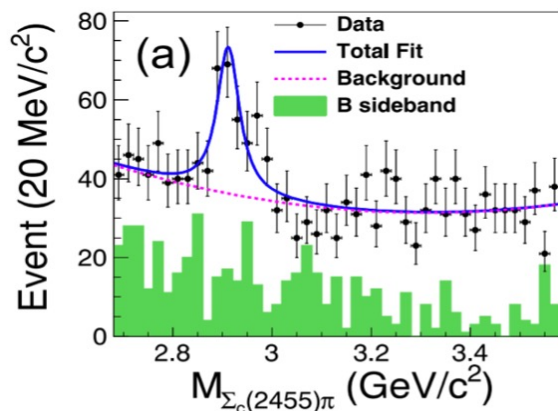


Belle: EPJC 78 252 (2018)



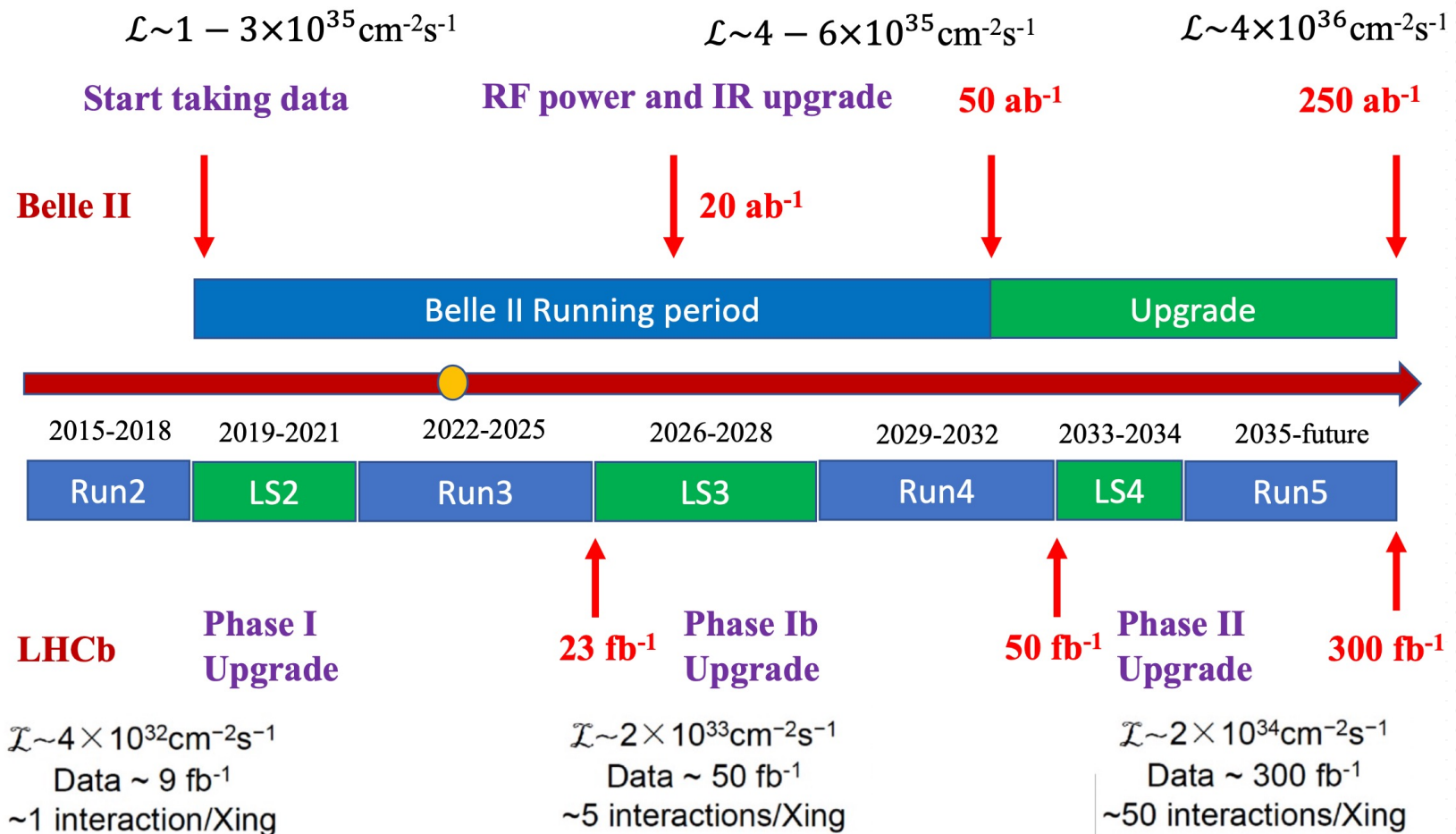
$$\bar{B}^0 \rightarrow \Sigma_c(2455) \pi^-$$

Belle: PRL 130, 031901 (2023)



Possible $J^P = \frac{1}{2}^-$, agrees with $\Lambda_c \left(\frac{1}{2}^-, 2P \right)$,
named: $\Lambda_c(2910)$

Future



The more we know, the more we do not know!
路漫漫其修远兮，吾将上下而求索



西安交通大学
XI'AN JIAOTONG UNIVERSITY

谢谢大家



CKM	Process	Observables		Theoretical inputs	
$ V_{ud} $	$0^+ \rightarrow 0^+ \beta$	$ V_{ud} _{\text{nucl}}$	$=$	$0.97420 \pm 0 \pm 0.00021$	Nuclear matrix elements
$ V_{us} $	$K \rightarrow \pi \ell \nu$ $K \rightarrow e \nu$ $K \rightarrow \mu \nu$ $\tau \rightarrow K \nu$	$ V_{us} _{\text{SL}} f_+^{K \rightarrow \pi}(0)$ $\mathcal{B}(K \rightarrow e \nu)$ $\mathcal{B}(K \rightarrow \mu \nu)$ $\mathcal{B}(\tau \rightarrow K \nu)$	$=$ $=$ $=$ $=$	0.2165 ± 0.0004 $(1.582 \pm 0.007) \cdot 10^{-5}$ 0.6356 ± 0.0011 $(0.6960 \pm 0.0096) \cdot 10^{-2}$	$f_+^{K \rightarrow \pi}(0) = 0.9681 \pm 0.0014 \pm 0.0022$ $f_K = 155.6 \pm 0.2 \pm 0.6 \text{ MeV}$
$\frac{ V_{us} }{ V_{ud} }$	$K \rightarrow \mu \nu / \pi \rightarrow \mu \nu$ $\tau \rightarrow K \nu / \tau \rightarrow \pi \nu$	$\frac{\mathcal{B}(K \rightarrow \mu \nu)}{\mathcal{B}(\pi \rightarrow \mu \nu)}$ $\frac{\mathcal{B}(\tau \rightarrow K \nu)}{\mathcal{B}(\tau \rightarrow \pi \nu)}$	$=$ $=$	1.3367 ± 0.0029 $(6.438 \pm 0.094) \cdot 10^{-2}$	$f_K/f_\pi = 1.1959 \pm 0.0007 \pm 0.0029$
$ V_{cd} $	νN $D \rightarrow \mu \nu$ $D \rightarrow \pi \ell \nu$	$ V_{cd} _{\text{not lattice}}$ $\mathcal{B}(D \rightarrow \mu \nu)$ $ V_{cd} f_+^{D \rightarrow \pi}(0)$	$=$ $=$ $=$	0.230 ± 0.011 $(3.74 \pm 0.17) \cdot 10^{-4}$ 0.1426 ± 0.0019	$f_{D_s}/f_D = 1.175 \pm 0.001 \pm 0.004$ $f_+^{D \rightarrow \pi}(0) = 0.621 \pm 0.016 \pm 0.012$
$ V_{cs} $	$W \rightarrow c \bar{s}$ $D_s \rightarrow \tau \nu$ $D_s \rightarrow \mu \nu$ $D \rightarrow K \ell \nu$	$ V_{cs} _{\text{not lattice}}$ $\mathcal{B}(D_s \rightarrow \tau \nu)$ $\mathcal{B}(D_s \rightarrow \mu \nu)$ $ V_{cs} f_+^{D \rightarrow K}(0)$	$=$ $=$ $=$ $=$	$0.94_{-0.26}^{+0.32} \pm 0.13$ $(5.55 \pm 0.24) \cdot 10^{-2}$ $(5.39 \pm 0.16) \cdot 10^{-3}$ 0.7226 ± 0.0034	$f_{D_s} = 247.8 \pm 0.3 \pm 2.0 \text{ MeV}$ $f_+^{D \rightarrow K}(0) = 0.741 \pm 0.010 \pm 0.012$
$ V_{ub} $	semileptonic B $B \rightarrow \tau \nu$	$ V_{ub} _{\text{SL}}$ $\mathcal{B}(B \rightarrow \tau \nu)$	$=$ $=$	$(3.98 \pm 0.08 \pm 0.22) \cdot 10^{-3}$ $(1.08 \pm 0.21) \cdot 10^{-4}$	form factors, shape functions $f_{B_s}/f_B = 1.205 \pm 0.004 \pm 0.006$
$ V_{cb} $	semileptonic B	$ V_{cb} _{\text{SL}}$	$=$	$(41.8 \pm 0.4 \pm 0.6) \cdot 10^{-3}$	form factors, OPE matrix elements
$ V_{ub}/V_{cb} $	semileptonic Λ_b	$\frac{\mathcal{B}(\Lambda_p \rightarrow p \mu^- \bar{\nu})_{q^2 > 15}}{\mathcal{B}(\Lambda_p \rightarrow \Lambda_c \mu^- \bar{\nu})_{q^2 > 7}}$	$=$	$(0.947 \pm 0.081) \cdot 10^{-2}$	$\frac{\zeta(\Lambda_p \rightarrow p \mu^- \bar{\nu})_{q^2 > 15}}{\zeta(\Lambda_p \rightarrow \Lambda_c \mu^- \bar{\nu})_{q^2 > 7}} = 1.471 \pm 0.096 \pm 0.290$
α	$B \rightarrow \pi \pi, \rho \pi, \rho \rho$	branching ratios, CP asymmetries		isospin symmetry	
β	$B \rightarrow (c \bar{c}) K$	$\sin(2\beta)_{[c \bar{c}]}$	$=$	0.699 ± 0.017	subleading penguins neglected
$\cos(2\beta)$	$B^0 \rightarrow D^{(*)} h^0$	$\cos(2\beta)$	$=$	0.91 ± 0.25	
γ	$B \rightarrow D^{(*)} K^{(*)}$	inputs for the 3 methods		GGSZ, GLW, ADS methods	
ϕ_s	$B_s \rightarrow J/\psi(KK, \pi\pi)$	$(\phi_s)_{b \rightarrow c \bar{c} s}$	$=$	-0.021 ± 0.031	
$V_{tq}^* V_{tq'}$	Δm_d Δm_s $B_s \rightarrow \mu \mu$	Δm_d Δm_s $\mathcal{B}(B_s \rightarrow \mu \mu)$	$=$ $=$ $=$	$0.5065 \pm 0.0019 \text{ ps}^{-1}$ $17.757 \pm 0.021 \text{ ps}^{-1}$ $(2.8_{-0.6}^{+0.7}) \cdot 10^{-9} [\times (1 - 0.063)]$	$\hat{B}_{B_s}/\hat{B}_{B_d} = 1.007 \pm 0.013 \pm 0.014$ $\hat{B}_{B_s} = 1.327 \pm 0.016 \pm 0.030$ $f_{B_s} = 226.0 \pm 1.3 \pm 2.0 \text{ MeV}$
$V_{td}^* V_{ts}$ and $V_{cd}^* V_{cs}$	ε_K	$ \varepsilon_K $	$=$	$(2.228 \pm 0.011) \cdot 10^{-3}$	$\hat{B}_K = 0.7567 \pm 0.0021 \pm 0.0123$ $\kappa_\varepsilon = 0.940 \pm 0.013 \pm 0.023$

https://indico.cern.ch/event/684284/contributions/2952455/attachments/1719296/2774804/Vale_Silva_3.pdf

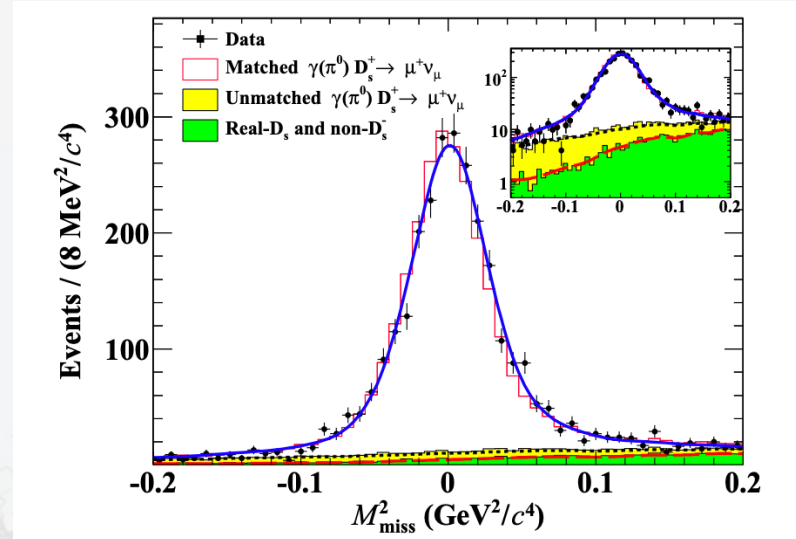
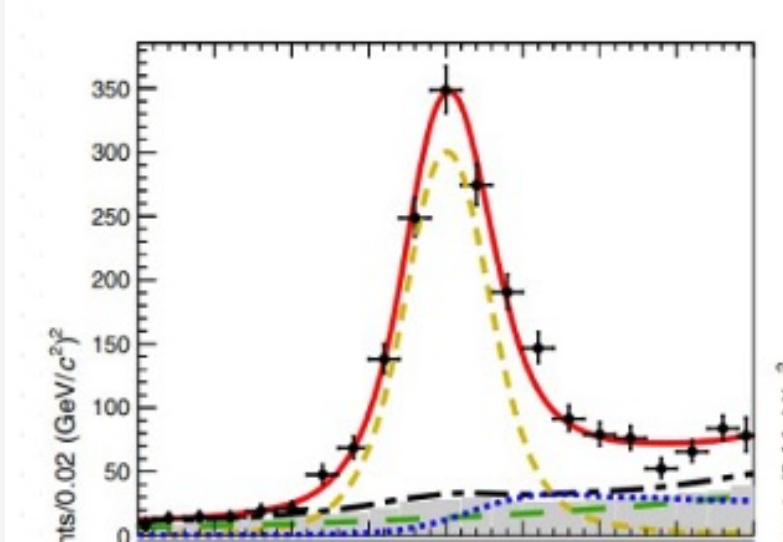
Experiment	Machine	Operation	C.M.	Lumin.	N(D^0)	efficiency	⊕advantage/⊗disadvantage
	CESR (e^+e^-)	2003-2008	3.77 4.18 GeV	0.8 fb $^{-1}$ 0.6 fb $^{-1}$	2.9 M D^+ : 2.3 M 0.6 M	~10-30%	⊕ extremely clean environment ⊕ pure D-beam, almost no bkg ⊕ quantum coherence ⊗ no CM boost, no T-dep analyses
	BEPC-II (e^+e^-)	2010-2011(2021-) 2016-2019 2014+2020	3.77 GeV 4.18-4.23 GeV 4.6-4.7 GeV	2.92($\rightarrow$ 20) fb $^{-1}$ 7.3 fb $^{-1}$ 4.5 fb $^{-1}$	10.5($\rightarrow$ 72) M D^+ : 8.4 M 4.6 M Λ_c^+ : ? M		
	SuperKEKB (e^+e^-)	2019-	10.58 GeV	428+ fb $^{-1}$	0.6+ G D^+ : 0.3 G	~5-10%	⊕ clear event environment ⊕ high trigger efficiency ⊕ high-efficiency detection of neutrals ⊕ many high-statistics control samples ⊕ time-dependent analysis ⊗ smaller cross-section than pp colliders
	KEKB (e^+e^-)	1999-2010	10.58 GeV	1000 fb $^{-1}$	1.4 G D^+ : 0.8 G		
	PEP-II (e^+e^-)	1999-2008	10.58 GeV	500 fb $^{-1}$	0.65 G		
	Tevatron ($p\bar{p}$)	2002-2011	1960	9.6 fb $^{-1}$	0.13 T	<0.5%	⊕ very large production cross-section ⊕ large boost ⊕ excellent time resolution ⊗ dedicated trigger required
	LHC (pp)	2011	7 TeV	1.0 fb $^{-1}$	5.0 T		
		2012	8 TeV	2.0 fb $^{-1}$	?		
		2015-2018	13 TeV	6 fb $^{-1}$	?		

here using $\sigma(D^0\bar{D}^0@3.77\text{ GeV})=3.61\text{ nb}$, $\sigma(D^+D^-@3.77\text{ GeV})=2.88\text{ nb}$, $\sigma(D_s^*D_s@4.17\text{ GeV})=0.967\text{ nb}$, $\sigma(c\bar{c}@10.58\text{ GeV})=1.3\text{ nb}$, $\sigma(D^0@CDF)=13.3\text{ }\mu\text{b}$, and $\sigma(D^0@LHCb)=1661\text{ }\mu\text{b}$, mainly referring to *Int. J. Mod. Phys. A* **29** (2014) 24, 14300518.

Charm Decays

leptonic decay of D_s

$$\text{SM : } R_{D^+} = m_\tau^2 \left(1 - \frac{m_{\tau^+}^2}{m_{D_q^+}^2} \right)^2 / m_\mu^2 \left(1 - \frac{m_\mu^2}{m_{D_q^+}^2} \right)^2 = 2.67$$



Experiment	E_{cm} (GeV)	Reaction chain	$\mathcal{B}$ (%)	$f_{D_s^+} V_{cs} $ (MeV)
CLEO [2]	4.170	$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	$0.565 \pm 0.045 \pm 0.017$	$249.8 \pm 10.0 \pm 3.8 \pm 1.0$
BaBar [5]	10.56	$e^+e^- \rightarrow DKX\gamma D_s^-$	$0.602 \pm 0.038 \pm 0.034$	$257.8 \pm 8.2 \pm 7.3 \pm 1.0$
Belle [6]	10.56	$e^+e^- \rightarrow DKX\gamma D_s^-$	$0.531 \pm 0.028 \pm 0.020$	$242.2 \pm 6.4 \pm 4.7 \pm 1.0$
BESIII ^b [7]	4.009	$e^+e^- \rightarrow D_s^+ D_s^-$	$0.517 \pm 0.075 \pm 0.021$	$238.9 \pm 17.5 \pm 4.9 \pm 0.9$
BESIII ^a [8]	4.178	$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	$0.549 \pm 0.016 \pm 0.015$	$246.2 \pm 3.6 \pm 3.4 \pm 1.0$
BESIII ^b [9]	4.178-4.226	$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	$0.535 \pm 0.013 \pm 0.016$	$243.1 \pm 3.0 \pm 3.6 \pm 1.0$
This work^a	4.128-4.226	$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	$0.5294 \pm 0.0108 \pm 0.0085$	$241.8 \pm 2.5 \pm 2.2 \pm 1.0$

Charm Decays

Semi-leptonic decay of $D_{(s)}$

$$\frac{d\Gamma(D_{(s)} \rightarrow P \ell^+ \nu_\ell)}{dq^2} = \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p_{f_0}^3 |f_+(q^2)|^2$$

$$\frac{d^2\Gamma(D_{(s)} \rightarrow S \ell^+ \nu_\ell)}{ds dq^2} = \frac{G_F^2 |V_{cd(s)}|^2}{192\pi^4 m_{D_{(s)}}^3} \lambda^{3/2}(m_{D_s}^2, s, q^2) |f_+(q^2)|^2 P(s)$$

$$P(s) = \begin{cases} \frac{g_1 \rho_{\pi\pi}}{|m_0^2 - s - i(g_1 \rho_{\pi\pi} + g_1 \rho_{KK})|^2}, & \text{Flatte for } a_0(980)/f_0(980) \\ \frac{m_{f_0} \Gamma(s)}{(s - m_{f_0}^2)^2 + m_{f_0}^2 \Gamma^2(s)}, & \text{RBW for } f_0(500) \end{cases}$$

– Single pole form

$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/M_{pole}^2}$$

– Modified pole model

$$f_+(q^2) = \frac{f_+(0)}{\left(1 - \frac{q^2}{M_{pole}^2}\right) \left(1 - \alpha \frac{q^2}{M_{pole}^2}\right)}$$

– ISGW2 model

$$f_+(q^2) = f_+(q_{max}^2) \left(1 + \frac{r^2}{12}(q_{max}^2 - q^2)\right)^{-2}$$

– Series expansion model

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

Charm Decays

Phys. Rev. D. 105, L031101 (2022)

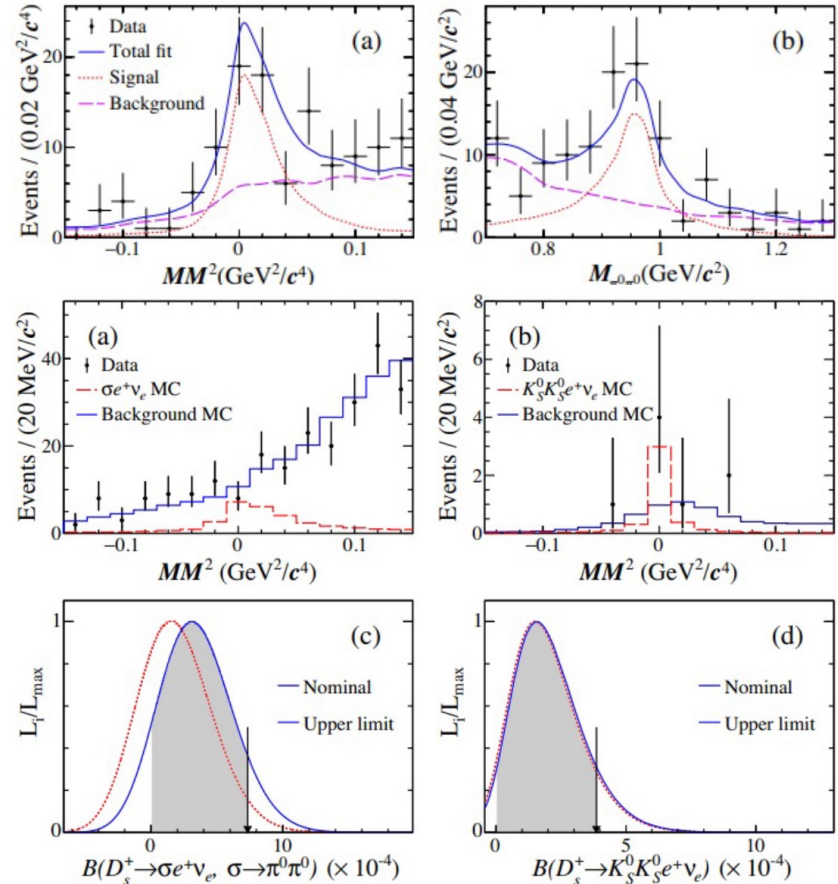
- 6.32 fb⁻¹ data @ 4.178 - 4.226 GeV
- $N_{sig}^{f_0(980)} = 54.8 \pm 10.1$ (7.8 σ significance)
- First BF's Measurement:

$$\mathcal{B}(D_s^+ \rightarrow f_0(980)e^+ \nu_e, f_0(980) \rightarrow \pi^0 \pi^0)$$

$$= (7.9 \pm 1.4 \pm 0.4) \times 10^{-4}$$
- No significant signal and upper limit on BF @90% C.L. :

$$\mathcal{B}(D_s^+ \rightarrow f_0(500)e^+ \nu_e, f_0(500) \rightarrow \pi^0 \pi^0) < 7.3 \times 10^{-4}$$

$$\mathcal{B}(D_s^+ \rightarrow K_S^0 K_S^0 e^+ \nu_e) < 3.8 \times 10^{-4}$$
- BF's help to understand the nature of the $f_0(500)$ and $f_0(980)$, and test different theoretical calculations.



Charm Decays

$$\Gamma(D_{(s)} \rightarrow V(S)\ell^+v_\ell) \propto |V_{cd(s)}|^2 \mathfrak{T}(A_1(q^2), A_2(q^2), V(q^2), \dots) dm^2 dq^2 d\cos(\theta_h) d\cos(\theta_\ell) d\chi$$

$V: \rho, \omega, K^*, \phi$

$S: f_0(500), f_0(980)$

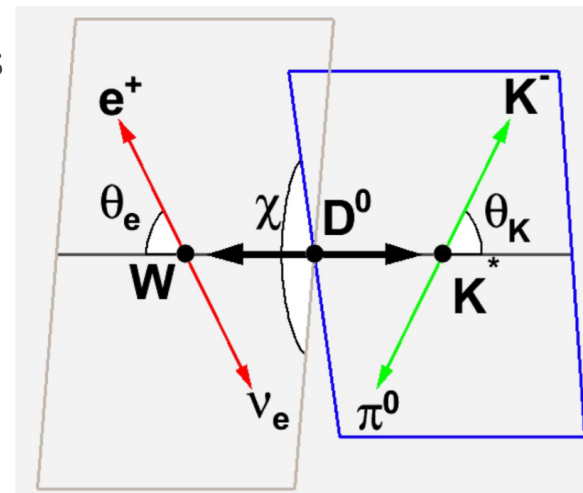
Formula: Phys. Rev. **137**, B438 (1965)

Phys. Rev. D **46**, 5040 (1992)

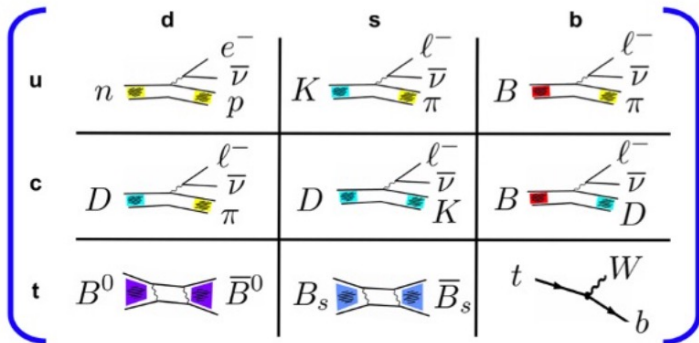
- Decay intensity $\mathfrak{T}$ include S, P, D wave components
- Un-binned Maximum likelihood (Based on RooFit)
- FF parameterization (single pole)

$$A_i(q^2) = \frac{A_i(0)}{1 - q^2/M_A^2} \quad V(q^2) = \frac{V(0)}{1 - q^2/M_V^2}$$

$$r_V = \frac{V(0)}{A_1(0)} \quad r_2 = \frac{A_2(0)}{A_1(0)}$$



Charm Decays



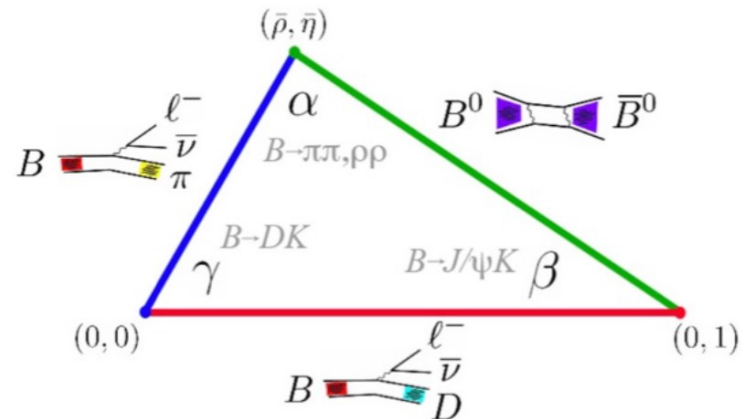
From S. Descotes-Genon

$|V_{cs}|, |V_{cd}|$: (semi-)leptonic charm decays

(can be done and should be done, but none has done anything yet)

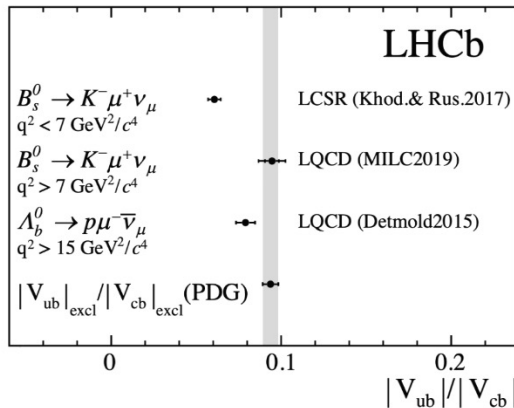
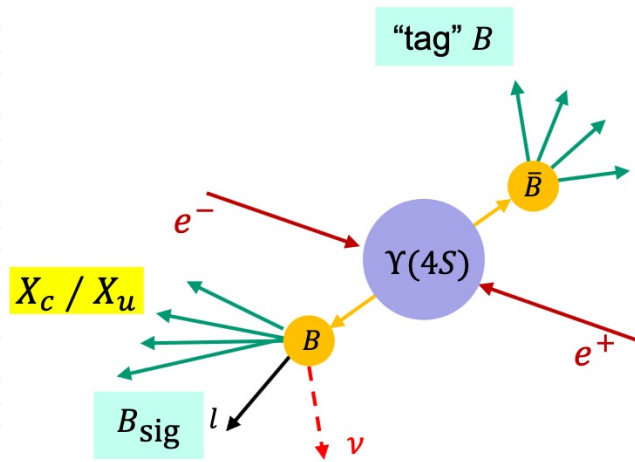
$|V_{ub}|, |V_{cb}|$: (semi-)leptonic B decays

$|V_{td}|, |V_{ts}|$: $\Delta m_d, \Delta m_s$



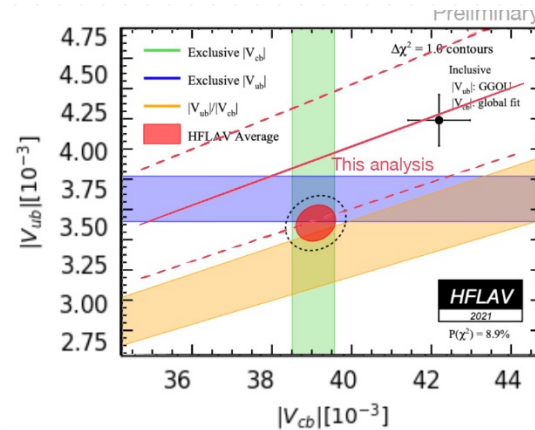
- α : $B \rightarrow \pi\pi, B \rightarrow \rho\pi, B \rightarrow \rho\rho$, isospin analyses
- β : $B \rightarrow (\bar{c}c)K, B \rightarrow Dh^0$, time-dependent CP violation
- γ : $B \rightarrow DK$, ADS/GLW/GGSZ
- ϕ_s : $B_s^0 \rightarrow (c\bar{c})(KK, \pi\pi)$, time-dependent CP violation
- $-2\beta_c + \gamma$: $B_c \rightarrow D_s K$

$$\phi_s^{s\bar{s}s} = -0.042 \pm 0.075 \pm 0.009 \text{ rad},$$



$$|V_{ub}|/|V_{cb}|(\text{low}) = 0.0607 \pm 0.0015(\text{stat}) \pm 0.0013(\text{syst}) \pm 0.0008(D_s) \pm 0.0030(\text{FF}),$$

$$|V_{ub}|/|V_{cb}|(\text{high}) = 0.0946 \pm 0.0030(\text{stat})^{+0.0024}_{-0.0025}(\text{syst}) \pm 0.0013(D_s) \pm 0.0068(\text{FF}),$$



Belle Preliminary
711 fb⁻¹

- Belle: inclusive $|V_{ub}|$ measurement complicated
 - ✓ Large “bg” contribution from $B \rightarrow X_c l \nu$
- Treat $B \rightarrow X_c l \nu$ as part of signal
 - ✓ Simultaneously measure $|V_{ub}|$ & $|V_{cb}|$
 - ✓ $B \rightarrow X_u l \nu$ dominate (>86%) in high p_l^B bins

- LHCb: 2 fb⁻¹ data at 8 pp collisions

- Observation of $B_s^0 \rightarrow K^- \mu^+ \nu_\mu l$

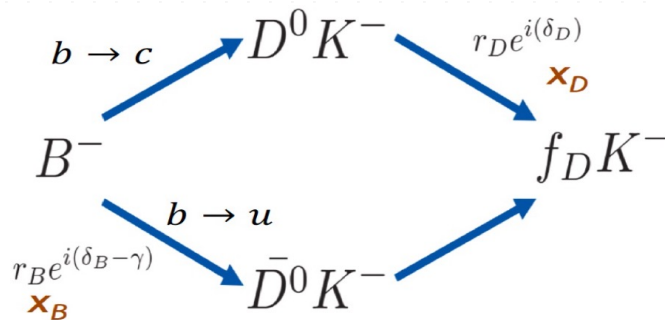
- ✓ Branching fraction measurement

$$R_{BF} = \frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)}$$

- ✓ Determination of $|V_{ub}| / |V_{cb}|$ in low/high q^2 bins

LHCb, PRL126.081804(2021), [arXiv: 2303.17309]

- A few selected recent measurements from Belle(II) and LHCb experiments
 - ✓ Measurements of $|V_{cb}|$ & $|V_{ub}|$
 - ✓ Tests of lepton universality
- Discrepancies ($> 3\sigma$) of measured $|V_{cb}|$ and $|V_{ub}|$ between inclusive and exclusive final states remains
 - ✓ Measurements not limited by statistical precision
 - ✓ Better design analysis choice to reduce systematic uncertainties
 - ✓ Many systematic uncertainties can be reduced with more data
 - ✓ Important to improve precision of theoretical calculations
- Deviation of measured $R_{D^{(*)}}$ from the SM prediction remains ($> 3\sigma$)
 - ✓ More precise measurement expected with more coming data
 - ✓ Measurements as a function of q^2 and angular distributions
- Test muon and electron universality: inclusive and angular distributions
 - ✓ Systematic uncertainties that will further be reduced with more data
- **Semileptonic b -hadron offer reach opportunities to look for NP, expect new results soon**



D^0 and $\bar{D}^0$ decay to same final states to interference

GLW: D = CP eigenstates, e.g. KK , $\pi\pi$

PLB 253 (1991) 483
PLB 265 (1991) 172

ADS: D = quasi-flavour-specific states e.g. $K\pi$

PRL 78 (1997) 3257

GGSZ: D = self-conjugate multi(3)-body states e.g. $K_s\pi\pi$

PRD 68 (2003) 054018

GLS: ADS variant with singly Cabibbo-suppressed decay $D \rightarrow K_s K\pi$

PRD 67 (2003) 071301

time-dependent $B_s \rightarrow D_s K$, $B^0 \rightarrow D\pi$ etc

Nucl. phys. B 672 (2003) 459

Dalitz (GW) method: $B^0 \rightarrow DK\pi$

PRD 79 (2009) 051301

Sensitivities of γ from many channels, important to measure as many as possible

GLS result (Belle+BelleII!)

- $B^\pm \rightarrow DK^\pm$ with $D \rightarrow K_S^0 K^+ \pi^-$ (SS) or $D \rightarrow K_S^0 K^- \pi^+$ (OS)
- Measure 4 Acp and 3 BR ratios.
- Get results in full D phase space and in the K^*K region (large δ_D).

$$A_{SS}^{DK} = \frac{2r_B^{DK} r_D \kappa_D \sin(\delta_B^{DK} - \delta_D) \sin \phi_3}{1 + (r_B^{DK})^2 r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} - \delta_D) \cos \phi_3},$$

$$A_{OS}^{DK} = \frac{2r_B^{DK} r_D \kappa_D \sin(\delta_B^{DK} + \delta_D) \sin \phi_3}{(r_B^{DK})^2 + r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} + \delta_D) \cos \phi_3},$$

$$A_{SS}^{D\pi} = \frac{2r_B^{D\pi} r_D \kappa_D \sin(\delta_B^{D\pi} - \delta_D) \sin \phi_3}{1 + (r_B^{D\pi})^2 r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} - \delta_D) \cos \phi_3},$$

$$A_{OS}^{D\pi} = \frac{2r_B^{D\pi} r_D \kappa_D \sin(\delta_B^{D\pi} + \delta_D) \sin \phi_3}{(r_B^{D\pi})^2 + r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} + \delta_D) \cos \phi_3}.$$

$$R_{SS}^{DK/D\pi} = R \frac{1 + (r_B^{DK})^2 r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} - \delta_D) \cos \phi_3}{1 + (r_B^{D\pi})^2 r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} - \delta_D) \cos \phi_3},$$

$$R_{OS}^{DK/D\pi} = R \frac{(r_B^{DK})^2 + r_D^2 + 2r_B^{DK} r_D \kappa_D \cos(\delta_B^{DK} + \delta_D) \cos \phi_3}{(r_B^{D\pi})^2 + r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} + \delta_D) \cos \phi_3},$$

$$R_{SS/OS}^{D\pi} = \frac{1 + (r_B^{D\pi})^2 r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} - \delta_D) \cos \phi_3}{(r_B^{D\pi})^2 + r_D^2 + 2r_B^{D\pi} r_D \kappa_D \cos(\delta_B^{D\pi} + \delta_D) \cos \phi_3}.$$

- 2D Fit ($\Delta E, C'$) of 8 categories ($DK, D\pi$)x(SS, OS)x(+, -)

GLS result (Belle+BelleII!)

- $B^\pm \rightarrow DK^\pm$ with $D \rightarrow K_S^0 K^+ \pi^-$ (SS) or $D \rightarrow K_S^0 K^- \pi^+$ (OS)
- Measure 4 Acp and 3 BR ratios.
- Get results in full D phase space and in the K^*K region (large δ_D).

In K^*K region:

$$A_{SS}^{DK} = 0.055 \pm 0.119 \pm 0.020,$$

$$A_{OS}^{DK} = 0.231 \pm 0.184 \pm 0.014,$$

$$A_{SS}^{D\pi} = 0.046 \pm 0.029 \pm 0.016,$$

$$A_{OS}^{D\pi} = 0.009 \pm 0.046 \pm 0.009,$$

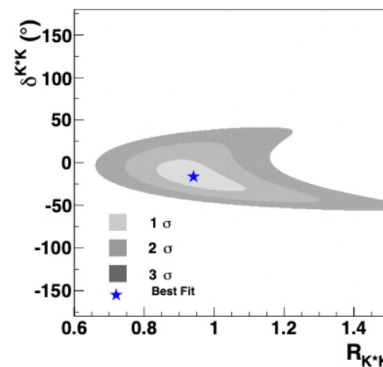
$$R_{SS}^{DK/D\pi} = 0.093 \pm 0.012 \pm 0.005,$$

$$R_{OS}^{DK/D\pi} = 0.103 \pm 0.020 \pm 0.006,$$

$$R_{SS/OS}^{D\pi} = 2.412 \pm 0.132 \pm 0.019,$$

[arXiv:2306.02940](https://arxiv.org/abs/2306.02940)

- First Belle/Belle II result from this channel.
- The precision is worse than LCHb's 😞 [[arXiv:2002.08858](https://arxiv.org/abs/2002.08858)]
- With the D information from CLEO-c, will contributed in a combined ϕ_3 from Belle/BelleII. (May get out this summer)



- Model-independent result from CLEO-c. [[arXiv:1203.3804](https://arxiv.org/abs/1203.3804)]

GLW result (Belle+BelleII!)

- $B^\pm \rightarrow DK^\pm$ with $D \rightarrow K_S^0 \pi^0$ (CP-odd) or $D \rightarrow K^+ K^-$ (CP-even)

$$R_{CP\pm} = \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D^0 K^-) + \mathcal{B}(B^+ \rightarrow \bar{D}^0 K^+)},$$

$$= 1 + r_B^2 + 2\eta_{CP} r_B \cos(\delta_B) \cos(\phi_3),$$

$$A_{CP\pm} = \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) - \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)},$$

$$= 2\eta_{CP} r_B \sin(\delta_B) \sin(\phi_3) / R_{CP\pm}.$$

	68.3% CL	95.4% CL
ϕ_3 (°)	[8.5, 16.5]	[5.0, 22.0]
	[84.5, 95.5]	[80.0, 100.0]
	[163.3, 171.5]	[157.5, 175.0]
r_B	[0.321, 0.465]	[0.241, 0.522]

$$\mathcal{R}_{CP+} = 1.164 \pm 0.081 \pm 0.036,$$

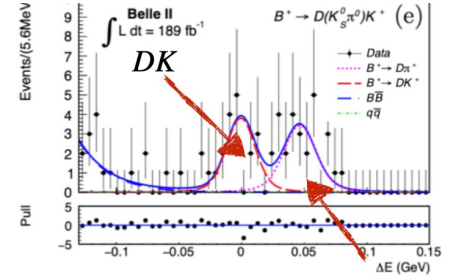
$$\mathcal{R}_{CP-} = 1.151 \pm 0.074 \pm 0.019,$$

$$\mathcal{A}_{CP+} = (+12.5 \pm 5.8 \pm 1.4)\%,$$

$$\mathcal{A}_{CP-} = (-16.7 \pm 5.7 \pm 0.6)\%.$$

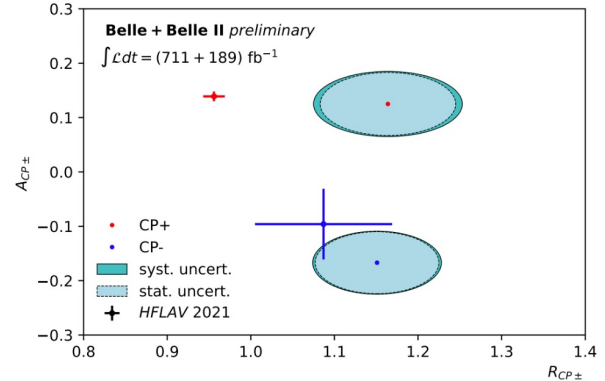
$\leftrightarrow 3.5\sigma$

world average: ϕ_3 (°) = $66.2^{+3.4}_{-3.6}$ $r_B = 0.0996 \pm 0.0026$



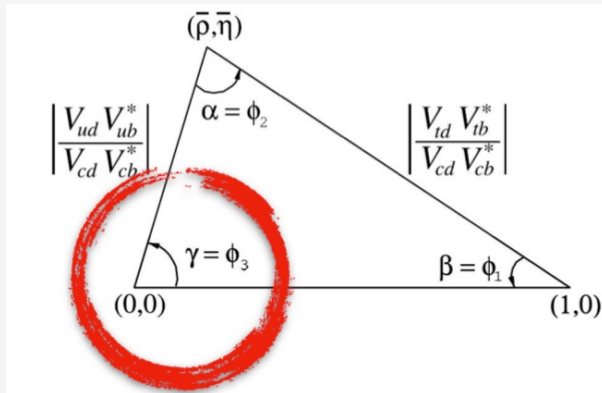
- 2D Fit ($\Delta E, C'$) of 6 categories $\text{misID } D\pi$
($DK, D\pi$) $\times$ ($K_S^0 \pi^0, K^+ K^-, K^- \pi^+$)

Large R_{CP+} than W.A.
Competitive R_{CP-} and A_{CP-} with W.A.



Measurement of CKM angle ϕ_3

- ⊙ Theoretical uncertainty on measurement is $\frac{\delta\phi_3}{\phi_3} \sim 10^{-7}$
arxiv:1308.5663
- ⊙ Test physics beyond SM
- ⊙ CPV in the interference $b \rightarrow c\bar{u}s$ and $b \rightarrow u\bar{c}s$:

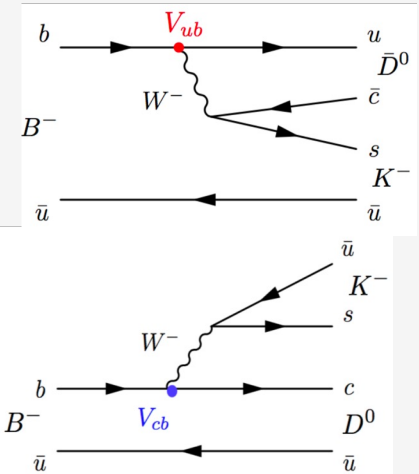
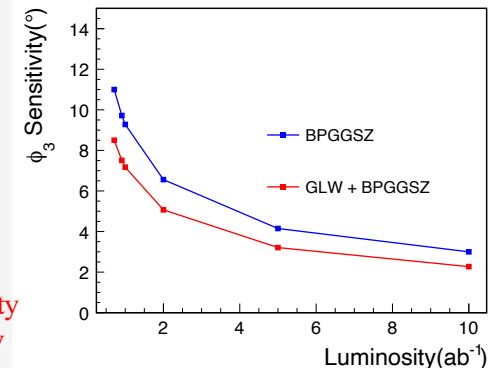


$$\frac{A^{suppr.}[B^- \rightarrow \bar{D}^0 K^-]}{A^{favor.}[B^- \rightarrow D^0 K^-]} = r_B e^{i(\delta_B - \phi_3)}$$

$$\phi_3 = \arg\left[\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right]$$

- ⊙ Foreseen precision of ϕ_3 is expected (current world-average $\delta\phi \sim 4^\circ$) with the future Belle II dataset

The expected uncertainty of ϕ_3 versus luminosity



Belle II Measurements of CKM angle ϕ_3

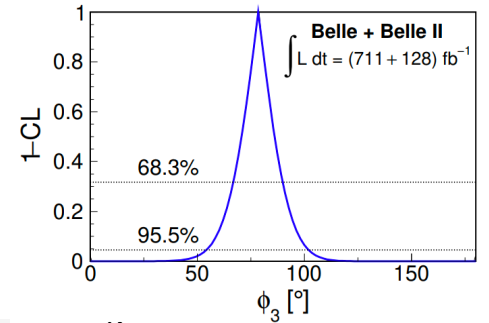
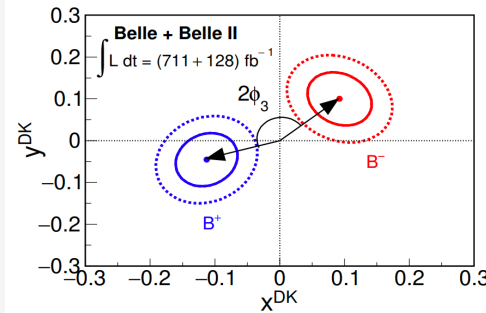
⊙ $(\Delta E, C')$ 2D simultaneous fit for all methods

⊙ GGSZ method with $B^- \rightarrow D(\rightarrow K_S h^+ h^-) h^-$ decays

-- The CP observables of interests

$$\begin{aligned} x_- &= +(9.24 \pm 3.27 \pm 0.17 \pm 0.23) \times 10^{-2} \\ x_+ &= -(11.28 \pm 3.15 \pm 0.18 \pm 0.22) \times 10^{-2} \\ y_- &= +(10.00 \pm 4.20 \pm 0.23 \pm 0.67) \times 10^{-2} \\ y_+ &= -(4.55 \pm 4.20 \pm 0.11 \pm 0.55) \times 10^{-2} \end{aligned}$$

JHEP02(2022)063



$$\phi_3 = (78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ$$

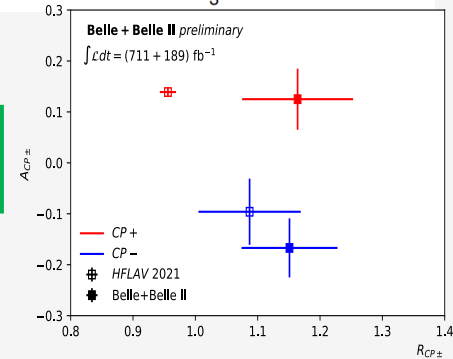
⊙ GLW method $A_{CP\pm} = \pm 2r_B \sin \delta_B \sin \phi_3 / R_{CP\pm}$
arXiv:2308.05048

$$R_{CP\pm} = 1 + r_B^2 \pm 2r_B \cos \delta_B \cos \phi_3$$

$$\begin{aligned} A_{CP+} &= (+12.5 \pm 5.8(stat.) \pm 1.4(syst.))\% & R_{CP+} &= 1.164 \pm 0.081(stat.) \pm 0.036(syst.) \\ A_{CP-} &= (-16.7 \pm 5.7(stat.) \pm 0.6(syst.))\% & R_{CP-} &= 1.151 \pm 0.074(stat.) \pm 0.019(syst.) \end{aligned}$$

⊙ GLS method with $B^- \rightarrow D(\rightarrow K_S K^\pm \pi^\mp) h^-$ decays arXiv:2306.02940

- 7 CP observables: 4 asymmetries, 3 BRs ratios
- Measurement performed in full D phase space and in the enhanced-interference $D \rightarrow K^* K$ region
- These results can provide constraint on ϕ_3



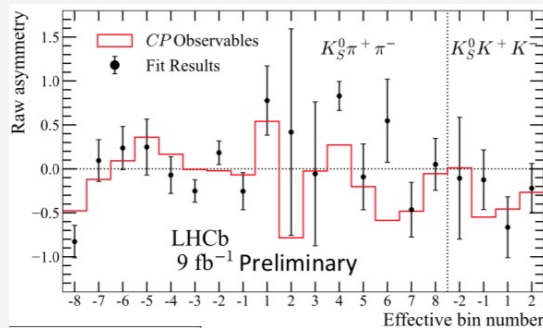
LHCb Measurements of CKM angle ϕ_3

⊙ GGSZ method

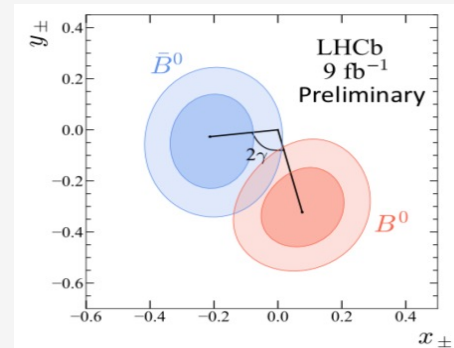
-- $B^0 \rightarrow D(\rightarrow K_S h^+ h^-) K^{*0}$

- Limited statistics,
- CPV still observed in some bins

$$\phi_3 = (49_{-18}^{+23})^\circ$$

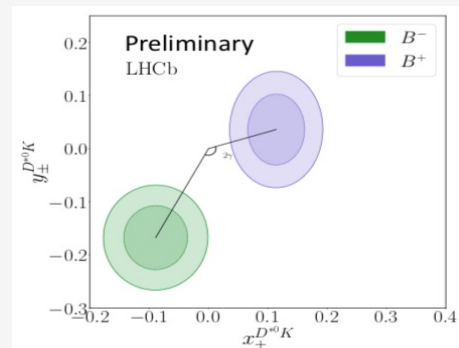


LHCb-PAPER-2023-009



-- $B^- \rightarrow D^*(\rightarrow D(\rightarrow K_S h^+ h^-) \pi^0 / \gamma) h^-$

LHCb-PAPER-2023-012

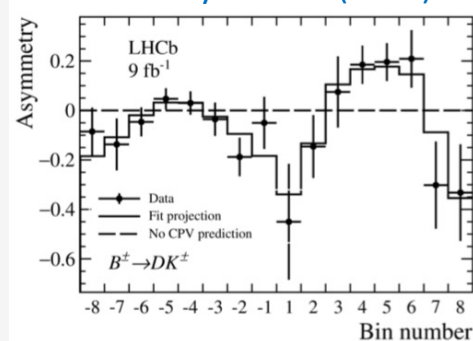


- Opposite CPV between $D^{*0} \rightarrow D\pi$ and $D^{*0} \rightarrow D\gamma$
- Irreducible bkg
- 2D invariant mass fit

$$\phi_3 = (69 \pm 14)^\circ$$

-- $B^- \rightarrow D(\rightarrow K^+ K^- \pi^+ \pi^-) h^-$

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- Measured firstly
- Complicated binning scheme

$$\phi_3 = (116_{-14}^{+12})^\circ$$